5

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#### musthave/vimrc.txt

```
1
                      < F9 > :wall! < CR > :!g++ - Wall - Wextra - Wshadow -\longleftrightarrow Wno-unused-result -o \%:r \% - std=c++14 - DHOME -\longleftrightarrow
1
                      \verb|Wno-unused-result -o| %:r % -std=c++14 -DHOME -\leftarrow
\mathbf{2}
                       02 < CR >
                     <F8> :wall! <CR> :!ulimit -s 500000 && ./\%:r <CR\hookleftarrow
       3
\mathbf{2}
              inoremap \{< CR> \ \{< CR>\} < ESC> 0
\mathbf{2}
              \mathtt{map} \  \, < \mathtt{c-a} > \  \, \mathtt{ggVG}
              set nu
\mathbf{3}
       9
              set rnu
     10
              syntax on
     11
3
              \mathtt{map} \  \, <\! \mathtt{c-t} \! > \  \, :\mathtt{tabnew} \  \, <\! \mathtt{CR} \! >
              \mathtt{map} <\mathtt{c-1}> : \mathtt{tabn} <\mathtt{CR}>
              \mathtt{map} \  \, <\! \mathtt{c-h} \! > \  \, \mathtt{:tabp} \  \, <\! \mathtt{CR} \! > \\
4
     16
4
     17
              \mathtt{set} \mathtt{sw} = 4
              \mathtt{set} \quad \mathtt{so} \!=\! 99
              \operatorname{\mathfrak{set}} \operatorname{\mathfrak{bs}}=2
4
     20
              \mathtt{set} \mathtt{sts} \! = \! 4
\mathbf{5}
```

#### musthave/template.cpp

```
5
             team : SPb ITMO University
 5
          #include < bits / stdc++.h>
 6
          #define F first
          #define S second
          #define pb push_back
 6
          #define forn(i, n) for(int i = 0; (i) < (n); ++i) #define eprintf(...) fprintf(stderr, _VA_ARGS_), \leftarrow
               fflush (stderr)
 6
          #define sz(a) ((int)(a).size())
#define all(a) (a).begin(),a.end()
#define pw(x) (1LL<<(x))
     10
 7
     11
     13
          using namespace std;
 7
          typedef long long 11;
          typedef double dbl;
     16
 8
          typedef vector < int > vi;
typedef pair < int , int > pi;
     17
     18
 8
     20
          9
     23
          /* ---- main part ---- */
10
     25
10
     28
     29
     30
          int main()
          define TASK ""
          #ifdef home
            assert(freopen(TASK".in", "r", stdin));
//assert(freopen(TASK".out", "w", stdout));
     35
     36
          #endif
     37
     39
     40
     41
     42
     43
          #ifdef home
             eprintf("time = \%d ms\n", (int)(clock() * 1000. / \hookleftarrow
     44
               CLOCKS_PER_SEC));
     45
          #endif
             return = 0;
     46
     47
```

13

17

19

 $\frac{20}{21}$ 

22

### musthave/crt.cpp

## musthave/fastIO.cpp

```
25
    #include <cstdio>
#include <algorithm>
                                                                     26
                                                                     27
                                                                     28
    /** Interface */
                                                                     29
    inline int readInt();
inline int readUInt();
                                                                     31
    inline bool isEof();
                                                                     33
                                                                     34
     /** Read */
                                                                     35
                                                                     36
    38
                                                                     39
                                                                     40
     inline bool isEof()
       if (pos == buf_len) {
         19
         if (pos == buf len) return 1:
                                                                     46
21
       return 0;
                                                                     47
                                                                     48
23
    24
         ++]; }
                                                                     51
    inline int readChar() {
                                                                     52
27
          c = getChar();
                                                                     53
      while (c != -1 \&\& c <= 32) c = getChar();
28
29
      return c;
30
31
                                                                     56
    inline int readUInt() {
                                                                     57
      int c = readChar(), x = 0;
while ('0' <= c && c <= '9') x = x * 10 + c - '0', \leftarrow
33
                                                                     58
34
          c = getChar();
      return x:
                                                                     62
                                                                     63
    inline int readInt() {
                                                                     64
39
      int s = 1, c = readChar();
                                                                     65
      int x = 0;

if (c == '-') s = -1, c = getChar();

while ('0') <= c && c <= '9') x = x * 10 + c - '0', \leftrightarrow
40
41
42
      c = getChar();
return s == 1 ? x : -x;
                                                                     69
                                                                     70
45
46
                                                                     73
       10M int [0..1e9)
cin 3.02
47
                                                                     74
                                                                     75
                                                                     76
       cin sync_with_stdio(false) 0.71
fastRead getchar 0.53
fastRead fread 0.15
                                                                     77
51
```

## musthave/fft.cpp

```
};
const dbl PI = acos(-1);
num root [maxN];
int rev[maxN];
bool rootsPrepared = false;
void prepRoots()
     i\,f\ (\,\mathtt{rootsPrepared}\,)\ \ \mathtt{return}\;;
     \label{eq:control_repared} \begin{array}{ll} \texttt{rootsPrepared} &= \texttt{true}\,;\\ \texttt{root}\,[\,1\,] &= \texttt{num}\,(\,1\,,\,\,0\,)\,;\\ \texttt{for}\,\,(\,\texttt{int}\,\,\,\texttt{k}\,=\,1\,;\,\,\texttt{k}\,<\,\texttt{maxBase}\,;\,\,+\!+\!\texttt{k}\,) \end{array}
          \begin{array}{lll} {\tt num} & {\tt x(2 * PI / pw(k+1));} \\ {\tt for} & ({\tt int i} = {\tt pw(k-1);} & {\tt i} < {\tt pw(k);} & +\!\!+\!\!{\tt i)} \end{array}
               int base, N;
int lastRevN = -1;
void prepRev()
     if (lastRevN == N) return;
     \begin{array}{lll} \mathtt{num} \ \mathbf{z} = \mathbf{f} \big[ \, \mathbf{i} \, + \, \mathbf{j} \, + \, \mathbf{k} \, \big] \ * \ \mathtt{root} \big[ \, \mathbf{j} \, + \, \mathbf{k} \, \big] \, ; \\ \mathbf{f} \big[ \, \mathbf{i} \, + \, \mathbf{j} \, + \, \mathbf{k} \, \big] = \mathbf{f} \big[ \, \mathbf{i} \, + \, \mathbf{j} \, \big] \, - \, \mathbf{z} \, ; \\ \mathbf{f} \big[ \, \mathbf{i} \, + \, \mathbf{j} \, \big] \, = \, \mathbf{f} \big[ \, \mathbf{i} \, + \, \mathbf{j} \, \big] \, + \, \mathbf{z} \, ; \end{array}
void _multMod(int mod)
      forn(i, N)
          int x = A[i] \% mod;
         a[i] = num(x & (pw(15) - 1), x >> 15);
      forn(i, N)
         \begin{array}{lll} & & & & & int & x = B[i] \% \ mod; \\ & & & & & & & \\ b[i] = & num(x \& (pw(15) - 1), x >> 15); \end{array}
     fft(a, f);
fft(b, g);
         \begin{array}{lll} & \text{int} & \text{j} = (\, \mathbb{N} \, - \, \mathbf{i} \, ) \, \, \, \& \, \, (\, \mathbb{N} \, - \, 1 \, ) \, \, ; \\ & \text{num a1} = (\, \mathbf{f} \, [\, \mathbf{i} \, ] \, + \, \mathbf{conj} \, (\, \mathbf{f} \, [\, \mathbf{j} \, ] \, ) \, \, \, * \, \, \mathbf{num} \, (\, 0 \, . \, 5 \, , \, \, 0 \, ) \, ; \\ & \text{num a2} = (\, \mathbf{f} \, [\, \mathbf{i} \, ] \, - \, \mathbf{conj} \, (\, \mathbf{f} \, [\, \mathbf{j} \, ] \, ) \, ) \, \, * \, \, \mathbf{num} \, (\, 0 \, . \, 5 \, , \, \, 0 \, ) \, ; \\ & \text{num b1} = (\, \mathbf{g} \, [\, \mathbf{i} \, ] \, + \, \mathbf{conj} \, (\, \mathbf{g} \, [\, \mathbf{j} \, ] \, ) \, ) \, \, * \, \, \mathbf{num} \, (\, 0 \, . \, 5 \, , \, \, N \, , \, \, 0 \, ) \, \hookleftarrow \end{array}
          \mathtt{num} \ \ \mathtt{b2} \ = \ ( \ \mathtt{g} \ [ \ \mathtt{i} \ ] \ - \ \mathtt{conj} \ ( \ \mathtt{g} \ [ \ \mathtt{j} \ ] \ ) \ \ * \ \mathtt{num} \ ( \ 0 \ , \ \ -0.5 \ \ / \ \ \mathtt{N} \hookleftarrow
           \begin{bmatrix} \mathtt{j} \\ \mathtt{b} \\ \mathtt{[j]} \end{bmatrix} = \mathtt{a1} \ * \ \mathtt{b1} \ + \ \mathtt{a2} \ * \ \mathtt{b2} \ * \ \mathtt{num} \left( \mathtt{0} \ , \ \mathtt{1} \right); 
      fft(b, g);
```

