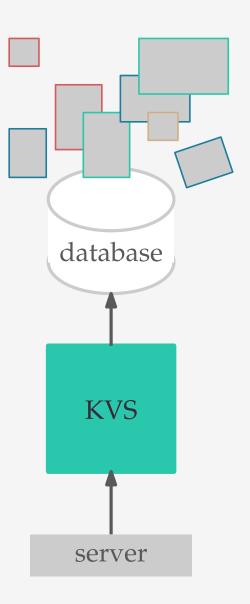
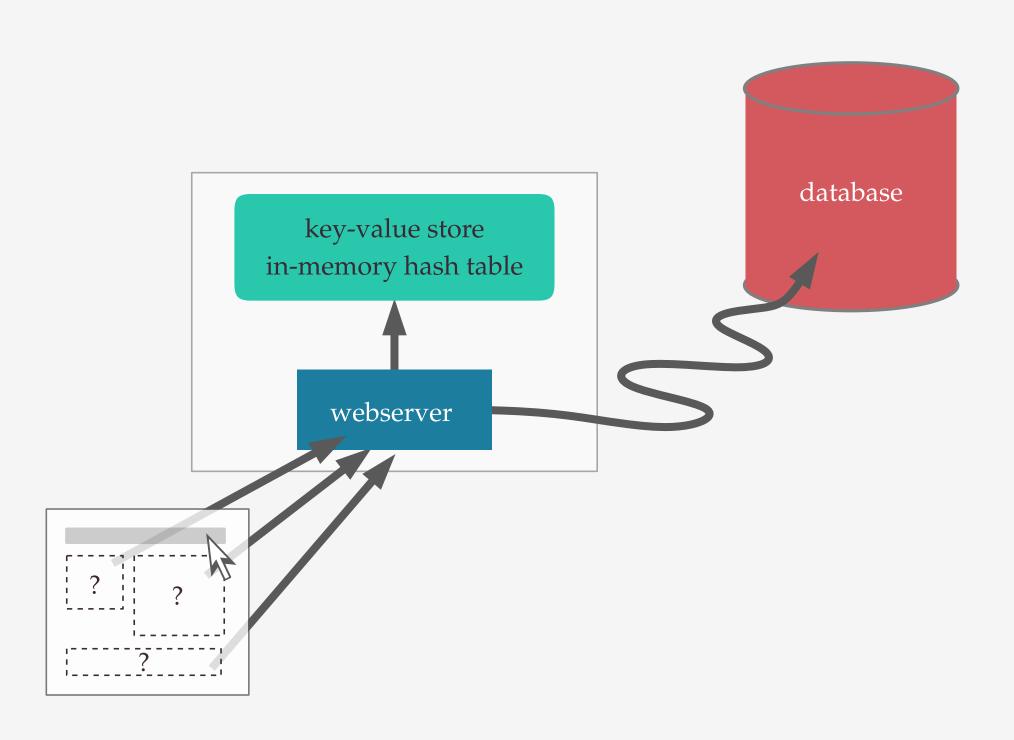
## CACHE OPTIMIZATION FOR THE MODERN WEB

Jenny Lam

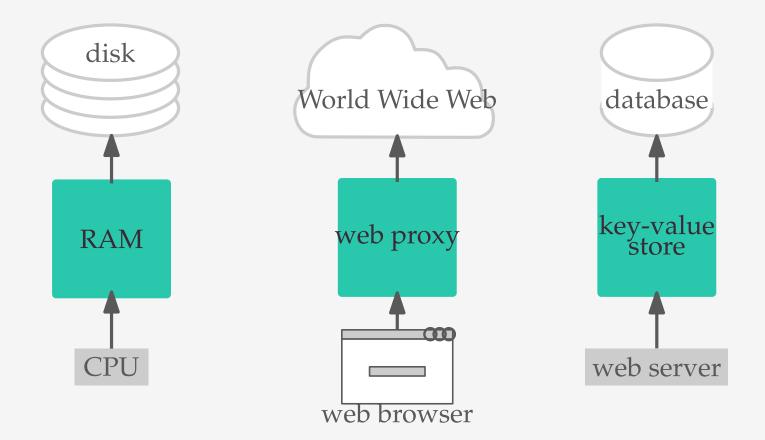
JOINT WORK WITH

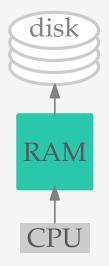
Shahram Ghandeharizadeh Sandy Irani Jason Yap

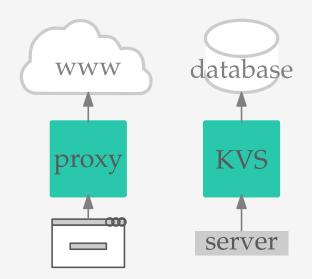




Scaling Memcache at Facebook, Nishtala et al., NSDI 2013.







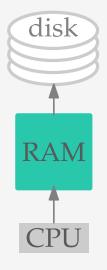


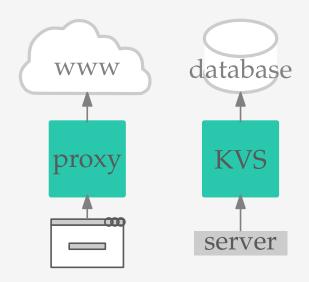
minimize number of cache misses



minimize

total cost of cache misses







minimize number of cache misses

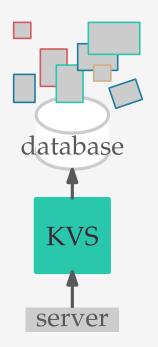
minimize
total cost of cache misses

**GENERALIZED** 

Least Recently Used (LRU)

GreedyDual-Size (GDS)

# EVICTION POLICY GDS → CAMP



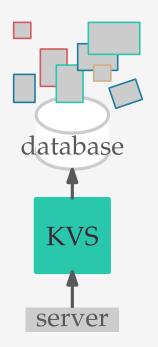
#### PLACEMENT POLICY

generalized managed memory caching caching

### MEMORY HIERARCHY

2-level cache — multi-level cache

EVICTION POLICY
GDS → CAMP



#### PLACEMENT POLICY

generalized managed memory caching caching

### MEMORY HIERARCHY

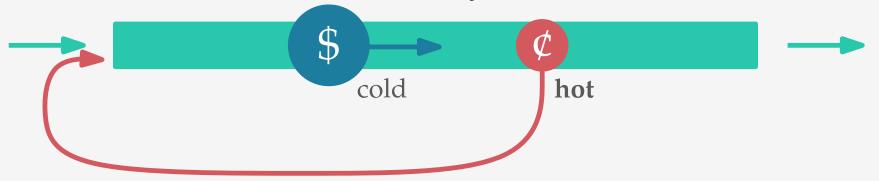
2-level cache — multi-level cache

## Least Recently Used

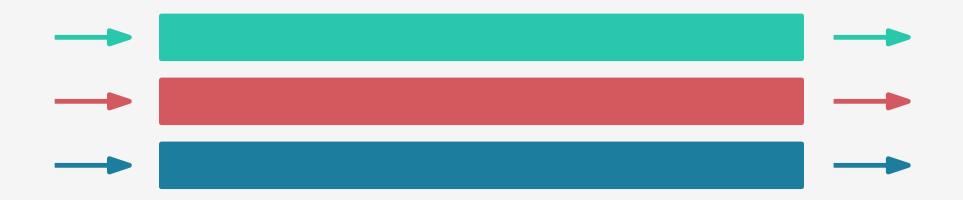




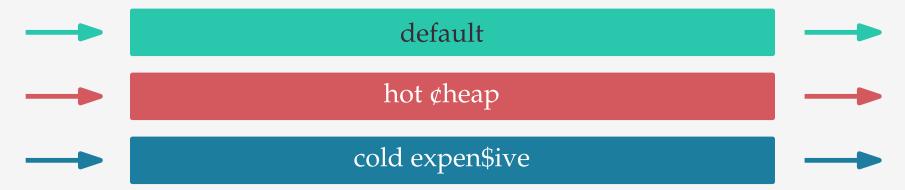
## Least Recently Used





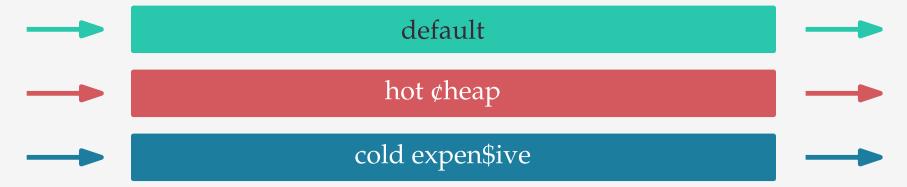


## pooled Least Recently Used



Scaling Memcache at Facebook, Nishtala et al., NSDI 2013.

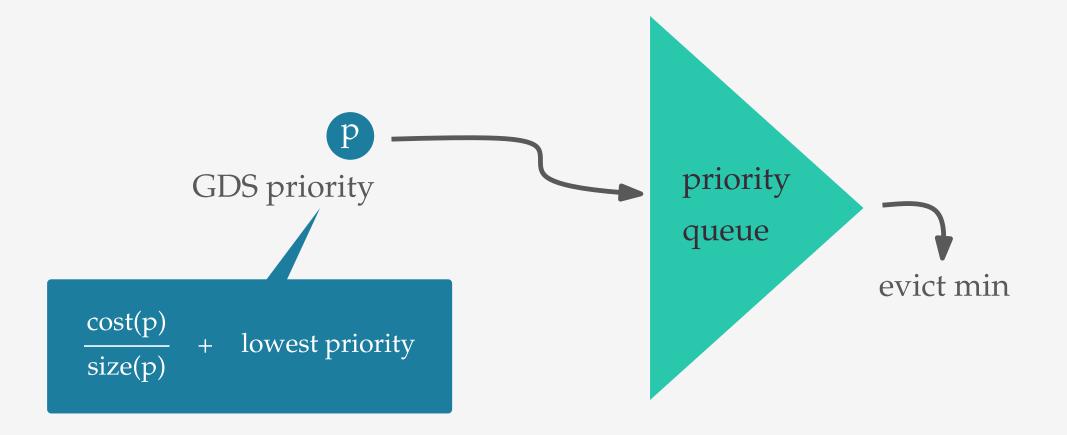
## pooled Least Recently Used



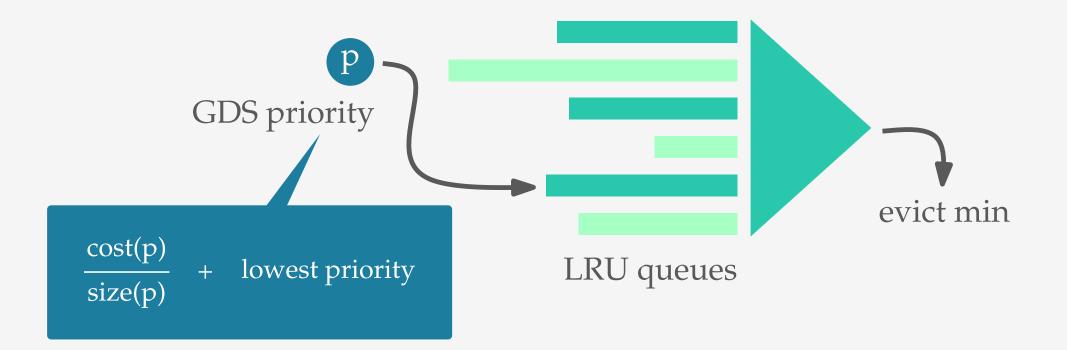
Scaling Memcache at Facebook, Nishtala et al., NSDI 2013.

