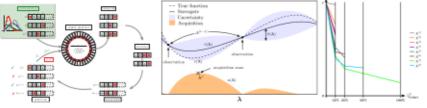
### **HPO - MANY APPROACHES**

- Evolutionary algorithms
- Bayesian / model-based optimization
- Multi-fidelity optimization, e.g. Hyperband



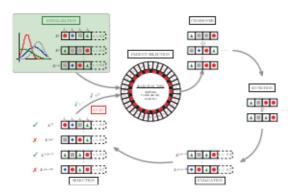
HPO methods can be characterized by:

- how the exploration vs. exploitation trade-off is handled
- how the inference vs. search trade-off is handled

Further aspects: Parallelizability, local vs. global behavior, handling of noisy observations, multifidelity and search space complexity.



# **EVOLUTIONARY STRATEGIES**



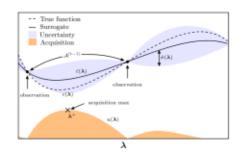


- Are a class of stochastic population-based optimization methods inspired by the concepts of biological evolution
- · Are applicable to HPO since they do not require gradients
- Mutation is the (randomized) change of one or a few HP values in a configuration.
- Crossover creates a new HPC by (randomly) mixing the values of two other configurations.

BO sequentially iterates:

- Approximate  $\lambda \mapsto c(\lambda)$  by (nonlin) regression model  $\hat{c}(\lambda)$ , from evaluated configurations (archive)
- Propose candidates via optimizing an acquisition function that is based on the surrogate ĉ(λ)
- Evaluate candidate(s) proposed in 2, then go to 1

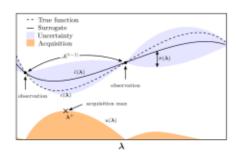
Important trade-off: **Exploration** (evaluate candidates in under-explored areas) vs. **exploitation** (search near promising areas)





### Surrogate Model:

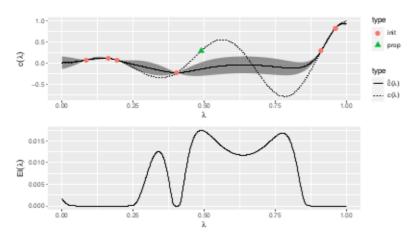
- Probabilistic modeling of C(λ) ~ (ĉ(λ), ô(λ)) with posterior mean ĉ(λ) and uncertainty ô(λ).
- Typical choices for numeric spaces are Gaussian Processes; random forests for mixed spaces





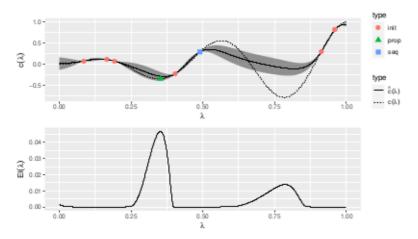
#### **Acquisition Function:**

- Balance exploration (high σ̂) vs. exploitation (low ĉ).
- Lower confidence bound (LCB):  $a(\lambda) = \hat{c}(\lambda) \kappa \cdot \hat{\sigma}(\lambda)$
- Expected improvement (EI):  $a(\lambda) = \mathbb{E}[\max\{c_{\min} C(\lambda), 0\}]$  where  $(c_{\min}$  is best cost value from archive)
- Optimizing a(λ) is still difficult, but cheap(er)



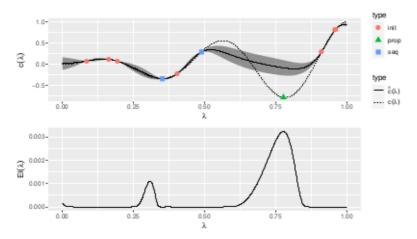


Upper plot: The surrogate model (black, solid) models the *unknown* relationship between input and output (black, dashed) based on the initial design (red points).



