

- 시스템의 출력 (영입력 응답 + 영상태 응답)

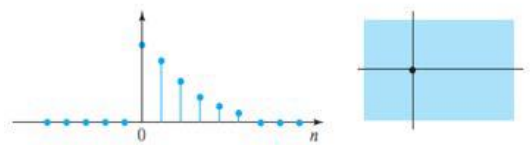
$$y(n) = y_{ZI}(n) + y_{ZS}(n) \\ = (C_0\lambda_0^n + C_1\lambda_1^n + \dots)u(n) + h(n) * x(n)$$

$$a^n u(n) * b^n u(n) = \frac{a^{n+1} - b^{n+1}}{a - b} u(n)$$

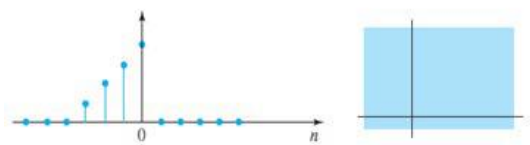
- z-Transform

$$Z\{x(n)\} = X(z) = \sum_{n=-\infty}^{\infty} x(n)z^{-n}$$

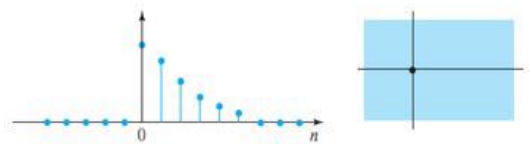
- ROC



Causal: All z-plane except $z = 0$



Non-causal: All z-plane except $z = \infty$



Causal & Non-causal: All z-plane except $z = 0$ and ∞

- Properties of z-T

$$Z\{a_1x_1(n) + a_2x_2(n)\} = a_1X_1(z) + a_2X_2(z)$$

$$Z\{x(n-k)\} = z^{-k}X(z)$$

$$Z\{a^n x(n)\} = X(a^{-1}z)$$

$$Z\{nx(n)\} = -z \frac{d}{dz} X(z)$$

$$Z\{x_1(n) * x_2(n)\} = X_1(z)X_2(z)$$

- z-T Table

$Z\{\delta(n)\}$	=	1
$Z\{\delta(n-m)\}$	=	z^{-m}
$Z\{u(n)\}$	=	$\frac{z}{z-1}$
$Z\{a^n\}$	=	$\frac{z}{z-a}$

- Transfer Function

$$y(n) = h(n) * x(n) \xrightarrow{Z} Y(z) = H(z)X(z) \rightarrow H(z) = \frac{Y(z)}{X(z)}$$

- z-T Zero(영점) Pole(극점)

Zero: $H(z) = 0$ 을 만족하는 z 값들

Pole: $H(z) = \infty$ 를 만족하는 z 값들

- 단방향 Properties of z-T

$$Z\{x(n-k)\} = z^{-k} \left[X(z) + \sum_{n=1}^k x(-n)z^n \right], k > 0$$

$$Z\{x(n+k)\} = z^k \left[X(z) - \sum_{n=1}^{k-1} x(n)z^{-n} \right], k > 0$$

- 연속시간 Fourier Series

$$x(t) = \sum_{k=-\infty}^{\infty} c_k e^{j2\pi k F_0 t}$$

$$c_k = \frac{1}{T} \int_{-0.5T}^{0.5T} x(t) e^{-j2\pi F_0 t} dt$$

- Power Spectrum Density (PSD)

$$P = \frac{1}{T} \int_{-0.5T}^{0.5T} |x(t)|^2 dt = \sum_{k=-\infty}^{\infty} |c_k|^2$$

- a

- a

-