

Lecture 10: Camera

DHBW, Computer Graphics

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8.3.2023.

Syllabus

- 3D scene
 - Object
 - Light
 - Camera
 - Rendering
 - Image and display
- Camera
 - Real camera system
 - Image formation
 - Pinhole camera model
 - Virtual pinhole camera
- 

Where is camera?



<https://sciencebehindpixar.org/pipeline/sets-and-cameras>

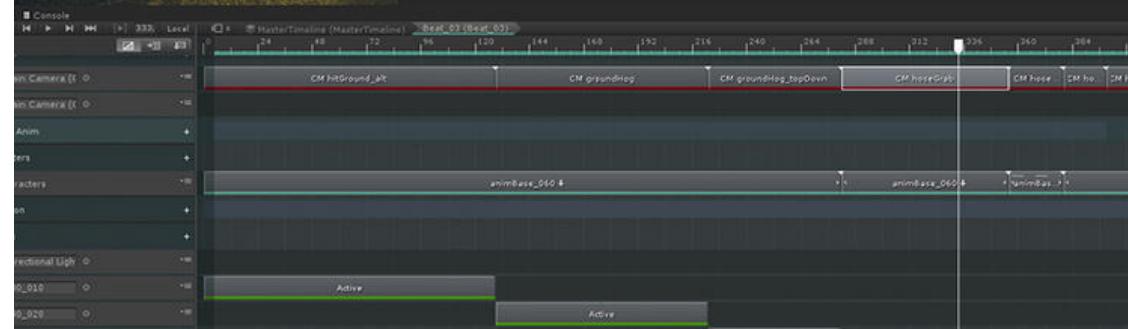
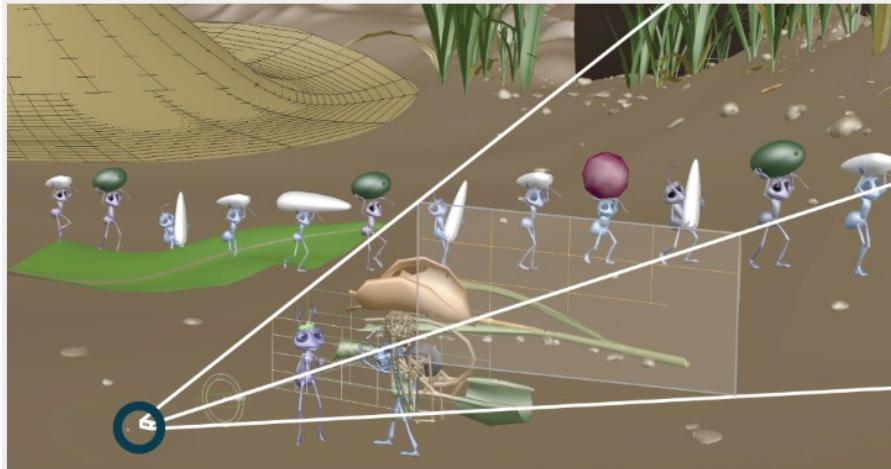


<https://www.half-life.com/en/alyx/>



<https://unity.com/solutions/film-animation-cinematics>

Where is camera?



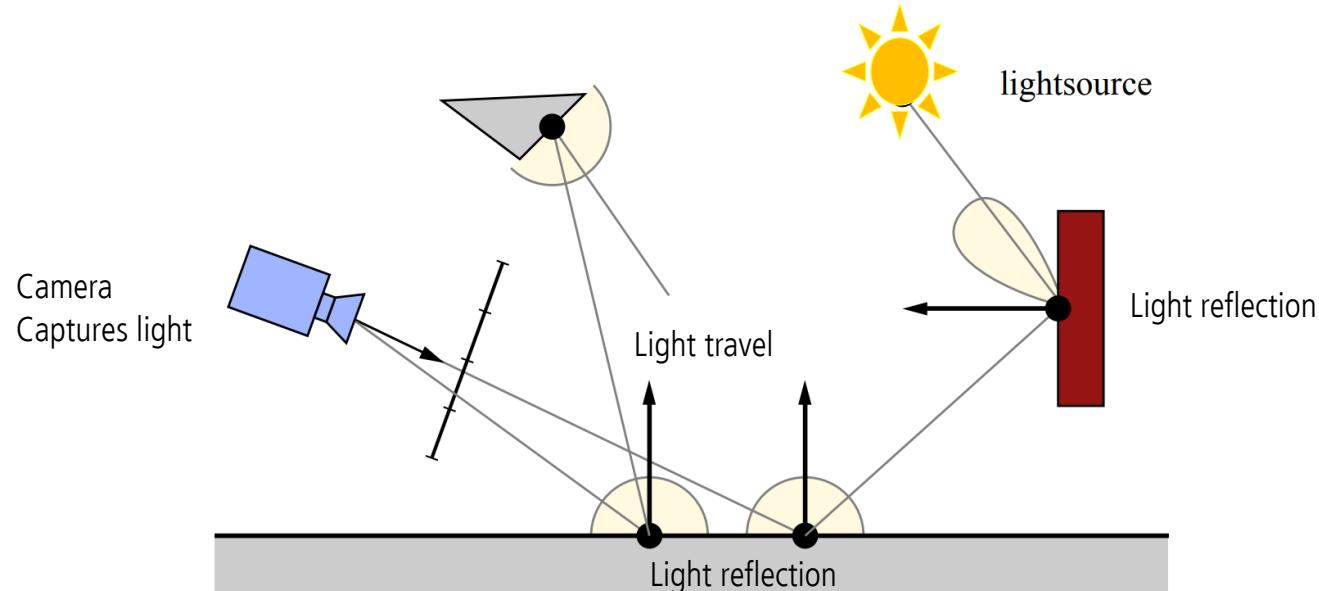
Where is camera?

- In rendered images, camera is not seen – it defines what we see.



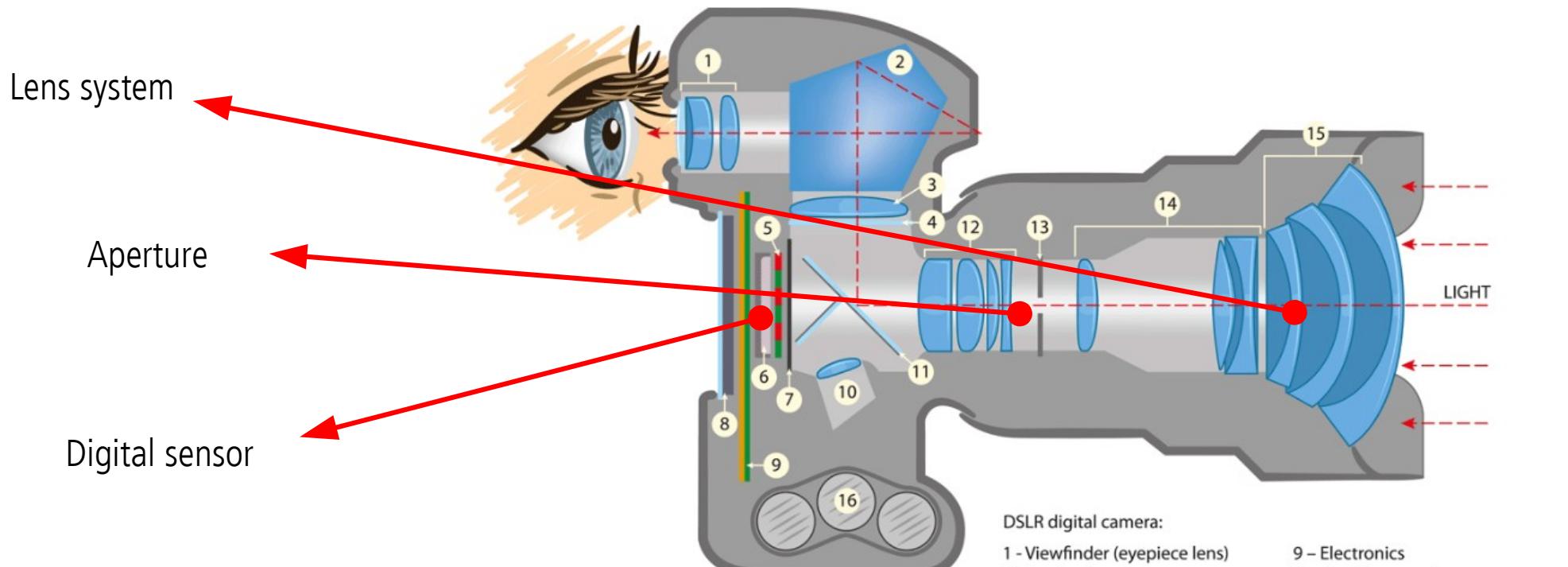
Camera in rendering

- Camera defines a portion of visible scene
- Light falling on camera sensor forms an image
- To find light contributing to pixel colors, rays are traced from camera to 3D scene
 - Backward tracing



Real camera systems

Real camera systems



DSLR digital camera:

- | | |
|--------------------------------|-------------------------------------|
| 1 - Viewfinder (eyepiece lens) | 9 - Electronics |
| 2 - Pentaprism | 10 - Autofocus system |
| 3 - Focusing screen | 11 - Reflex and relay mirror |
| 4 - Condenser lens | 12 - Focusing elements |
| 5 - Color and infrared filter | 13 - Aperture |
| 6 - Digital sensor | 14 - Zoom elements |
| 7 - Shutter | 15 - Front light gathering elements |
| 8 - Display | 16 - Batteries |