forn(i. N)

81

82 83

86

```
96
                  11 aa = f[i].x + 0.5;
                 11 bb = g[i] \cdot x + 0.5;
11 cc = f[i] \cdot y + 0.5;
 97
 98
               99
101
102
           103
104
105
               base = 1:
107
               while'(N < n1 + n2) base++, N <<= 1;
108
               109
110
111
112
               prepRoots();
113
              prepRev();
114
115
116
           void mult(int n1, int n2)
117
              \begin{array}{lll} {\tt prepAB}\,(\,{\tt n1}\,,\,\,\,{\tt n2}\,)\;;\\ {\tt forn}\,(\,{\tt i}\,,\,\,\,{\tt N}\,) & {\tt a}\,[\,{\tt i}\,] & = & {\tt num}\,(\,{\tt A}\,[\,{\tt i}\,]\,,\,\,\,{\tt B}\,[\,{\tt i}\,]\,)\;;\\ {\tt fft}\,(\,{\tt a}\,,\,\,\,{\tt f})\;; \end{array}
118
119
120
121
               \mathtt{forn}\,(\,\mathtt{i}\,\,,\,\,\,\,\mathtt{N}\,)
122
                \begin{array}{l} {\rm int} \ \ j = ({\tt N-i}) \ \& \ ({\tt N-1}) \ ; \\ {\tt a[i]} = ({\tt f[j]} \ * \ {\tt f[j]} - {\tt conj}({\tt f[i]} \ * \ {\tt f[i]})) \ * \ {\tt num} \ \longleftrightarrow \\ (0 \ , \ -0.25 \ / \ {\tt N}) \ ; \\ \end{array} 
123
124
125
126
               forn(i, N) C[i] = (11) round(f[i].x);
127
128
129
           void multMod(int n1, int n2, int mod)
131
132
133
               prepAB(n1, n2);
               _{\tt multMod(mod)};
134
135
           int D[maxN];
138
139
           {\tt void} \ {\tt multLL(int n1, int n2)}
140
              prepAB (n1, n2);
141
142
               int mod1 = 1.5e9;
144
               int mod2 = mod1 + 1;
145
146
               _multMod(mod1);
147
              forn(i, N) D[i] = C[i];
148
               \verb|_multMod(mod2)|;
150
151
152
               forn(i, N)
153
                 {\tt C[i]} \ = \ {\tt D[i]} \ + \ ({\tt C[i]} \ - \ {\tt D[i]} \ + \ ({\tt 11)} \, {\tt mod2}) \ * \ ({\tt 11}) \, \hookleftarrow
154
               mod1 % mod2 * mod1;
155
156
               HOW TO USE ::
157
               — set correct maxBase
— use mult(n1, n2), multMod(n1, n2, mod) and \leftrightarrow
158
159
               multLL(n1, n2)
— input : A[], B[]
160
161
               - output : C[]
162
```

# musthave/fftint.cpp

```
forn(i, N) rev[i] = (rev[i >> 1] >> 1) + ((i \& \leftarrow))
         1) << (base - 1);
int NN = N >> 1;
14
15
         int z = 1:
         forn(i, NN)
16
           root[i + NN] = z;
19
           z = z * (11) ROOT \% mod;
20
         21
         [2 * i];
22
24
       void fft(int *a, int *f)
25
         26
27
           \begin{array}{lll} i\,nt & z \,=\, f\,[\,i\,+\,j\,+\,k\,] & *\,\,(\,11\,)\,r\,oot\,[\,j\,+\,k\,] & \%\,\,m\,od\,;\\ f\,[\,i\,+\,j\,+\,k\,] & =\,\,(\,f\,[\,i\,+\,j\,] \,-\,z\,+\,m\,od\,) & \%\,\,m\,od\,;\\ f\,[\,i\,+\,j\,] & =\,\,(\,f\,[\,i\,+\,j\,] \,+\,z\,) & \%\,\,m\,od\,; \end{array}
30
31
32
33
      37
38
       39
         fft(A, F);
40
         if (eq) forn(i, N) G[i] = F[i];
else fft(B, G);
int invN = inv(N);
43
         forn(i, N) A[i] = F[i] * (11)G[i] % mod * invN %←
44
         reverse(A + 1, A + N);
         fft(A, C);
46
48
49
         void mult(int n1, int n2, int eq = 0) 
50
         51
53
55
         56
57
59
```