need to take **recomputation cost** into consideration

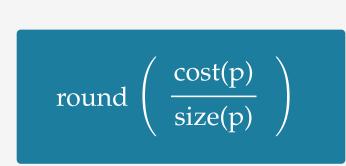






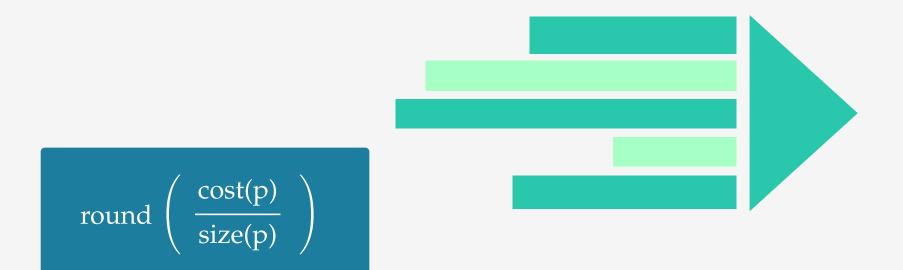




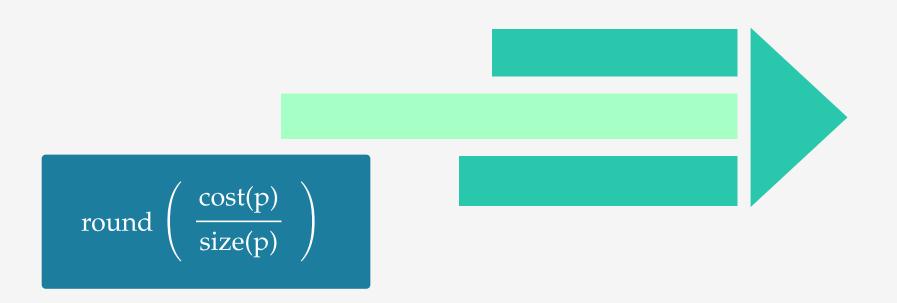




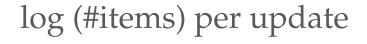






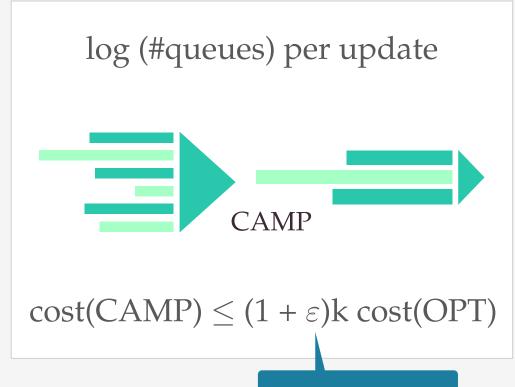




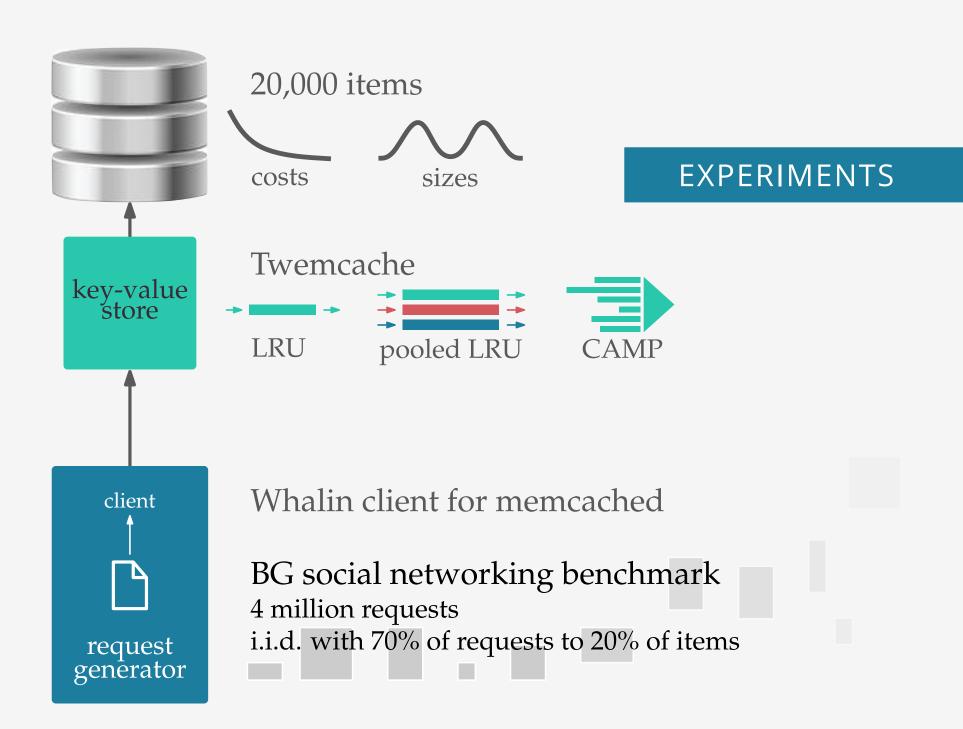


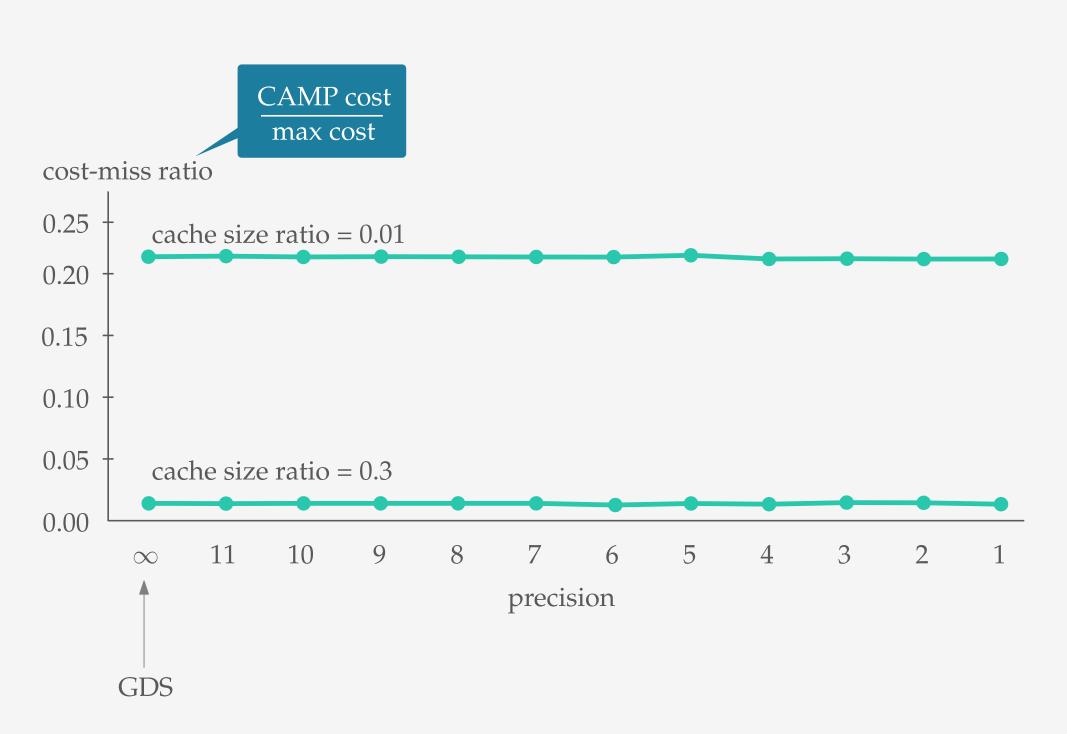


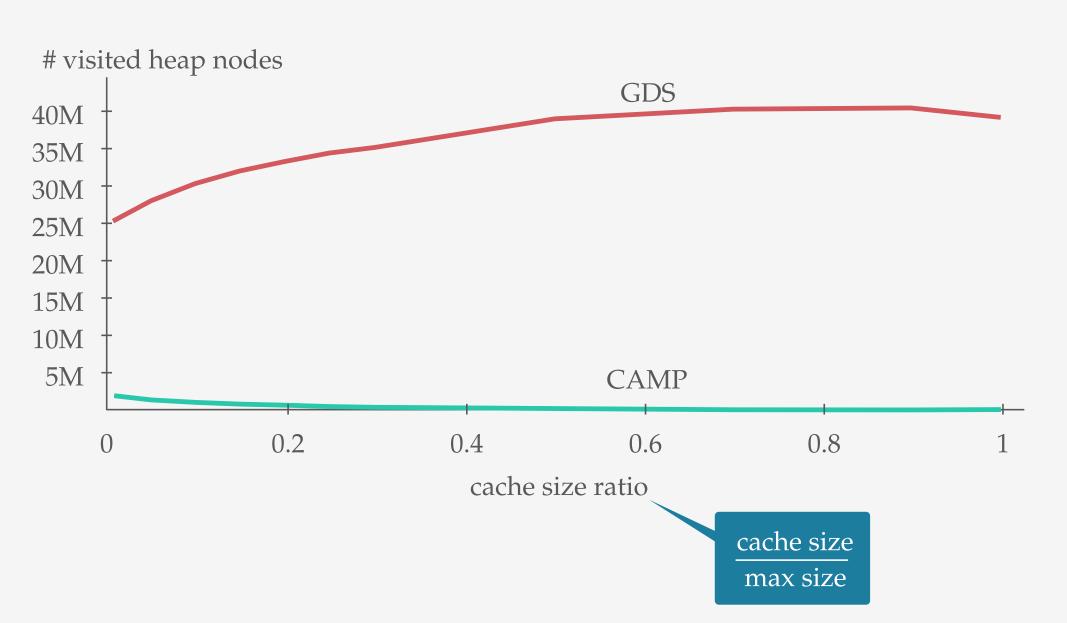
 $cost(GDS) \le k cost(OPT)$ 

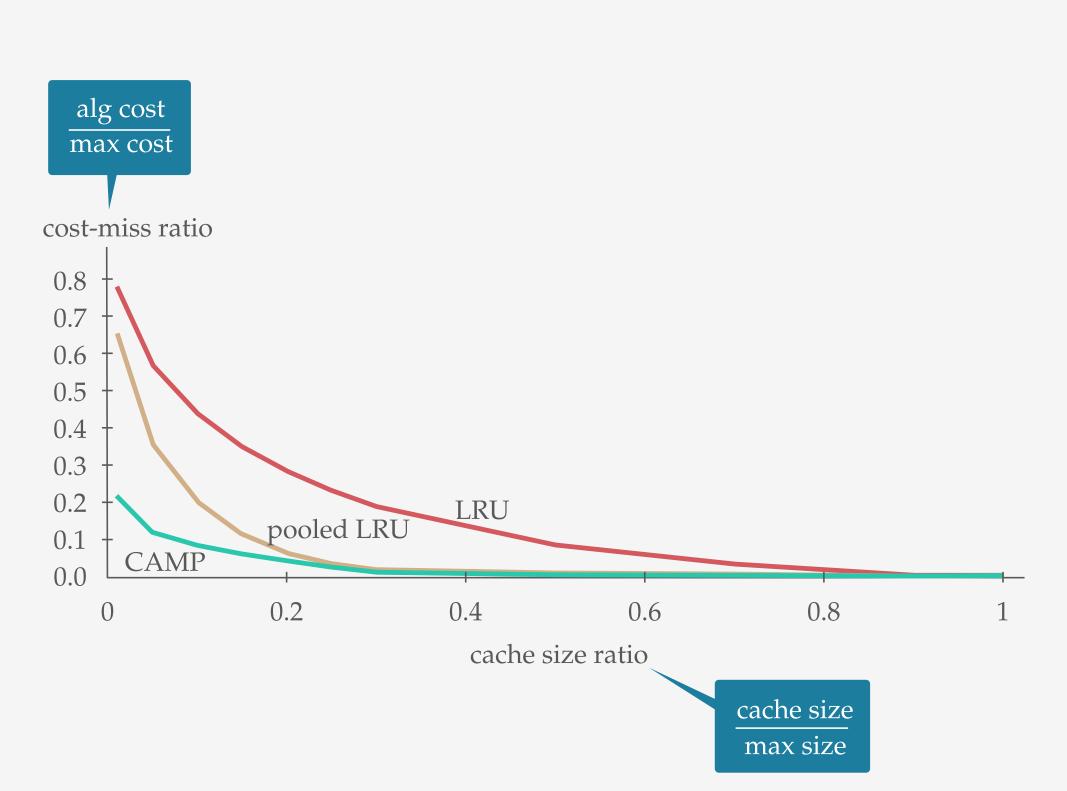


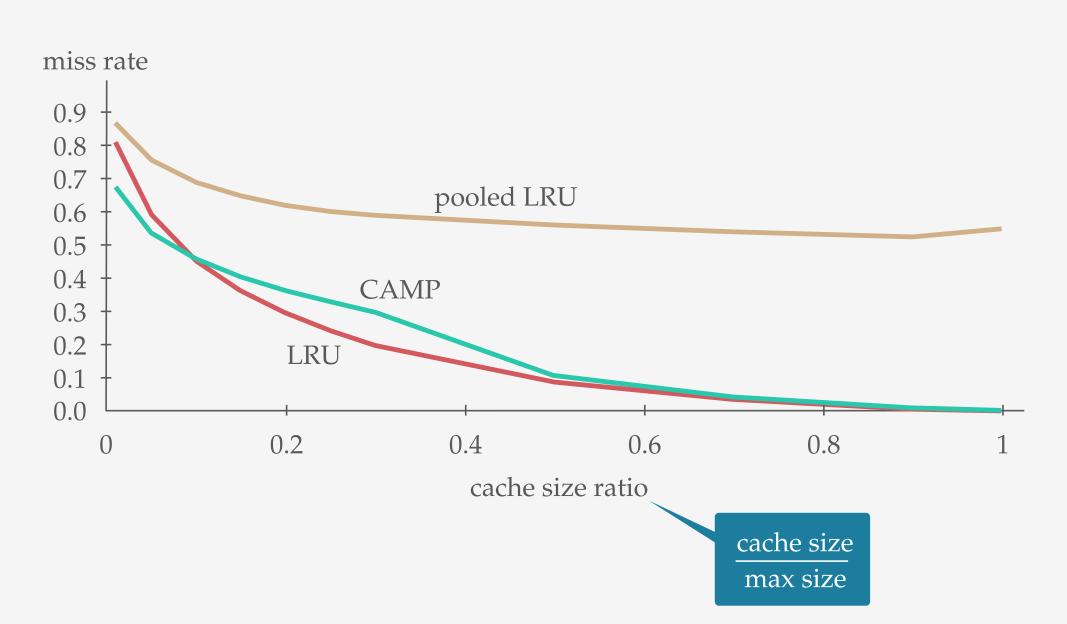
approximation parameter



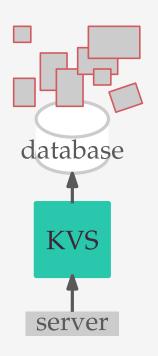








## EVICTION POLICY GDS → CAMP



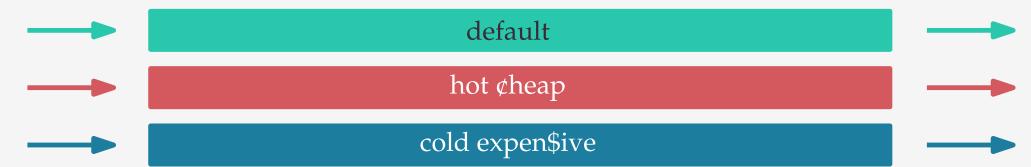
#### PLACEMENT POLICY

generalized managed memory caching caching

### MEMORY HIERARCHY

2-level cache — multi-level cache

## pooled Least Recently Used

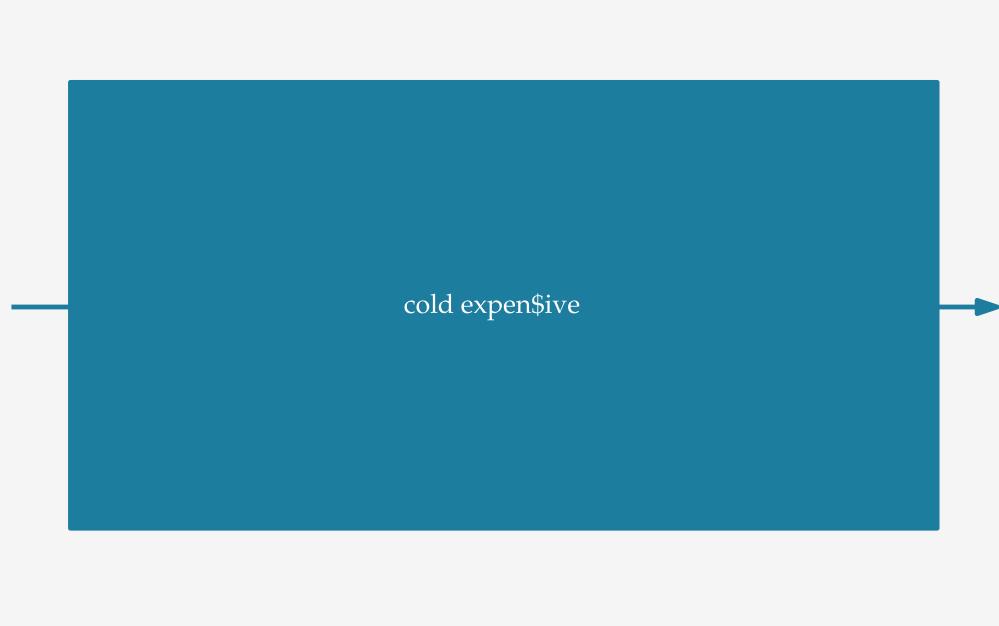


Scaling Memcache at Facebook, Nishtala et al., NSDI 2013.

