

1.

```
1 import itertools
2 Ω = list(itertools.product({"K", "Z"}, repeat=5))
3 print(f"Ω={Ω}")
4 E = [ω for ω in Ω if ω.count("K") == 2]
5 print(f"E={E}")
6 print(f"{len(E)} von {len(Ω)}")
7 print(f"p = {len(E)/len(Ω)}")
8
```

Ω=[('K', 'K', 'K', 'K', 'K'), ('K', 'K', 'K', 'K', 'Z'), ('K', 'K', 'K', 'Z', 'K'), ('K', 'K', 'K', 'Z', 'Z'), ('K', 'K', 'Z', 'K', 'K'), ('K', 'K', 'Z', 'K', 'Z'), ('K', 'K', 'Z', 'Z', 'K'), ('K', 'K', 'Z', 'Z', 'Z'), ('K', 'Z', 'K', 'K', 'K'), ('K', 'Z', 'K', 'K', 'Z'), ('K', 'Z', 'K', 'Z', 'K'), ('K', 'Z', 'K', 'Z', 'Z'), ('K', 'Z', 'Z', 'K', 'K'), ('K', 'Z', 'Z', 'K', 'Z'), ('K', 'Z', 'Z', 'Z', 'K'), ('K', 'Z', 'Z', 'Z', 'Z'), ('Z', 'K', 'K', 'K', 'K'), ('Z', 'K', 'K', 'K', 'Z'), ('Z', 'K', 'K', 'Z', 'K'), ('Z', 'K', 'K', 'Z', 'Z'), ('Z', 'K', 'Z', 'K', 'K'), ('Z', 'K', 'Z', 'K', 'Z'), ('Z', 'K', 'Z', 'Z', 'K'), ('Z', 'K', 'Z', 'Z', 'Z'), ('Z', 'Z', 'K', 'K', 'K'), ('Z', 'Z', 'K', 'K', 'Z'), ('Z', 'Z', 'K', 'Z', 'K'), ('Z', 'Z', 'K', 'Z', 'Z'), ('Z', 'Z', 'Z', 'K', 'K'), ('Z', 'Z', 'Z', 'K', 'Z'), ('Z', 'Z', 'Z', 'Z', 'K'), ('Z', 'Z', 'Z', 'Z', 'Z')]
E=[('K', 'K', 'Z', 'Z', 'Z'), ('K', 'Z', 'K', 'Z', 'Z'), ('K', 'Z', 'Z', 'K', 'Z'), ('K', 'Z', 'Z', 'Z', 'K'), ('Z', 'K', 'K', 'Z', 'Z'), ('Z', 'K', 'Z', 'K', 'Z'), ('Z', 'K', 'Z', 'Z', 'K'), ('Z', 'Z', 'K', 'K', 'Z'), ('Z', 'Z', 'K', 'K', 'Z'), ('Z', 'Z', 'K', 'Z', 'K'), ('Z', 'Z', 'K', 'Z', 'Z'), ('Z', 'Z', 'Z', 'K', 'K'), ('Z', 'Z', 'Z', 'K', 'Z'), ('Z', 'Z', 'Z', 'Z', 'K'), ('Z', 'Z', 'Z', 'Z', 'Z')]
10 von 32
p = 0.3125

- a.) Eine faire Münze mit den Seiten „Kopf“ und „Zahl“ wird 5-mal hintereinander geworfen. Berechne die Wahrscheinlichkeit, dass genau 2-mal Kopf geworden wird
- b.) Mittels Kombinatorik ermittelt man die Anzahl an möglichen Ereignissen und dividiert diese durch die Anzahl aller Ereignisse. Daraus folgt die Formel

$$\frac{\binom{5}{2}}{2^5}$$

c.) Leider habe ich es nicht geschafft das System zum Laufen zu bringen.

```
Python Run ▶

1 import itertools
2 Ω = list(itertools.product("K", "Z", repeat=5))
3 Ω = {"".join(Ausgang) for Ausgang in Ω}
4 print(f"Ω={Ω}")
5 E = [ω for ω in Ω if ω.count("K") == 2]
6 print(f"E={E}")
7 print(f"{len(E)} von {len(Ω)}")
8 print(f"p = {len(E)/len(Ω)}")
9
```