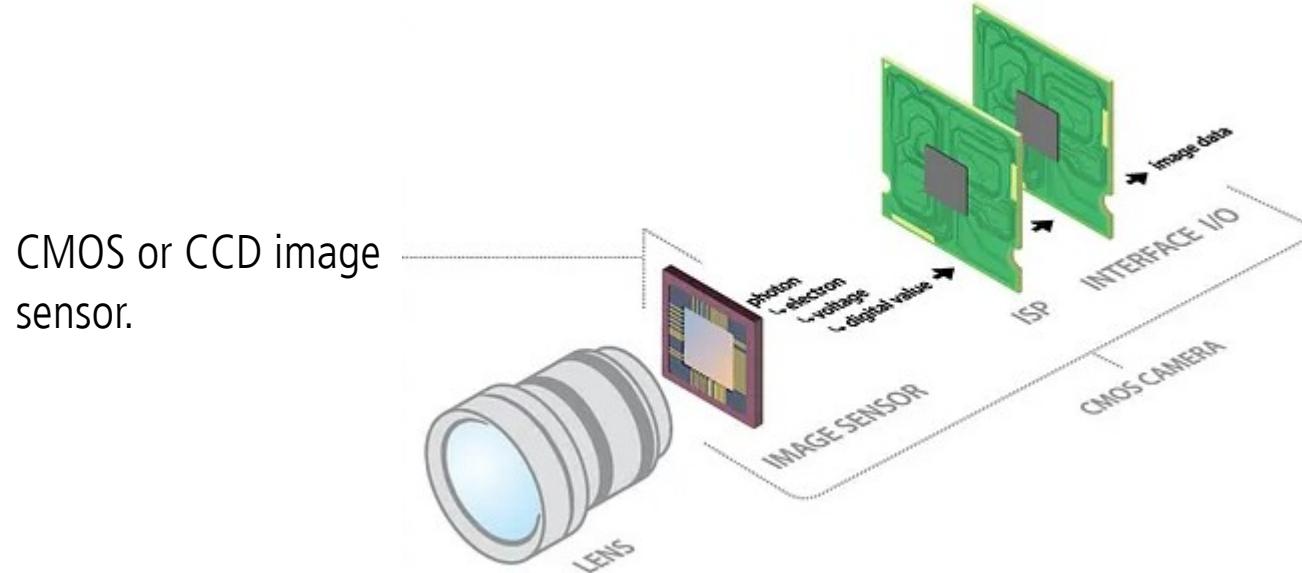
Basic Parts of a DSLR Camera

Real camera systems

- Camera contains many small discrete **sensors**: CMOS/CCD
 - Each measures incoming **radiance** values and converts it to **color** signal
 - Radiance: light energy per ray
- Sensors are placed into light-proof enclosure with small opening - **aperture**
 - Such setup restricts light where light can enter and strike sensor
- **Lens** is placed at the aperture to focus the light so each sensor receives light from only a small set of incoming directions

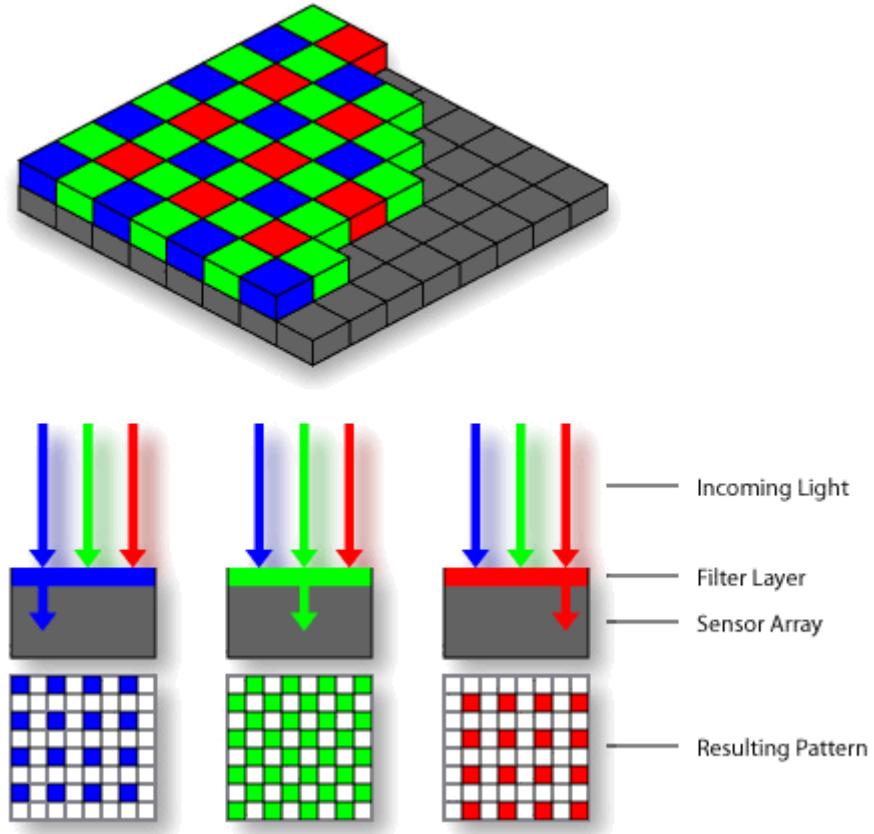
Camera image sensor

- Sensor converts incident light energy into analog signal (e.g., voltage) which is later represented as color
- Array of sensors are used to form an image



Camera image sensor

- Each sensor records incoming light energy per second
- Only one signal over whole cell area is captured
- Sensor measures only R,G,B wavelengths
- Sensor cell can be seen as a pixel

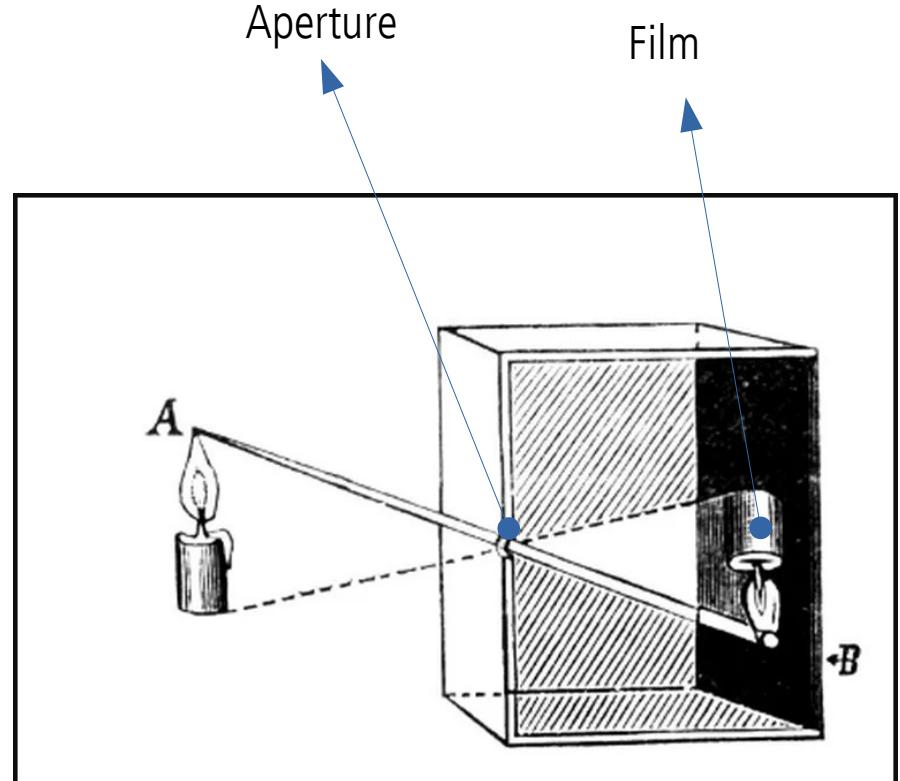


https://simple.wikipedia.org/wiki/Bayer_filter

Image formation

Camera obscura

- Lightproof box with:
 - Black interior (to prevent light reflection)
 - Very small opening: **aperture**
 - Light-sensitive **film** opposite to aperture
- When aperture is opened, film is exposed to light
 - Light passing through the hole forms an inverted image of the external scene on the film
 - Time which aperture must be opened to capture image on film is called **exposure**
- A foundation for modern photographic cameras



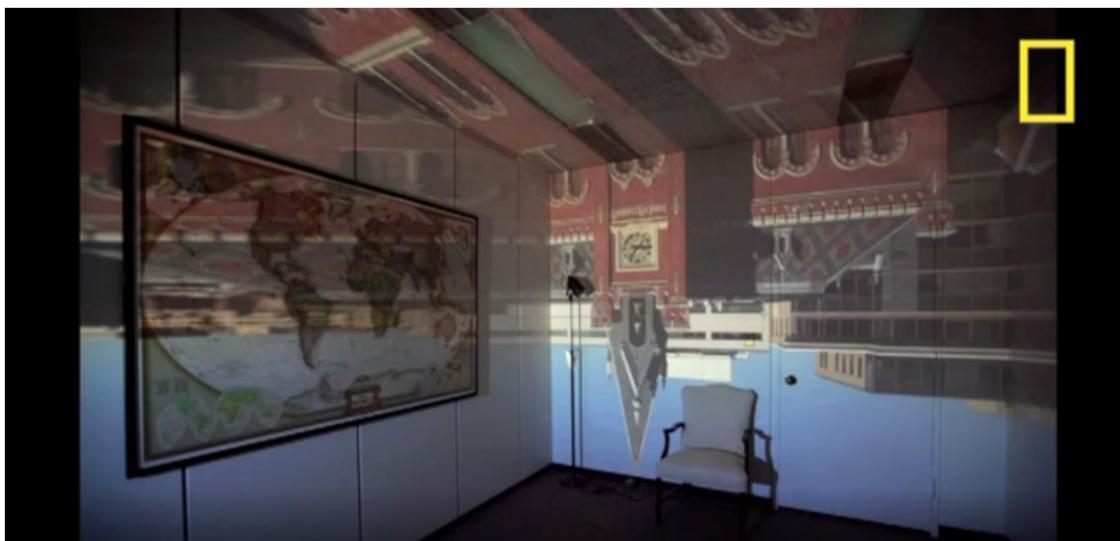
https://www.inquirer.com/philly/entertainment/20160806_Camera_Obscura_at_Fleisch_er_throws_new_light_on_photography.html

Camera obscura = Dark room



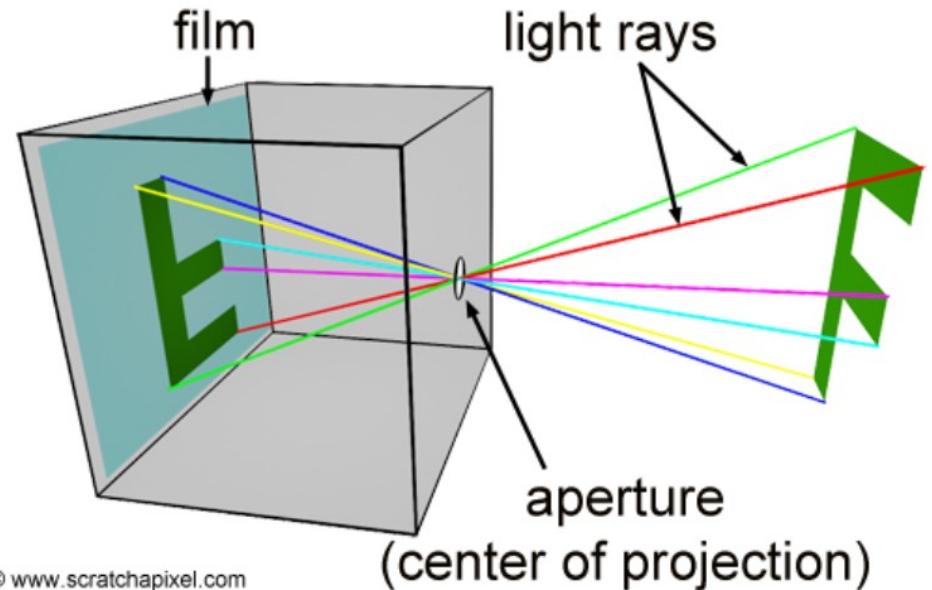
View from the window.

