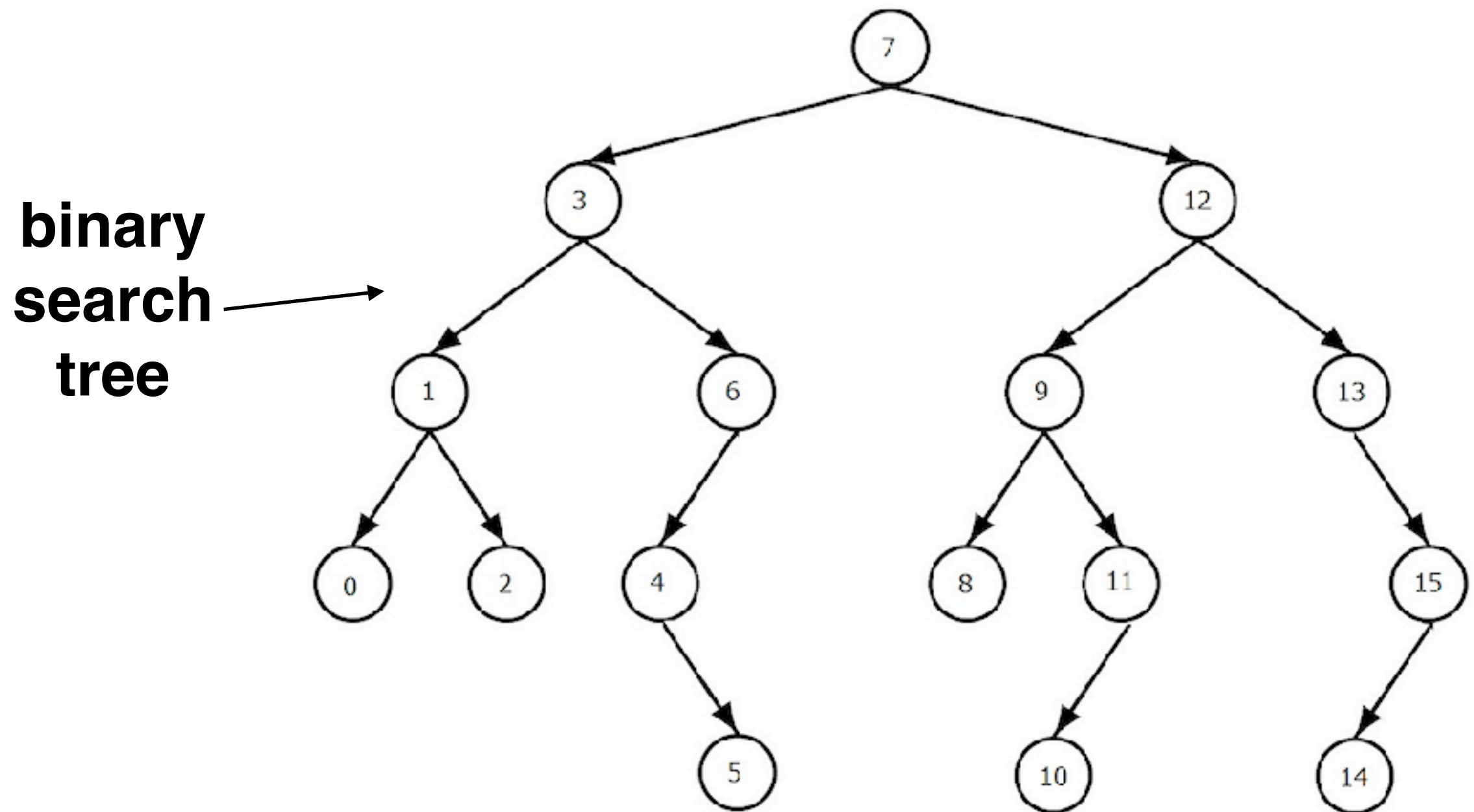


# Binary search trees and skiplists

CS 146 - Spring 2017

## Review question (from 46B)

