Working With Algebraic Data Types



- An approach to defining types that model certain patterns of data
 - Different to OO approach
 - Well suited to functional programming
- Product types
 - Based on the "has-a and" relationship
 - · A has a B and a C
- Sum types
 - Based on "is-a or" relationship
 - A is a B or a C
- Scala provides support for both of these

Product Types

- Models the "has-a and" relationship
- · Implement using case classes
 - · Cartesian product

```
case class Trade ( id: String, // A trade has an id side: String, // and a side sym: String, // and a symbol amount: Int, // and an amount unitPrice: Double // and a unitPrice
```

```
case class Person ( fName: String, // A person has a first name lName: String, age: Int // and a last name // and an age
```

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Sum Types

- Models the "is-a or" relationship
- Implement using sealed traits and subtypes

```
sealed trait User // A user
final case class Normal() extends User // is a normal user
final case class Privileged() extends User // or privileged
final case class Admin() extends User // or an admin user
```

```
sealed trait Account
final case class Current() extends Account
final case class Savings() extends User
final case class Investment() extends User
// or investment
```

Working With ADTs

- Code structure follows data structure
 - Product types straightforward
 - Scala.Product trait
- Sum types offer a choice
 - Traditional OO polymorphism?

```
sealed trait Account {
  def accountNo: String
}
final case class Current( accno: String ) extends Account {
  def accountNo = s"C${accno}"
}
final case class Savings ( accno: String ) extends Account {
  def accountNo = s"S${accno}"
}
final case class Investment ( accno: String ) extends Account {
  def accountNo = s"I${accno}"
}
```

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Working With ADTs

- Alternative approach to working with Sum Types is Structural Recursion
 - · Implemented using pattern matching

```
sealed trait Account {
  def accountNo = this match {
    case Current(anum) => s"C${anum}"
    case Savings(anum) => s"S${anum}"
    case Investment(anum) => s"I${anum}" }
}

final case class Current ( accno: String ) extends Account
  final case class Savings ( accno: String ) extends Account
  final case class Investment ( accno: String ) extends Account
```

OO Polymorphism or Structural Recursion?

- Different approaches suit different situations
 - · OO approach favours polymorphism
 - Functional approach favours structural recursion

	Add a new method	Add new data
00	Change existing code	No change to existing code
FP	No change to existing code	Change existing code

- OO approach handles data extensibility slightly better
 - New data types have localised functionality
- Functional approach handles functionality extensibility better
 - · New functionality added in base type only
- Scala supports both approaches

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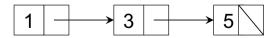
Recursive Types

- Many types can be defined as recursive sum types
 - Eg List of Int values

```
sealed trait IntList
final case object End extends IntList
final case class Cons ( head: Int,
tail: IntList )
extends IntList

// An IntList
// is empty
// or an Int,
// followed by an IntList
```

```
scala> val l1: IntList = Cons ( 1, Cons(3, Cons(5, End) ) )
l1: IntList = Cons(1,Cons(3,Cons(5,End)))
```



Recursive Types

Recursive sum types can be processed using structural recursion

Recursive Types

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• Different operations follow a similar pattern

```
def sum ( 1: IntList ): Int =
    l match {
    case End => 0
    case Cons(head, tail) => head + sum(tail)
}

def square( 1: IntList ): IntList =
    l match {
        case End => End
        case Cons(head, tail) => Cons(head * head, square(tail))
    }

scala> sum(l1)
    res6: Int = 9

scala> square(l1)
    res5: IntList = Cons(1,Cons(9,Cons(25,End)))

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```

5

Recursive Types

- Add operations to the type
 - FP approach

```
sealed trait IntList {
  def length: Int = this match {
    case End => 0
    case Cons(hd, tl) => 1 + tl.length
  }
  def sum: Int = this match {
    case End => 0
    case Cons(hd, tl) => hd + tl.sum
  }
}

final case object End extends IntList
  final case class Cons(hd: Int, tl: IntList) extends IntList
scala> val l1: IntList =
    Cons(1, Cons(3, Cons(5, End)))

l1: IntList = Cons(1, Cons(3, Cons(5, End)))
scala> l1.sum
res85: Int = 9
```

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Improving the Method Definitions

Abstract over repeated code

```
sealed trait IntList {
  def process (baseCase: Int, f: (Int, Int) => Int ): Int =
    this match {
    case End => baseCase
    case Cons(hd, tl) => f( hd, tl.process(baseCase, f) )
  }
}

final case object End extends IntList
final case class Cons(hd: Int, tl: IntList) extends IntList
```

Improving the Method Definitions

Abstract over repeated code