Room made into camera obscura projecting view from the window on the wall.



Pinhole camera

- Main elements:
 - **Aperture**: center of projection: all rays entering converge here and diverge from it to the other side
 - **Film**: light hitting the film forms the image
- Image formation
 - Aperture is opened to expose film to light
 - Ray reflected from the world in point P enters the camera and intersects film in one point
 - Each point in the visible portion of the scene corresponds to a single point on the film

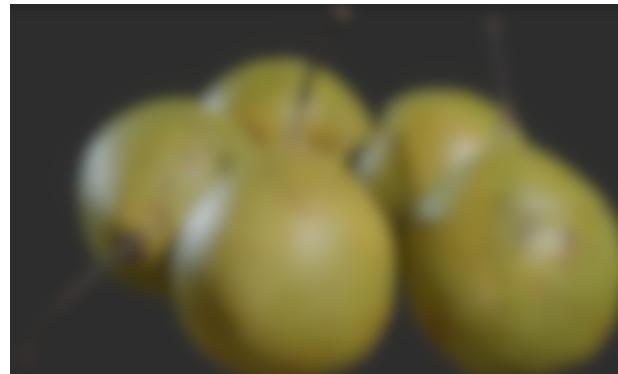


© www.scratchapixel.com

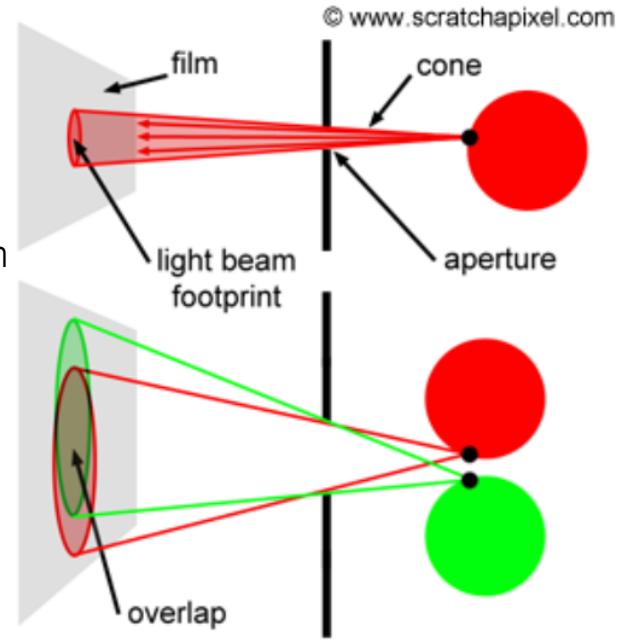
<https://www.scratchapixel.com/lessons/3d-basic-rendering/3d-viewing-pinhole-camera>

Aperture size

- **Ideal pinhole:** aperture is so small that only one ray passes through it
 - Formed image is **sharp** since each point of the object maps to the one point of the film
- **Aperture has certain size**
 - Angle of cone of rays is determined by the size of aperture
 - Smaller aperture → smaller cone → sharper image
 - Larger aperture → larger cone → blurred image



https://polyhaven.com/a/food_pears_asian_01

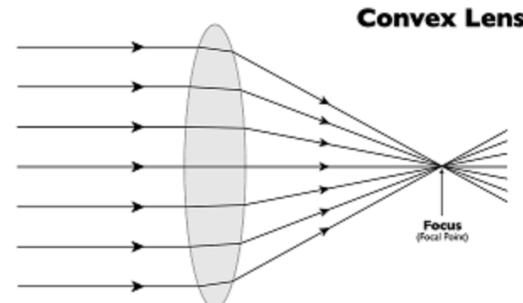
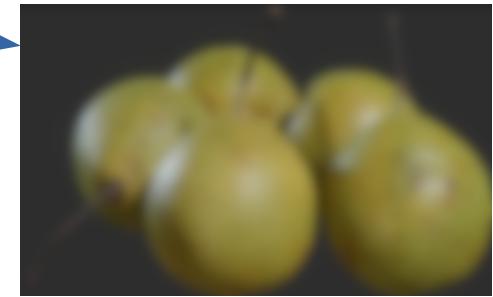


Cones are overlapping and single point appears multiple times on film
→ blur (out of focus).

<https://www.scratchapixel.com/lessons/3d-basic-rendering/3d-viewing-pinhole-camera>

Aperture and Lenses

- Small aperture: sharp image, but long exposure times needed leading to motion blur
- Large aperture: shorter exposure time but image will be blurred
- Solution is to use lens in front of aperture
 - Rays entering camera are gathered (converged) and focused to one point on a film plane
 - Aperture can now be larger enabling smaller exposure time while blur is canceled with lens



Depth of field

- **Lens camera** introduce **depth of field**: distance between nearest and the farthest object from the scene that appears sharp in the formed image
- **Pinhole cameras have infinite depth of field**
 - Because of this, images rendered with pinhole cameras are completely sharp and thus look artificial



Depth of field: <https://www.adobe.com/uk/creativecloud/photography/discover/bokeh-effect.html>

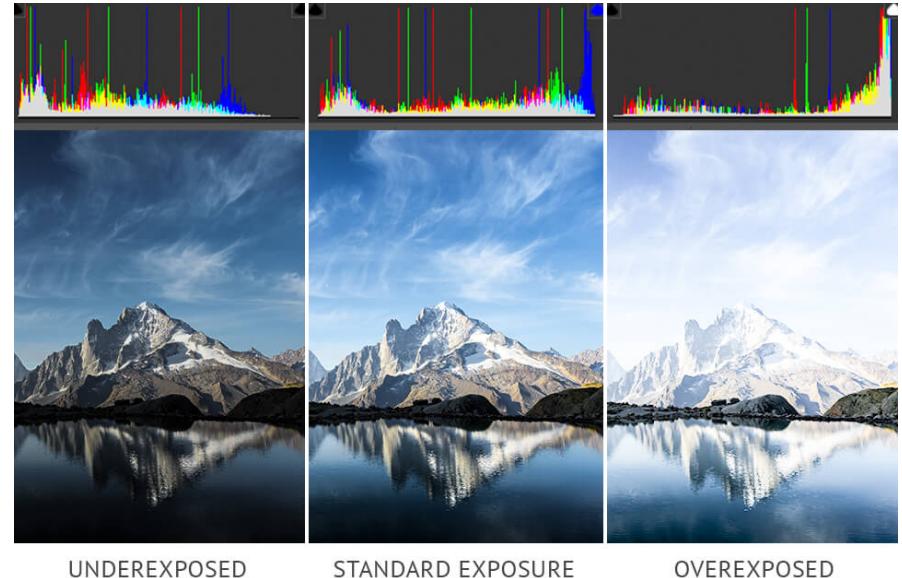
Bokeh



Lights out of focus are aesthetically pleasing → bokeh effect.

Exposure

- Time in which the film is exposed to light is called **exposure** time
 - Determines image brightness
- **High-contrast image** contains both dark shadows and bright highlights
- **Dynamic range**: ratio between the maximum and minimum measurable light intensities
 - Determines amount of visible details in lit and shadowed areas
 - Real world and 3D scenes can have high difference in dynamic range, but cameras and display devices are limited in capturing and showing them



<https://fixthephoto.com/what-is-exposure-composition.html>

Exposure

- If aperture is small, longer time is needed for image to form on a film
 - In this case, **motion blur** can appear for objects which are not perfectly still



Earth rotation causes motion blur in long-exposure photos



https://en.wikipedia.org/wiki/Motion_blur

Exposure

- Exposure is controlled with:
 - Aperture size (f-stop) → depth of field
 - Shutter speed → motion blur
 - Sensitivity (ISO) (gain) → noise



<https://photonify.com/3-steps-for-adjusting-the-depth-of-field-on-your-camera/>

<https://petapixel.com/exposure-triangle/>

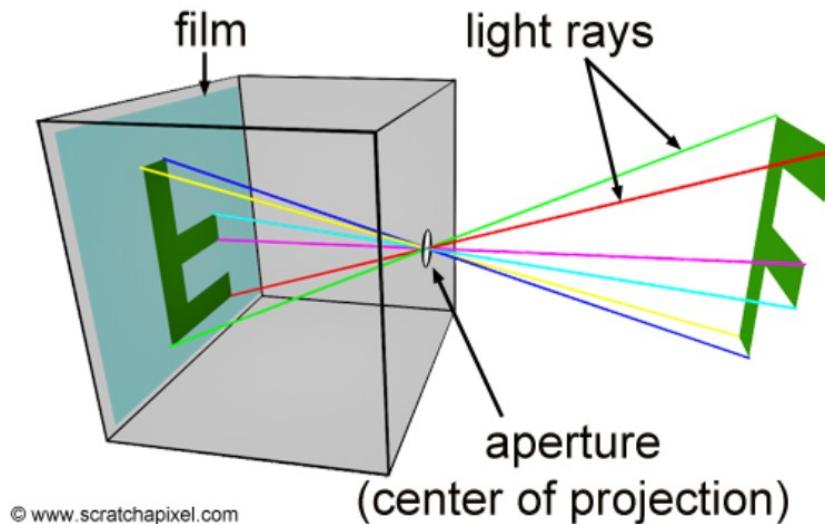
<https://actioncamera.blog/2017/02/22/the-exposure-triangle/>

<https://www.shutterbug.com/content/give-photos-dramatic-perspective-motion-and-blur-simple-photoshop-technique-video>