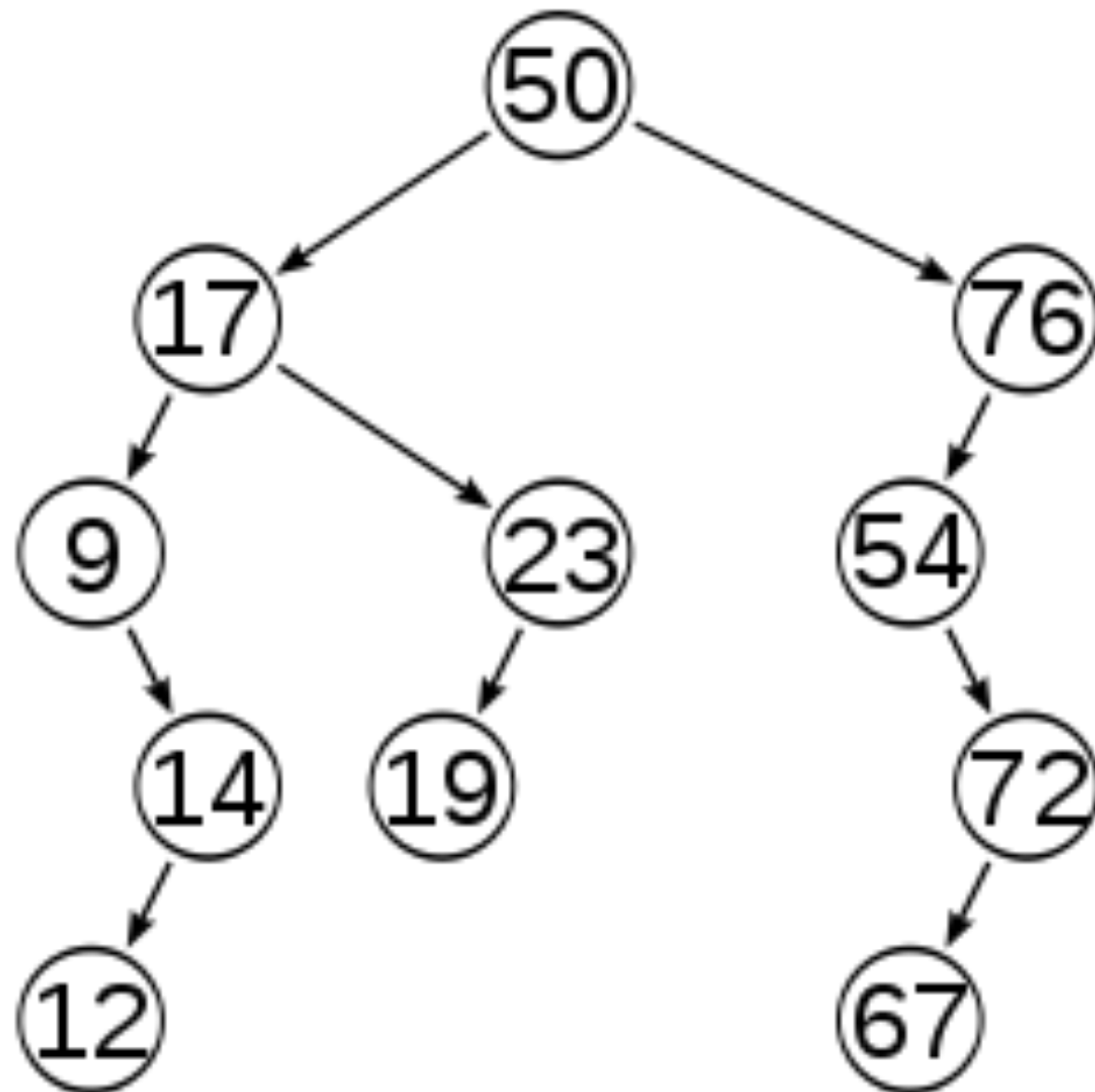


- Who is the successor of 12? 3? 8?
- What is the pattern for finding the successor?