```
sealed trait IntList {
  def process (baseCase: Int, f: (Int, Int) => Int ): Int =
      this match {
      case End => baseCase
      case Cons(hd, tl) => f( hd, tl.process(baseCase, f) )
    }
  def sum: Int = process(0, (hd, tl) => hd + tl)
  def length: Int = process(0, (_, tl) => 1 + tl)
}
final case object End extends IntList
final case class Cons(hd: Int, tl: IntList) extends IntList
```

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Improving the Method Definitions

Abstract over repeated code

```
sealed trait IntList {
  def fold (baseCase: Int, f: (Int, Int) => Int ): Int =
    this match {
     case End => baseCase
     case Cons(hd, tl) => f( hd, tl.process(baseCase, f) )
  }
  def sum: Int = process(0, (hd, tl) => hd + tl)
  def length: Int = process(0, (_, tl) => 1 + tl)
}

final case object End extends IntList
final case class Cons(hd: Int, tl: IntList) extends IntList
```

Generalising the fold Method

- Currently we can only use fold for sum and length
 - Return type fixed as Int
- The square method cannot be implemented in this way
 - Return type is IntList
- Add type parameter to method definition

```
def fold[A] (baseCase: A, f:(Int, A) => A): A =
    this match {
    case End => baseCase
    case Cons(hd, tl) => f( hd, tl.fold(baseCase, f) )
    }
    def sum: Int = fold[Int](0, (hd, tl) => hd + tl)
    def square: IntList = fold[IntList](End, (hd, tl) => Cons(hd*hd, tl) )
    ...
```

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Generic Algebraic Data Types

ADTs can be parameterised like any other type

```
sealed trait MyList[A] {

...

Must be case class
as can't parameterise
an object

case class End[A]() extends MyList[A]

case class Cons[A]( hd: A, tl: MyList[A]) extends MyList[A]
```

```
scala> val ml1: MyList[String] = Cons("Hello", Cons("world", End()))
ml1: MyList[String] = Cons(Hello,Cons(world,End()))
scala> val ml2: MyList[Int] = Cons(2, Cons(4, Cons(6, End() ) )
ml2: MyList[Int] = Cons(2,Cons(4,Cons(6,End())))
```

Fold for Generic ADT

- Possible to generalise fold method for generic ADTs
 - Not all methods can be implemented
 - Length works as always returns Int

```
sealed trait MyList[A] {

def fold[B] ( end: B, f: (A, B) => B ): B =
    this match {
    case End() => end
    case Cons(hd, tl) => f( hd, tl.fold(end, f) )
    }

def length = fold [Int]( 0, (_, b) => 1 + b )

scala> ml1.length
    res89: Int = 2

scala> ml2.length
    res90: Int = 3
```

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Fold for Generic ADT

• We can use fold directly to implement other functionality

```
scala> ml2.fold[Int] (0, (a,b) => a + b)
res92: Int = 12
scala> ml1.fold[String] ( "", (a,b) => s"$a $b" )
res93: String = "Hello world "
```

- Notice we must explicitly instantiate the type parameter
 - Type inference in the compiler unable to work out correct type

Fold for Generic ADT

- It is possible to help type inference
 - Use multiple argument lists in function

```
def fold[B] (end: B) (f: (A, B) => B ): B =
    this match {
    case End() => end
    case Cons(hd, tl) => f( hd, tl.fold(end)(f) )
}

def length = fold [Int](0) ((_, b) => 1 + b )
...

scala> ml1.fold("")( (a,b) => s"$a $b" )
    res97: String = "Hello world "

scala> ml2.fold(0)( (a,b) => a + b )
    res98: Int = 12
```

Generic ADTs as Containers

ADT can be used to represent a simple container type

```
sealed trait Box[A]
final case class Empty[A]() extends Box[A]
final case class Full[A](value: A) extends Box[A]
```

• A Box is either

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- Empty
- Full, containing a value of type A
- Like type Option[T]
- What does fold mean for such a type?

Using fold on Generic Container ADT

- Structural recursion can be applied to container types
 - Fold method will still work

```
scala> val emptyBox: Box[Int] = Empty()
emptyBox: Box[Int] = Empty()

scala> val fullBox: Box[Int] = Full(10)
fullBox: Box[Int] = Full(10)

scala> emptyBox.fold(-1)(i => i)
res100: Int = -1

scala> fullBox.fold(-1)(i => i)
res101: Int = 10

scala> emptyBox.fold(-1)(i => i + 3 )
res104: Int = -1

scala> fullBox.fold(-1)(i => i + 3)
res102: Int = 13
```