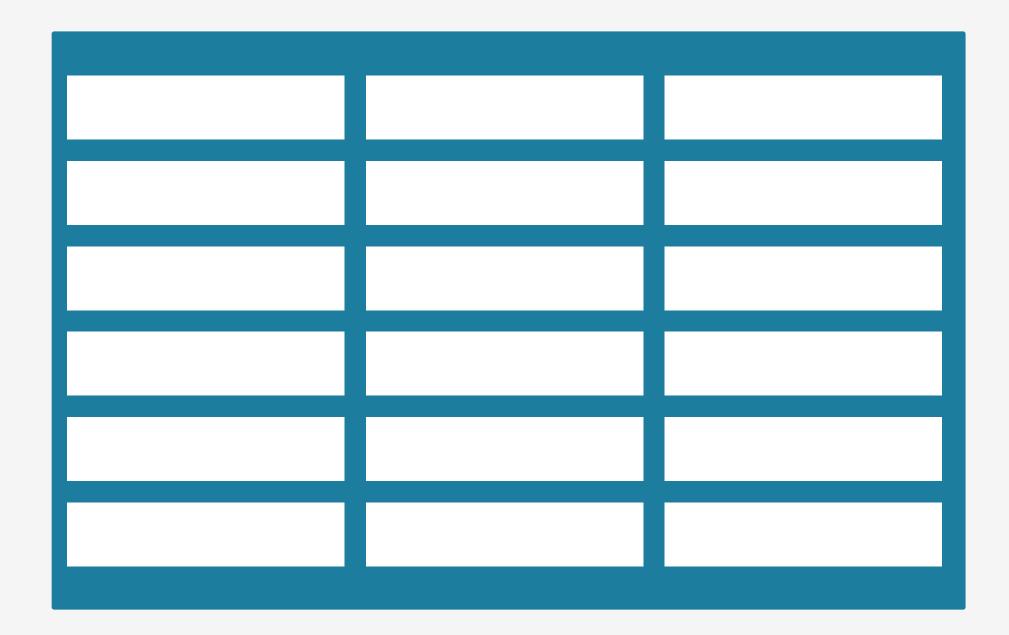


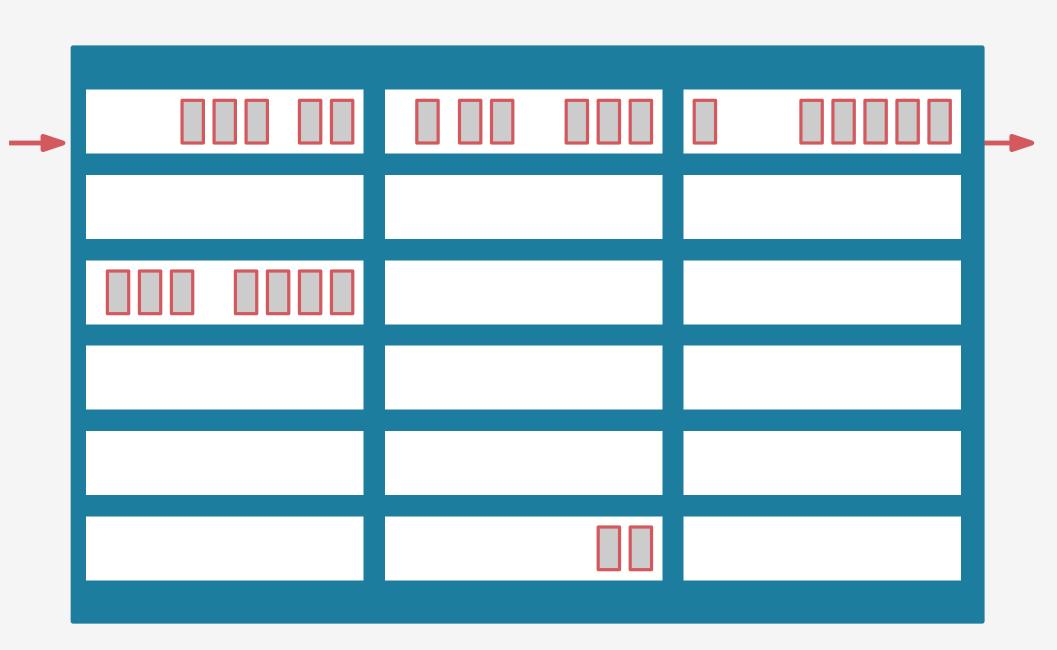


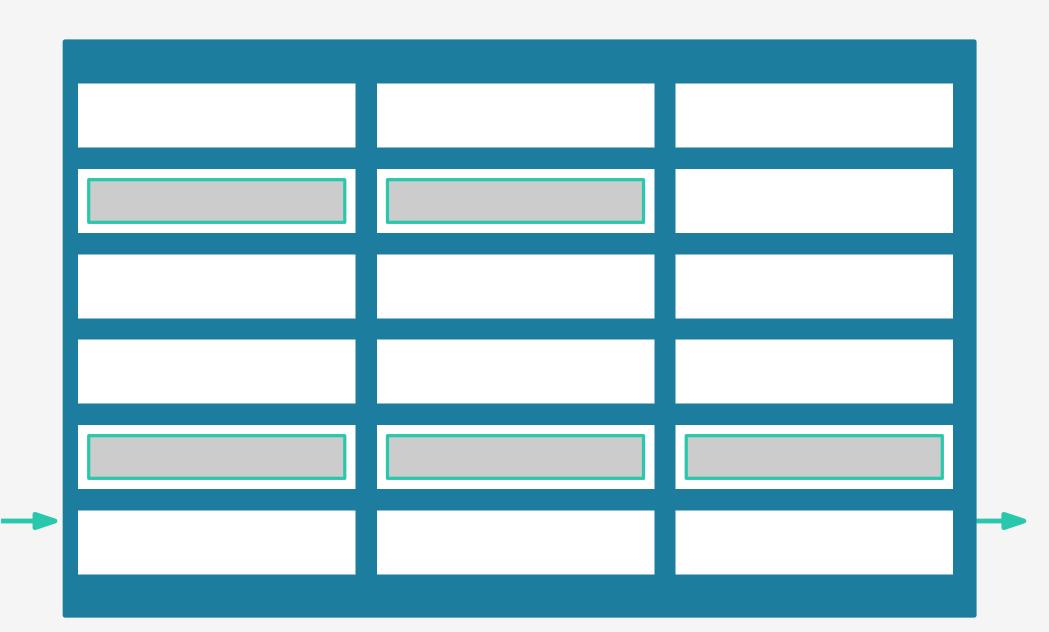


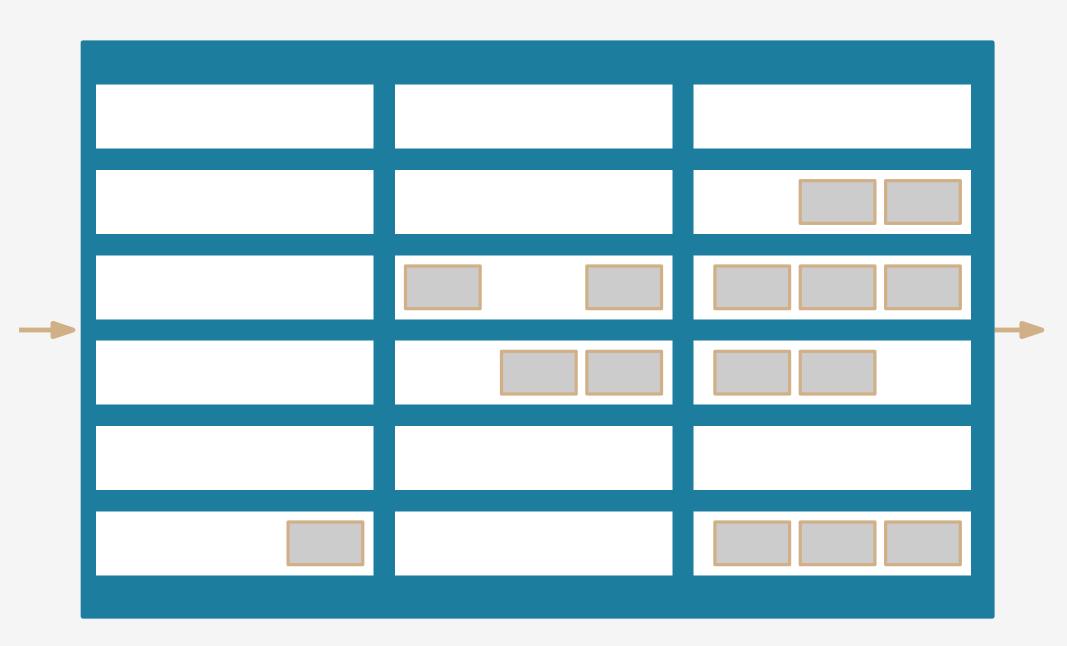


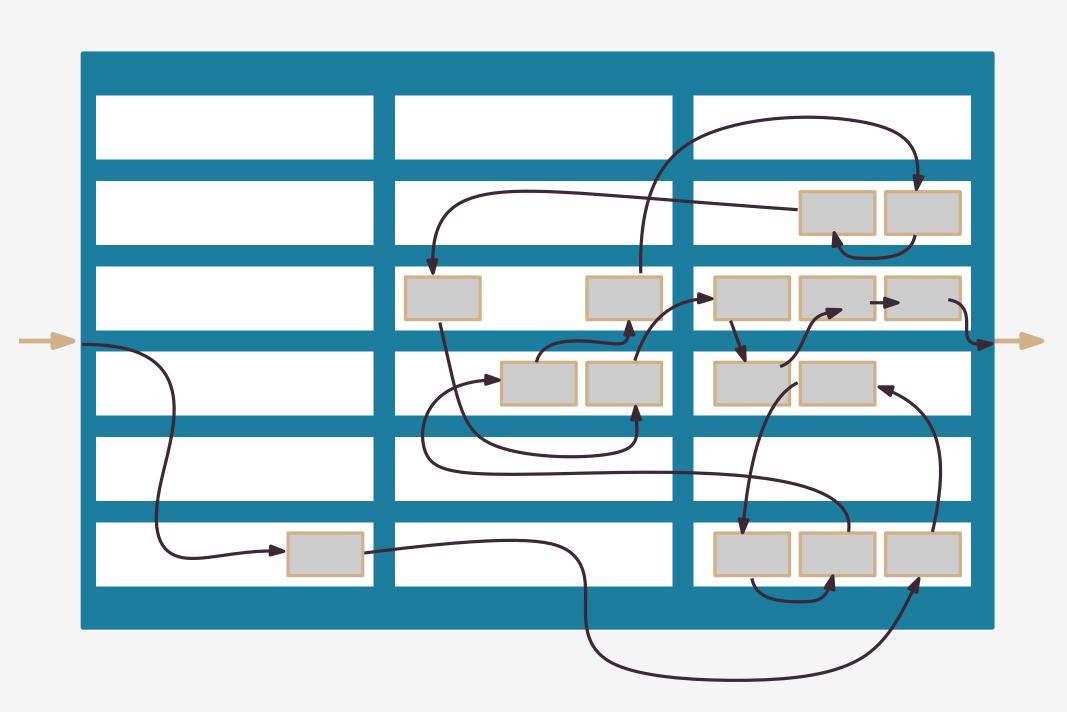


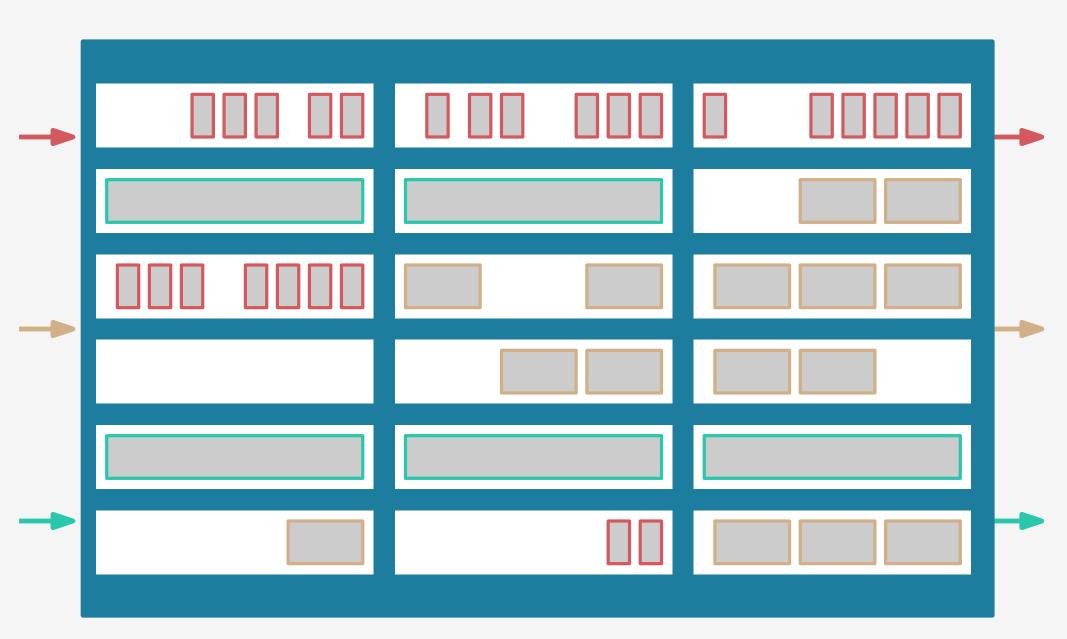


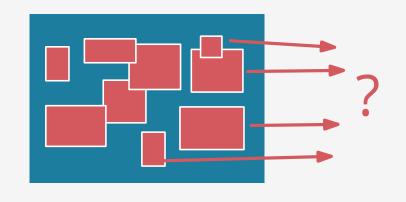


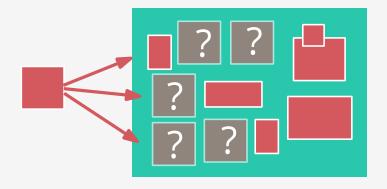










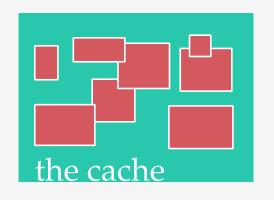


**EVICTION POLICY** 

PLACEMENT POLICY

## THE GENERALIZED CACHING PROBLEM

variable size and cost



GOAL

minimize total cost of cache misses

SUBJECT TO

total size of items in cache cannot exceed the cache size

## THE MANAGED MEMORY CACHING PROBLEM

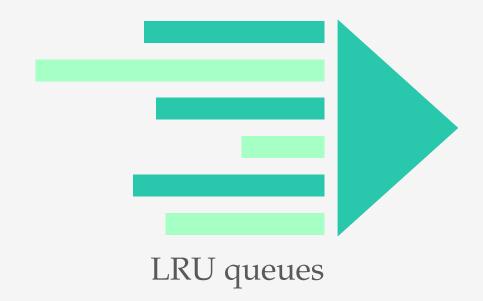
variable size and cost

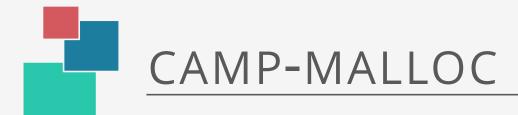
the cache

