

**Problem 1.1 – Streamlines.** Consider the flow given by

$$\mathbf{u} = [x, x(x - 1)(y + 1), 0].$$

Find an equation for the streamlines of the flow and plot them.

---

**Solution by Mohammed Muddassir**

We start by parameterizing the streamline curve and comparing the velocity equations such that:

$$\frac{dx/d\xi}{u} = \frac{dy/d\xi}{v} \quad (Eq\ 1.7)$$

Since  $\mathbf{u}$  describes two dimensional flow, we can ignore the  $w$  and  $z$  components.

We can simplify by multiplying by  $d\xi$  on both sides. And after substituting the corresponding equations for  $u$  and  $v$ , we have:

$$\frac{dx}{x} = \frac{dy}{x(x - 1)(y + 1)}.$$

After separating variables and simplifying,

$$(x - 1)dx = \frac{dy}{y + 1}.$$

Now we integrate both sides:

$$\int (x - 1) dx = \int \frac{dy}{y + 1},$$

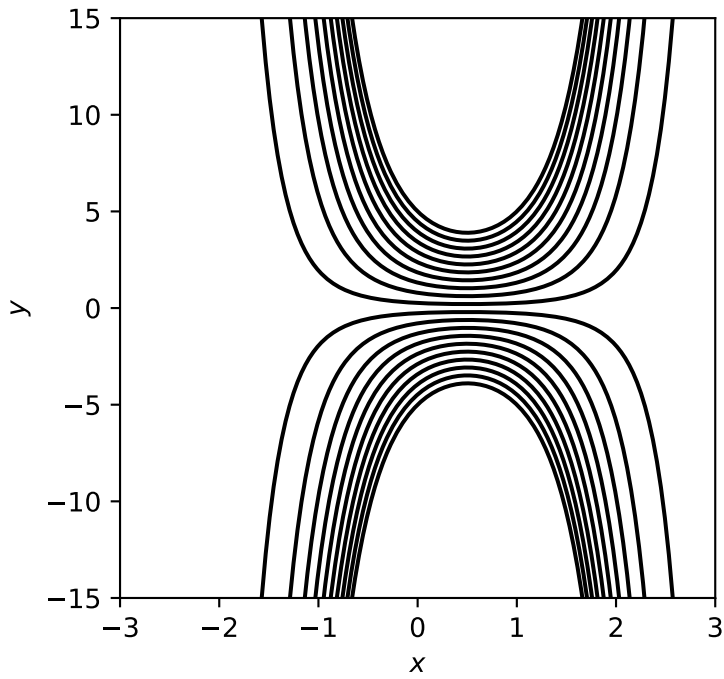
$$x^2 - x + c = \ln(y + 1),$$

with  $c$  as the integration constant, and solve for  $y$ ,

$$y = Ae^{x^2 - x} - 1$$

where  $A = e^c$ .

You can use python or any other method to produce the plot.



**Figure 0.1:** Streamline Plot for Problem 1.1