# Today

- 2 OrderedSet implementations
  - Binary search tree
  - Skiplist

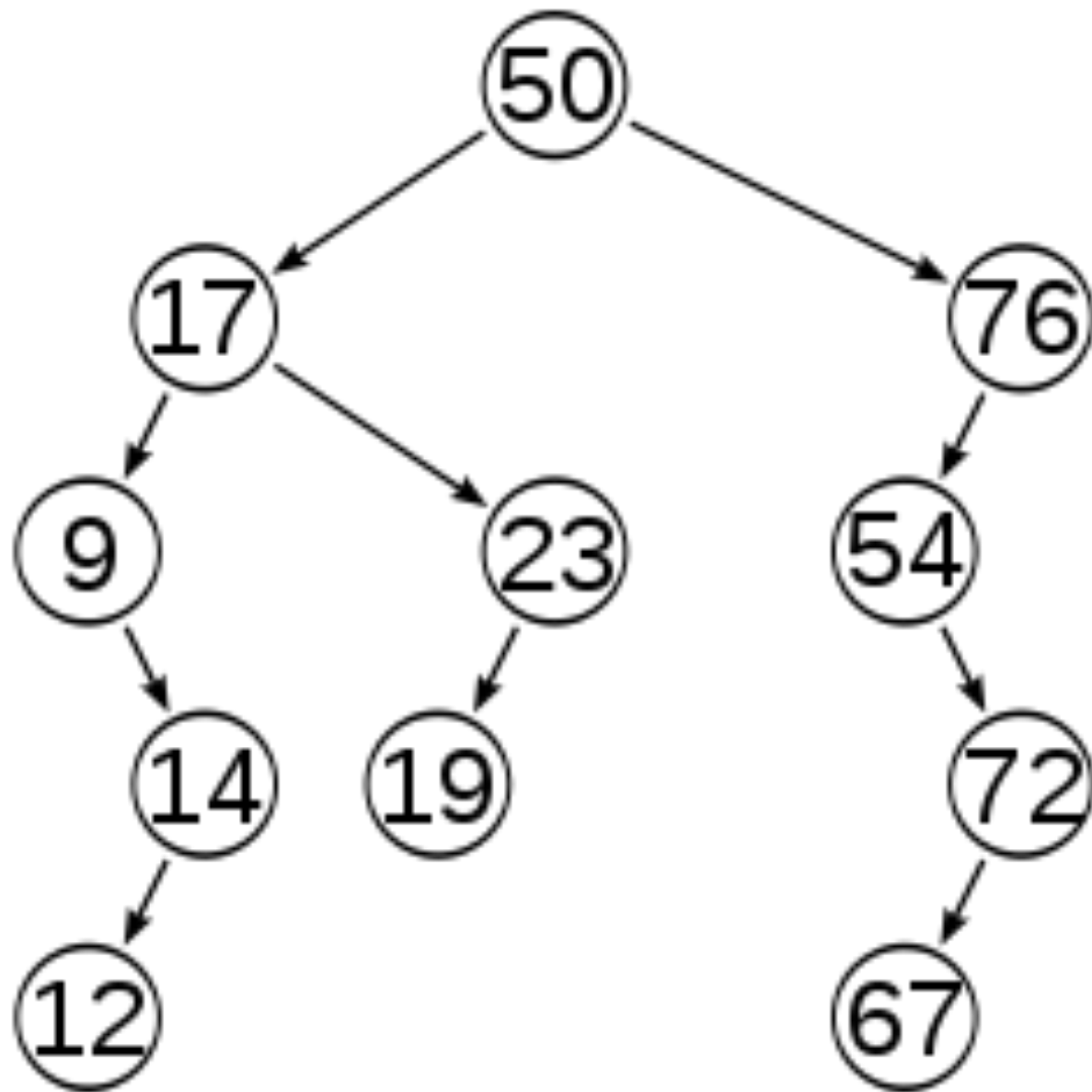
# Binary search tree is



- a binary tree with...
- the **binary search tree property**

for every node  
if  $x$  is in the node's left subtree,  
 $x.\text{key} \leq \text{node.key}$   
if  $x$  is in the node's right subtree,  
 $\text{node.key} \leq x.\text{key}$