every item must fit in a contiguous segment of memory

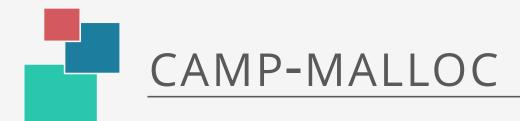
CACHE REPLACEMENT
MEMORY ALLOCATION





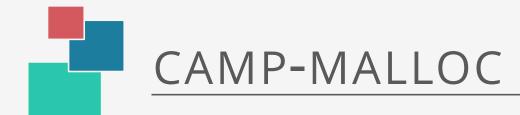






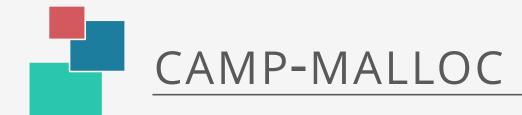




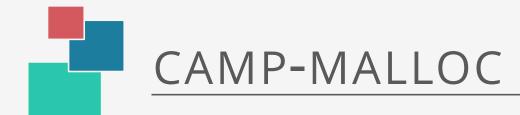






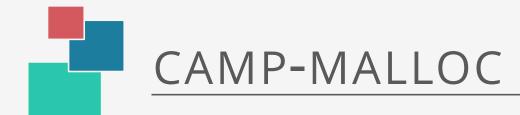


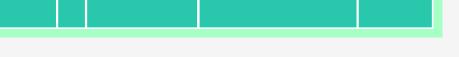




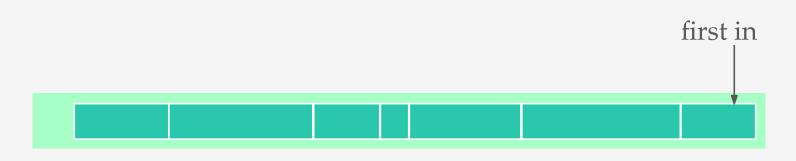












FIFO queue





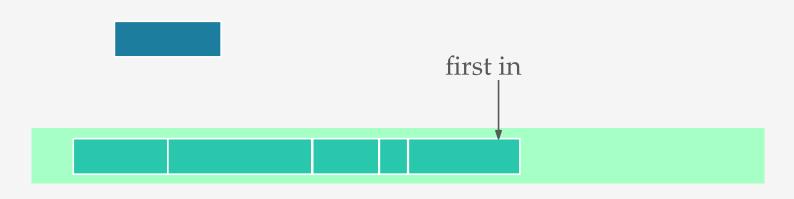
FIFO queue





FIFO queue





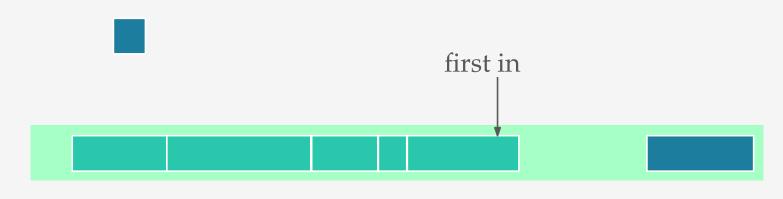
FIFO queue





FIFO queue





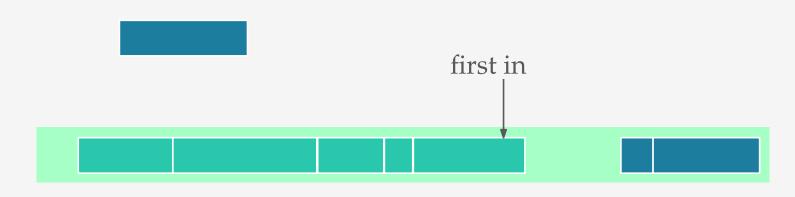
FIFO queue





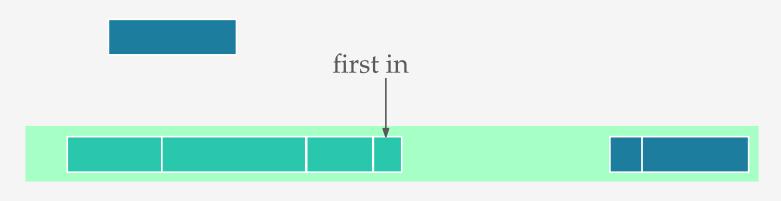
FIFO queue





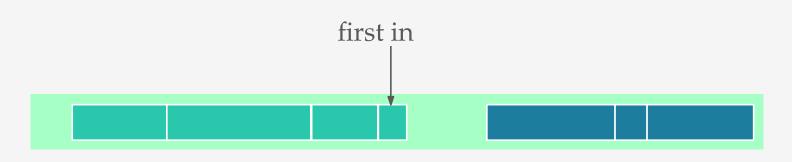
FIFO queue





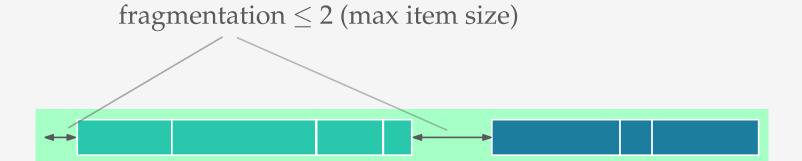
FIFO queue