Pinhole camera model

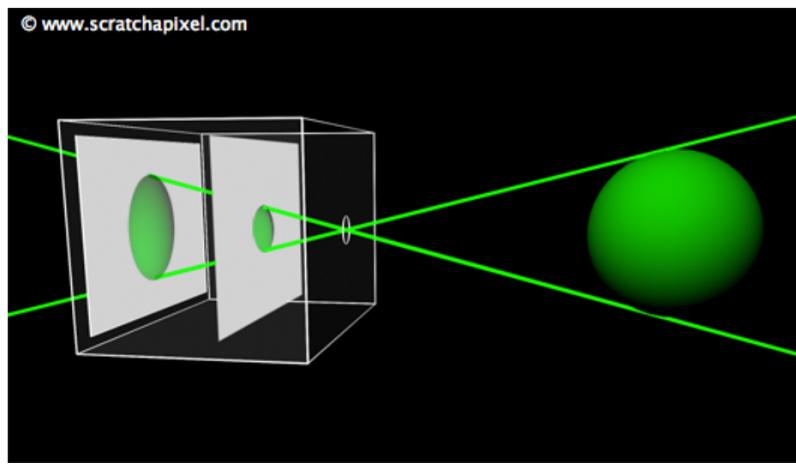
Pinhole camera model

- Complex lens system is simplified: **pinhole camera**
- Main elements:
 - **Film** (image plane)
 - **Aperture** (small opening)
- Parameters:
 - Focal length
 - Angle of view
 - Film size

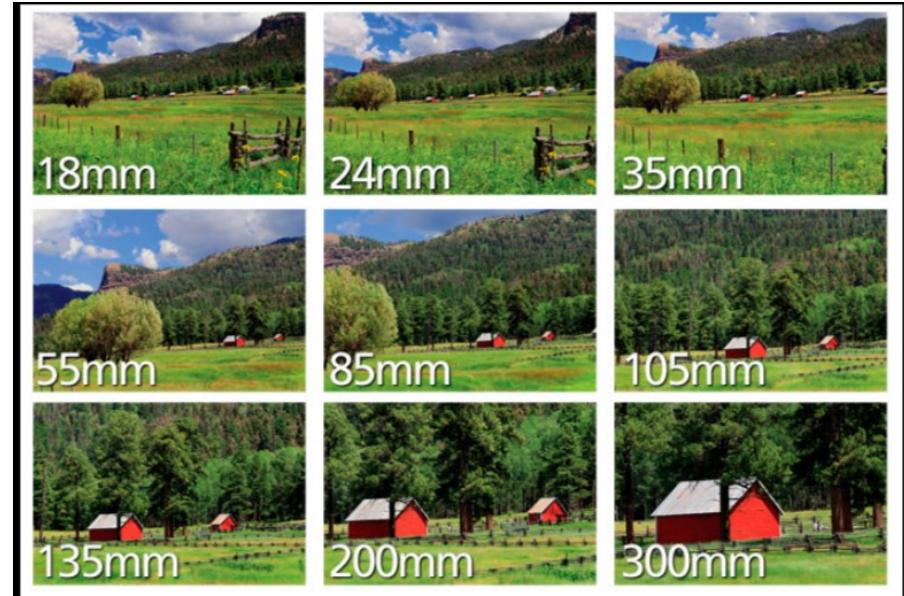


Focal length

- Distance of film plane from aperture defines amount of scene that we see
 - Moving image plane (film plane) closer to aperture effectively performs **zoom out**
 - Moving film plane away from aperture effectively performs **zooming in**
- This parameter is called **focal length** or **focal distance**

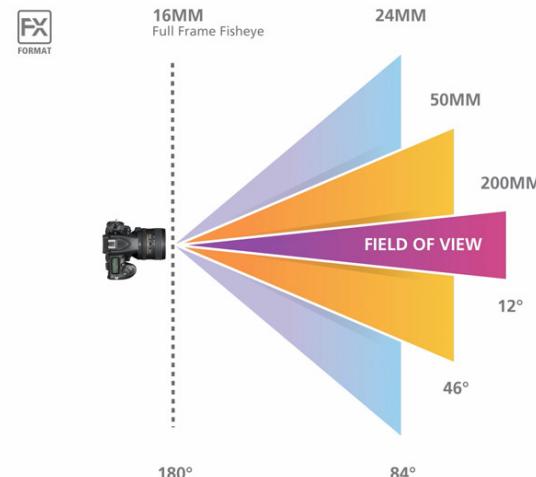
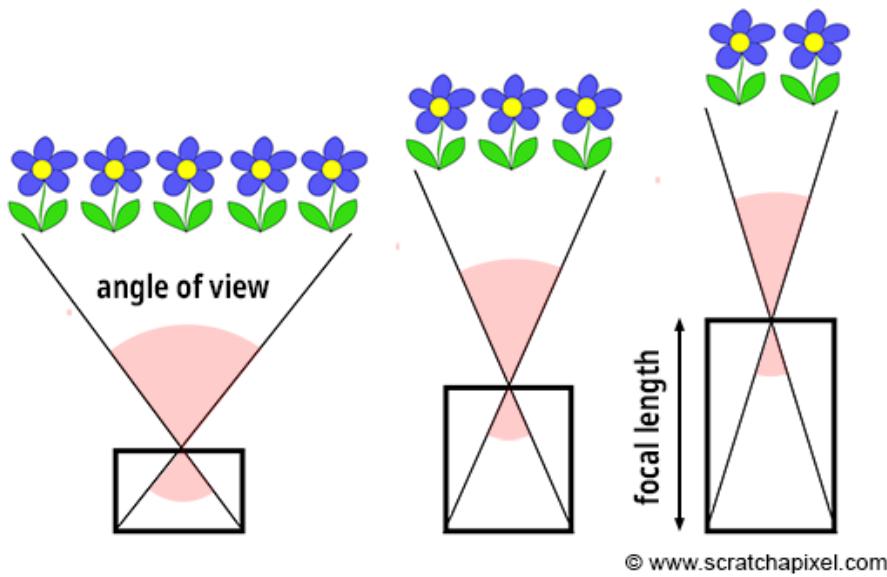


<https://www.nikonusa.com/en/learn-and-explore/a/tips-and-techniques/understanding-focal-length.html>



Angle of view

- Angle of triangle apex defined with aperture and film edges is called angle of view (AOV) or field of view (FOV)
- Changing focal length, changes AOV/FOV



Focal length and corresponding field of view
<https://www.nikonusa.com/en/learn-and-explore/a/tips-and-techniques/understanding-focal-length.html>

Focal length and angle of view

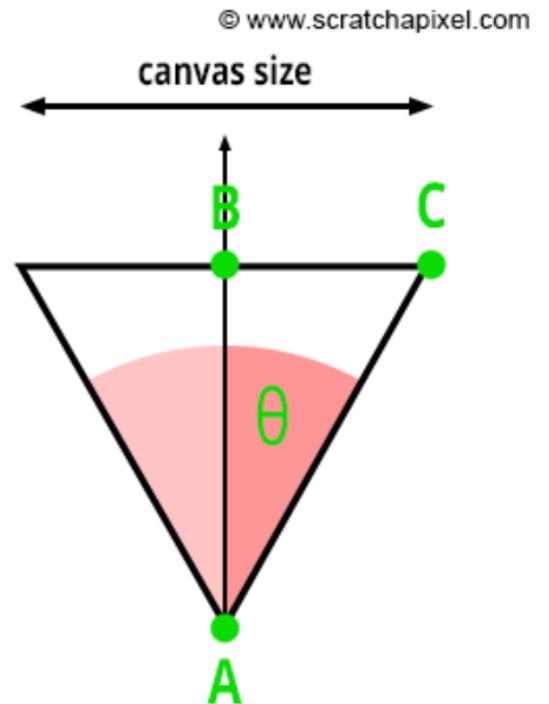
- Relation between focal length ($f = AB$) and angle of view (θ)
- Longer focal lengths result in smaller FOV (more zoom)
- Short focal length results in larger FOV (less zoom)

$$\tan(\theta) = \frac{BC}{AB}$$

$$BC = \tan(\theta) * AB$$

$$\text{Canvas Size} = 2 * \tan(\theta) * AB$$

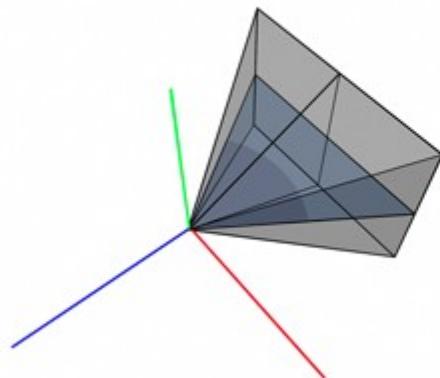
$$\text{Canvas Size} = 2 * \tan(\theta) * \text{Distance to Canvas} .$$



Field of view

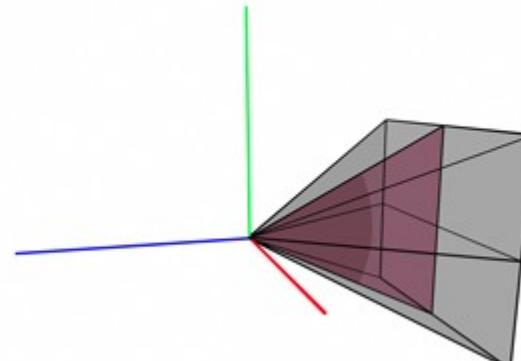
- Triangle defined with aperture and film edges is a pyramid and we distinguish **horizontal and vertical angle (field) of view (AOV/FOV)**
- Using fixed film aspect ratio, horizontal field of view determines vertical field of view and vice versa

Horizontal Field of View



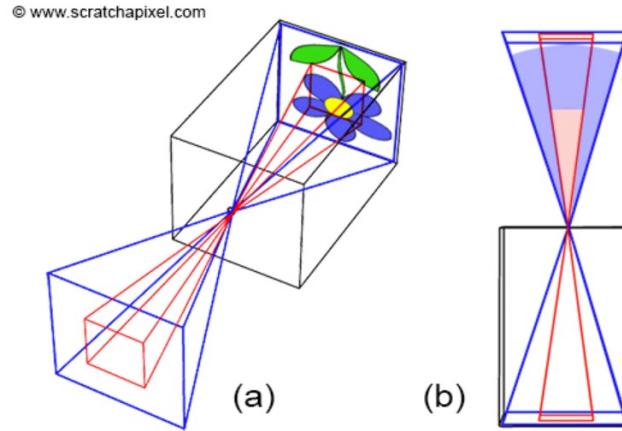
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Vertical Field of View