File "main.py", line 4  
print(f"Ω={Ω}")  
^  
SyntaxError: invalid syntax  
❗

```
1 import itertools
2 Ω = list(itertools.product("K", "Z", repeat=5))
3 #Ω = {"".join(Ausgang) for Ausgang in Ω}
4 print(f"Ω={Ω}")
5 E = [ω for ω in Ω if ω.count("K") == 2]
6 print(f"E={E}")
7 print(f"{len(E)} von {len(Ω)}")
8 print(f"p = {len(E)/len(Ω)}")

Ω=[('K', 'K', 'K', 'K', 'K'), ('K', 'K', 'K', 'K', 'Z'), ('K', 'K', 'K', 'Z', 'K'), ('K', 'K', 'K', 'Z', 'Z'), ('K', 'K', 'Z', 'K', 'K'), ('K', 'K', 'Z', 'K', 'Z'), ('K', 'K', 'Z', 'Z', 'K'), ('K', 'K', 'Z', 'Z', 'Z'), ('K', 'Z', 'K', 'K', 'K'), ('K', 'Z', 'K', 'K', 'Z'), ('K', 'Z', 'K', 'Z', 'K'), ('K', 'Z', 'K', 'Z', 'Z'), ('K', 'Z', 'Z', 'K', 'K'), ('K', 'Z', 'Z', 'K', 'Z'), ('K', 'Z', 'Z', 'Z', 'K'), ('K', 'Z', 'Z', 'Z', 'Z'), ('Z', 'K', 'K', 'K', 'K'), ('Z', 'K', 'K', 'K', 'Z'), ('Z', 'K', 'K', 'Z', 'K'), ('Z', 'K', 'K', 'Z', 'Z'), ('Z', 'K', 'Z', 'K', 'K'), ('Z', 'K', 'Z', 'K', 'Z'), ('Z', 'K', 'Z', 'Z', 'K'), ('Z', 'K', 'Z', 'Z', 'Z'), ('Z', 'Z', 'K', 'K', 'K'), ('Z', 'Z', 'K', 'K', 'Z'), ('Z', 'Z', 'K', 'Z', 'K'), ('Z', 'Z', 'K', 'Z', 'Z'), ('Z', 'Z', 'Z', 'K', 'K'), ('Z', 'Z', 'Z', 'K', 'Z'), ('Z', 'Z', 'Z', 'K', 'Z'), ('Z', 'Z', 'Z', 'Z', 'K'), ('Z', 'Z', 'Z', 'Z', 'Z')]
E=[('K', 'K', 'Z', 'Z', 'Z'), ('K', 'Z', 'K', 'Z', 'Z'), ('K', 'Z', 'Z', 'K', 'Z'), ('K', 'Z', 'Z', 'Z', 'K'), ('Z', 'K', 'K', 'Z', 'Z'), ('Z', 'K', 'K', 'Z', 'Z'), ('Z', 'K', 'Z', 'K', 'Z'), ('Z', 'K', 'Z', 'K', 'Z'), ('Z', 'K', 'Z', 'Z', 'K'), ('Z', 'K', 'Z', 'Z', 'Z'), ('Z', 'Z', 'K', 'K', 'Z'), ('Z', 'Z', 'K', 'K', 'Z'), ('Z', 'Z', 'K', 'Z', 'K'), ('Z', 'Z', 'K', 'Z', 'Z'), ('Z', 'Z', 'Z', 'K', 'K'), ('Z', 'Z', 'Z', 'K', 'Z'), ('Z', 'Z', 'Z', 'Z', 'K'), ('Z', 'Z', 'Z', 'Z', 'Z')]
10 von 32
p = 0.3125
```

2.

```
1 import itertools
2 Ω = set(itertools.product({"K", "Z"}, repeat=5))
3 Erwartungswert = 0
4 for ω in Ω:
5     Erwartungswert = Erwartungswert + ω.count("K")
6 Erwartungswert = Erwartungswert / len(Ω)
7 print(f"Erwartungswert = {Erwartungswert}")
8 print(len(Ω))
```

```
Erwartungswert = 2.5
32
❖
```

Ich habe die 8. Zeile hinzugefügt um den Befehl `len(Ω)` besser zu verstehen.

a)  $X$  ist die Menge der ZV {Kopf, Zahl}.

b) Der Erwartungswert ist die Summe aller Möglichkeiten multipliziert mit deren Wahrscheinlichkeit.

$$E(X) = \sum_{i=0}^n x_i \cdot P(X=x_i)$$

In diesem Fall (Binomialverteilung) kann man auch die Formel verwenden:

$$E = n \cdot p$$

```

1 import itertools
2  $\Omega$  = set(itertools.product({"K", "Z"}, repeat=10))
3 Erwartungswert = 0
4 for  $\omega$  in  $\Omega$ :
5     Erwartungswert = Erwartungswert +  $\omega$ .count("K")
6 Erwartungswert = Erwartungswert / len( $\Omega$ )
7 print(f"Erwartungswert = {Erwartungswert}")
8 print(len( $\Omega$ ))

```

```

Erwartungswert = 5.0
1024

```

```

1 import itertools
2  $\Omega$  = set(itertools.product({"K", "Z"}, repeat=2))
3 Erwartungswert = 0
4 for  $\omega$  in  $\Omega$ :
5     Erwartungswert = Erwartungswert +  $\omega$ .count("K")
6 Erwartungswert = Erwartungswert / len( $\Omega$ )
7 print(f"Erwartungswert = {Erwartungswert}")
8 print(len( $\Omega$ ))

```

```

Erwartungswert = 1.0
4

```

c)

```
1 import itertools
2  $\Omega$  = set(itertools.product({"K", "Z"}, repeat=5))
3 Erwartungswert = 0
4 for  $\omega$  in  $\Omega$ :
5     Erwartungswert = Erwartungswert +  $\omega$ .count("K")
6 Erwartungswert = Erwartungswert / len( $\Omega$ )
7 Varianz = Erwartungswert*(0.5)
8 print(f"Varianz = {Varianz}")
9 print( len( $\Omega$ ))
```

Varianz = 1.25

32

❖ []