FIFO queue

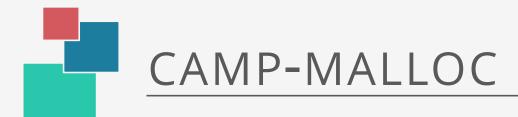


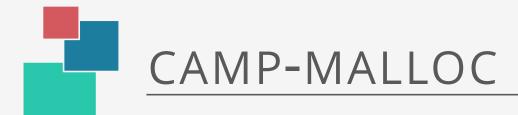


FIFO queue



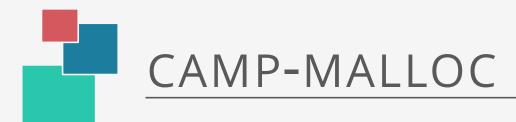


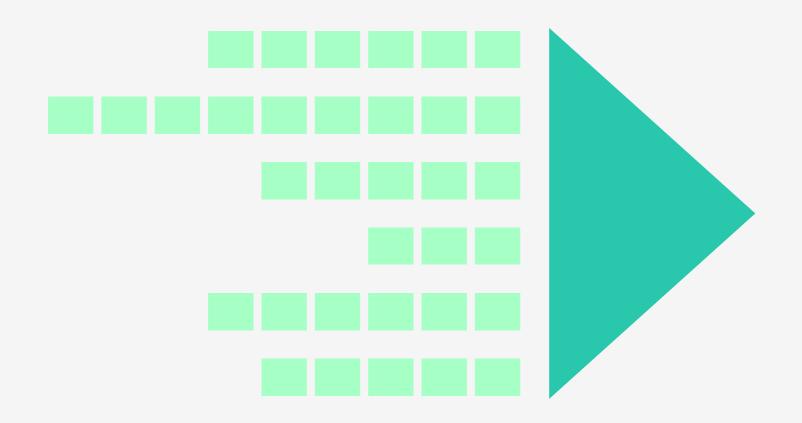




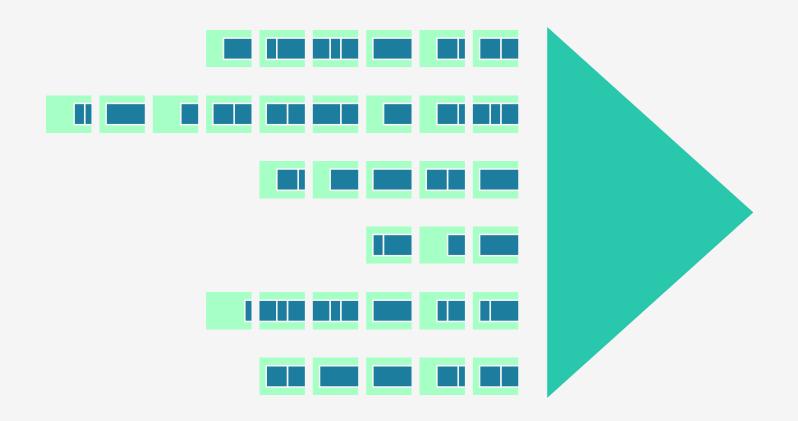


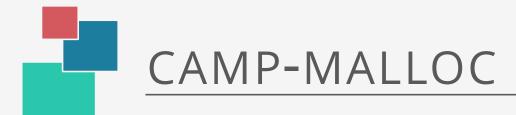


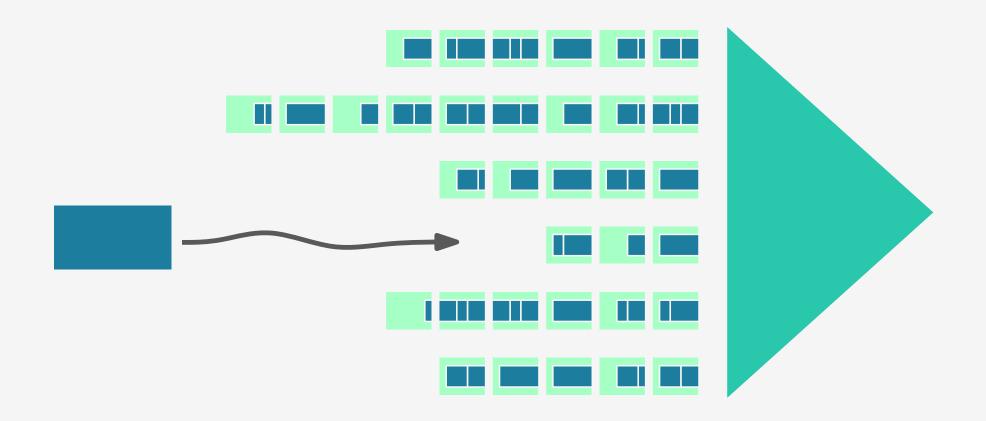




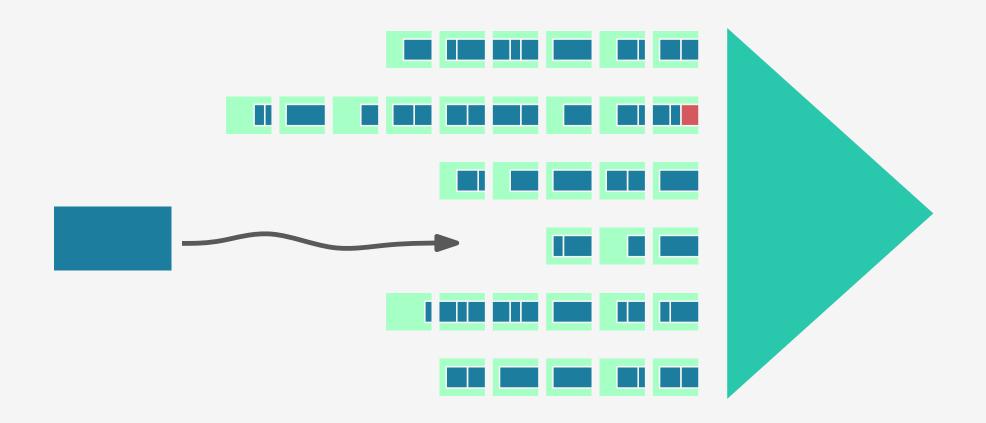




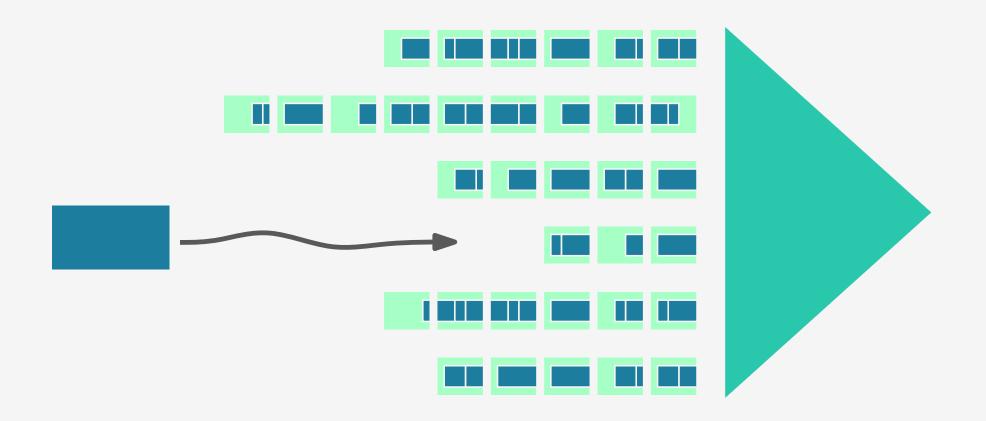


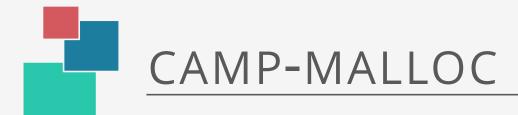


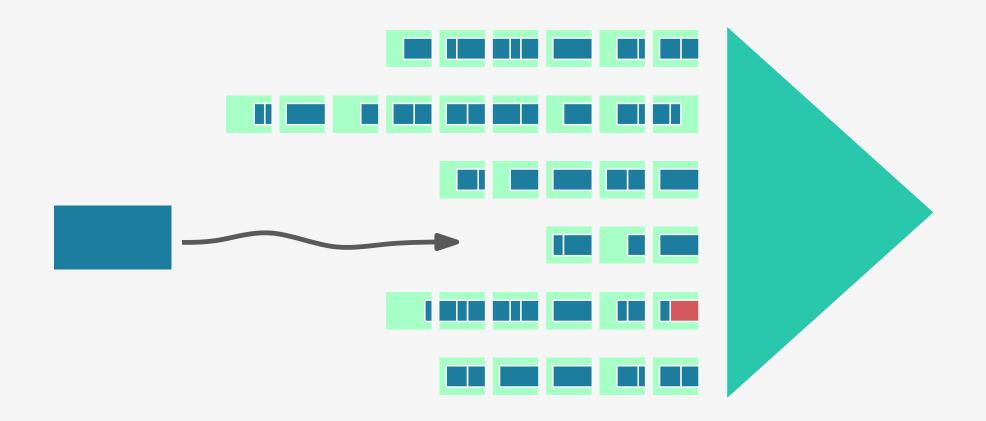




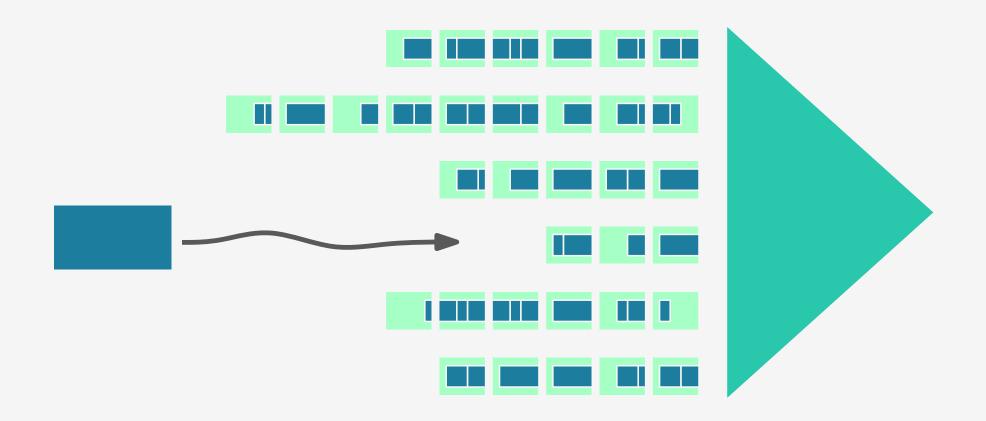




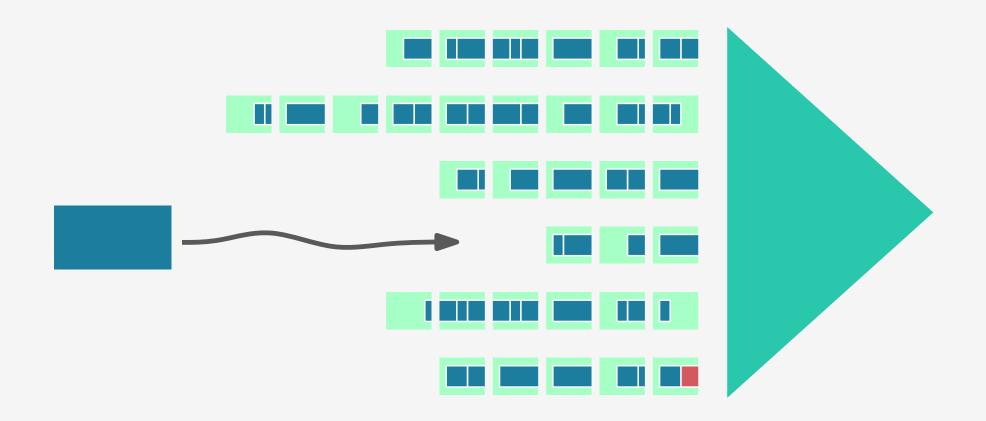




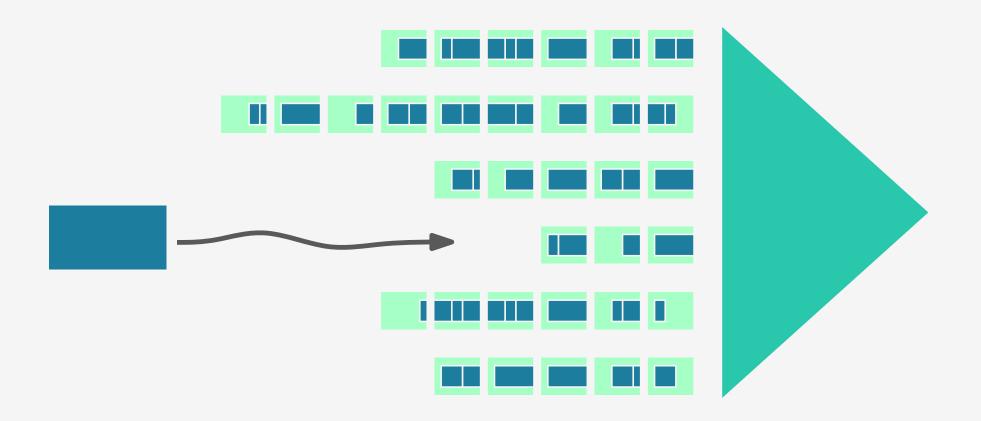




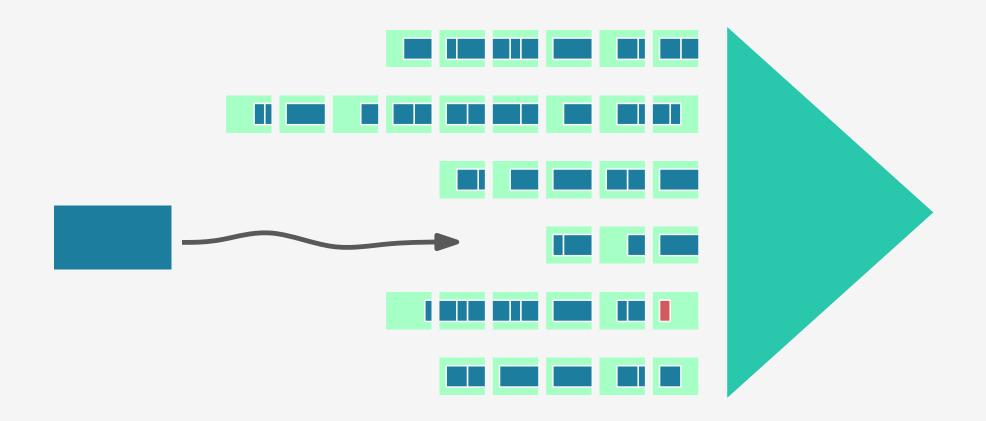


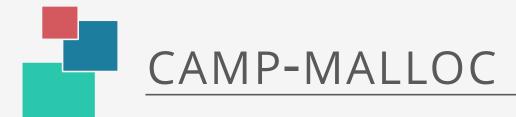


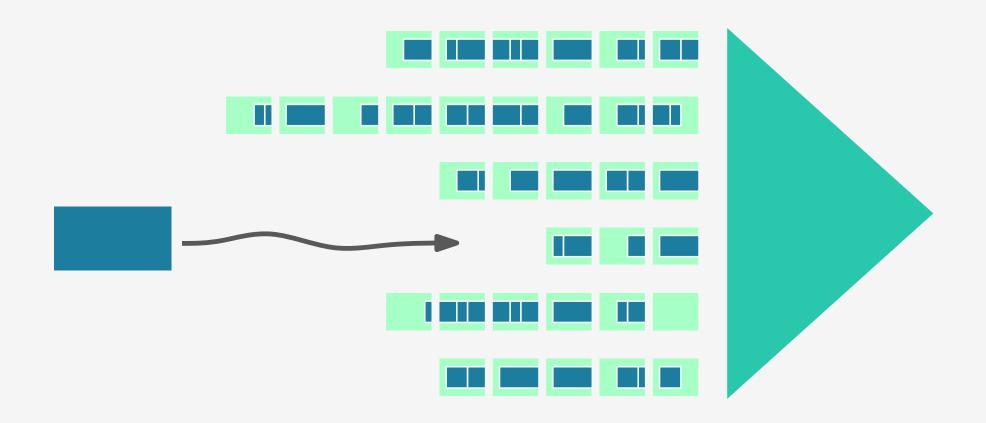




