

Jacobian

$$\mathbf{J} = \begin{bmatrix} \frac{\partial \mathbf{f}}{\partial x_1} & \dots & \frac{\partial \mathbf{f}}{\partial x_n} \end{bmatrix} = \begin{bmatrix} \nabla f_1 \\ \vdots \\ \nabla f_m \end{bmatrix} = \begin{bmatrix} \frac{\partial f_1}{\partial x_1} & \dots & \frac{\partial f_1}{\partial x_n} \\ \vdots & \ddots & \vdots \\ \frac{\partial f_m}{\partial x_1} & \dots & \frac{\partial f_m}{\partial x_n} \end{bmatrix}$$

Equilibrium point

$$\dot{x}_0 = F(x_0) = 0$$

Linearization

$$\dot{x} \approx F(x_0) + J(x_0)(x - x_0)$$

Newtons Method

$$\mathbf{x}_{n+1} = \mathbf{x}_n - J_F(\mathbf{x}_n)^{-1} F(\mathbf{x}_n)$$

Polar coordinates

$$x = r \cos \theta$$

$$y = r \sin \theta$$

$$r = \sqrt{x^2 + y^2}$$

$$\theta = \arctan\left(\frac{y}{x}\right) + k\pi, \quad x \neq 0$$

Spherical coordinates

$$x = R \sin \phi \cos \theta$$

$$y = R \sin \phi \sin \theta$$

$$z = R \cos \phi$$

$$R^2 = x^2 + y^2 + z^2 = r^2 + z^2$$

$$r = \sqrt{x^2 + y^2} = R \sin(\phi)$$

$$\tan(\phi) = \frac{r}{z} = \frac{\sqrt{x^2 + y^2}}{z}$$

$$\tan(\theta) = \frac{y}{x}$$

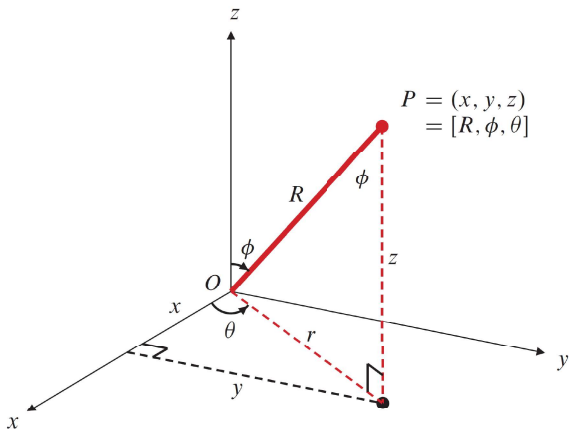


Figure 1: Spherical coordinates as explained in Adams, R. A. & Essex, C. *Calculus* - Ninth Edition.

Trigonometrics

$$\tan x = \frac{\sin x}{\cos x}$$

$$\csc x = \frac{1}{\sin x}$$

$$\sec x = \frac{1}{\cos x}$$

$$\cot x = \frac{1}{\tan x}$$

$$\sinh x = \frac{e^x - e^{-x}}{2}$$

$$\cosh x = \frac{e^x + e^{-x}}{2}$$

$$\sin' x = \cos x$$

$$\cos' x = -\sin x$$

$$\tan' x = \sec^2 x$$

$$\cot' x = -\csc^2 x$$

$$\sec' x = \tan x \sec x$$

$$\csc' x = -\cot x \csc x$$

$$\sinh' x = \cosh x$$

$$\cosh' x = \sinh x$$

$$\tanh' x = \frac{1}{\cosh^2 x} = 1 - \tanh^2 x$$