Lecture 9: Light, Color and Shadows

DHBW, Computer Graphics

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22.2.2023.

Syllabus

- 3D scene
  - Object
  - Light
  - Camera
- Rendering
- Image and display


FLY
https://discover.therookies.co/2018/06/24/learn-how-to-light-and-render-like-a-pixar-artist/

https://discover.therookies.co/2018/06/24/learn-how-to-light-and-render-like-a-pixar-artist/

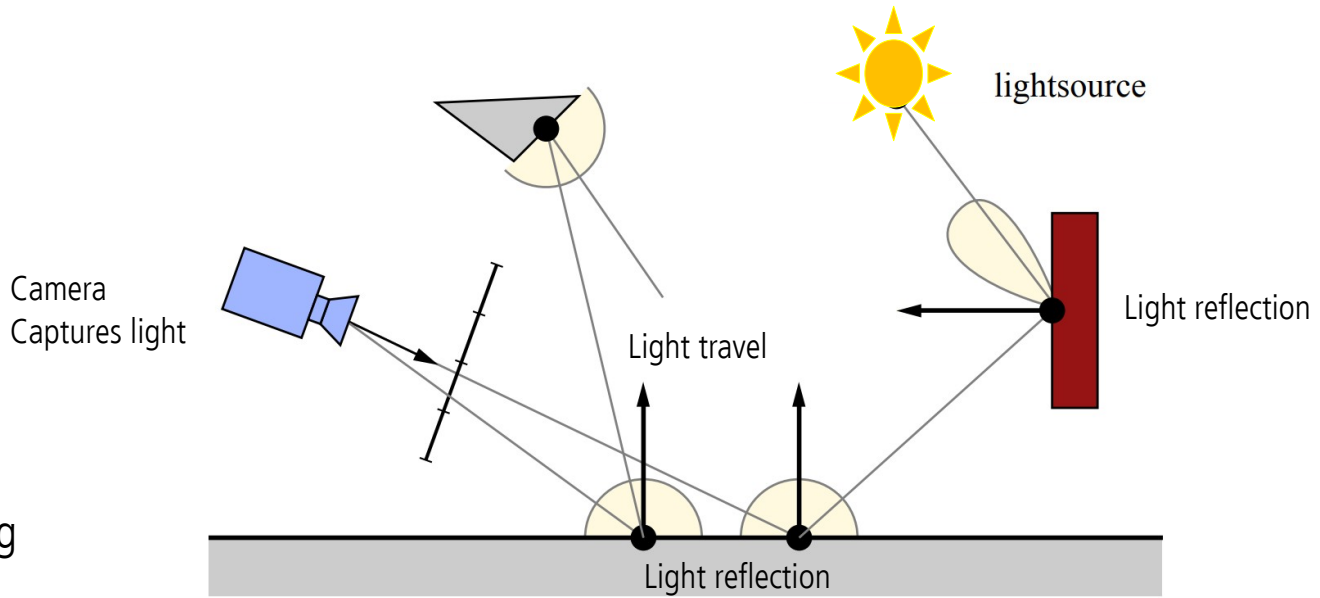
Light is important because without light...

Light sources with size and shape would be visible if we would look towards them.

Light and color

Light and image formation

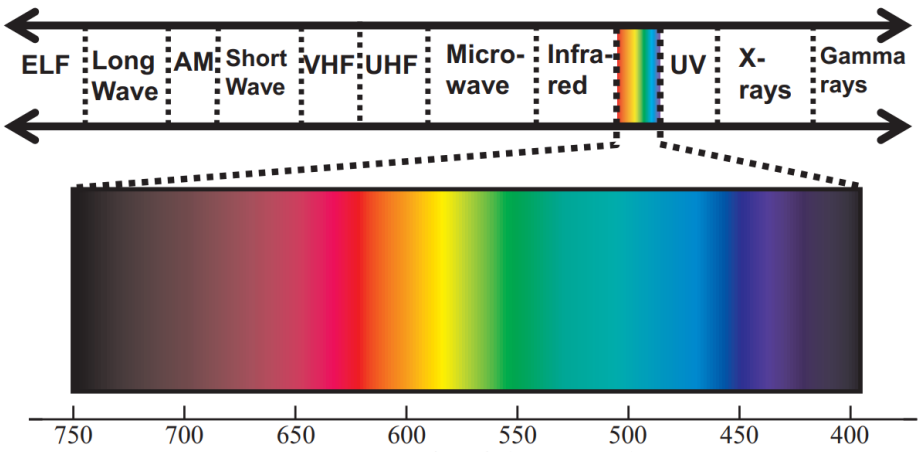
- Light is emitted from light sources, travels along rays and interacts with object in the scene (e.g., surface reflection)
- Image created when light falls on the sensor (e.g., camera film)
- This process is described with **rendering equation**



