

HW - 6 Becerra

Saturday, February 20, 2021 10:11 PM

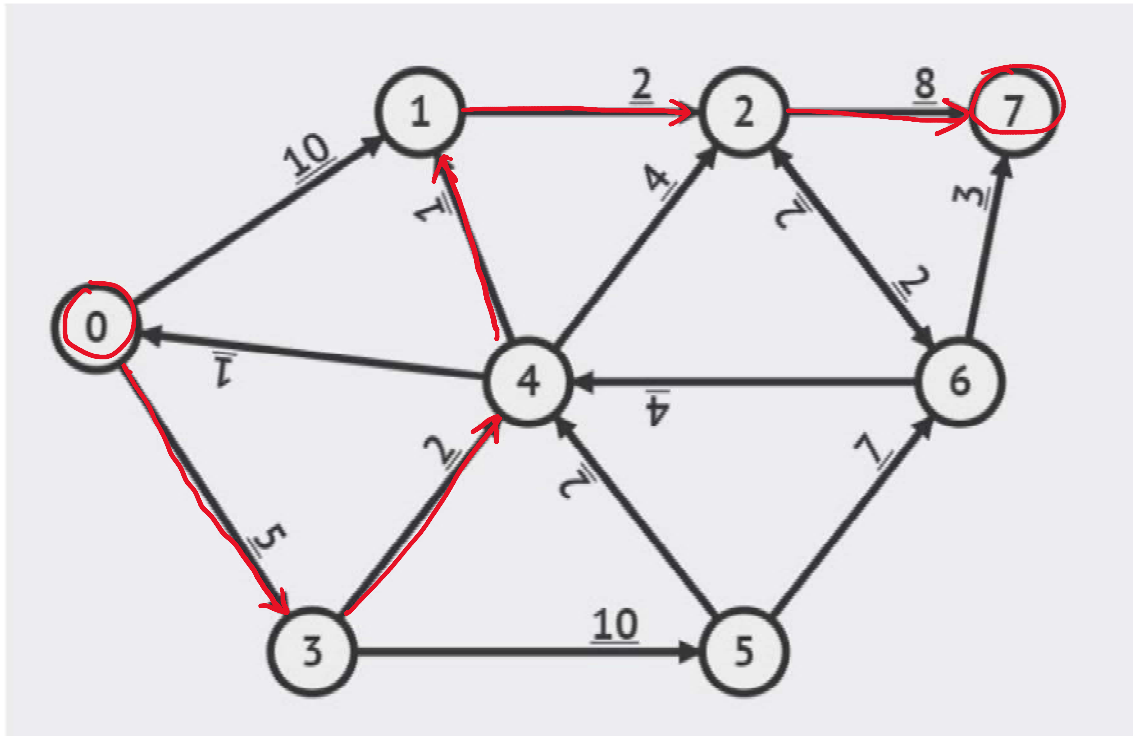
Problem 1

Objective function = $\max dt$

Constraints =

$$ds = 0$$

$$dv - du \leq w(u, v) \quad \forall (u, v) \in E$$



a -

The shortest distance from a source vertex "s" to a terminal vertex "t" is found by taking all possible solutions in terms of the distances between s and t, and finding the smallest

$$d7 = \{0, 3, 4, 1, 2, 7\}$$

$$d7 = 5 + 2 + 1 + 2 + 8 = 18$$

b -

$$d1 = \{3, 4, 1\}$$

$$d1 = 5 + 2 + 1 = 8$$

$$d2 = \{3, 4, 1, 2\}$$

$$d2 = 5 + 2 + 1 + 2 = 10$$

$$d3 = \{3\}$$

$$d3 = 5$$

$$d4 = \{3, 4\}$$

$$d4 = 5 + 2 = 7$$

$$d5 = \{3, 5\}$$

$$d5 = 5 + 10 = 15$$

$$d6 = \{3, 4, 2, 6\}$$

$$d6 = 5+2+4+2 = 13$$

Problem 2

Constraints -

Minimum amount sold per tie per month

$$6000 \leq s \leq 7000$$

$$10000 \leq p \leq 14000$$

$$13000 \leq b \leq 16000$$

$$6000 \leq c \leq 8500$$

Material used per type per month

$$0.125s \leq 1000$$

$$0.08p + 0.05b + 0.03c \leq 2000$$

$$0.05b + 0.07c \leq 1250$$

Objective -

Max p

$$p = s(6.70 - 0.75 - (0.125 \cdot 20)) + p(3.55 - 0.75 - (0.08 \cdot 6)) + b(4.31 - 0.75 - (0.05 \cdot 6 + 0.05 \cdot 9)) + c(4.81 - 0.75 - (0.03 \cdot 6 + 0.07 \cdot 9))$$

$$p = s(3.45) + p(2.32) + b(2.81) + c(3.25)$$

Profit:	\$ 120,196.00	
Type of tie	Profit per tie	Number of ties
Silk(s)	\$ 3.45	7000
Polyester(p)	\$ 2.32	13625
Blend 1(b)	\$ 2.81	13100
Blend 2(c)	\$ 3.25	8500
Total ties		42225