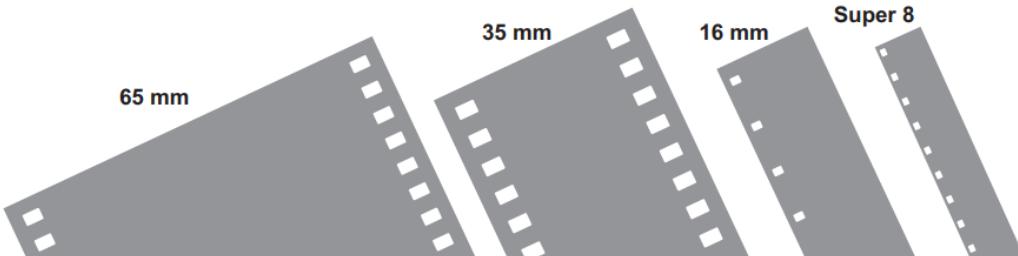
Film size

- Angle of view depends on film (image plane) size
 - Film has horizontal and vertical dimensions
 - Using fixed film aspect ratio, horizontal dimension determines vertical dimension
- Smaller area of film size implies smaller angle of view and vice versa.
 - Capturing the same extent of the scene with larger film requires adjusting focal length



Film size

- Larger film formats were developed enabling more details and better image quality
 - In digital cameras, film is replaced with sensor, thus we talk about sensor size
 - Sensor size has the same role as film size



Gauge refers to the width of film. Four are common: 65mm, 35mm, 16mm, Super 8.

http://www.theodoropoulos.info/attachments/076_kodak05_Film_Types_and_Formats.pdf

35 mm / 135	120 / Medium Format	4x5 / Large Format			
  24 mm	 4.5 cm	 6 cm	 7 cm	 4 inch	 5 inch

<https://www.learnfilm.photography/guide-to-medium-format-photography/>

1920x1080

Sensor size and image resolution

- **Image resolution:** width × height pixels
- **Size of sensor and number of pixels on sensor are independent parameters**
 - Angle of view doesn't depend on number of pixels on image sensor
- Image quality depends on:
 - Image sensor size
 - Number of pixels on sensor (resolution)
- Higher resolution images will have more details



20% of 1920x1080



Image resolution and aspect ratio

- Image aspect ratio (device aspect ratio) is calculated from image resolution (width and height):

$$\text{Image (or Device) Aspect Ratio} = \frac{\text{width}}{\text{height}}$$

- Film and display devices (computer screens, television) have standardized aspect ratios

- 4:3

- Old television systems and computer monitors (e.g., resolution 640x480)
 - Default for digital cameras; 35mm films

- 5:3 and 1.85:1

- Often used for film

- 16:9

- Aspect ratio used by HD TV, monitors and laptops (e.g., resolution: 1920x1080)



<https://photographylife.com/aspect-ratio>

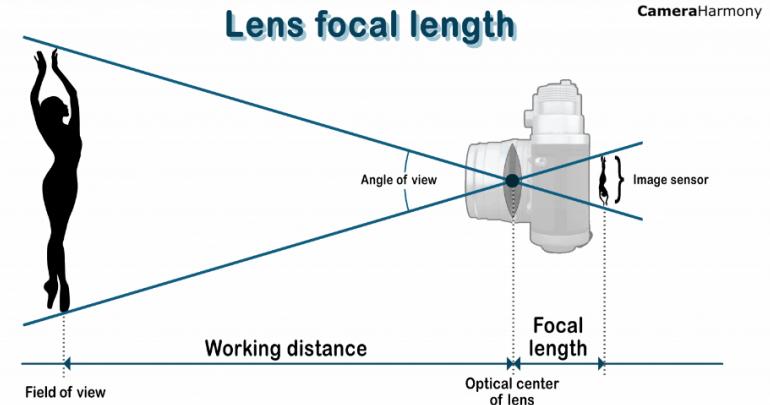
<https://www.studiobinder.com/blog/aspect-ratio/>

Film and image aspect ratio*

- In computer graphic camera model, sensor (film/canvas) aspect ratio can be different from the image (device) aspect ratio.
 - Difference leads to stretching the image in either x or y directions
- Solution: canvas aspect ratio is often directly computed from the image aspect ratio
 - Example, if image resolution is 640x480, canvas aspect ratio will be set to 4:3.

Pinhole camera parameters: recap

- Parameters:
 - Focal length (focal distance)
 - Angle of view (field of view)
 - Film size
- With two parameters we can always infer the third one
- **Angle of view is determined by:**
 - **Focal length:** longer focal length → narrower angle of view
 - **Film size:** larger film size → wider angle of view



Virtual pinhole camera

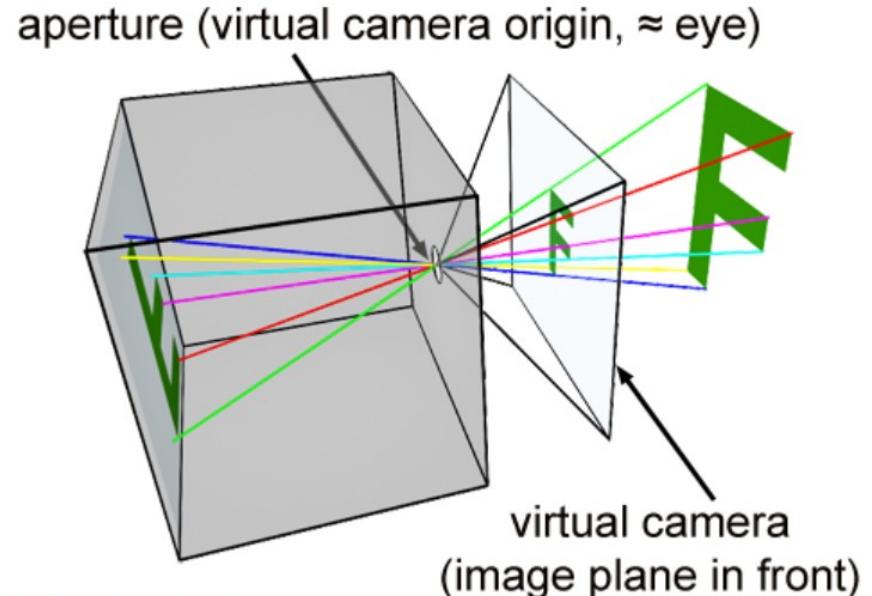
Camera model for rendering

Virtual pinhole camera

- Virtual pinhole camera model in rendering is used to deliver image similar to those produced by a real camera
 - Size and shape of real and rendered object must be the same
 - Combining rendered and live action footage must be possible
 - Expressive and artistic possibilities must be enabled
- Pinhole camera model is used in almost all production software
 - Godot: https://docs.godotengine.org/en/stable/classes/class_camera.html
 - Unity: <https://docs.unity3d.com/ScriptReference/Camera.html>
 - Blender: <https://docs.blender.org/manual/en/latest/render/cameras.html>
 - Houdini: <https://www.sidefx.com/docs/houdini/nodes/obj/cam.html>

Virtual pinhole camera

- In graphics, pinhole camera geometry is not directly simulated
- Virtual pinhole camera simulates only directions from which sensors (pixel) receive light
- Virtual image plane is placed in front of aperture and rays are traced from aperture to each pixel in virtual image plane
 - Camera rays → color of virtual image plane pixels

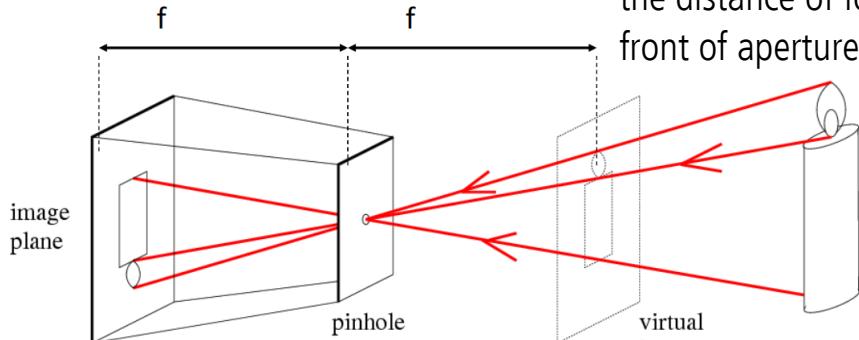


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<https://www.scratchapixel.com/lessons/3d-basic-rendering/3d-viewing-pinhole-camera/virtual-pinhole-camera-model>

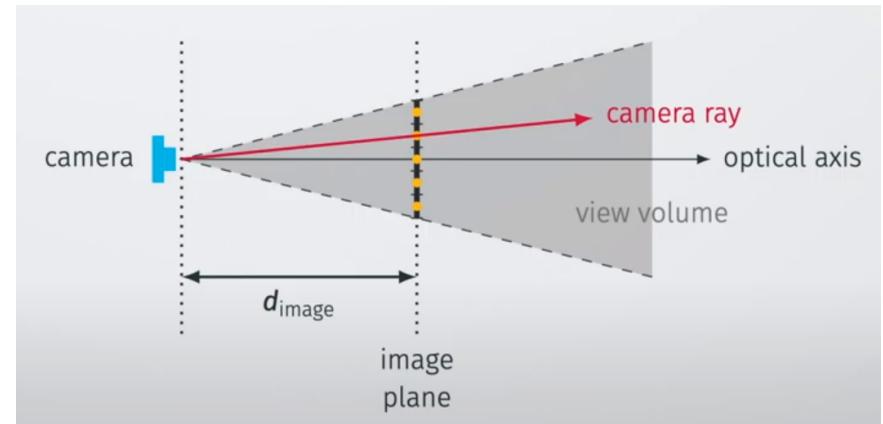
Virtual pinhole camera

- Following rays from aperture to image plane pixels and into the scene forms image on image plane
 - This results in **perspective projection**