## ${ m musthave/blackbox.cpp}$

```
namespace blackbox
               int B[N];
               int C[N];
                int magic (int k, int x)
10
                     C[k] = (C[k] + A[0] * (11)B[k]) \% \text{ mod};
                     \begin{array}{lll} & \text{int } \mathbf{z} = 1; \\ & \text{if } (\mathbf{k} == \mathbb{N} - 1) \text{ return } \mathbb{C}[\mathbf{k}]; \\ & \text{while } ((\mathbf{k} \& (\mathbf{z} - 1)) == (\mathbf{z} - 1)) \end{array}
11
12
13
14
                          //mult B[k - z + 1 ... k] x A[z .. 2 * z - 1] forn(i, z) fft::A[i] = A[z + i]; forn(i, z) fft::B[i] = B[k - z + 1 + i];
16
17
                     \begin{array}{ll} {\tt fft::multMod(z,\,z,\,mod);} \\ {\tt forn\,(i,\,2\,*\,z\,-\,1)\,\,\,C\,[\,k\,+\,1\,+\,i\,]} \,=\, (\,C\,[\,k\,+\,1\,+\,i\,\longleftrightarrow\,] \\ {\tt ]\,\,+\,\,fft::C\,[\,i\,])\,\,\,\%\,\,\,mod\,;} \end{array}
18
19
                         z <<= 1;
22
                     return C[k];
23
                ]// A — constant array
// magic(k, x):: B[k] = x, returns C[k]
// !! WARNING !! better to set N twice the size ↔
24
27
```

#### musthave/halfplaneIntersection.cpp

```
int getPart(pt v) {
          return less(0, v.y) || (equal(0, v.y) && less(v.x, ←
               0));
      int partB = getPart(b);
         if (partA < partB) return -1;
if (partA > partB) return 1;
if (equal(0, a * b)) return 0;
if (0 < a * b) return -1;
return 1;</pre>
15
       {\tt double\ planeInt(vector{<}Line{>}\ 1)}\ \{
          int n = 1.size();
sort(all(1), [](Line a, Line b) {
   int r = cmpV(a.v, b.v);
   if (r != 0) return r < 0;</pre>
16
17
18
                 20
              });
22
          31
          l[i].id = i;
33
34
          \begin{array}{lll} \mathbf{i}\,\mathbf{n}\,\mathbf{t} & \mathtt{flagUp} \; = \; 0\,; \end{array}
          int flagDown = 0;
          for (int i = 0; i < n; i++) {
37
              int part = getPart(1[i].v);
             if (part == 1) flagUp = 1;
if (part == 0) flagDown = 1;
38
39
40
41
          if (!flagUp || !flagDown) return -1;
          for (int i = 0; i < n; i++) {
             pt v = 1[i].v;
pt u = 1[(i + 1) % n].v;
if (equal(0, v * u) && less(v % u, 0)) {
  pt dir = 1[i].v.rotate();
44
45
46
                  if (lessE(1[(i+1) \% n].0 \% dir, 1[i].0 \% dir \leftarrow
                 return -1:
50
              if (less(v * u, 0))
51
52
                return -1;
55
          ful = 0;
vector < Line > st(n * 2);
for (int tt = 0; tt < 2; tt++) {
  for (int i = 0; i < n; i++) {
    for (; cur >= 2; cur --) {
      pt G = st[cur - 1] * 1[i];
    }
}
56
57
                     if (! lessE(st[cur - 2].v * (G - st[cur - 2]. \leftarrow)]
              0), 0))
62
63
                  \begin{array}{l} \texttt{st} \left[ \mathtt{cur} + + \right] = 1 \left[ \mathtt{i} \right]; \\ \texttt{if} \left( \mathtt{cur} >= 2 \ \&\& \ \mathtt{lessE} \left( \mathtt{st} \left[ \mathtt{cur} - 2 \right]. \mathtt{v} \ * \ \mathtt{st} \left[ \mathtt{cur} - \leftrightarrow \right] \right]. \\ \end{array} 
                1].v, 0)) return 0;
66
67
          Jector < int > use(n, -1);
int left = -1, right = -1;
for (int i = 0; i < cur; i++) {
   if (use[st[i].id] == -1) {</pre>
68
69
71
72
73
                use[st[i].id] = i;
74
              else {
   left = use[st[i].id];
                 right = i;
79
80
          vector < Line > tmp;
for (int i = left; i < right; i++)</pre>
             tmp.pb(st[i]);
```

```
83 | vector < pt > res;
for (int i = 0; i < (int)tmp.size(); i++)
res.pb(tmp[i] * tmp[(i + 1) % tmp.size()]);
double area = 0;
for (int i = 0; i < (int)res.size(); i++)
area += res[i] * res[(i + 1) % res.size()];
return area / 2;
}
```

#### musthave/commonTangents.cpp

```
3
     \verb|vector| < Line> | \verb|commonTangents| (pt A, dbl rA, pt B, dbl \leftarrow
        rB) {
vector < Line > res;
        \mathtt{pt} \ \mathtt{C} = \mathtt{B} - \mathtt{A};
        dbl z = C.len2();
        pt magic = pt(r, d) / z;
pt v(magic % C, magic * C);
dbl CC = (rA * i - v % A) / v.len2();
pt 0 = v * -CC;
res ph(linc() 2);
14
15
16
             17
20
^{21}
22
        HOW TO USE ::
23
               *D*----
                *...* - -*...*
               * . . . . . * -
                                - *....*
27
              *...A...* -- *...B...*

*....* -- *....*

*....* -- *....*

*...* -- *....*
28
29
30
        -- res = {CE, CF, DE, DF}
```

## musthave/minDisc.cpp

```
pair < pt, dbl > minDisc(vector < pt > p) {
        int n = p.size();
pt 0 = pt(0, 0);
dbl R = 0;
        random_shuffle(all(p));
for (int i = 0; i < n; i++) {
  if (ls(R, (0 - p[i]).len())) {</pre>
              0 = p[i];
           R = 0:
11
15
16
17
                          R = (p[i] - 0).len();
20
21
                }
25
26
27
        \mathtt{return} \ \left\{ \mathtt{0} \ , \ \mathtt{R} \right\};
28
```

4

6

9 10

 $\frac{11}{12}$ 

16

21

22

23

28

29

30

35 36

40

41

42

43

46

47 48

49

50

53

54

#### musthave/polygonArcCut.cpp

```
dbl R;
    6
                      };
                       const Meta SEG = \{0, pt(0, 0), 0\};
10
                      \verb"vector!<|pair|<|pt|, ||Meta>> ||cut|(|vector|<|pair|<|pt|, ||Meta>> ||p|, \hookleftarrow
                                  Line 1) {
vector < pair < pt , Meta >> res;
                                   int n = p.size();
                                  for (int i = 0; i < n; i++) {
14
                                            pt A = p[i].F;
                                              pt B = \hat{p}[(i + 1) \% n].F;
15
                                              \begin{array}{lll} & \text{ if } & (\text{le}(0,\ 1.\text{v}\ *\ (\text{A}\ -\ 1.0)))\ \{ & \text{ if } & (\text{eq}(0,\ 1.\text{v}\ *\ (\text{A}\ -\ 1.0))\ \&\&\ p[\text{i}].S.type == 1 \leftrightarrow \&\&\ ls(0,\ 1.\text{v}\ \%\ (p[\text{i}].S.0\ -\ A))) \end{array}
16
17
                                                                    res.pb({A, SEG});
19
20
                                                                    res.pb(p[i]);
21
                                              f (p[i].S.type == 0) {
   if (sign(1.v * (A - 1.0)) * sign(1.v * (B - 1.←)
0)) == -1) {
   pt FF = Line(A, B) * 1;
   pt FF = Line(B, B) * 1;
  pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF = Line(B, B) * 1;
   pt FF 
22
25
                                                                    {\tt res.pb} \, (\, {\tt make\_pair} \, (\, {\tt FF} \, \, , \, \, \, {\tt SEG} \, ) \, ) \, \, ;
26
27
                                               else {
                                                        pt È, F;
                                                         if (intCL(p[i].S.0, p[i].S.R, 1, E, F)) {
   if (onArc(p[i].S.0, A, E, B))
     res.pb({E, SEG});
   if (onArc(p[i].S.0, A, F, B))
     res.pb({F, p[i].S});
31
32
33
34
                                                       }
36
                                           }
37
38
                                   return res;
```