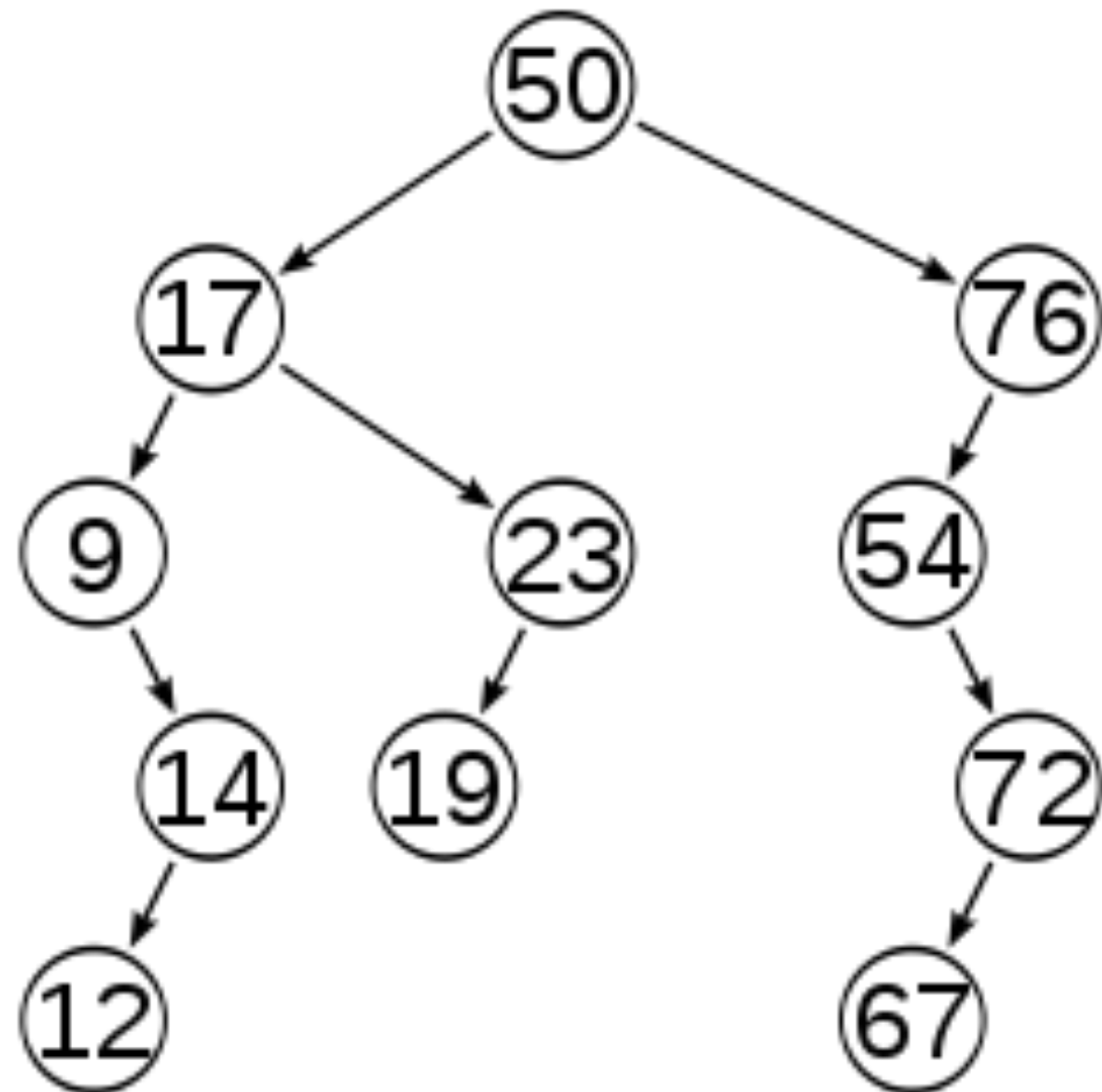
# To search for a key in a BST



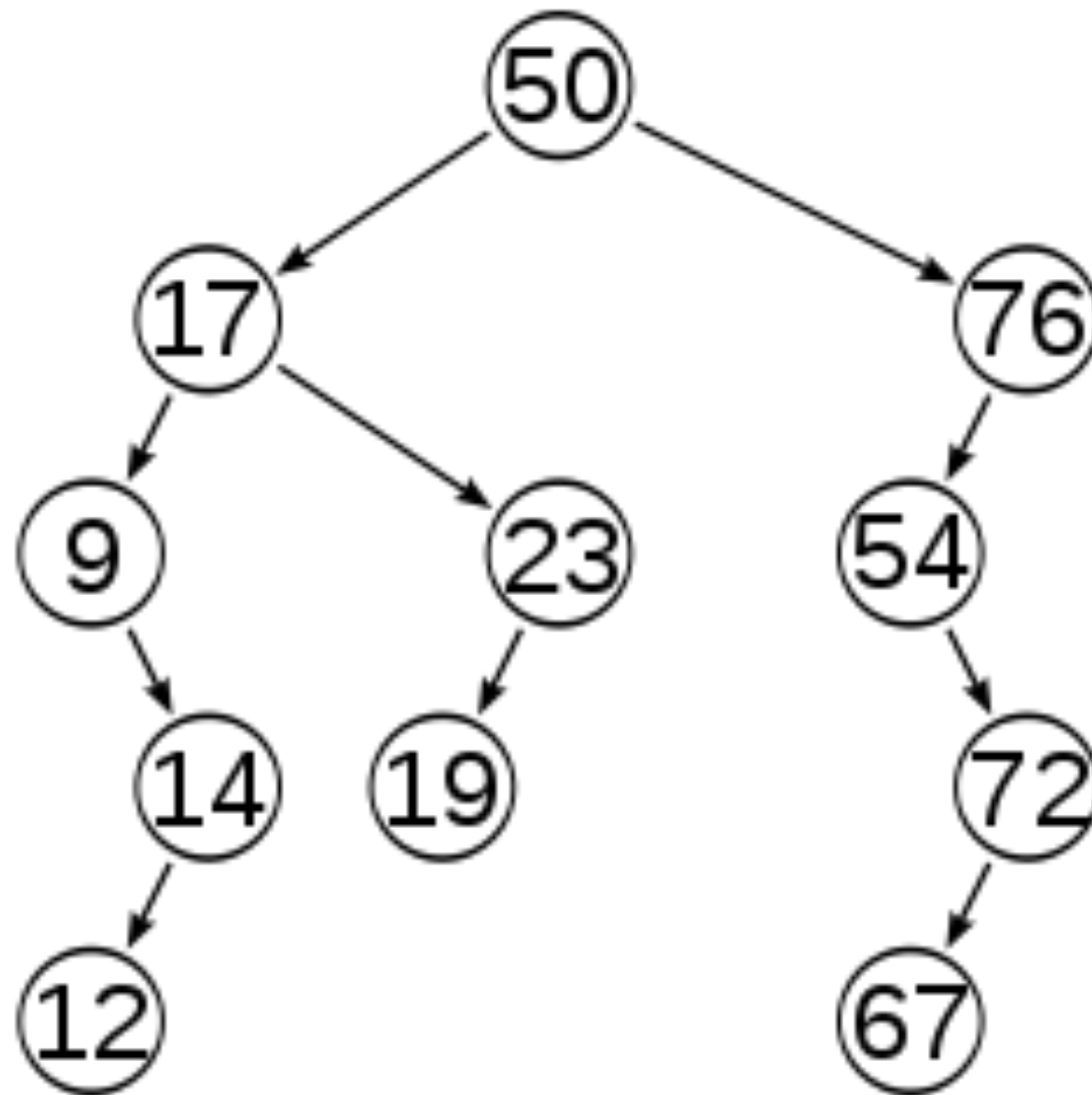
- start at root
- if `key == node.key`
  - (Key found!) return
- else if `node.key < key`
  - search left or
  - return (NOT FOUND) if no left
- else (`key < node.key`)
  - search right or
  - return (NOT FOUND) if no right