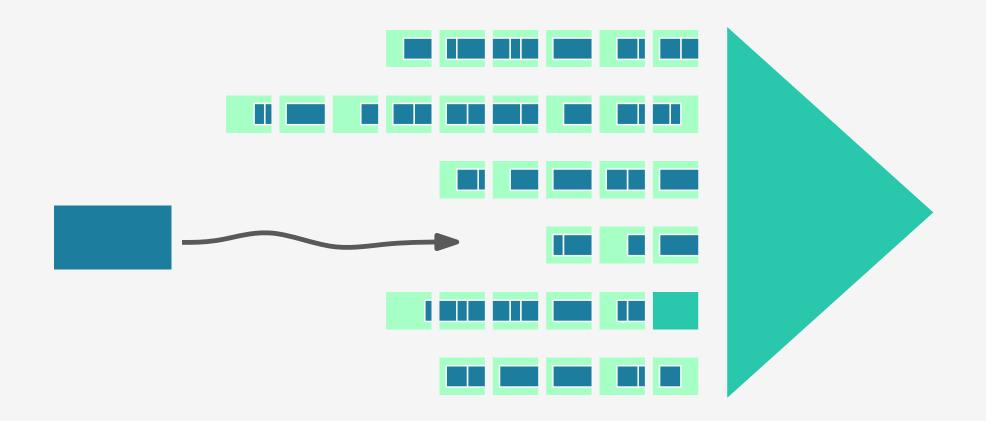




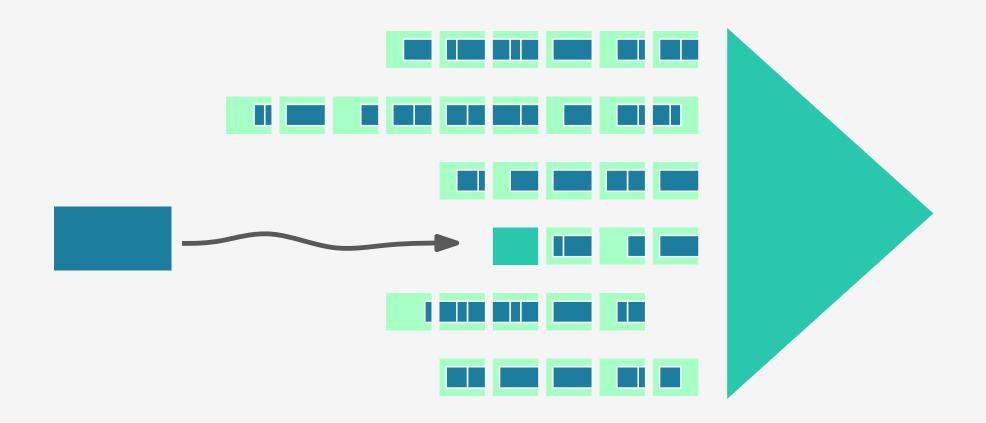


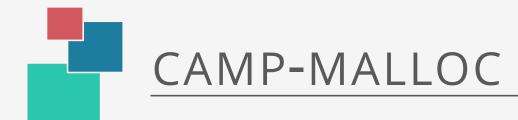


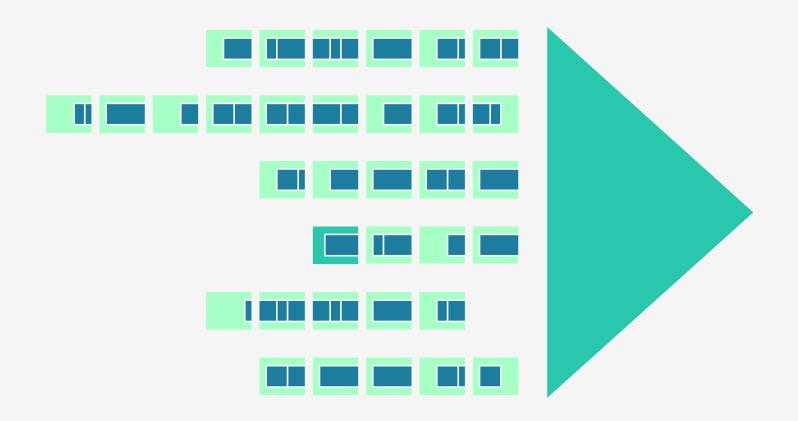


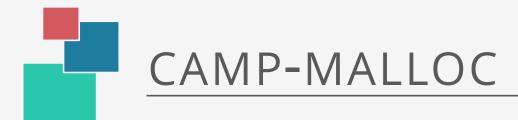


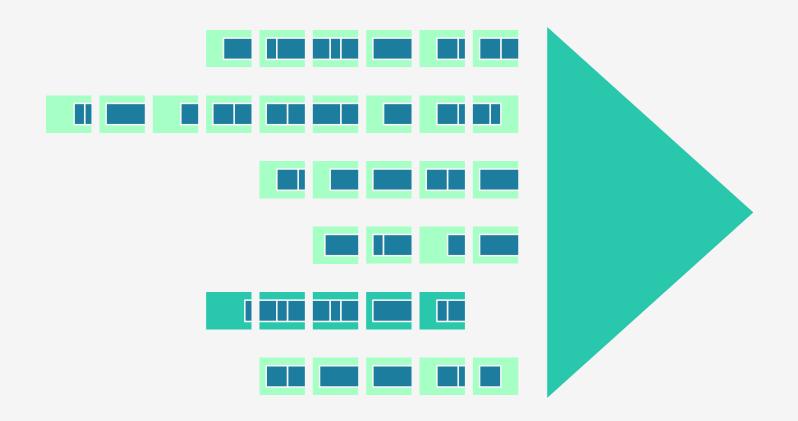




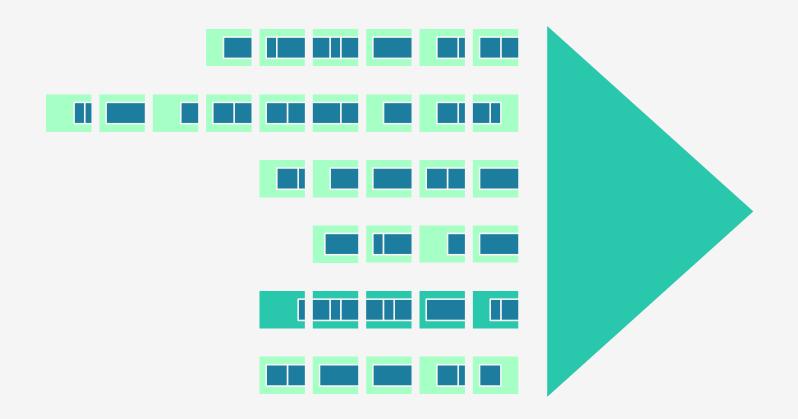




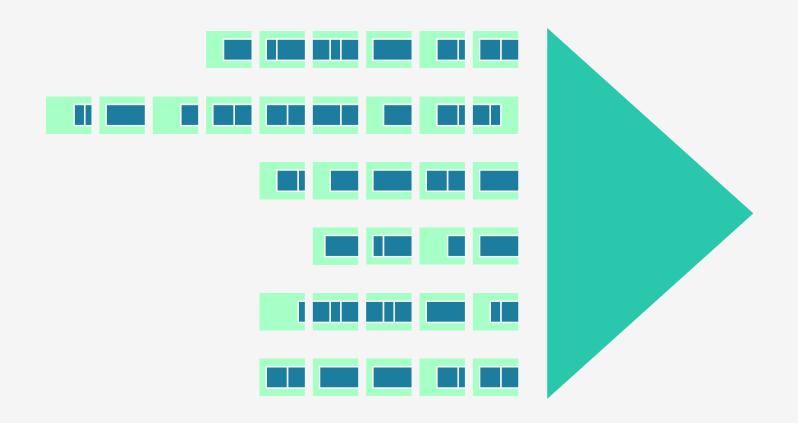


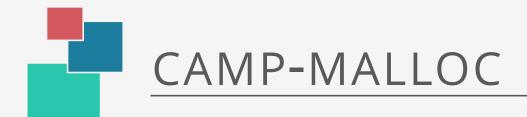


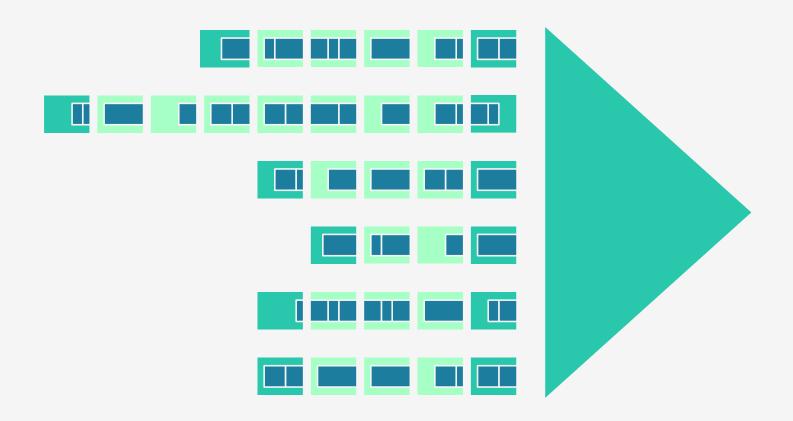












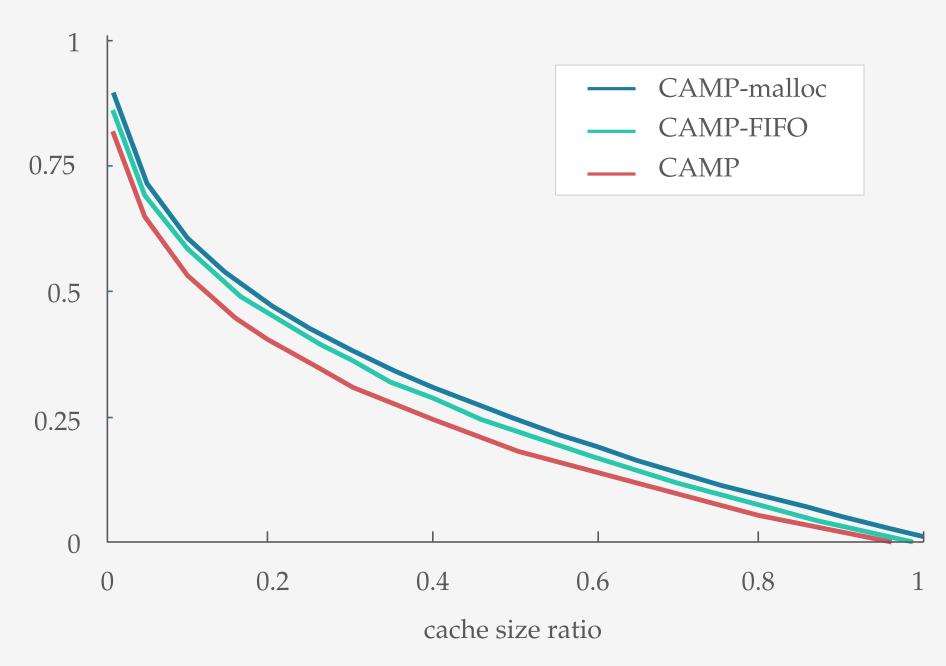


## CAMP-MALLOC

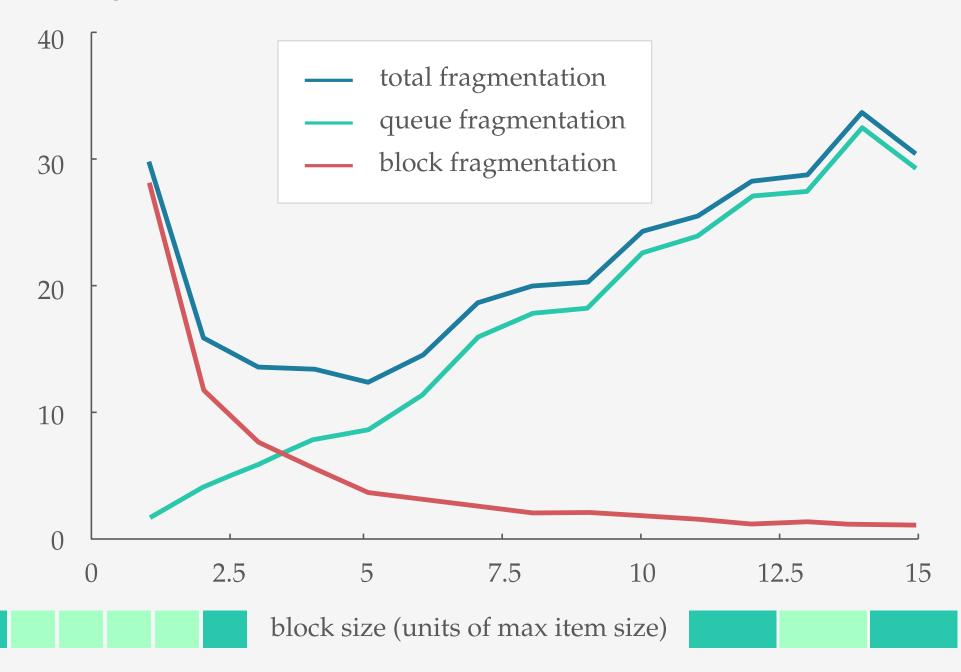
is competitive if memory augmented

if 
$$\frac{\text{OPT's}}{\text{cache size}} \le \frac{\text{C-M's}}{\text{cache size}} - \frac{\text{fragmentation}}{\text{bound}}$$
 then  $\cot(\text{C-M}) \le \frac{\text{C-M's}}{\text{min item size}} \cot(\text{OPT})$ 