## musthave/hashTable.cpp

```
template < const int \ max\_size \ , \ class \ HashType \ , \ class \ \hookleftarrow
       Data, const Data default_value>
    struct hashTable {
     HashType hash[max_size];
Data f[max_size];
     int size;
     int i = H \% max_size;
       if (++i == max_size)
i = 0;
10
11
12
     }
13
14
15
     16
       17
19
              = default_value;
20
         f[i]
21
         size++;
22
23
       return f[i];
     }
   };
   \verb|hashTable| < 13, | | int|, | | int|, | | 0 > | h|;
```

## ${\bf must have/hungary.cpp}$

```
namespace hungary
           const int N = 210;
            int a[N][N];
           int ans[N];
            int calc(int n, int m)
                    ++\mathbf{n} , ++\mathbf{m} ;
                      vi mn(m, inf);
                                  vi was(m,
                                  while (p[x])
                                             was[x] = 1;
                                             forn(j, m)
                                                        \begin{array}{lll} & \mbox{if} & (\,\mbox{\,was\,\,}[\,\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox{\,\i}\,\mbox
                                  while (x)
                                             \begin{array}{lll} \textbf{int} & \textbf{y} \ = \ \textbf{prev} \ [ \ \textbf{x} \ ] \ ; \end{array}
                                           p[x] = p[y];
                                            \mathtt{x} \ = \ \mathtt{y} \ ;
                       for (int j = 1; j < m; ++j)
                                 {\tt ans} \, [\, {\tt p} \, [\, {\tt j} \, ]\, ] \,\, = \,\, {\tt j} \, ;
                         HOW TO USE ::
                          -- set values to a[1..n][1..m] (n <= m)
                           -- run calc(n, m) to find MINIMUM
                           -- to restore permutation use ans[]
                           -- everything works on negative numbers
                        !! i don't understand this code, it's \hookleftarrow copypasted from e-maxx (and rewrited by enot110 \hookleftarrow
```

### must have/mod Reverse One Line.cpp

```
1  int rev(int x, int m)
2  {
3     if (x == 1) return 1;
    return (1 - rev(m % x, x) * (ll)m) / x + m;
5  }
```

## musthave/optimizations.cpp

 $70\\71$ 

74

80

81

82

83

86

87

92

93

 $\frac{94}{95}$ 

97

98

99

100

101

102

103

104

105

106

107

109

110

111

 $\frac{112}{113}$ 

116

117

118

119

```
: "d" (xh), "a" (xl), "r" (y)
       #else
13
                                                                                                               51
14
                                                                                                               52
              mov edx, dword ptr [xh];
mov eax, dword ptr [xl];
div dword ptr [y];
                                                                                                               53
15
16
                                                                                                               54
              mov dword ptr[d], eax;
mov dword ptr[m], edx;
19
                                                                                                               57
20
                                                                                                               58
21
       #endif
                                                                                                               59
                                                                                                               60
          out_d = d; out_m = m;
24
       // have no idea what sse flags are really cool; list \leftarrow
                                                                                                               64
      // have no idea what sse flags are really cool, flow—
of some of them
// — very good with bitsets
#pragma GCC optimize("O3")
#pragma GCC target("sse,sse2,sse3,ssse3,sse4,popcnt,←)
                                                                                                               69
```

## musthave/plane3DInt.cpp

```
1 //(A, v) * (B, u) -> (O, n)
2 
3 pt n = v * u;
4 pt m = v * n;
5 double t = (B - A) % u / (u % m);
6 pt 0 = A - m * t;
```

#### musthave/simplex.cpp

```
3
            dbl a[MAX_M][MAX_N];
            dbl b MAX_M
            dbl c[MAX_N];
            dbl v;
            {\tt 11} \ {\tt n} \ , \ {\tt m} \ ;
            int left[MAX_M];
            int up[MAX_N];
11
            int pos[MAX_N
13
            dbl res[MAX_N]
14
            15
16
               n = nn;
                m = mm;
                v = 0;
for (int i = 0; i < m; i++)
  for (int j = 0; j < n; j++)
    a[i][j] = 0;
for (int i = 0; i < m; i++)
    b[i] = 0;
for (int i = 0; i < n; i++)</pre>
19
20
21
24
25
                    c[\dot{i}] = 0;
26
27
            void pivot(int x, int y) {
  swap(left[x], up[y]);
  dbl k = a[x][y];
28
30
31
                \mathtt{a}\,[\,\mathtt{x}\,]\,[\,\mathtt{y}\,] \;=\;
32
                b[x] /= k;
                for (int i = 0;
for (int i = 0; i < n; i++) {
   a[x][i] = a[x][i] / k;
   if (!eq(a[x][i], 0))
    pos[cur++] = i;
}</pre>
33
34
37
38
39
                for (int i = 0; i < m; i++) {
   if (i == x || eq(a[i][y], 0)) continue;
   dbl cof = a[i][y];
   b[i] -= cof * b[x];
   a[i][y] = 0;
   for (int j = 0; j < cur; j++)
        a[i][pos[j]] -= cof * a[x][pos[j]];
}</pre>
40
41
43
45
46
                 dbl cof = c[y];
```

```
v += cof * b[x];
   for (int i = 0; i < cur; i++) {
  c[pos[i]] -= cof * a[x][pos[i]];
left[i] = i + n;
    while (1) {
       int x = -1;

for (int i = 0; i < m; i++)

if (ls(b[i], 0) && (x == -1 || b[i] < b[x])) \leftrightarrow
        \begin{array}{l} {\rm i\, f\,}^f(\, x == -1) \  \, {\rm b\, reak}\,; \\ {\rm i\, nt\,} \  \, y = -1; \\ {\rm fo\, r\,} \  \, (\, {\rm i\, nt\,} \  \, j = 0\,; \  \, j < n\,; \  \, j++) \\ {\rm i\, f\,} \  \, (\, {\rm l\, s\,} \big(\, a\,[\, x\,]\,[\, j\,]\,, \  \, 0\,)\,)\,\, \, \, \{ \end{array} 
        \begin{tabular}{ll} $\{$ if $(y==-1)$ & \\ & assert(false); // no solution \end{tabular} 
       pivot(x, y);
    while (1) {
       int y = -1;
for (int i = 0; i < n; i++)
           if (1s(0, c[i]) && (y == -1 || (c[i] > c[y]) \leftarrow
             y = i;
       if'(y == -1) break;
       x ] [ y ] ) ) {
                  x = i;
              }
          }
        if (y == -1) {
          assert(false); // infinite solution
       pivot(x, y);
    memset (res, 0, sizeof (res));
       r (int i = 0; i < m; i++) {
if (left[i] < n) {
  res[left[i]] = b[i];
   }
// HOW TO USE ::
// -- call init(n, m)
// -- call solve()
// -- variables in "up" equals to zero
// -- variables in "left" equals to b
// -- variac...
// -- max: c * x
// -- b[i] >= a[i] * x
 // -- sertificate in "res"
```