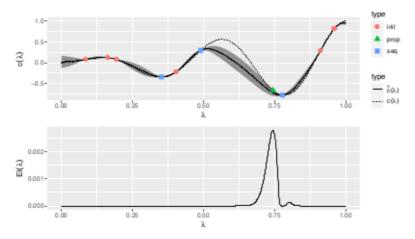


Upper plot: The surrogate model (black, solid) models the unknown relationship between input and output (black, dashed) based on the initial design (red points).





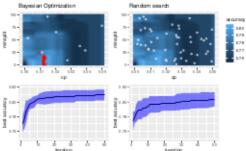
Upper plot: The surrogate model (black, solid) models the unknown relationship between input and output (black, dashed) based on the initial design (red points).

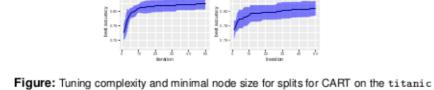


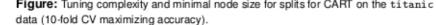


Upper plot: The surrogate model (black, solid) models the unknown relationship between input and output (black, dashed) based on the initial design (red points).

Since we use the sequentially updated surrogate model predictions of performance to propose new configurations, we are guided to "interesting" regions of  $\Lambda$  and avoid irrelevant evaluations:







Left panel: BO, 50 configurations; right panel: random search, 50 iterations.

Top panel: one run (initial design of BO is white); bottom panel: mean  $\pm$  std of 10 runs.



# BAYESIAN OPTIMIZATION 730 N

- Prerequiste: Fidelity HP  $\lambda_{\rm fid}$ , i.e., a component of  $\lambda$ , which influences the computational cost of the fitting procedure in a monotonically increasing manner
- Methods of multifidelity optimization in HPO are all tuning approaches that can efficiently handle a  $\mathcal I$  with a HP  $\lambda_{\rm fid}$
- The lower we set λ<sub>fid</sub>, the more points we can explore in our search space, albeit with much less reliable information w.r.t. their true performance.
- We assume to know box-constraints of  $\lambda_{\text{fid}}$ , so  $\lambda_{\text{fid}} \in [\lambda_{\text{fid}}^{\text{low}}, \lambda_{\text{fid}}^{\text{upp}}]$ , where the upper limit implies the highest fidelity returning values closest to the true objective value at the highest computational cost.



#### MULTIFIDELITY OPTIMIZATION

- Prerequiste: Fidelity HP λ<sub>fid</sub>, i.e., a component of λ, which
- Rinfluences the computational cost of the fitting procedure in a
- Idmonotonically increasing manner
  - Methods of multifidelity optimization in HPO are all tuning
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- Repeat until budget depleted or single HPC remains



### SUCCESSIVE HALVING ZATION - HYPERBAND

#### Problem with SH

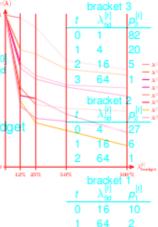
For  $\eta = 4$ 

Races down set lof IHPCs to the bestarly,

Idea: Discard bad configurations

### Soluëarly Hyperband

- Train HPCs with fraction of full budgets λ budget (SGD epochs, training set
- size); the control param for this is called multi-fidelity HP
- Each bracket consumes ca. the same but
- Continue with better  $1/\eta$  fraction of HPCs (w.r.t  $\widehat{\mathrm{GE}}$ ); with  $\eta$  times budget (usually  $\eta=2,3$ )
- Repeat until budget depleted or single HPC remains







#### MULTIFIDELITY OPTIMIZATION - HYPERBAND

Problem with SH techniques besides model-based or fiorwize two and the

Good HPCs could be killed off too early,

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# Solution: Hyperbandms / CMAES

- Repeat SH with different start budgets  $\lambda_{\rm int}^{[0]}$ and initial number of HPCs p[0]
- bracket 2 Each SH run is called bracket

r more information see *Hyperparameter Optimization<u>:</u> Foux ation is* Each bracket consumes ca. the same budget, Bischi 02021) 27

	bracket	1	
t	$\lambda_{\mathrm{fid}}^{[l]}$	$p_1^{[t]}$	
0	16	10	
4	0.4	_	

bracket 3

	bracket	0
t	$\lambda_{fid}^{[t]}$	$\rho_0^{[t]}$
0	64	5