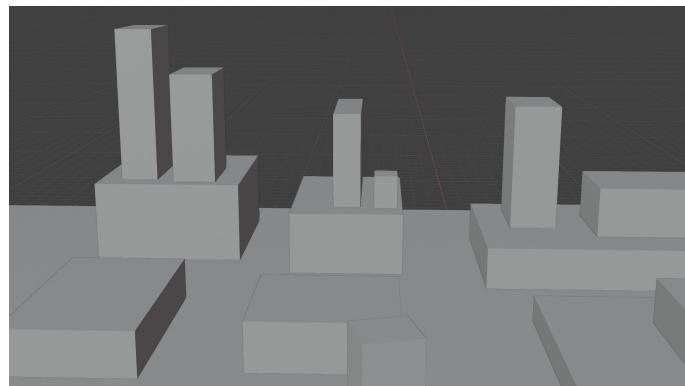
Real pinhole camera produces images which are upside down

Simulated pinhole camera produces images which are correctly orientated

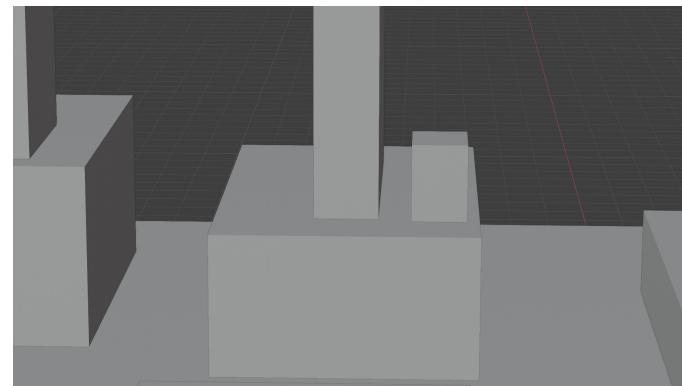


Viewing frustum

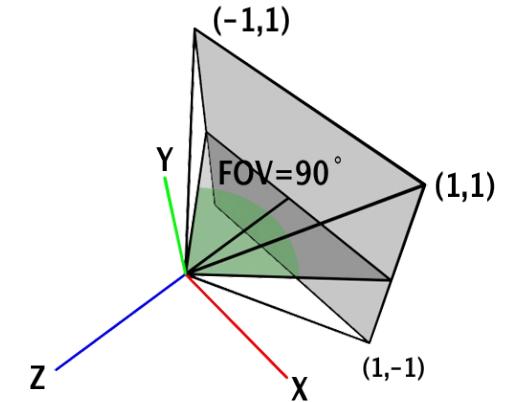
- Viewing frustum defines portion of scene visible to camera
- Viewing frustum of pinhole camera is defined with:
 - Camera origin (eye, aperture)
 - Field (angle) of view: film size and focal length



Focal length 50mm



Focal length 120mm



Near and far clipping planes

- Virtual pinhole camera additionally has near and far clipping planes
 - Virtual planes placed in front of camera and parallel to image plane.
 - Location of clipping planes is measured along camera's line of sight (camera's local z axis)
- Objects in 3D scene closer than near or further than far plane are not visible in image plane.
- Near and far clipping planes are needed for resolving precision issues
 - Precision can be lost if distance between closest and furthest object is too large

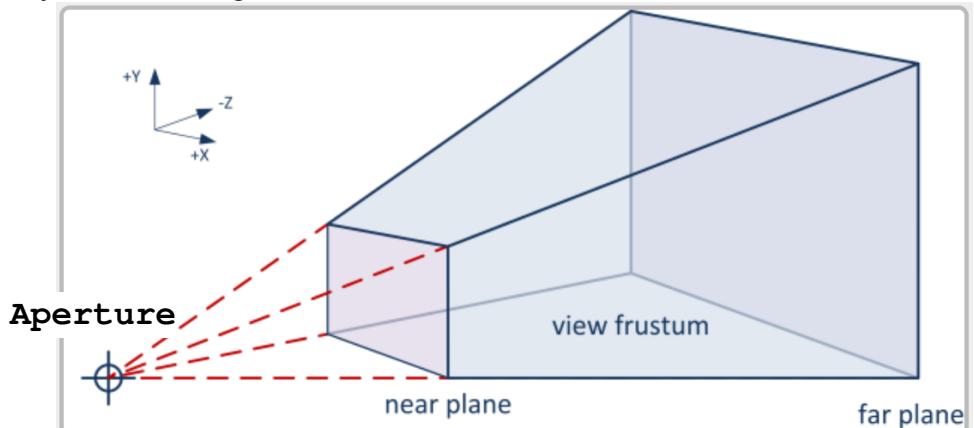
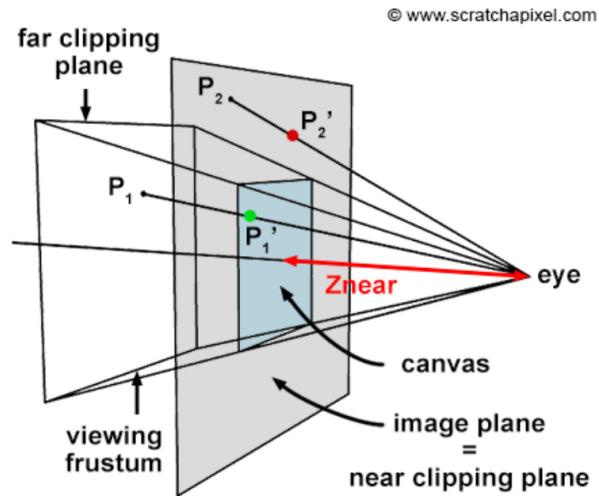
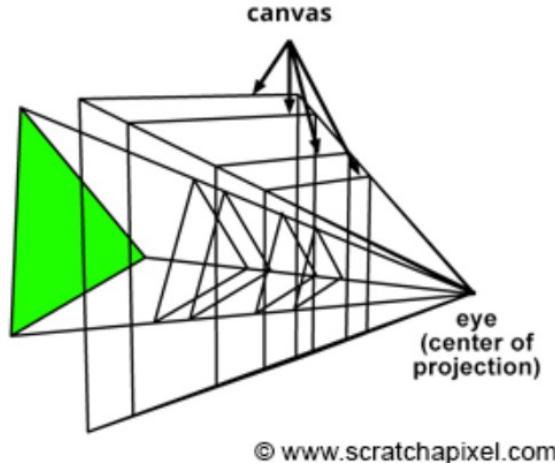


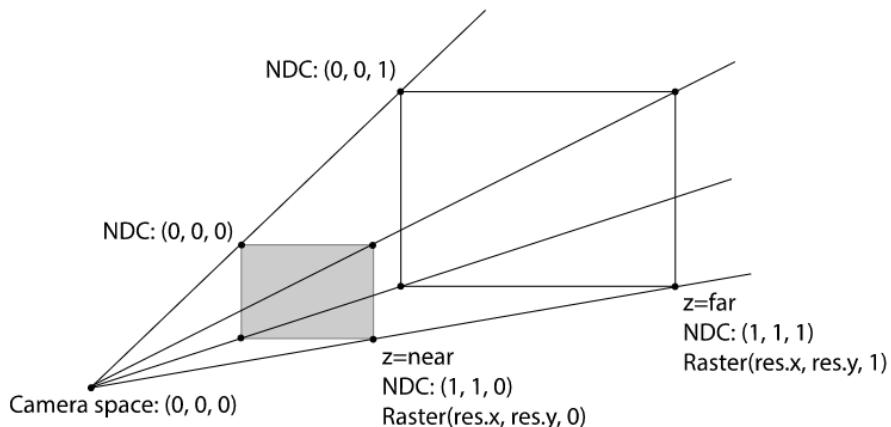
Image plane and clipping planes

- Image plane is often placed at near clipping plane for computation simplicity
 - Image plane can be placed anywhere on camera's line of sight (camera's local z axis) between near and far clipping planes
 - Size of image plane depends on distance from eye.



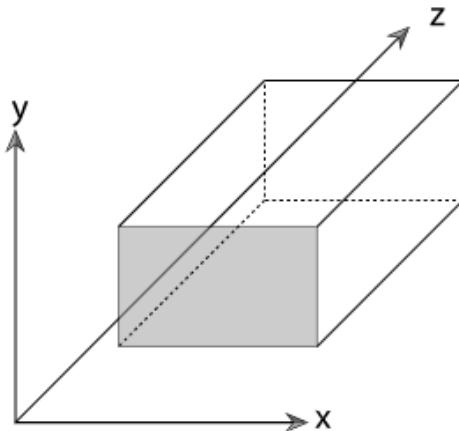
Perspective camera

- Most often used from film and game rendering
- Rays are generated from one point (eye, aperture) through virtual image plane
- **Simulates foreshortening effect:** more distant objects appear smaller



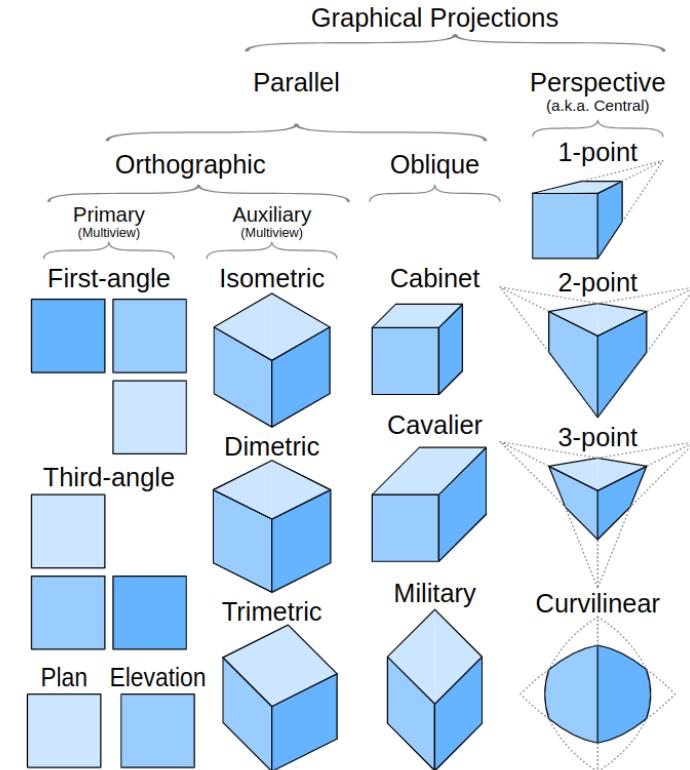
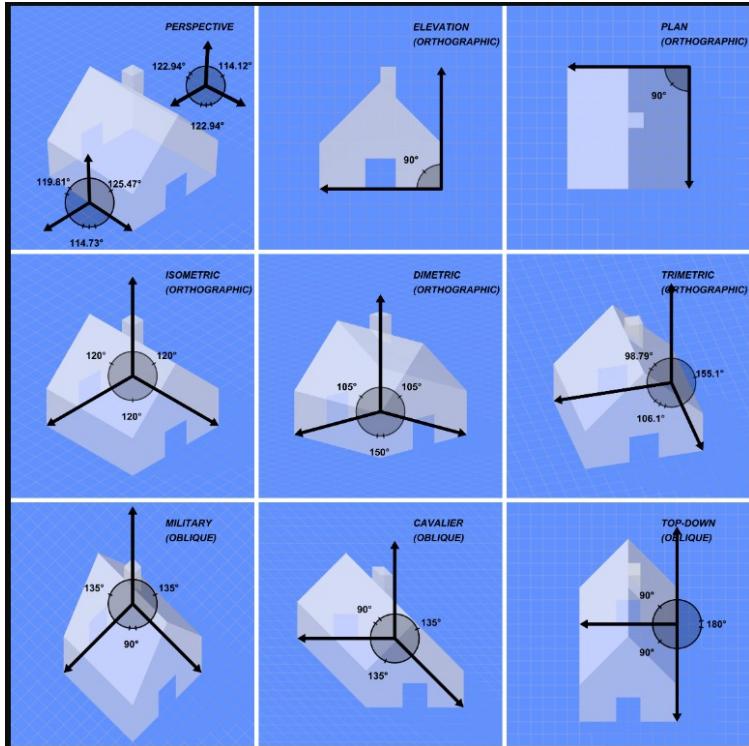
Orthographic camera