## musthave/std-rb-tree.cpp

11

1.5

16

17

 $18 \\ 19 \\ 20$ 

#### musthave/sufAutomaton.cpp

```
21
         namespace SA {
             22
                                                                                                                                         23
 3
                                                                                                                                         24
             int nxt[MAXN][SIGMA];
int link[MAXN], len[MAXN], pos[MAXN];
                                                                                                                                         27
             void init() {
  memset(nxt, -1, sizeof(nxt));
  memset(link, -1, sizeof(link));
                                                                                                                                         28
                                                                                                                                         29
10
11
                                                                                                                                         31
12
                  {\tt memset(len, 0, sizeof(len))};\\
13
                  last = 0;
                                                                                                                                         33
14
                 \mathbf{sz} = 1;
                                                                                                                                         34
15
                                                                                                                                         35
16
                                                                                                                                         36
             v\,o\,i\,d\quad a\,d\,d\,\left(\begin{array}{ccc}i\,n\,t&c\,\right)\quad\{
17
                 int cur = sz++;
len[cur] = len[last] + 1;
pos[cur] = len[cur];
int p = last;
last = cur;
for (; p != -1 && nxt[p][c] == -1; p = link[p]) \Leftarrow
nxt[p][c] = cur;
if (p == -1) {
    link[cur] = 0;
    return;
                  int cur = sz++;
                                                                                                                                         38
19
                                                                                                                                         39
20
                                                                                                                                         40
21
22
25
                                                                                                                                         46
26
                      return:
27
                                                                                                                                         47
                 int q = nxt[p][c];
if (len[p] + 1 == len[q]) {
  link[cur] = q;
30
31
                                                                                                                                         50
32
                                                                                                                                         51
33
                  int clone = sz++;
                                                                                                                                         52
                  {\tt memcpy} \, (\, {\tt nxt} \, [\, {\tt clone} \, ]^{'} \, , \quad {\tt nxt} \, [\, {\tt q} \, ] \, \, , \quad {\tt sizeof} \, (\, {\tt nxt} \, [\, {\tt q} \, ] \, ) \, \, ;
                  len[clone] = len[p] + 1;
pos[clone] = pos[q];
36
                 | pos[q];
| link[clone] = link[q];
| link[q] = link[cur] = clone;
| for (; p != -1 && nxt[p][c] == q; p = link[p]) ← nxt[p][c] = clone;
37
                                                                                                                                         56
38
                                                                                                                                         57
                                                                                                                                         58
41
             int n;
42
             string s;
int l[MAXN], r[MAXN];
int e[MAXN][SIGMA];
                                                                                                                                         62
43
                                                                                                                                         63
44
                                                                                                                                         64
45
                                                                                                                                         65
             \begin{array}{ccc} \textbf{void} & \texttt{getSufTree} \left( \, \texttt{string \_s} \, \right) & \{ \\ & \texttt{memset} \left( \, \texttt{e} \, , \, \, -1 \, , \, \, \, \texttt{sizeof} \left( \, \texttt{e} \, \right) \, \right) \, ; \end{array}
                                                                                                                                         67
                                                                                                                                         68
49
                                                                                                                                         69
                  {\tt n} = {\tt s.length}();
                  {\tt reverse}\,(\,{\tt s.begin}\,(\,)\,\,,\,\,\,{\tt s.end}\,(\,)\,\,)\,\,;
                                                                                                                                         70
51
                                                                                                                                         71
                  for (int i = 0; i < n; i++) add(s[i] - 'a');
                  reverse(s.begin(), s.end());
                  for (int i = 1; i < sz; i++) {
   int j = link[i];
56
                     l[i] = n - pos[i] + len[j];
r[i] = n - pos[i] + len[i];
e[j][s[l[i]] - 'a'] = i;
57
                                                                                                                                         76
60
                                                                                                                                         79
61
            }
                                                                                                                                         80
        }
                                                                                                                                         81
                                                                                                                                         82
```

### musthave/generalMatching.cpp

```
//COPYPASTED FROM E-MAXX
namespace GeneralMatching {
    const int MAXN = 256;
    int n;
    vector < int > g [MAXN];
    int match [MAXN], p [MAXN], base [MAXN], q [MAXN];
```

```
bool used [MAXN], blossom [MAXN];
for (;;) {
    a = base[a];
    used[a] = true;
    if (match[a] == -1) break;
        a = p[match[a]];
    for (;;) {
       b = base[b];
if (used[b]) return b;
        b = p[match[b]];
blossom [base [v]] = blossom [base [match [v]]] = \leftarrow
        p[v] = children;
         \begin{array}{ll} \textbf{children} &=& \mathtt{match} \, [\, \mathtt{v} \, ] \, ; \\  \, \mathtt{v} &=& \mathtt{p} \, [\, \mathtt{match} \, [\, \mathtt{v} \, ] \, ] \, ; \\  \, \end{array} 
\mathtt{used}\,[\,\mathtt{root}\,] \ = \ t\,\mathtt{r}\,\mathtt{u}\,\mathtt{e}\;;
    int qh=0, qt=0;
q[qt++] = root;
while (qh < qt) {
        int \quad v = q[qh++];
         for (size_t i=0; i<g[v].size(); ++i) {
            \begin{array}{lll} & \text{int to} = g[v][i]; \\ & \text{if (base}[v] == base[to] \mid\mid match[v] == to) \end{array} \longleftrightarrow
            continue; if (to == root || (match[to] != -1 && p[\leftrightarrow match[to]] != -1)) { int curbase = lca (v, to); memset (blossom, 0, Sizeof blossom);
                mark_path (v, curbase, to);
mark_path (to, curbase, v);
for (int i=0; i<n; ++i)
   if (blossom[base[i]]) {</pre>
                         base[i] = curbase;
                        if (!used[i]) {
  used[i] = true;
                            q[qt++] = i;
                   }
             else if (p[to] == -1) {
                p[to] =
                 if (match[to] == -1)
                   return to;
                \mathtt{to} \; = \; \mathtt{match} \, [\, \mathtt{to} \, ] \, ;
                used [to] = true;
                q[qt++] = to;
       }
    return -1;
\begin{array}{lll} {\tt vector}\!<\!{\tt pair}\!<\!{\tt int}\;,\;\; {\tt int}\!>\;>\; {\tt solve}\,(\;{\tt int}\;\;\_{\tt n}\;,\;\; {\tt vector}\!<\!{\tt pair}\!<\!\!\leftarrow\!\!\rightarrow\; {\tt int}\;,\;\; {\tt int}\!>\;>\; {\tt edges}\,)\;\;\{ \end{array}
    n = _n;
for (int i = 0; i < n; i++) g[i].clear();
for (auto o : edges) {</pre>
        g[o.first].push_back(o.second);
g[o.second].push_back(o.first);
    fmemset (match, -1, sizeof match);
for (int i=0; i<n; ++i) {
   if (match[i] == -1) {
     int v = find_path (i);
}</pre>
            while (v != -1) {
  int pv = p[v], ppv = match[pv];
  match[v] = pv, match[pv] = v;
                v = ppv;
   }
    \verb"vector<|pair<|int|, |int>> |ans|;
    for (int i = 0; i < n; i++) {
  if (match[i] > i) {
            ans.push_back(make_pair(i, match[i]));
```