# To insert

- perform a search until you can't keep going down
- insert there



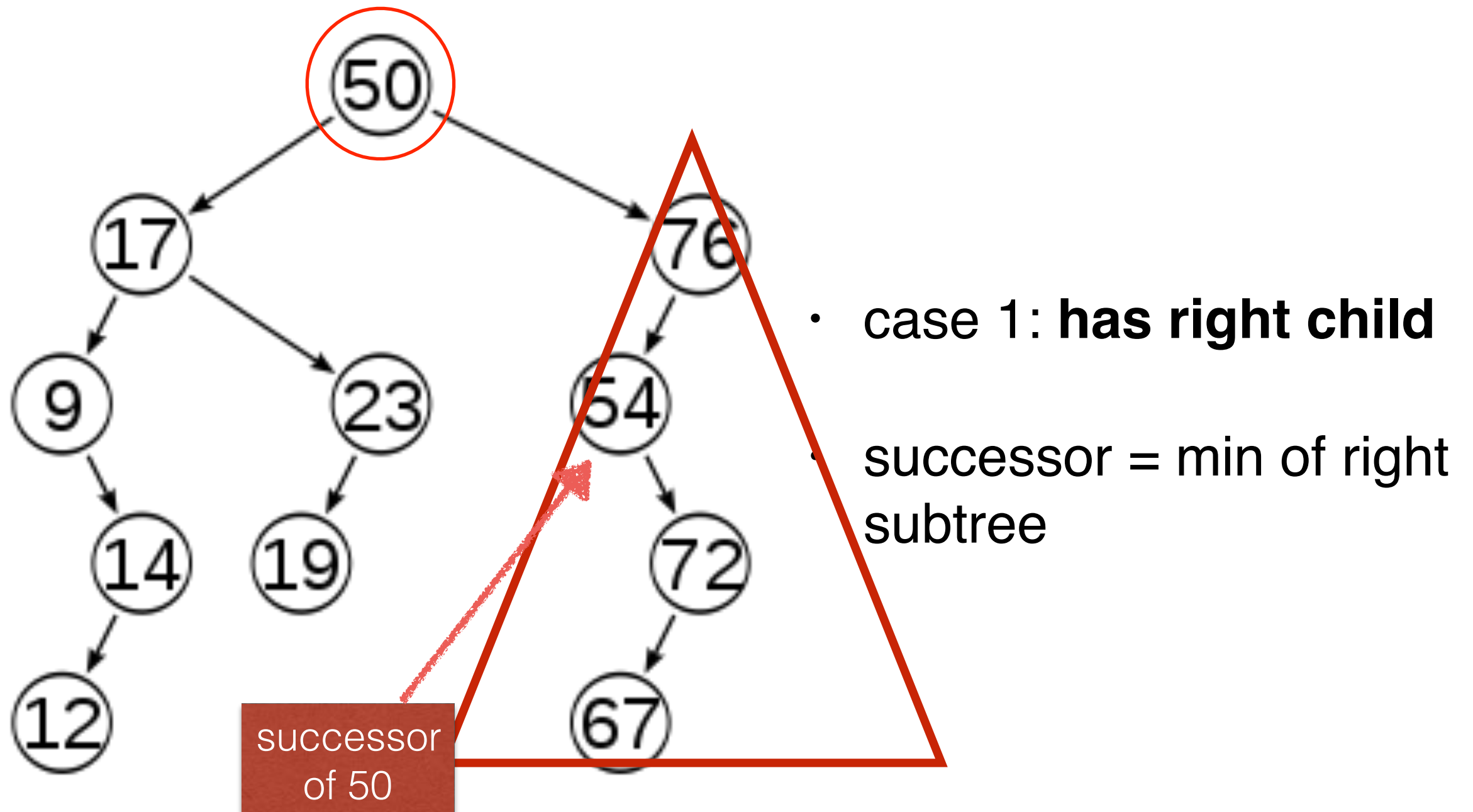
# To find min



- keep going to the left child until you can't

similar idea with finding max

# To find successor (1/2)

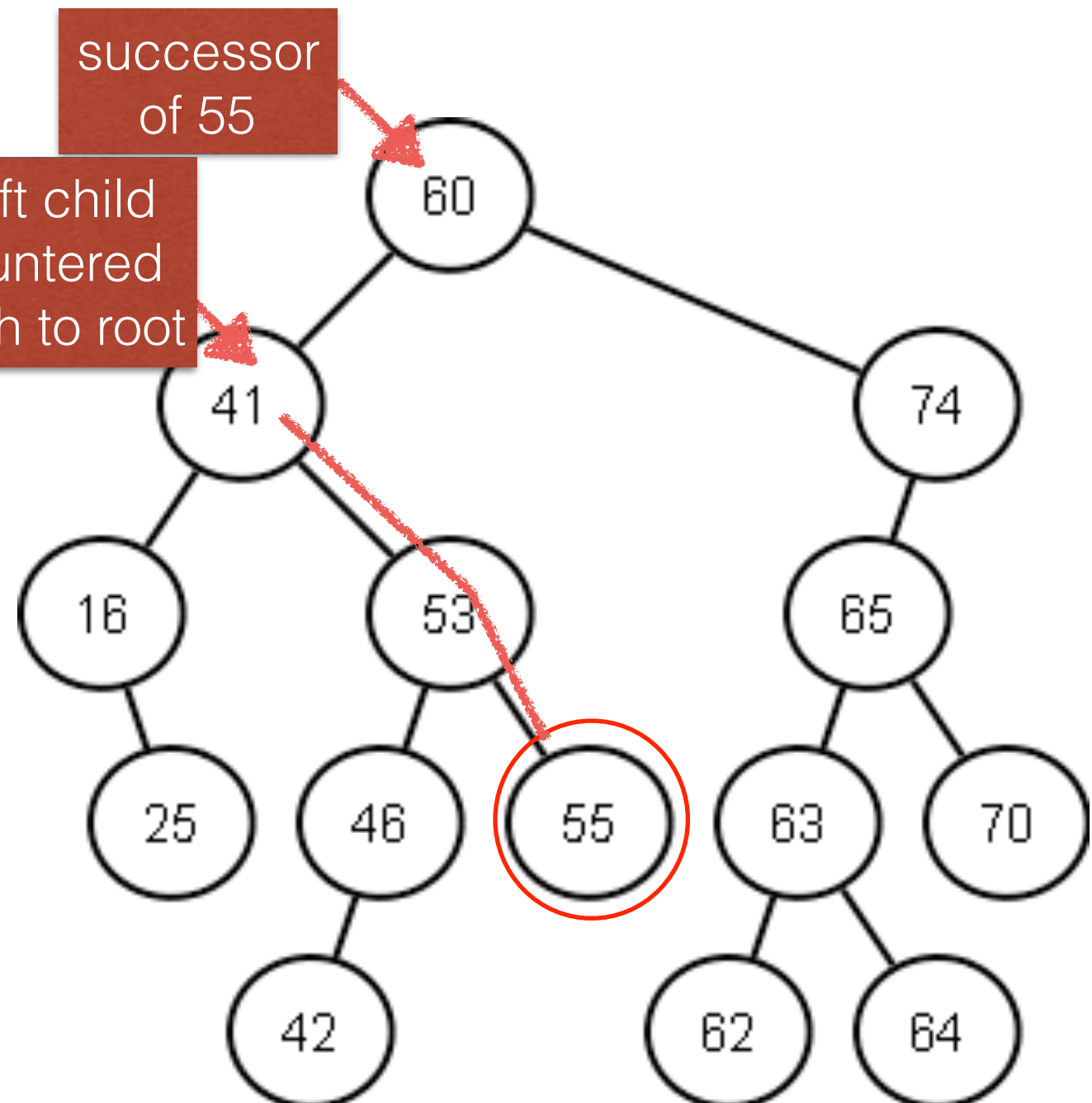


