

# Lean Certificate Excerpt (CKM + Neutrino Sector)

This page is a 1-to-1 mirror of the Lean certificate fields.

## Lean sources:

`IndisputableMonolith/Verification/CKMCert.lean`

`IndisputableMonolith/Verification/NeutrinoSectorCert.lean`

## CKM certificate (`CKMCert.Cert`)

- `vcb_geometric_origin`:  $V_{cb}^{\text{geom}} = \frac{1}{2 \cdot \text{cube\_edges}(3)}$  (hence = 1/24).
- `vcb_match`:  $|V_{cb}^{\text{pred}} - 0.04182| < 0.00085$ .
- `alpha_lower_bound`:  $0.00729 < \alpha$ .
- `alpha_upper_bound`:  $\alpha < 0.00731$ .
- `phi_inv3_lower_bound`:  $0.2360 < \phi^{-3}$ .
- `phi_inv3_upper_bound`:  $\phi^{-3} < 0.2361$ .
- `vub_match`:  $|V_{ub}^{\text{pred}} - 0.00369| < 0.00011$ .
- `vus_match`:  $|V_{us}^{\text{pred}} - 0.22500| < 0.00067$ .

## Neutrino sector certificate (`NeutrinoSectorCert.Cert`)

- `nu3_bounds`:  $0.04987 < m_3^{\text{pred}} < 0.04993$  eV.
- `nu2_bounds`:  $0.00924 < m_2^{\text{pred}} < 0.00928$  eV.
- `nu1_bounds`:  $0.00352 < m_1^{\text{pred}} < 0.00355$  eV.
- `dm2_21_in_nufit_1sigma`:  $7.21 \times 10^{-5} < \Delta m_{21}^2{}^{\text{pred}} < 7.62 \times 10^{-5}$  eV<sup>2</sup>.
- `dm2_31_in_nufit_2sigma`:  $2.455 \times 10^{-3} < \Delta m_{31}^2{}^{\text{pred}} < 2.567 \times 10^{-3}$  eV<sup>2</sup>.
- `dm2_ratio_phi7`:  $\frac{(\phi^{r_3})^2}{(\phi^{r_2})^2} = \phi^7$  (exact, structural).
- `theta13_match`:  $|\sin^2 \theta_{13}^{\text{pred}} - 0.022| < 0.002$ .
- `theta12_match`:  $|\sin^2 \theta_{12}^{\text{pred}} - 0.307| < 0.01$ .
- `theta23_match`:  $|\sin^2 \theta_{23}^{\text{pred}} - 0.546| < 0.01$ .
- `jarlskog_match`:  $|J^{\text{pred}} - 3.08 \times 10^{-5}| < 0.6 \times 10^{-5}$ .
- `jarlskog_pos`:  $J^{\text{pred}} > 0$ .