88

#### useful/dinica.cpp

namespace flow

```
const int maxn = 1e5 + 10;
        const int maxe = 2 * maxn;
 6
        int head [maxn], next [maxe], to [maxe], f [maxe], ec \leftarrow
        int ST', EN, N = maxn;
        inline void setN(int n)
        {
          ST = n;
11
          EN = n + 1;

N = n + 2;
12
13
14
        inline void _add(int x, int y, int ff)
17
          ++ec:
18
          to [ec] = y;
next [ec] = head [x];
head [x] = ec;
19
20
          f[ec] = ff;
^{22}
23
24
25
        inline int add(int x, int y, int ff)
26
          29
30
31
        void clear()
32
34
          forn(i, N) head[i] = 0;
35
          \verb"ec"=1;
36
37
        int d[maxn];
38
39
        int q [maxn], st = 0, en = 0;
40
41
42
          43
          st = 0, en = 0;
d[ST] = 0;
44
45
           q[en++] = ST;
46
47
           while (st < en)
49
              int x = q[st++];
             if (x == EN) return 1;
for (int e = head[x]; e; e = next[e])
50
51
                int y = to[e];
                if (d[y] == 1e9 && f[e])
55
                   {\tt d} \, [\, {\tt y} \, ] \ = \, {\tt d} \, [\, {\tt x} \, ] \ + \ 1 \, ;
56
                   q [en++] = y;
57
                }
             }
60
61
           return 0;
62
63
64
        int pushed;
        int fst[maxn];
67
        int dfs(int x, int flow = 1e9)
68
           69
70
71
             pushed = flow;
             return 1;
73
74
           \begin{array}{lll} \textbf{for} & (\;;\;\; \textbf{fst}\,[\,\textbf{x}\,]\;;\;\; \textbf{fst}\,[\,\textbf{x}\,] \;=\; \textbf{next}\,[\,\textbf{fst}\,[\,\textbf{x}\,]\,]\,) \end{array}
75
76
             int e = fst[x];
             int y = to [e];
```

```
if (d[y] == d[x] + 1 \&\& f[e] \&\& dfs(y, min(f[e \leftarrow
             ], flow)))
79
                  f[e] -= pushed;
f[e^1] += pushed;
return 1;
80
81
               }
85
             return 0;
86
87
88
          ll calcFlow()
90
91
            11 res = 0;
92
             {\color{red}\mathbf{w}\,h\,il\,e}\quad (\,{\color{bfs}\,\mathsf{bfs}\,(\,)\,}\,)
93
                {\tt forn}\,({\tt i}\,,\ {\tt N}\,)\ {\tt fst}\,[{\tt i}\,]\ =\ {\tt head}\,[{\tt i}\,]\,;
94
                while (dfs(ST))
97
                   \mathtt{res} \ + = \ \mathtt{pushed} \ ;
                }
98
99
100
             return res;
101
102
103
           / HOW TO USE ::
             104
105
              -- run calcFlow
106
107
```

#### useful/max-flow-min-cost.cpp

```
namespace flow
 3
         const int maxn = 2e5 + 10;
         const int maxe = 2 * maxn;
 6
         cost[maxe], ec = 1;

int ST, EN, N = maxn;
         inline void setN(int n)
10
           ST = n;
11
           EN = n + 1;

N = n + 2;
12
13
14
16
         inline\ void\ \_add(int\ x\ ,\ int\ y\ ,\ int\ f\ ,\ int\ c)
17
18
           tro[cc] = y;
next[ec] = head[x];
head[x] = ec;
flow[ec] = f;
cost[ec] = c;
19
20
21
^{23}
24
25
26
         in \, line \ int \ add \, (int \ x \, , \ int \ y \, , \ int \ f \, , \ int \ c \, )
28
            _{add}(x, y, f, c);
            -add(y, x, 0, -c);

-eturn ec - 1;
29
30
31
32
33
         void clear()
35
           {\tt forn}\,(\,{\tt i}\,,\ \,{\tt N}\,)\ \ {\tt head}\,[\,{\tt i}\,]\ =\ 0\,;
36
37
38
         {\tt ll} \ {\tt d[maxn]} \ , \ {\tt p[maxn]} \ ;
39
40
         int last [maxn];
         int used [maxn];
42
43
         \mathtt{pair} < \mathtt{ll} \;, \;\; \mathtt{ll} > \; \mathtt{\_calc} \, (\, \mathtt{int} \;\; \mathtt{flag} \,)
44
            const 11 INF = 1e12;
45
           forn(i, N) p[i] = INF;
p[ST] = 0;
            forn(\_, N) forn(x, N) for (int e = head[x]; e; e \leftarrow
48
             = next[e]) if (flow[e] > 0)
49
              50
               if (p[y] > p[x] + cost[e])
```

```
53
                      p[y] = p[x] + cost[e];
 54
 55
                                                                                                              11
 56
                                                                                                              12
 57
                11 \text{ resFlow} = 0, \text{ resCost} = 0;
                while (1)
 59
 60
                   forn(i, N) d[i] = INF, used[i] = 0;
 61
                   \mathtt{d} \, [\, \mathtt{ST} \, ] \,\, = \,\, 0 \, ;
                                                                                                              17
 62
                   forn(_, N)
                                                                                                              18
 63
                       \begin{array}{lll} & int & x = -1; \\ & forn(i, N) & if & (!used[i] & \& & (x == -1 \ || \ d[x] & \hookleftarrow \end{array}
 65
                   d[i])) x = i;
 66
                       used[x] = 1;
                                                                                                              23
                       if (d[x] = INF) break;
                                                                                                              24
 67
                       for (int e = head[x]; e; e = next[e]) if (\leftarrow)
 68
                                                                                                              25
                \texttt{flow} \; [\; \texttt{e} \;] \; \stackrel{\cdot}{>} \; 0 \,)
                                                                                                              26
  70
                          int y = to[e];
                                                                                                              28
                          11 len = cost[e] + p[x] - p[y];
if (d[y] > d[x] + len)
  71
                                                                                                              29
  72
                                                                                                              30
 73
                                                                                                              31
  74
                              d[y] = d[x] + len;
                              last[y] = e;
                                                                                                              33
  76
  77
                      }
                                                                                                              35
 78
                   }
 79
                                                                                                              37
                   if (d[EN] = INF) break;
 80
                                                                                                              38
                   \begin{array}{lll} \textbf{11} & \texttt{realCost} &= \texttt{d} \left[\, \texttt{EN} \,\right] \, + \, \texttt{p} \left[\, \texttt{EN} \,\right] \, - \, \texttt{p} \left[\, \texttt{ST} \,\right] \,; \\ \textbf{if} & (\, \texttt{flag} \, \, \&\& \, \, \texttt{realCost} \, > \, 0 \,) \, \, \, \, \texttt{break} \,; \end{array}
                                                                                                              40
 83
                                                                                                              41
 84
                                                                                                              42
                   \begin{array}{lll} & \verb"int" & \verb"pushed" = \verb"inf";\\ & \verb"int" & \verb"x" = EN"; \end{array}
 85
 86
                                                                                                              44
                    while (x != ST)
                                                                                                              45
 89
                       int e = last[x];
                                                                                                              47
                       pushed = min(pushed, flow[e]);
x = to[e ^ 1];
 90
                                                                                                              48
 91
                                                                                                              49
 92
                                                                                                              50
 94
                   {\tt resCost} \ +\!\!\!= \ {\tt realCost} \ * \ {\tt pushed} \ ;
 95
                   resFlow += pushed;
 96
                                                                                                              54
                   x = EN:
 97
                                                                                                              55
                    while (x != ST)
 98
                                                                                                              56
                                                                                                              57
                       int e = last[x];
                      flow[e] -= pushed;
flow[e ^ 1] += pushed;
x = to[e ^ 1];
1.01
                                                                                                              59
102
103
                                                                                                              61
104
                                                                                                              62
105
                                                                                                              63
                   forn(i, N) p[i] += d[i];
                                                                                                              64
107
108
                return mp(resFlow , resCost);
                                                                                                              66
109
                                                                                                              67
110
                                                                                                              68
            \verb"pair"<|11|, | |11>| | | |maxFlow|()|
                                                                                                              69
111
                                                                                                              71
113
                return _calc(0);
114
115
            \verb"pair<11", 11> \min \texttt{Cost}()
116
                                                                                                              74
117
118
               return \_calc(1);
119
120
121
              / HOW TO USE::
122
                -- add adges using add(x, y, f, c), call set N(n \leftarrow
123
                      run maxFlow/minCost, returns pair(flow, cost←
                                                                                                              85
```