- Useful for architecture, engineering, design, isometric games, etc.
- Rays are generated parallel through virtual image plane
- Objects are of same size regardless of distance



https://store.steampowered.com/app/1573390/Lilas_Sky_Ark/

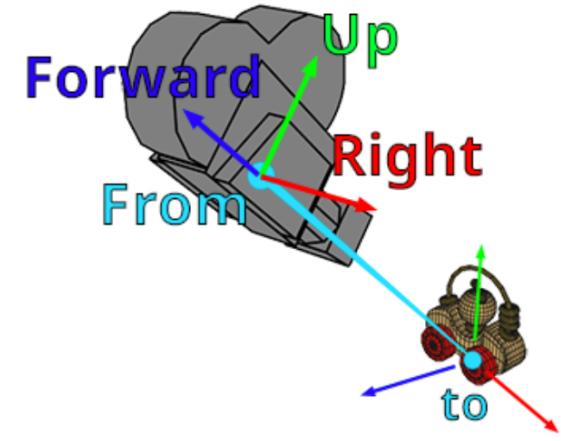
Other camera projection types



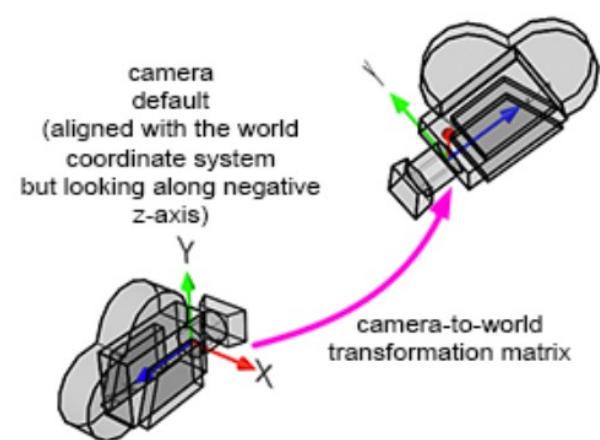
https://en.wikipedia.org/wiki/Orthographic_projection

Camera orientation and position

- Camera orientation is defined with Forward, Up, Right vectors.
- Camera orientation and position can be defined with **look-at** notation:
 - Point in space where camera is positioned (**From**)
 - Point in space where camera is looking (**To**)
- **Look-at matrix**
 - Forward, Up, Right can be calculated based on From, To
 - Forward, Up, Right, From define look-at matrix
 - Defines complete transformation needed for moving camera in 3D scene



www.scratchapixel.com



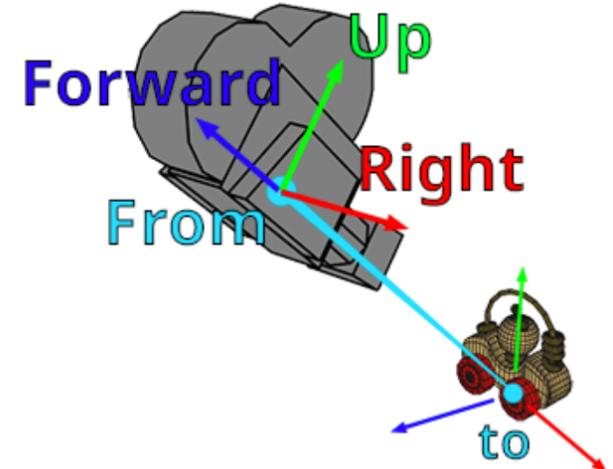
Look at matrix

- 4x4 transformation matrix → transformation of camera from its local (camera) space to world space in 3D scene: **camera-to-world** and its inverse **world-to-camera** matrix

Forward = normalize(From - To)

Right = crossProduct(randomVec, Forward)

Up = crossProduct(forward, right)



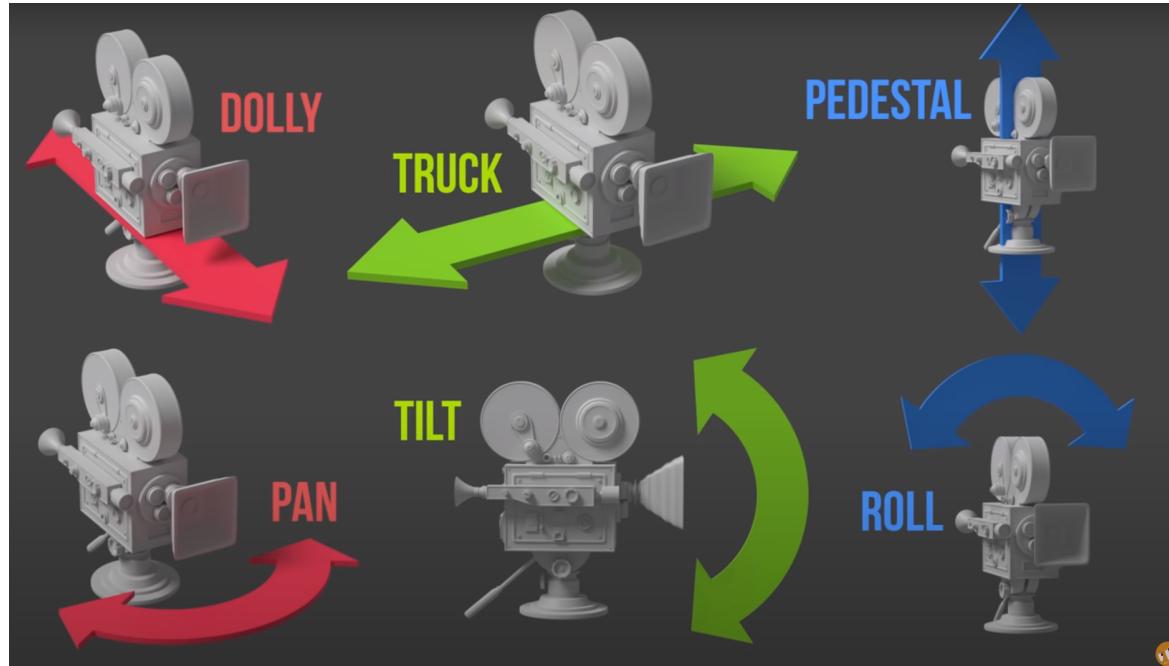
www.scratchapixel.com

$Right_x$	$Right_y$	$Right_z$	0
Up_x	Up_y	Up_z	0
$Forward_x$	$Forward_y$	$Forward_z$	0
$From_x$	$From_y$	$From_z$	1

RandomVec = (0, 1, 0) or other if Forward is close to (0, 1, 0) or (0, -1, 0)

Moving camera*

- Translations: moving in axis directions
- Rotations: rotation around axis

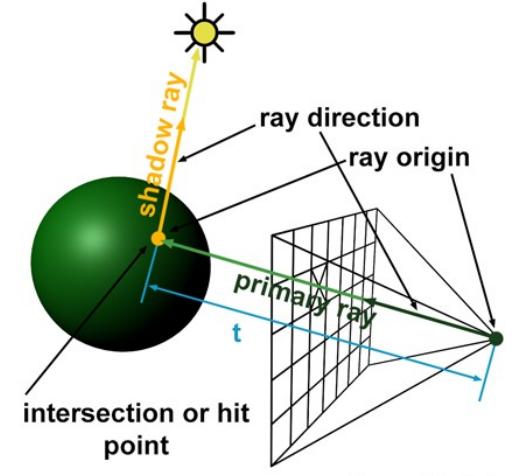


Virtual pinhole camera image formation

- How image is formed using virtual pinhole camera depends on rendering techniques:
 - Ray-tracing-based rendering
 - Rasterization-based rendering

Camera in ray-tracing

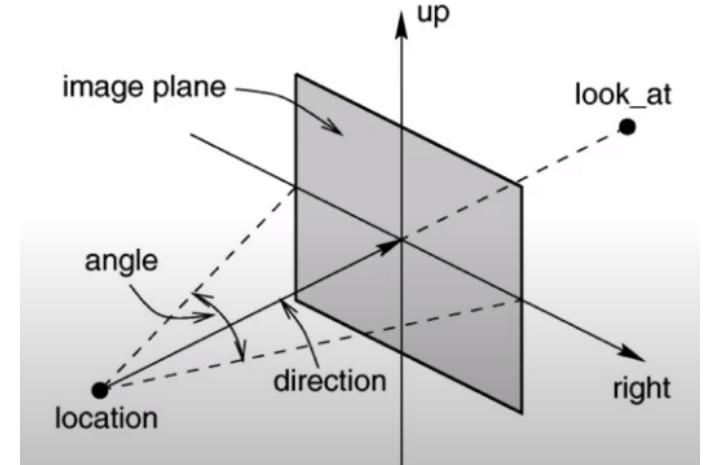
- **Image centric approach:** generate ray for each pixel of virtual image plane
 - Ray is generated using camera eye position and pixel position in camera image plane.
 - Ray is traced into the 3D scene where it intersects the objects – **ray casting** (foundational method for ray-tracing).
 - Color that is computed from intersecting the object is assigned to pixel