similar idea with finding predecessor



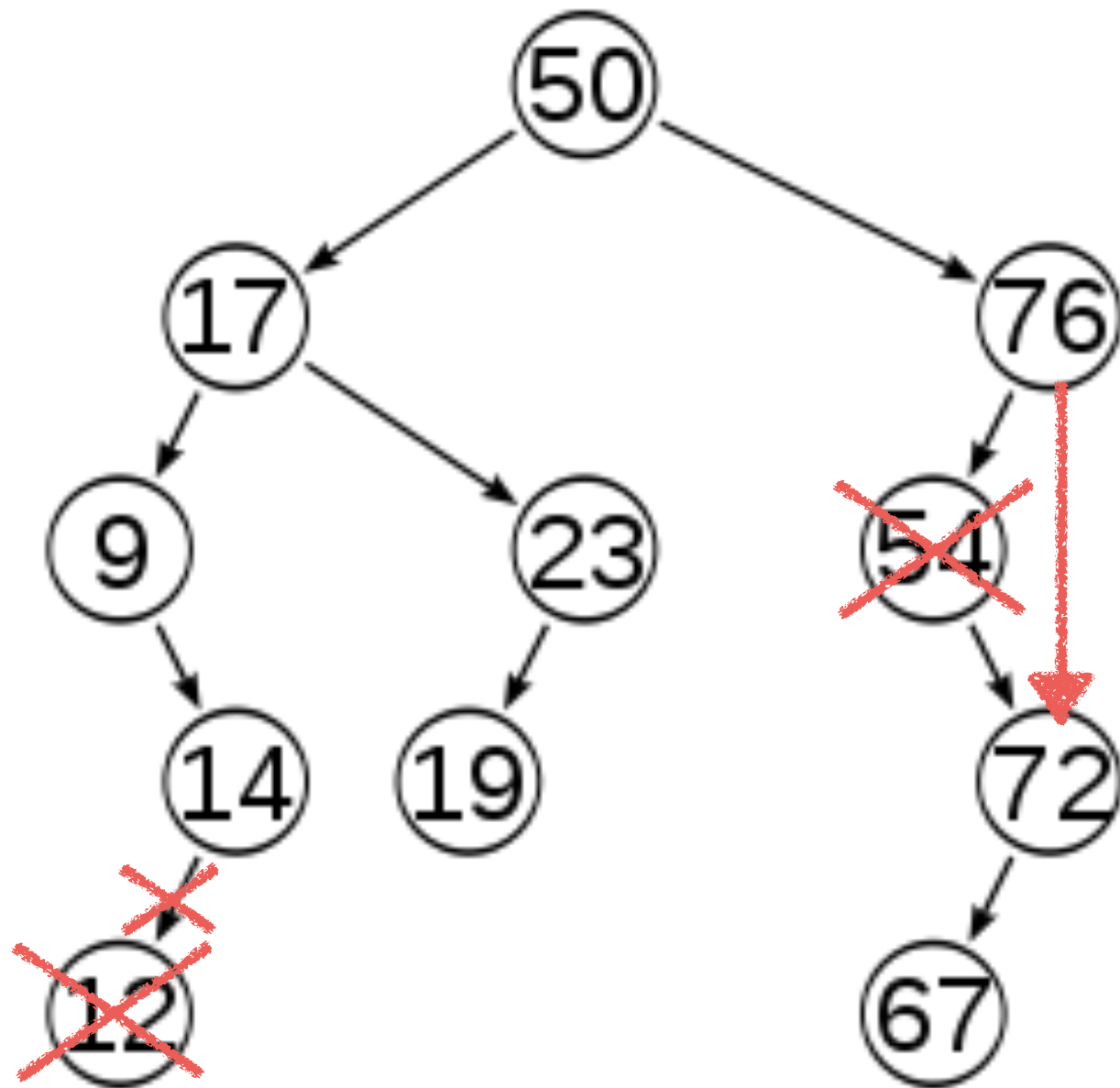
# To find successor (2/2)

- case 2: **no right child**
- go up towards the root
- stop when you are a left child
- your parent is the successor
- note: if you're never a left child and you reach the root, you had no successor