# useful/poly.cpp

```
1 struct poly
2 {
3     vi v;
4     poly() {}
5     poly(vi vv)
6     v = vv;
90
7
```

```
}
int size()
 9
10
                    return (int)v.size();
13
               \verb"poly cut" (int maxLen")
                    if (maxLen < sz(v)) v.resize(maxLen);
16
                    return *this;
               {\tt poly norm} \; (\;)
19
                     while (sz(v) > 1 \&\& v.back() == 0) v.pop_back();
               inline int& operator [] (int i)
                    return v[i];
                void out(string name="")
                    stringstream ss;
                    \begin{array}{lll} \textbf{if} & (\, \texttt{sz} \, (\, \texttt{name} \, ) \,) & \texttt{ss} & << \, \texttt{name} & << \, "=" \,; \end{array}
                             fst = 1;
                    \mathtt{forn}\,(\,\mathtt{i}\,,\,\,\mathtt{sz}\,(\,\overset{\,\,{}_{\phantom{1}}}{\mathtt{v}}\,)\,)\quad \, \overset{\,\,{}_{\phantom{1}}}{\mathtt{i}}\,\mathbf{f}\quad(\,\mathtt{v}\,[\,\mathtt{i}\,]\,)
                         int sgn =
                         36
                         else if (!fst) ss << "+";
                         fst = 0;
                         if (!i || x != 1)
                              if (i > 0) ss << "*x"; if (i > 1) ss << "^* < i;
43
                         {
                              ss << "x";
                             if (i > 1) ss << i''
                     \inf (fst) ss << 0;
53
                    string s;
                    eprintf("%s \n", s.data());
          };
          poly operator + (poly A, poly B)
60
               \ddot{\mathbf{C}}.\ddot{\mathbf{v}} = \ddot{\mathbf{v}}\dot{\mathbf{i}}(\mathbf{max}(\mathbf{sz}(\mathbf{A}), \mathbf{sz}(\mathbf{B})));
               forn (i, sz(C))
                    \begin{array}{lll} if & (\ i \ < \ sz \, (\ A) \, ) & C \, [\ i \, ] \ = \ (\ C \, [\ i \, ] \ + \ A \, [\ i \, ] \, ) & \% & \ mod \ ; \\ if & (\ i \ < \ sz \, (\ B) \, ) & C \, [\ i \, ] \ = \ (\ C \, [\ i \, ] \ + \ B \, [\ i \, ] \, ) & \% & \ mod \ ; \end{array}
               return C.norm();
          poly operator - (poly A, poly B)
72
73
               \ddot{\mathbf{C}}.\ddot{\mathbf{v}} = \ddot{\mathbf{v}}\dot{\mathbf{i}}(\mathbf{max}(\mathbf{sz}(\mathbf{A}), \mathbf{sz}(\mathbf{B})));
              forn (i, sz(C))
                   \begin{array}{lll} if & (i \, < \, sz\,(A)\,) & C\,[\,i\,] \, = \, (\,C\,[\,i\,] \, + \, A\,[\,i\,]\,) \,\,\,\% \,\,\, mod\,; \\ if & (i \, < \, sz\,(B)\,) & C\,[\,i\,] \, = \, (\,C\,[\,i\,] \, + \, mod\, - \, B\,[\,i\,]\,) \,\,\,\% \,\,\, mod\,; \end{array}
80
               return C.norm();
          poly operator * (poly A, poly B)
              \begin{array}{l} {\tt poly} \  \  \, {\tt C} \, ; \\ {\tt C.v} \  \, = \  \, {\tt vi} \, (\, {\tt sz} \, (\, {\tt A}) \  \, + \  \, {\tt sz} \, (\, {\tt B} \, ) \  \, - \  \, 1) \, \, ; \end{array}
86
87
88
              \begin{array}{lll} \texttt{forn}\,(\,\mathtt{i}\,\,,\,\,\, \mathtt{sz}\,(\,\mathtt{A}\,)\,) & \texttt{fft}\,::\,\mathtt{A}\,[\,\mathtt{i}\,] \,\,=\,\, \mathtt{A}\,[\,\mathtt{i}\,]\,;\\ \texttt{forn}\,(\,\mathtt{i}\,\,,\,\,\,\, \mathtt{sz}\,(\,\mathtt{B}\,)\,) & \texttt{fft}\,::\,\mathtt{B}\,[\,\mathtt{i}\,] \,\,=\,\, \mathtt{B}\,[\,\mathtt{i}\,]\,; \end{array}
              fft::multMod(sz(A), sz(B), mod);
forn(i, sz(C)) C[i] = fft::C[i];
90
91
               \textcolor{return}{\texttt{return}} \hspace{0.1cm} \texttt{C.norm}\hspace{0.1cm} (\hspace{0.1cm}) \hspace{0.1cm} ;
92
93
          \verb"poly inv"(\verb"poly A", int n") // returns A^-1 mod x^n
               {\tt assert} \, (\, {\tt sz} \, (\, {\tt A}\, ) \, \, \, \&\& \, \, \, {\tt A} \, [\, 0\, ] \  \, != \, \, 0\, ) \; ;
              A.cut(n);
              auto cutPoly = [](poly &from, int 1, int r)
```

```
namespace retro
102
                     poly R;
103
                     R.v.resize(r-1);
                                                                                                                                                                   const int N = 4e5 + 10;
104
                     for (int i = 1; i < r; ++i)
                                                                                                                                                       4
105
                                                                                                                                                                    vi v[N]
106
                          if (i < sz(from)) R[i - 1] = from[i];
                                                                                                                                                                   vi vrev[N];
                                                                                                                                                                    void add(int x, int y)
109
                };
110
                                                                                                                                                                       v [x].pb(y);
                \mathtt{function} \hspace{0.1em} < \hspace{0.1em} \mathtt{int} \hspace{0.1em} (\hspace{0.1em} \mathtt{int} \hspace{0.1em}, \hspace{0.1em} \mathtt{int} \hspace{0.1em}) \hspace{0.1em} > \hspace{0.1em} \mathtt{rev} \hspace{0.1em} = \hspace{0.1em} [\hspace{0.1em} \&\hspace{0.1em} \mathtt{rev} \hspace{0.1em}] \hspace{0.1em} (\hspace{0.1em} \mathtt{int} \hspace{0.1em} \hspace{0.1em} \mathtt{x} \hspace{0.1em}, \hspace{0.1em} \hspace{0.1em} \mathtt{int} \hspace{0.1em} \hspace{0.1em} \mathtt{m} \hspace{0.1em}) \hspace{0.1em} \leftarrow \hspace{0.1em}
                                                                                                                                                     1.0
111
                                                                                                                                                                        vrev[y].pb(x);
                                                                                                                                                     12
                     113
                                                                                                                                                                    const int UD = 0;
114
                                                                                                                                                                    const int WIN = 1;
                                                                                                                                                     1.5
115
                                                                                                                                                     16
                                                                                                                                                                    const int LOSE = 2;
116
                \begin{array}{lll} {\tt poly} & {\tt R} \, (\, \{\, {\tt rev} \, (\, {\tt A} \, [\, 0\, ]\,\, , \,\, \, {\tt mod} \, )\, \}\, )\, ; \\ {\tt for} & (\, {\tt int} \,\, k \, = \, 1\, ; \,\, k \, < \, n\, ; \,\, k \, < < = \, 1\, ) \end{array}
                                                                                                                                                     17
117
