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Group 5

1 Problem Definition

Predictive Policing is defined as "the application of analytical techniques, particularly quantitative techniques, to identify likely targets for police intervention and prevent crime or solve past crimes by making statistical predictions." [9]. Considering the research subject, it can be categorized into four main classes, which are Predicting Places of Increased Crime Risk, Predicting Potential Offenders, Predicting Group/Population Crime Patterns and Predicting Potential Victims.

2 Existing Systems and Modelling Approaches

Depending on different perspecitives, the prediction can be either place-based or people-based, or a combination of both. Place-based prediction focuses on the relationship between geographic locations and crime rates, which is effective but proved to be biased against racial minorities and would possibly lead to negative loops[1]. People-based prediction, on the other hand, aims to identify individuals or groups at high risk of committing or being victims of crime, which is also controversial due to ethical concerns, such as privacy and discrimination. Currently many of PredPol[5, 4], Chicago's Strategic Subject List (SSL)[14], Risk Terrain Modeling (RTM)[3], Real-Time Crime Centers (RTCC)[11], HunchLab[10], etc. are widely used in the U.S. and other countries.

2.1 Place-Based: PredPol (Geolitica)

Modelling Methods PredPol[5, 4], introduced around 2012, is one of the most commonly implemented predictive policing systems in the U.S.[8] and thus usually singled out in discussions. It learns from physical phenomena like chemical reactions as well as earthquakes and aftershocks to predict place-based or hotspot crime. Specifically, PredPol perceives crimes as contagions that spread from one location to another, similar to earthquakes and aftershocks, while adding "hotspot policing" could inhibit the process like in a chemical reaction. Two core mathematical ideas behind these are the reaction-diffusion model[13, 12] and the Epidemic-Type Aftershock Sequence (ETAS) model[7]. More details are listed below.

Reaction-Diffusion Model[13, 12] It assumes that crime spreads from one location to another similar to how chemicals diffuse in a liquid. We can model the risk of a site s being attacked at time t as:

$$B_s(t+\delta t) = \left[B_s(t) + \frac{\eta \ell^2}{z} \Delta B_s(t) \right] (1 - \omega \delta t) + \theta E_s(t)$$
 (1)

and discret Laplacian $\Delta B_s(t)$ means the tre crime would spread to its neighbors, also known as broken window effect.

$$\Delta B_s(t) = \frac{1}{\ell^2} \left(\sum_{s' \sim s} B_{s'}(t) - z B_s(t) \right) \tag{2}$$

Here ω is the time scale over which repeat victimizations are most likely. θ is the multiplier of $E_s(t)$, which is the number of burglary events at site s since time t. ℓ , z and η are grid size, number of neighboring sites and the significance of neighborhood effects ($0 \le \eta \le 1$), respectively. We can achieve a continuous-time and -space setting by taking limits as ℓ and $\delta t \to 0$.

ETAS Model[7] ETAS Model treats the dynamic occurrence of crime as a continuous-time, discrete-space epidemic-type aftershock sequence point process. The model assumes that crimes are not isolated events but are influenced by past crimes in the same area, so each event generates $N \sim Poisson(\theta)$ direct offspring events. The event rate in box n at time t is given by:

$$\lambda_n(t) = \mu_n + \sum_{t_n^i < t} \theta \omega e^{-\omega(t - t_n^i)}$$
(3)

where μ_n is the background rate of crime in box n, while t_n^i are the times of events in box n in the history of process. ω is the decay rate of influence of past events. The Expectation-Maximization (EM) algorithm can be used for parameter estimation[6].

Effectiveness Early assessments in cities like Santa Cruz, California, documented an approximately 19% decrease in burglaries within designated zones. In Los Angeles, pilot programs reported notable reductions in property crime, indicating that the model can help law enforcement allocate resources efficiently. Studies in 2019, such as those conducted in Oakland, revealed that reliance on historical crime data can reinforce existing disparities, leading to heightened police scrutiny of marginalized communities, raising ethical concerns regarding bias and over-policing.

2.2 People-Based: Chicago's Strategic Subject List (SSL)

Modelling Methods The key idea behind the SSL is to construct a **co-offending network** model of crime[14, 2], which is a graph representation of the relationships between individuals who have committed crimes together. Upon the network predictions and recommendations are made to the police department.

Effectiveness The SSL has been used in Chicago since 2013 to identify individuals at high risk of being involved in gun violence. The model has been criticized for its lack of transparency and potential for racial bias, as well as for the ethical implications of targeting individuals based on their social networks.

2.3 Hybrid: Risk Terrain Modeling (RTM) and Real-Time Crime Centers (RTCC)

Modelling Methods RTM[3] combines environmental factors like abandoned buildings and liquor stores with sociological data to reduce potential biases. RTCCs[11] use real-time data to identify crime patterns and allocate resources accordingly. Both of them are hybrid systems that combine place-based and people-based approaches.

Effectiveness RTM has been used in cities like Philadelphia to predict crime risk and allocate resources accordingly. RTCCs have been implemented in cities like New York and Los Angeles to monitor crime patterns in real time and respond to incidents more effectively. Both systems have been criticized for their potential to reinforce existing biases and for the ethical implications of targeting individuals based on their social networks.

2.4 Review of Mathematical Ideas in Modelling Approaches

Differential Equations Used in a continuous setting to model the spread of crime spatially and temporally.

Probabilistic Graphical Model Inference Used to model social networks and co-offending relationships, like the Sum-Product algorithm in a Bayesian network, or methods such as MCMC and Variational Inference.

Optimization Techniques Methods like Stochastic Gradient Descent (SGD) or the Expectation-Maximization (EM) algorithm are used to estimate parameters in models like the Epidemic-Type Aftershock Sequence (ETAS).

3 Feature Engineering Techniques

Temporal Features Includes day-of-week, time-of-day, and seasonality flags such as holidays.

Spatial Features Incorporates clusters, proximity measures, geohashes, distance to police stations, and environmental factors like bars and crime hotspots.

Crime Type Encoding Utilizes one-hot encoding, classification by severity, and further categorization into high-and low-risk groups for arrests.

Aggregated Rates Considers crime counts per area and time window, arrest counts per area and time window, and flags for repeat domestic incidents.

4 Evaluation Metrics and Their Appropriateness

Prediction Success Rate Measures the proportion of actual crimes that occur within the areas designated as crime hot spots. For example, a 2015 study by PredPol claimed that its model accurately predicted 4.7% of crimes and was twice as accurate as traditional methods.

Changes in Crime Rate Based on historical records, the Santa Cruz Police Department observed an 11% reduction in residential burglaries and a 27% reduction in robberies after deploying PredPol.

False Positive/Negative Rates Simulation studies suggest that feedback loops may cause the system to overpredict crime in certain neighborhoods. For example, an analysis of drug-related crime forecasts in Oakland found that communities of color were misidentified at roughly twice the rate of predominantly white areas.

5 Challenges and Ethical Considerations

Lack of Transparency Limited transparency exacerbates concerns about policing inequities, particularly among marginalized groups that have historically experienced disproportionate surveillance.

Oversimplification of Social Complexities By focusing primarily on spatial and temporal factors, predictive tools may overlook deeper social drivers of crime, such as poverty and educational inequality.

Short-Term Gains vs. Long-Term Consequences Even when short-term crime rates decline, community trust can suffer, potentially heightening tensions between law enforcement and the public in the long run.

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