LEARNING AS PARAMETER OPTIMIZATION /2

The ERM optimization problem is:

$$\hat{oldsymbol{ heta}} = rg \min_{oldsymbol{ heta} \in \Theta} \mathcal{R}_{ extsf{emp}}(oldsymbol{ heta}).$$

For a (global) minimum $\hat{\theta}$ it obviously holds that

$$\forall \boldsymbol{\theta} \in \Theta: \quad \mathcal{R}_{\text{emp}}(\boldsymbol{\hat{\theta}}) \leq \mathcal{R}_{\text{emp}}(\boldsymbol{\theta}).$$

This does not imply that $\hat{\theta}$ is unique.

Which kind of numerical technique is reasonable for this problem strongly depends on model and parameter structure (continuous params? uni-modal $\mathcal{R}_{emp}(\theta)$?). Here, we will only discuss very simple scenarios.



GRADIENT DESCENT - LEARNING RATE

- The negative gradient is a direction that looks locally promising to reduce Remo.
- Hence it weights components higher in which Remp decreases more.
- However, the length of ²/_{θθ} R_{emp} measures only the local decrease rate, i.e., there are no guarantees that we will not go "too far".
- We use a learning rate α to scale the step length in each iteration. Too much can lead to overstepping and no converge, too low leads to slow convergence.
- Usually, a simple constant rate or rate-decrease mechanisms to enforce local convergence are used