                                                                                                                                                                    int res[N]
118
                                                                                                                                                                    int moves [N];
119
                                                                                                                                                                    int deg[N];
120
                     {\tt poly} \  \  {\tt AO} \ = \ {\tt cutPoly} \, (\, {\tt A} \, , \  \  \, 0 \, , \  \, k \, ) \; ;
                     poly A1 = cutPoly(A, k, 2 * k);

poly H = A0 * R;

H = cutPoly(H, k, 2 * k);

poly R1 = (((A1 * R).cut(k) + H) * (poly({0}) - ←)
                                                                                                                                                     21
                                                                                                                                                                    int q[N], st, en;
121
                                                                                                                                                     22
122
                                                                                                                                                                    void calc(int n)
                                                                                                                                                     23
123
124
                                                                                                                                                                       \begin{array}{lll} {\tt forn}\,(\,{\tt i}\,,\  \, {\tt n}\,) & {\tt deg}\,[\,{\tt i}\,] \ = \ {\tt sz}\,(\,{\tt v}\,[\,{\tt i}\,]\,) \ ; \\ {\tt st} \ = \ {\tt en} \ = \ 0 \ ; \end{array}
                     R.v.resize(2 * k);
                                                                                                                                                                         forn(i, n) if (!deg[i])
126
                     forn(i, k) R[i + k] = R1[i];
127
                                                                                                                                                                             \begin{array}{l} {\tt q\,[\,e\,n++]\,=\,i\;;} \\ {\tt r\,e\,s\,[\,i\,]\,=\,L\,0\,S\,E\;;} \end{array}
                                                                                                                                                     29
128
                 return R.cut(n).norm():
                                                                                                                                                     30
129
           }
                                                                                                                                                     31
                                                                                                                                                                         while (st < en)
131
           {\tt pair}\!<\!{\tt poly}\ , \ {\tt poly}\!>\ {\tt divide}\,(\,{\tt poly}\ A\,,\ {\tt poly}\ B\,)
                                                                                                                                                     33
132
                                                                                                                                                     34
                                                                                                                                                                              int x = q[st++];
                133
                                                                                                                                                     35
                                                                                                                                                                              for (int y : vrev[x])
134
                                                                                                                                                                              \{ \quad \text{if } (\texttt{res}[\texttt{y}] == \texttt{UD} \&\& (\texttt{res}[\texttt{x}] == \texttt{LOSE} \mid\mid (--\leftrightarrow \texttt{vis}[\texttt{y}]) \} \} 
                                                                                                                                                     36
135
                auto rev = [](poly f)
                                                                                                                                                                         deg[y] \stackrel{\cdot}{=} 0 \stackrel{\cdot}{\&} \stackrel{\cdot}{\&} res[x] \stackrel{\cdot}{=} WIN \stackrel{\cdot}{)})
                   reverse(all(f.v));
137
138
                                                                                                                                                                                       \begin{array}{lll} {\tt res} \, [\, {\tt y}\, ] & = \, 3 \, \, - \, {\tt res} \, [\, {\tt x}\, ] \, ; \\ {\tt moves} \, [\, {\tt y}\, ] & = \, {\tt moves} \, [\, {\tt x}\, ] \, \, + \, \, 1 \, ; \\ {\tt q} \, [\, {\tt en} \, + \, + ] & = \, {\tt y} \, ; \end{array}
                                                                                                                                                     39
139
                                                                                                                                                     40
140
                41
141
                                                                                                                                                     42
142
                                                                                                                                                     44
143
                                                                                                                                                     45
                                                                                                                                                                  }
144
                \textcolor{return}{\texttt{return}} \hspace{0.1cm} \left\{ \hspace{0.1cm} \texttt{q} \hspace{0.1cm}, \hspace{0.1cm} \texttt{r} \hspace{0.1cm} \right\};
                                                                                                                                                     46
145
```

### useful/primes.cpp

```
namespace math
        const int maxP = 1e6;
 3
        void gen_primes()
           10
11
13
              if (pp[i] == i) p[pc++] = i;
            15
16
        bool is_prime(int x)
17
           \begin{array}{lll} if & (x < maxP) & return & pp \, [\, x\,] \, == \, x \, ; \\ for & (int \ i \, = \, 0; \ p \, [\, i\,] \, * \, p \, [\, i\,] \, \leqslant= \, x \, ; \, +\!\!\! +\!\! i \, ) & if & (x \, \% \, p \! \hookleftarrow \! \\ [\, i\,] & == \, 0) & return & false \, ; \\ return & true \, ; \end{array}
19
20
21
23
        /// pp[x] <— smallest prime divisor {x} (or -1 for \leftarrow {x < 2})
25
           p[0 ... pc - 1] \leftarrow list of primes < maxP
```

#### retro