



# DATA-GENERATING PROCESS

- We assume the observed data  $\mathcal{D}$  to be generated by a process that can be characterized by some probability distribution

$$\mathbb{P}_{xy},$$

defined on  $\mathcal{X} \times \mathcal{Y}$ .

- We denote the random variables following this distribution by lowercase  $\mathbf{x}$  and  $y$ .
- It is important to understand that the true distribution is essentially **unknown** to us. In a certain sense, learning (part of) its structure is what ML is all about.





## DATA-GENERATING PROCESS / 3

## Remarks:

- With a slight abuse of notation we write random variables, e.g.,  $\mathbf{x}$  and  $y$ , in lowercase, as normal variables or function arguments. The context will make clear what is meant.
- Often, distributions are characterized by a parameter vector  $\theta \in \Theta$ . We then write  $p(\mathbf{x}, y \mid \theta)$ .
- This lecture mostly takes a frequentist perspective. Distribution parameters  $\theta$  appear behind the  $|$  for improved legibility, not to imply that we condition on them in a probabilistic Bayesian sense. So, strictly speaking,  $p(\mathbf{x}|\theta)$  should usually be understood to mean  $p_{\theta}(\mathbf{x})$  or  $p(\mathbf{x}, \theta)$  or  $p(\mathbf{x}; \theta)$ . On the other hand, this notation makes it very easy to switch to a Bayesian view.