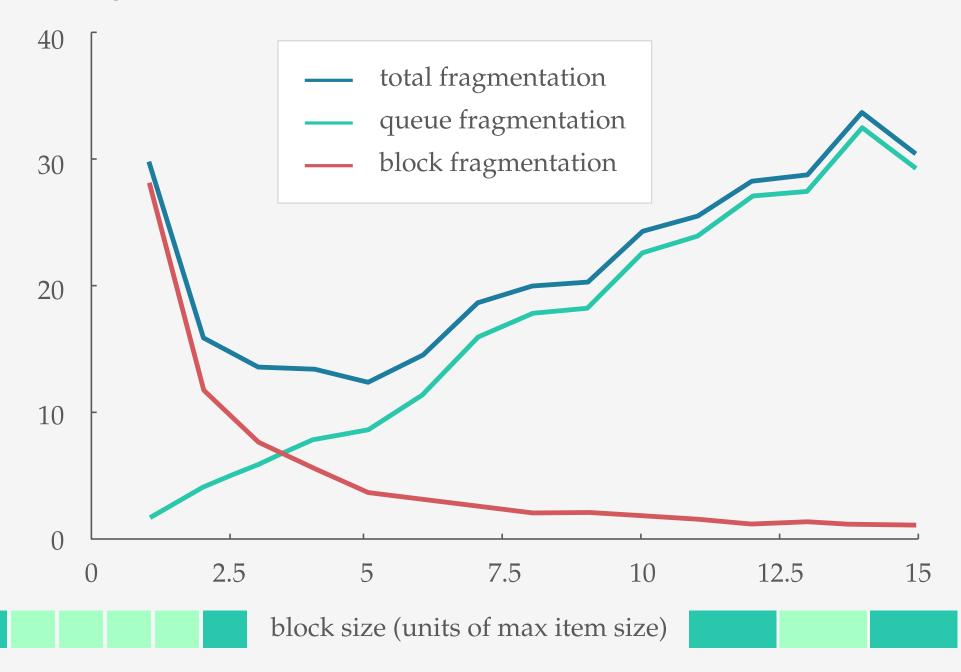


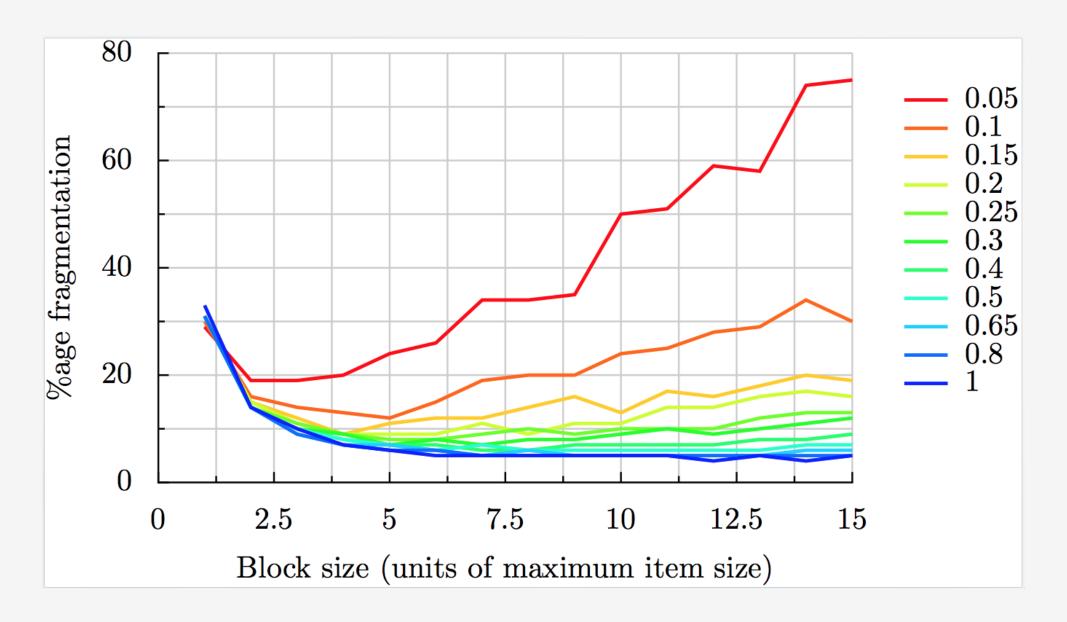


#### percent fragmentation



#### percent fragmentation





# EVICTION POLICY GDS → CAMP

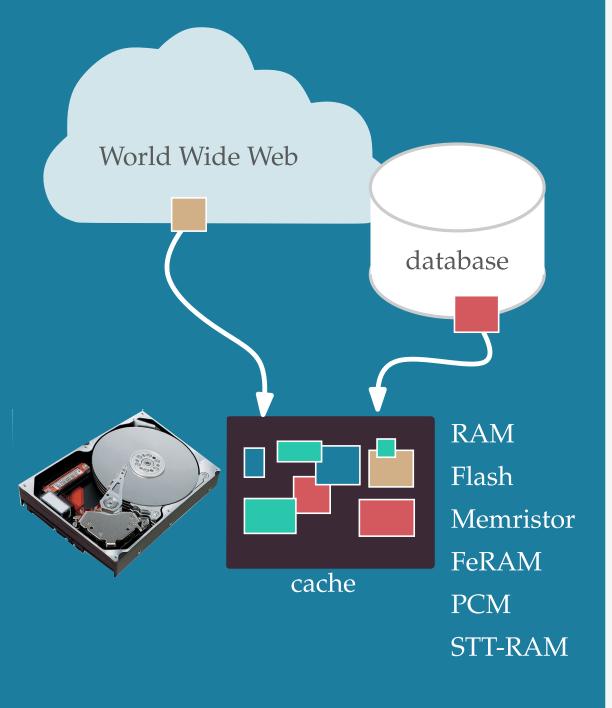


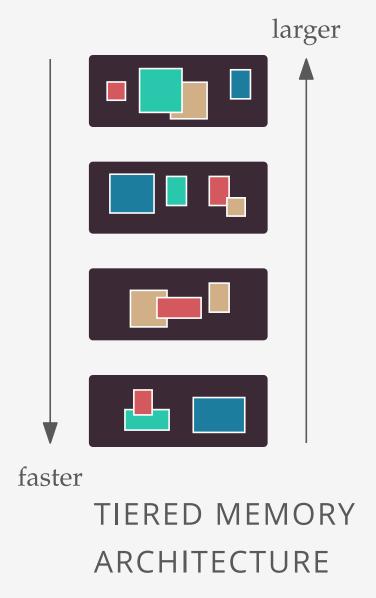
#### PLACEMENT POLICY



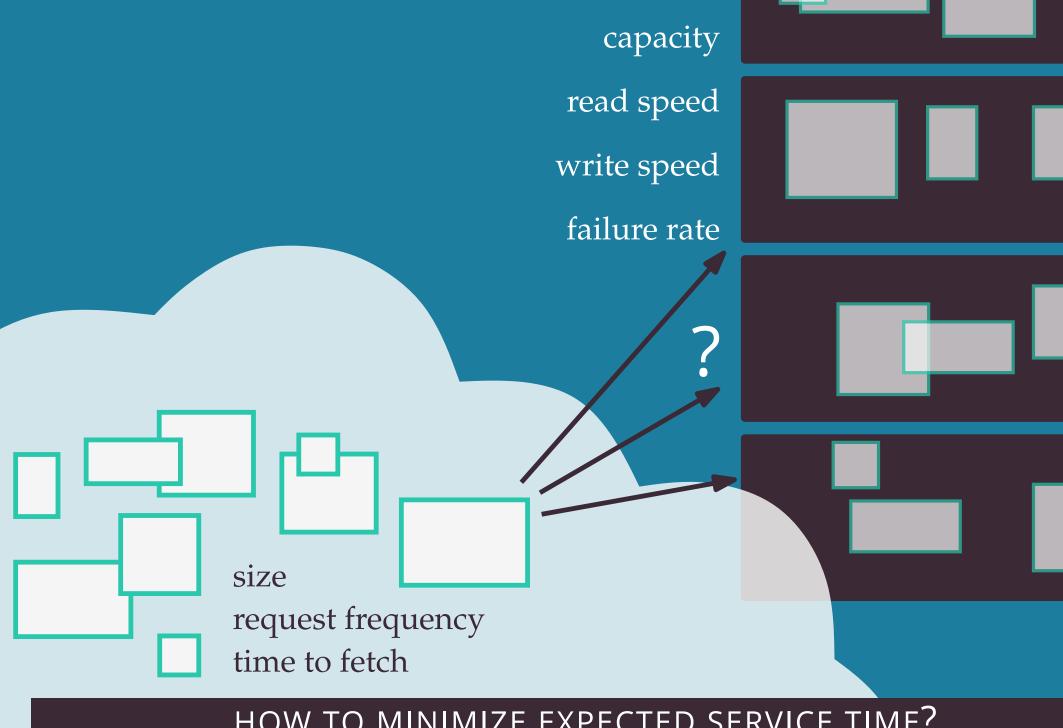
#### MEMORY HIERARCHY

2-level cache 
→ multi-level cache

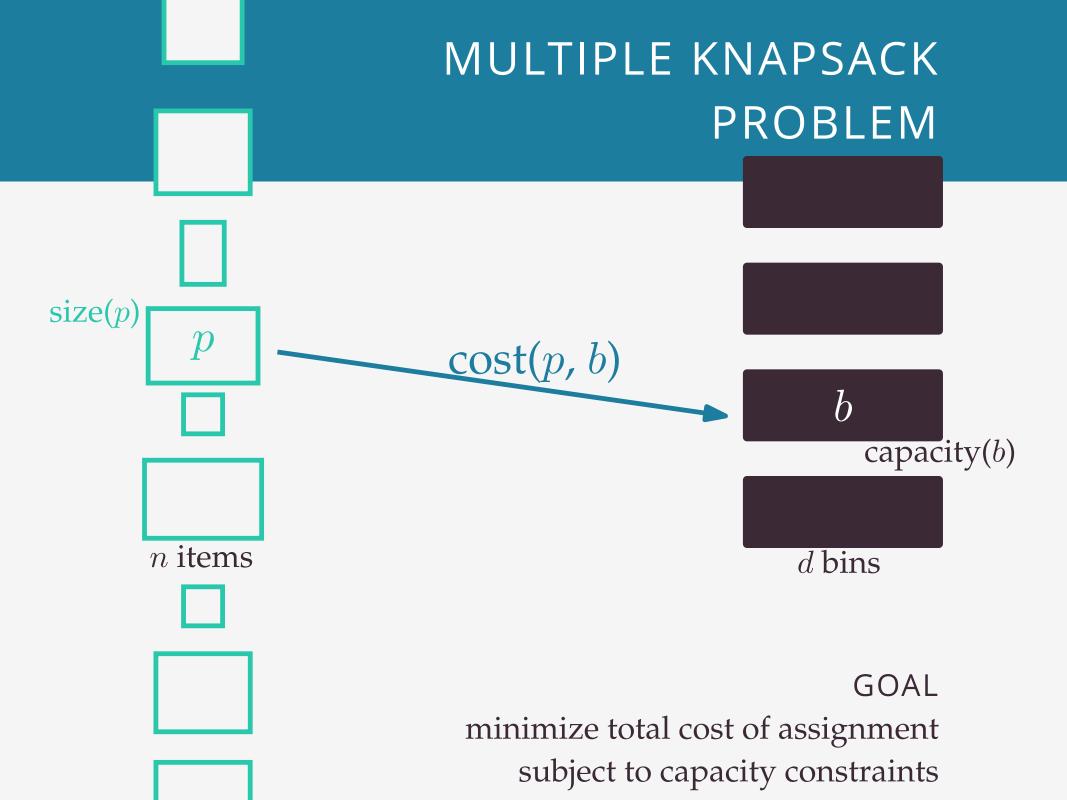




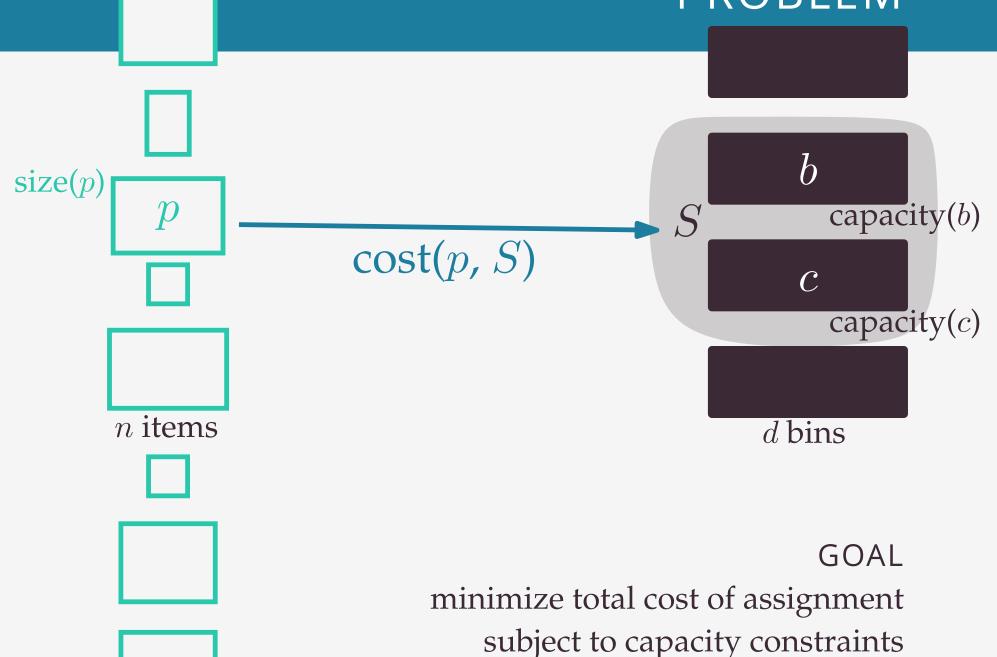
GENERALIZED CACHING

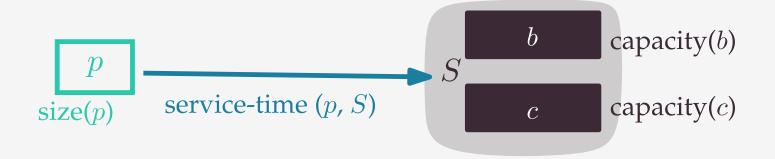


HOW TO MINIMIZE EXPECTED SERVICE TIME?

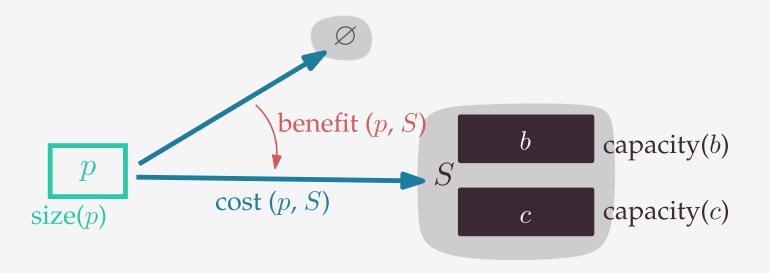


# SUBSET ASSIGNMENT PROBLEM





$$\begin{aligned} \text{service-time}(p,S) &= \text{read-frequency}(p) & \text{read-time}(p,S) \\ &+ & \text{write-frequency}(p) & \text{write-time}(p,S) \\ &+ & \sum_{F\subseteq S} \text{fail-freq}(F) & \Big( \text{read-time}(p,S\setminus F) \\ &+ & \text{write-time}(p,S\cap F) \Big) \end{aligned}$$



#### cache configuration

maximize  $\sum_{p,S}$  benefit(p,S) x(p,S)

$$\sum_{S} x(p, S) = 1$$

 $\sum_{p,S} \operatorname{price}(p,S) x(p,S) \leq \operatorname{budget}$ 

$$x = 0, 1$$

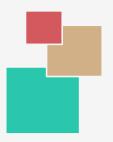
#### subset assignment

$$\text{minimize } \sum_{p,S} \cot(p,S) \, x(p,S)$$

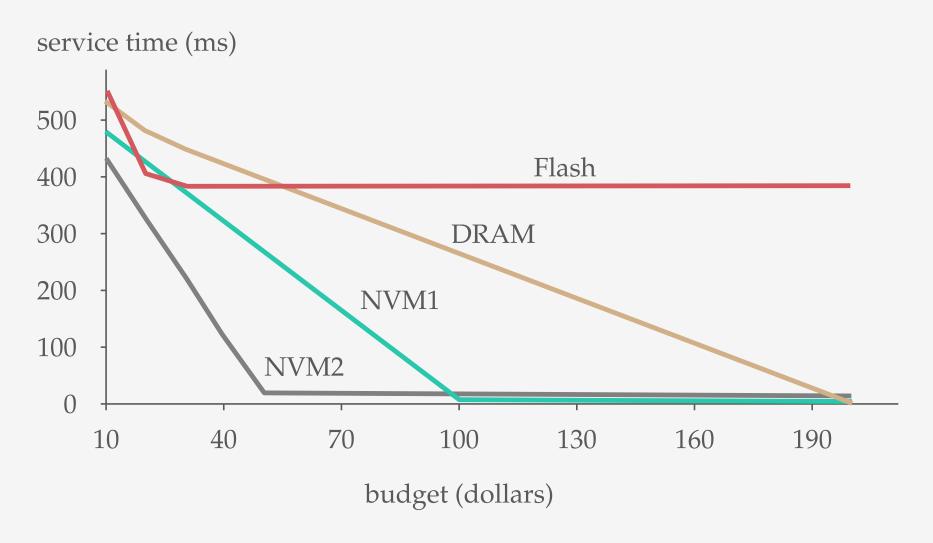
$$\sum_{S} x(p, S) = \operatorname{size}(p)$$