Excel file named "maximizeProfitsTies"

Problem 3

a -

i -

Objective

Minimize calories

$$\min (\text{calories} = t(21) + l(16) + s(40) + c(41) + ss(585) + st(120) + cp(164) + o(884))$$

Constraints

$$\text{protein} \geq 15g$$

$$2g \leq \text{fat} \leq 8g$$

$$\text{carbs} \geq 4g$$

$$\text{sodium} \leq 200mg$$

$$\text{spinach} + \text{lettuce} \geq 40\%$$

ii -

Included in Excel file named "minimizeCalories"

iii -

Total Calories	114.75		Total Cost	\$ 2.33				
Ingredients	Calories	Protein(g)	Fat(g)	Carb(g)	Sodium(mg)	cost(100g)		Servings
tomato	21	0.85	0.33	4.64	9	\$ 1.00		0
lettuce	16	1.62	0.2	2.37	28	\$ 0.75		0.585480711
spinach	40	2.86	0.39	3.63	65	\$ 0.50		0
carrot	41	0.93	0.24	9.58	69	\$ 0.50		0
sunflower seeds	585	23.4	48.7	15	3.8	\$ 0.45		0
smoked tofu	120	16	5	3	120	\$ 2.15		0.878220078
chickpeas	164	9	2.6	27	78	\$ 0.95		0
oil	884	0	100	0	0	\$ 2.00		0

b-

i -

Objective

Minimize cost

$$\min (\text{cost} = t(1) + l(.75) + s(.5) + c(.5) + ss(.45) + st(2.15) + cp(.95) + o(2))$$

Constraints

$$\text{protein} \geq 15g$$

$$2g \leq \text{fat} \leq 8g$$

$$\text{carbs} \geq 4g$$

$$\text{sodium} \leq 200mg$$

$$\text{spinach} + \text{lettuce} \geq 40\%$$

ii -

Included in Excel file named "minimize cost"

iii -

Total Calories	278.49		Total Cost	\$ 1.55				
Ingredients	Calories	Protein(g)	Fat(g)	Carb(g)	Sodium(mg)	cost(100g)		Servings
tomato	21	0.85	0.33	4.64	9	\$ 1.00		0
lettuce	16	1.62	0.2	2.37	28	\$ 0.75		0
spinach	40	2.86	0.39	3.63	65	\$ 0.50		0.832298354
carrot	41	0.93	0.24	9.58	69	\$ 0.50		0
sunflower seeds	585	23.4	48.7	15	3.8	\$ 0.45		0.096083302
smoked tofu	120	16	5	3	120	\$ 2.15		0
chickpeas	164	9	2.6	27	78	\$ 0.95		1.152364159
oil	884	0	100	0	0	\$ 2.00		0

Problem 4

Objective-

$$\min \text{fridge}$$

constraints -

$$p1w1 + p1w2 + p1w3 = 150$$

$$p2w1 + p2w2 + p2w3 = 450$$

$$p3w1 + p3w2 + p3w3 = 250$$

$$p4w1 + p4w2 + p4w3 = 150$$

Max Refrigerators

Total Cost	\$ 17,100.00							
Cost	W1	W2	W3					
P1	10	15	100000					
P2	11	8	100000					
P3	13	8	9					
P4	100000	14	8					
Cost	R1	R2	R3	R4	R5	R6	R7	
W1	5	6	7	10	100000	100000	100000	
W2	100000	100000	12	8	10	14	100000	
W3	100000	100000	100000	14	12	12	6	
Supply to Warehouse	W1	W2	W3					
P1	150	0	0	150				
P2	200	250	0	450				
P3	0	150	100	250				
P4	0	0	150	150				
	350	400	250					
Supply from Warehouse	R1	R2	R3	R4	R5	R6	R7	
W1	100	150	100	0	0	0	0	350
W2	0	0	0	200	200	0	0	400
W3	0	0	0	0	0	150	100	250
	100	150	100	200	200	150	100	