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function Correlation = CorrelationOfAdjacentPixels(Image)

%Chooses 6000 random pairs of adjacent pixels and computes correlation
  of
%the pair

Width = size(Image,1);
Height = size(Image,2);
PixelCouplesSample = 6000;

%Generates first point coordinates
x1 = randi(Width,1,PixelCouplesSample);
y1 = randi(Height,1,PixelCouplesSample);
%Generates second point coordinates keeping track of periodic boundary
%conditions
x2 = mod(x1+1,Width+1)+(x1==Width);
y2 = mod(y1+1,Height+1)+(y1==Height);

%Collects pixel values
FirstPixel = zeros(1,PixelCouplesSample);
SecondPixel = zeros(1,PixelCouplesSample);
for i = 1:PixelCouplesSample
    FirstPixel(i) = Image(x1(i),y1(i));
    SecondPixel(i) = Image(x2(i),y2(i));
end

Correlation = corr2(FirstPixel,SecondPixel);

end

```

```

function EncryptedImage = Encrypter(Image,Sequence,Rule,Iterations)

%Encrypts given image by permutating its pixel values according to
%evolution of Game of Life cellular Automata generated from given
%password via logistic map

%Generates board starting rounding pseudorandom sequence
Board = reshape(round(Sequence),size(Image));

%Records History
AlreadyOn = zeros(size(Image));
NewOrder = [];
for t = 1:Iterations
    NewlyOn = xor(Board,AlreadyOn) & Board;
    NewOrder = cat(1,NewOrder,find(NewlyOn));
    AlreadyOn = AlreadyOn | Board;
    Board = Evolve(Board,Rule);
end
NewOrder = cat(1,NewOrder,find(~AlreadyOn));

PartiallyEncrypted = reshape(Image(NewOrder),size(Image))';
EncryptedImage = reshape(PartiallyEncrypted(NewOrder),size(Image))
;

end

```

```

function NewBoard = Evolve(OldBoard,Rule)

%Evolves board of 2d cellular automata according to chosen rule,
    assuming
%periodic boundary conditions

switch Rule
    case 'Life'
        %Number of neighboring cells required for a dead cell to turn
            alive
        Birth = 3;
        %Number of neighboring cells required for an alive cell to
            survive
        Survival = [2 3];
    case 'Fredkin' %Chaotic rule, fill percentage converges to 50%
        Birth = 1:2:7;
        Survival = 0:2:8;
end

%Last column will be counted as adjacent to the first column, etc.
PeriodicBoard = ...
    [OldBoard(end,end), OldBoard(end,:),OldBoard(end,1)
    OldBoard(:,end),OldBoard,OldBoard(:,1)
    OldBoard(1,end), OldBoard(1,:), OldBoard(1,1)];

%Neighbors are positions reachable by a King
MooreNeighborhood = [1 1 1; 1 0 1; 1 1 1];
%Gives number of alive neighbors of each cell
Neighbors = conv2(PeriodicBoard, MooreNeighborhood, 'same');
%Modifies a cell state according to how many alive neighbors it has
NewBoard = ...
    ismember(Neighbors,Birth).*(1-PeriodicBoard)+...
    ismember(Neighbors,Survival).*PeriodicBoard;

%Removes the boundary copies
NewBoard = NewBoard(2:end-1,2:end-1);

end

```

```

function Sequence = LogisticRandomSequence(Length,Mu,X0)
%Generates random sequences of floats between 0 and 1 using logistic
  map
%with seed 3.9 < Mu < 4.0 and 0 < X0 < 1

Sequence = zeros(1,Length);
Sequence(1) = X0;
for i=1:Length-1
    Sequence(i+1) = Mu*Sequence(i)*(1-Sequence(i));
end

end

```

```

clc
close all
clear

RGBImage = imread('dogs.jpeg');
Image = rgb2gray(RGBImage);
Height = size(Image,1);
Width = size(Image,2);
Simulations = 1e3;
KeySensitivity = zeros(Simulations,2);
tic
for Iterations=[1000]
    filename = sprintf("KeySens%dSim%dIt.mat",Simulations,Iterations);
    for i=1:Simulations
        %% Encryption
        Password = [3.9+0.1*rand(),rand()];
        Mu = Password(1); %Logistic Map parameter:  $3.9 < \mu < 4.0$ 
        X0 = Password(2); %Logistic Map initial value:  $0 < X_0 < 1$ 
        Sequence = LogisticRandomSequence(Height*Width,Mu,X0);

        LifeEncoded = Encrypter(Image,Sequence,'Life',Iterations);
        FredkinEncoded = Encrypter(Image,Sequence,'Fredkin',Iterations);

        %% Key sensitivity test

        PerturbedSequence = Sequence;
        ChangedIndex = randi(length(PerturbedSequence));
        PerturbedSequence(ChangedIndex) = 1-PerturbedSequence(ChangedIndex);

        PerturbedLifeEncoded = Encrypter(Image,PerturbedSequence,'Life',
            Iterations);
        PerturbedFredkinEncoded = Encrypter(Image,PerturbedSequence,'Fredkin',
            Iterations);

        KeySensitivity(i,:) = ...
            [corr2(LifeEncoded,PerturbedLifeEncoded),...
            corr2(FredkinEncoded,PerturbedFredkinEncoded)];
        disp(100*i/Simulations)
    end
    save(strcat('data/',filename))
end
toc

```

```

clc
close all
clear

RGBImage = imread('dogs.jpeg');
Image = rgb2gray(RGBImage);
Height = size(Image,1);
Width = size(Image,2);
Simulations = 1e3;
KeySensitivity = zeros(Simulations,2);
tic
for Iterations=[1,10,100]
    filename = sprintf("OldKeySens%dSim%dIt.mat",Simulations,
        Iterations);
    for i=1:Simulations
        %% Encryption
        Password = [3.9+0.1*rand(),rand()];
        Mu = Password(1); %Logistic Map parameter:  $3.9 < \mu < 4.0$ 
        X0 = Password(2); %Logistic Map initial value:  $0 < X_0 < 1$ 
        Sequence = LogisticRandomSequence(Height*Width,Mu,X0);

        LifeEncoded = Encrypter(Image,Sequence,'Life',Iterations);
        FredkinEncoded = Encrypter(Image,Sequence,'Fredkin',Iterations);

        %% Key sensitivity test
        PerturbedSequence = LogisticRandomSequence(Height*Width,Mu+eps,X0+eps)
            ;

        PerturbedLifeEncoded = Encrypter(Image,PerturbedSequence,'Life',
            Iterations);
        PerturbedFredkinEncoded = Encrypter(Image,PerturbedSequence,'Fredkin',
            Iterations);

        KeySensitivity(i,:) = ...
            [corr2(LifeEncoded,PerturbedLifeEncoded),...
            corr2(FredkinEncoded,PerturbedFredkinEncoded)];
        disp(100*i/Simulations)
    end
    save(strcat('data/',filename))
end
toc

```

%% Key sensitivity test

```
PerturbedSequence = Sequence;  
ChangedIndex = randi(length(PerturbedSequence));  
PerturbedSequence(ChangedIndex) = 1-PerturbedSequence(ChangedIndex);  
  
PerturbedLifeEncoded = Encrypter(Image,PerturbedSequence,'Life',  
    Iterations);  
PerturbedFredkinEncoded = Encrypter(Image,PerturbedSequence,'Fredkin',  
    Iterations);  
  
KeySensitivity(i,:) = ...  
    [corr2(LifeEncoded,PerturbedLifeEncoded),  
     corr2(FredkinEncoded,PerturbedFredkinEncoded)];
```