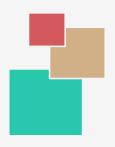
$$\sum_{p,S\ni b} x(p,S) \le \operatorname{capacity}(b)$$

$$x(p, S) = 0$$
, size $(p)$ 



## CACHE CONFIGURATION





## SUBSET ASSIGNMENT

HAVE

 $d \ll n$ 

sol to LP relaxation has few fractional assignments

GOAL

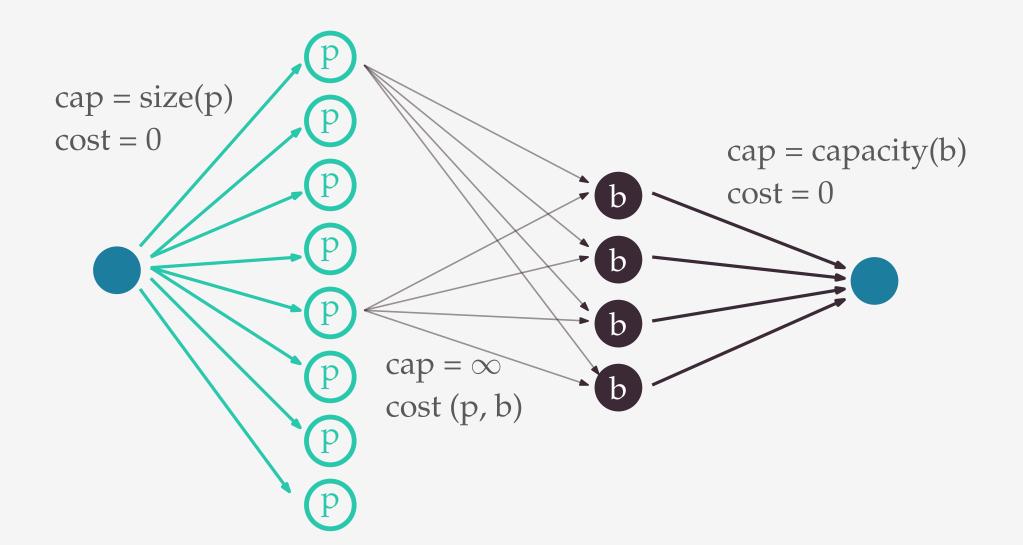
solve LP relaxation in f(d) poly(n)

### 1. cycle canceling algorithm

2. simplex algorithm

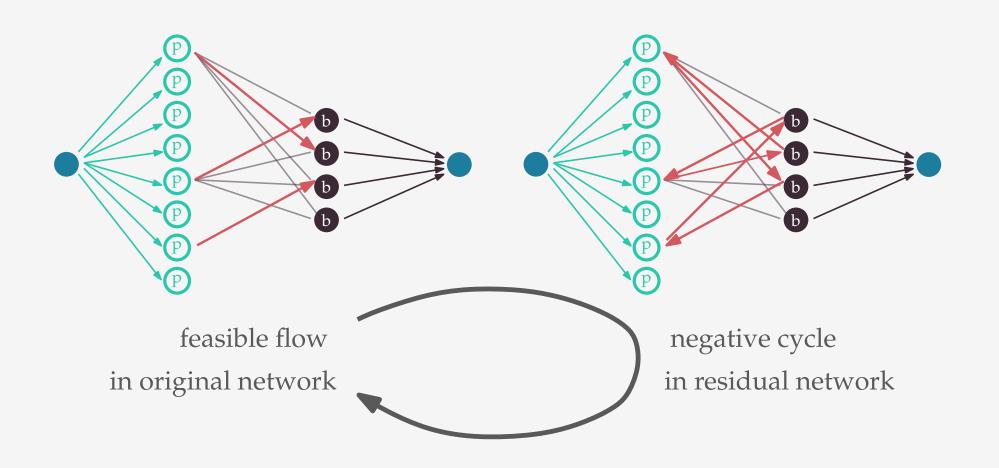


## MIN COST FLOW





## 1. cycle canceling algorithm



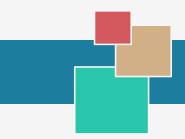


## "cycle" in subset assignment problem

augmentation 
$$S_i$$
  $p_i$   $T_i$ 

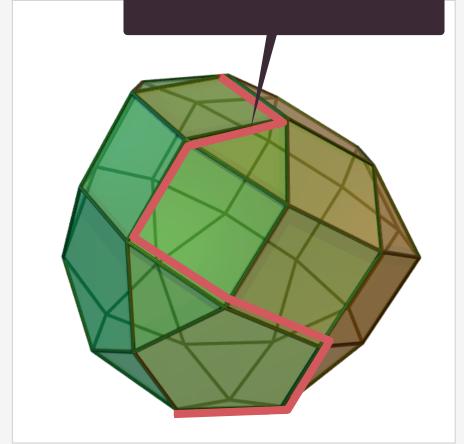
such that 
$$\sum_{i} \alpha_{i} \overrightarrow{S_{i}T_{i}} = \vec{0}$$

cost difference (negative) 
$$\sum_{i} \alpha_{i} \left( cost(p_{i}, T_{i}) - cost(p_{i}, S_{i}) \right)$$



## 2. simplex algorithm

basic feasible solution



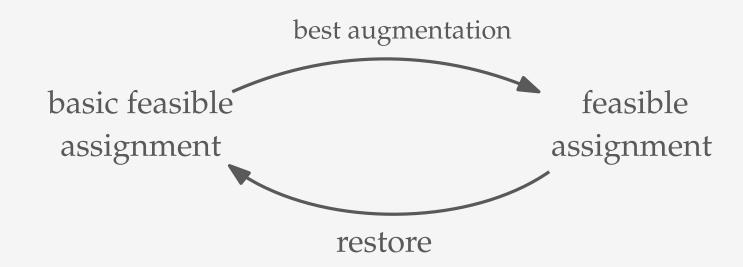
## BASIC FEASIBLE ASSIGNMENT

< 2d fractional assignments

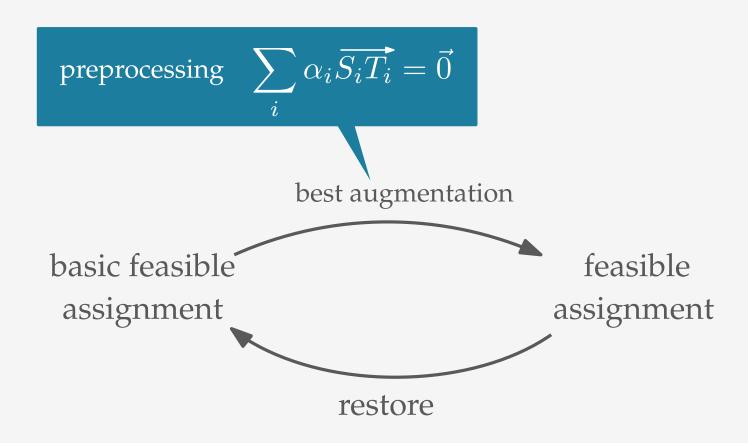
bound granularity of vars

$$x(p,S) = \frac{k}{\ell}$$



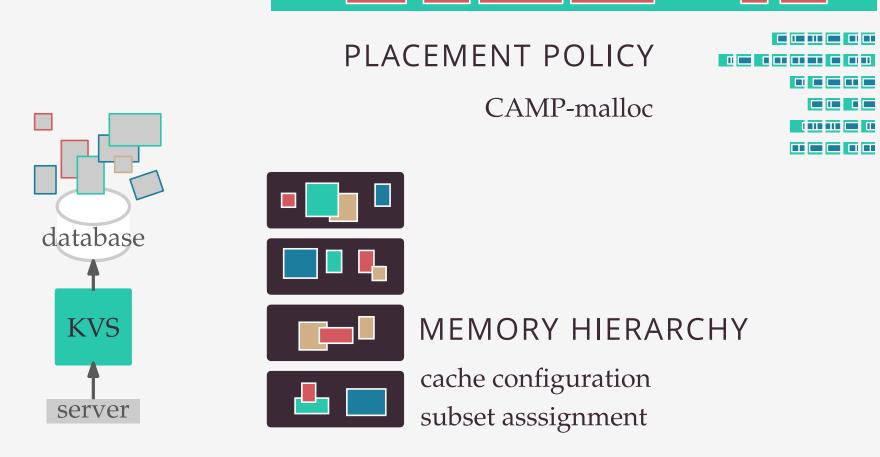




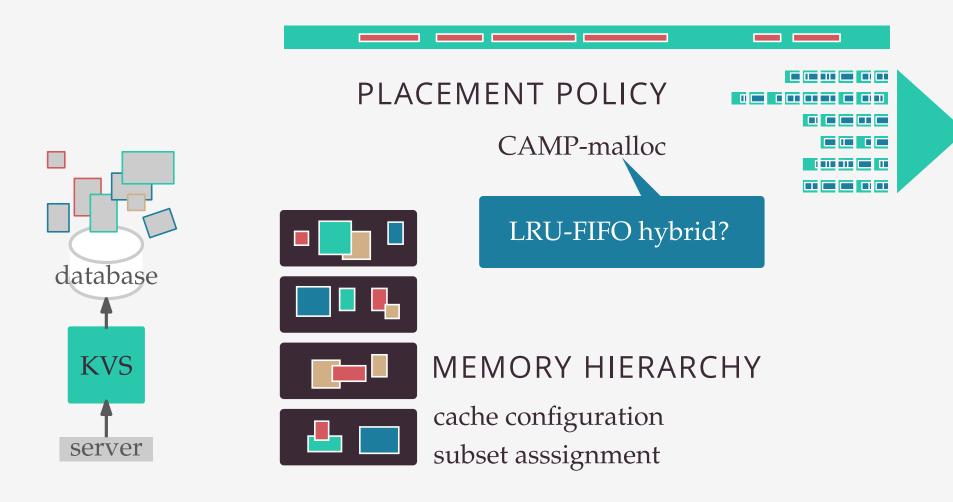


 $O(\exp(d(d+1)\operatorname{poly}(d) \ n\log(n)\log(nC)\log(S))$ 

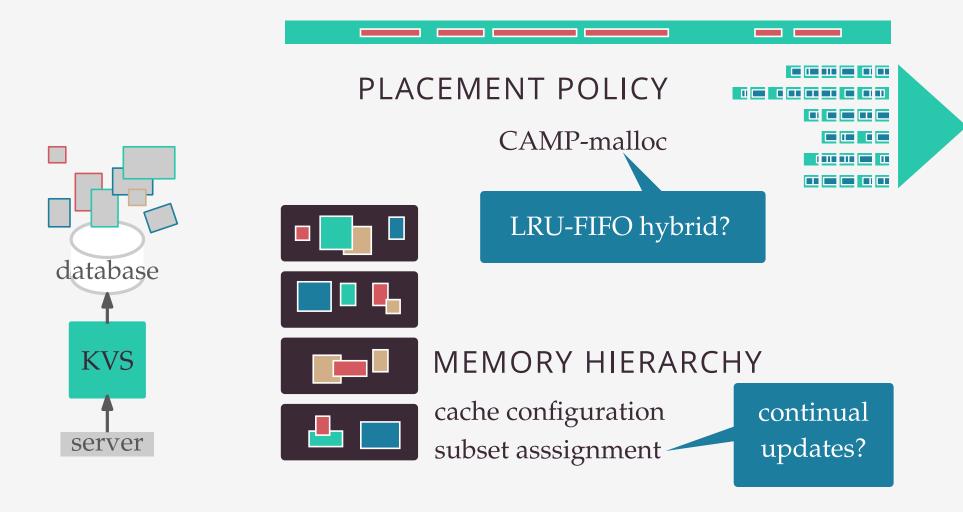




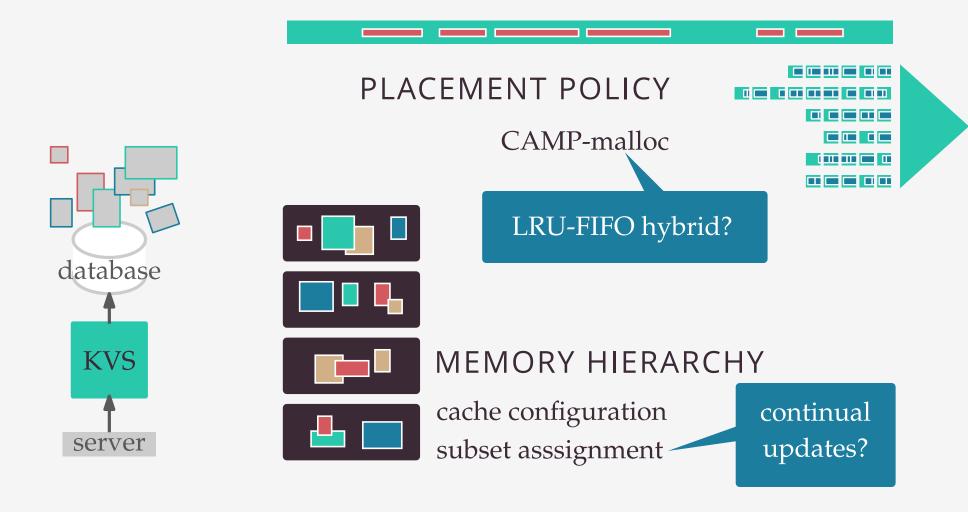










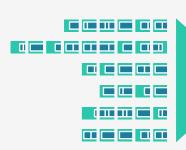


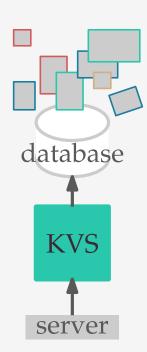


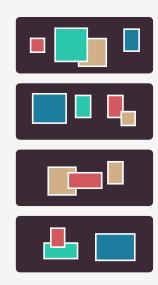
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