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Generating rays

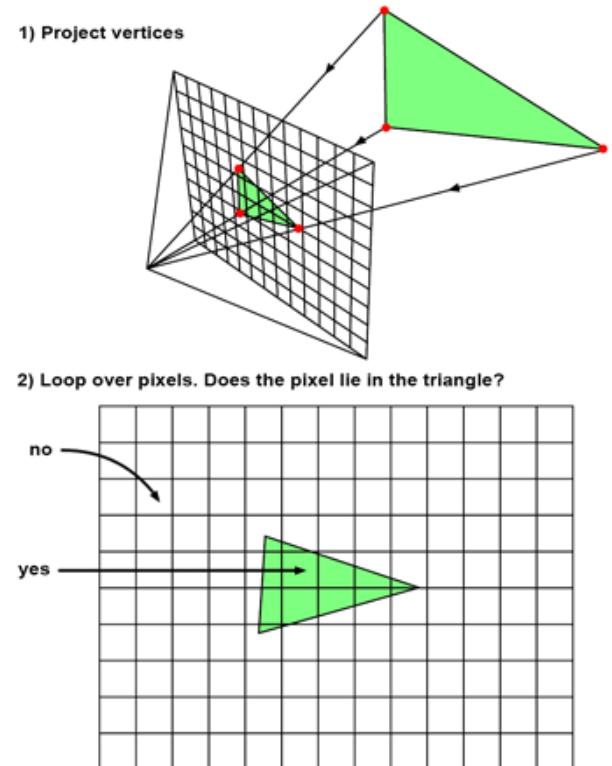
- Assume: image plane is $[-1, 1] \times [-1, 1]$
- Rays $r(t)$ can be generated if:
 - Image resolution $r_x \times r_y$ is given
 - Position of eye (aperture) e is given
 - Vectors Forward, Right, Up are given
 - Focal length f or angle of view α is given



$$r(t) = e + t * (f * \text{Forward} + (i + 0.5) / r_x * \text{Right} + (j + 0.5) / r_y * \text{Up})$$

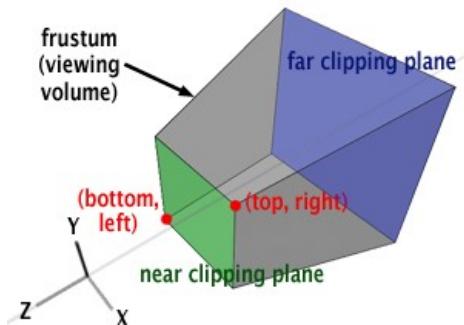
Camera in rasterization

- Rasterization-based rendering projects objects (triangles) from 3D scene onto image plane and for each pixel finds a position of projected object
 - Object centric approach
- The process of finding pixel coordinates on image plane of 3D point is done as follows:
 - 3D points from world space are transformed to camera space: **world-to-camera matrix**
 - **Projection matrix** is applied on transformed point
 - Resulting points are convert to raster space (image plane with pixels)

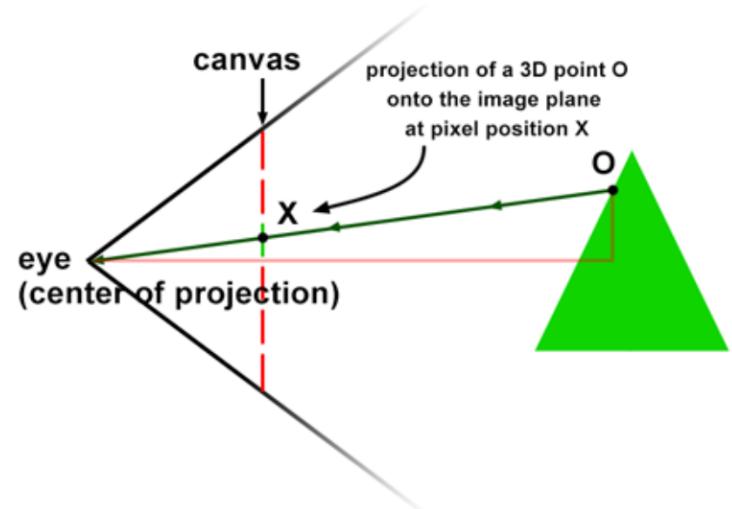


Projection matrix

- In rasterization, camera is used to define perspective projection matrix.
- General perspective projection matrix is defined with viewing frustum **near** (n), **far** (f), **left** (l), **right** (r), **top** (t) and **bottom** (b)



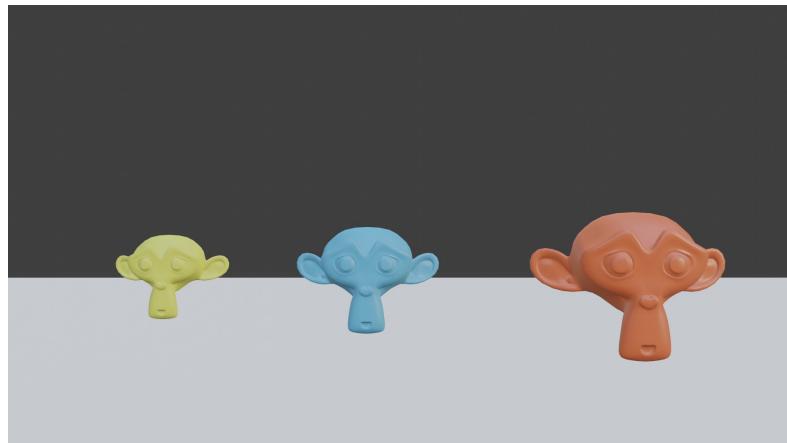
$$\begin{bmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{bmatrix}$$



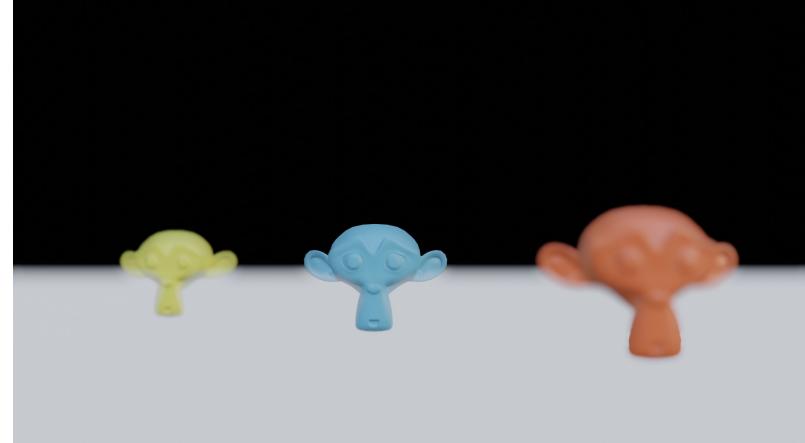
© www.scratchapixel.com

Virtual pinhole camera notes

- Virtual pinhole camera has infinitesimally small aperture
 - Image will be perfectly sharp
 - Additional methods are needed from simulating lens effects such as depth of field
 - Lens system introduce focus plane in 3D scene where objects are in sharp focus and blurred otherwise



Perfectly sharp image



Depth of field

Virtual pinhole camera notes

- Virtual pinhole camera has infinitesimally small aperture → light energy is carried instantaneously by ray
- Time in image plane is exposed to light doesn't affect amount of light falling on image plane
 - Exposure is simulated in already rendered image or adding it as parameter to lights

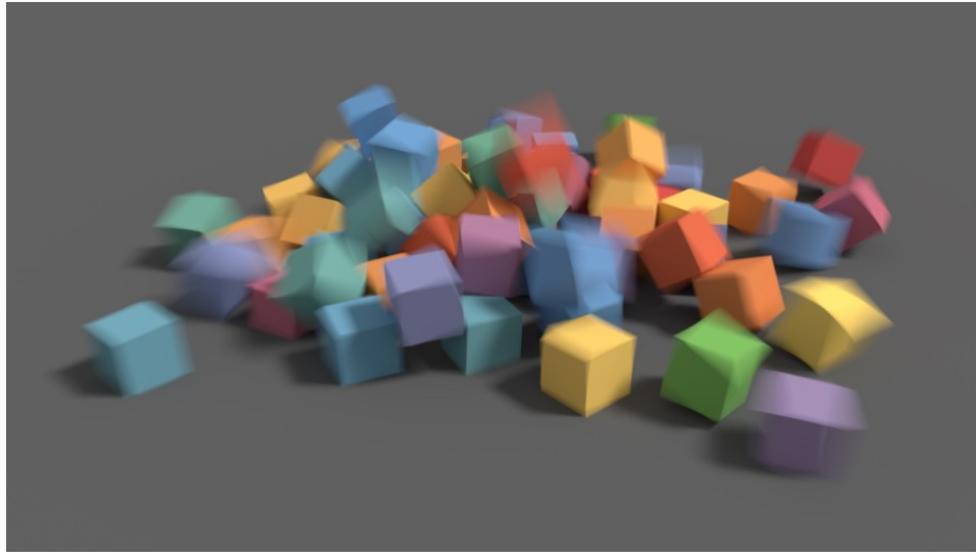


Different exposures of the same render:

https://docs.blender.org/manual/en/latest/render/color_management.html

Virtual pinhole camera notes

- In simulated camera, light transport is considered instant, therefore, simulation of motion blur requires additional simulation
- Motion blur must be additionally simulated using **shutter speed**: time in which camera door is opened to allow incoming light



Motion Blur

https://docs.blender.org/manual/en/latest/render/cycles/render_settings/motion_blur.html

More into topic

- More about camera film, aspect ratio:
<https://www.scratchapixel.com/lessons/3d-basic-rendering/3d-viewing-pinhole-camera/how-pinhole-camera-works-part-2>
- Simulating camera lenses:
 - https://www.pbr-book.org/3ed-2018/Camera_Models/Realistic_Cameras
 - <https://github.com/appleseedhq/appleseed/pull/2914>
 - <https://developer.nvidia.com/gpugems/gpugems/part-iv-image-processing/chapter-23-depth-field-survey-techniques>

Summary questions

- https://github.com/lorentzo/IntroductionToComputerGraphics/tree/main/lectures/9_light

Literature

- <https://github.com/lorentzo/IntroductionToComputerGraphics>
- ScrachAPixel lesson:
<https://www.scratchapixel.com/lessons/3d-basic-rendering/3d-viewing-pinhole-camera>