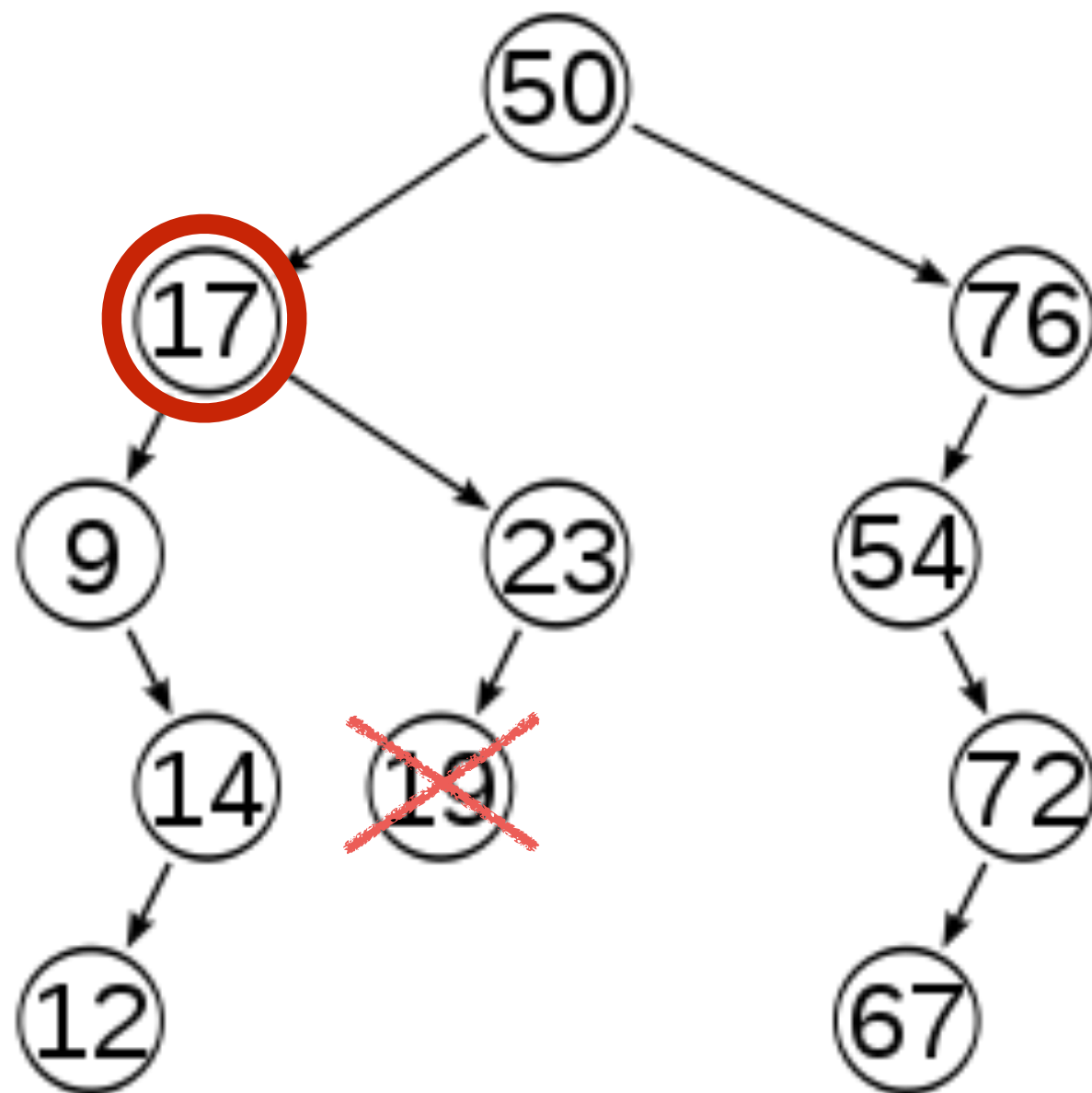
similar idea with finding predecessor

# To delete a node (1/2)



- case 1: **no children**
  - delete link parent->itself
- case 2: **one child**
  - relink parent and child

# To delete a node (2/2)



- case 3: **two children**
- find the node's successor
- **swap key** with successor
- delete successor

to delete 17, swap values 17 and 19 (or 14), then delete node that used to contain 19 (but now contains 17)

# Skiplists

For slides, go to

[https://www.cs.umd.edu/class/spring2008/cmsc420/  
L12.SkipLists.pdf](https://www.cs.umd.edu/class/spring2008/cmsc420/L12.SkipLists.pdf)

# Recap: BST vs skiplists

today

today

later: red-black, AVL, treaps, ...

today

**sorted set operations**

**BST (h means height)**

**unbalanced BST ( $h = O(n)$ )**

**balanced BST ( $h = O(\log n)$ )**

**skiplists**

add/delete

$O(h)$

$O(n)$

$O(\log n)$  +  
time to rebalance

$2 \log_2 n$

search

$O(h)$

$O(n)$

$O(\log n)$

$2 \log_2 n$

predecessor/  
successor

$O(h)$

$O(n)$

$O(\log n)$

$2 \log_2 n$

worst-case

worst-case

worst-case

on expectation,  
and with high  
probability