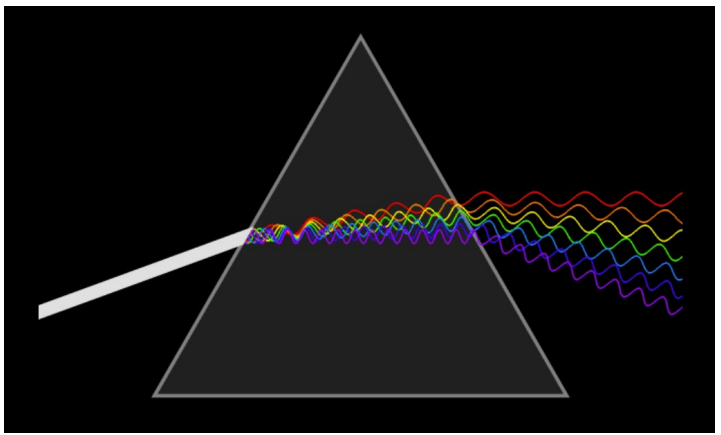
Forward tracing
VS
Backward tracing

Light frequency and color

- **Light is electromagnetic wave** (or particle) visible by eye
  - Visible spectrum: wavelength 400 – 700 nm
- Different wavelengths (frequencies) are perceived as different **color**
  - color is **perceptual (psychophysical)** phenomena rather than **physical** one



https://blog.selfshadow.com/publications/s2013-shading-course/#course_content

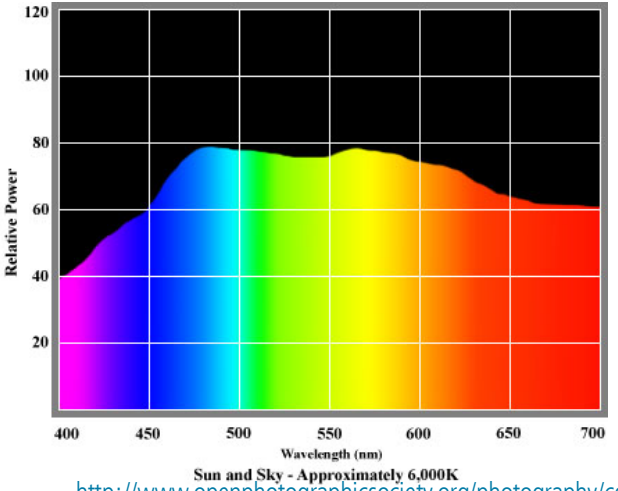


White light is made of all visible colors
https://en.wikipedia.org/wiki/Dispersive_prism

Spectral power distribution

- Light is characterized by **spectral power distribution (SPD)**
  - Range and intensity of colors light produces at each wavelength in the visible spectrum
- Sun (midday sun Western/Northern Europe) is reference for **natural light**
  - **Daylight illuminant** - **D65** by CIE - International Commission on Illumination

https://commons.wikimedia.org/wiki/File:Sun-in-the-sky.jpg

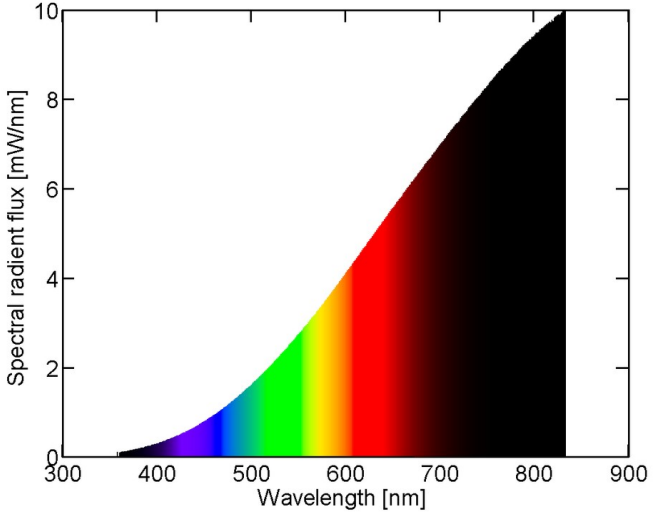


http://www.openphotographicsociety.org/photography/colour-light-and-optics/colour/203-spectral-power-distribution

Spectral power distribution

- Light sources can be grouped into either natural or artificial light sources.
- Color quality of artificial forms of lighting is compared to natural light
- **Color rendering index: ability of light source to reproduce color of object seen under D65 (natural light)**

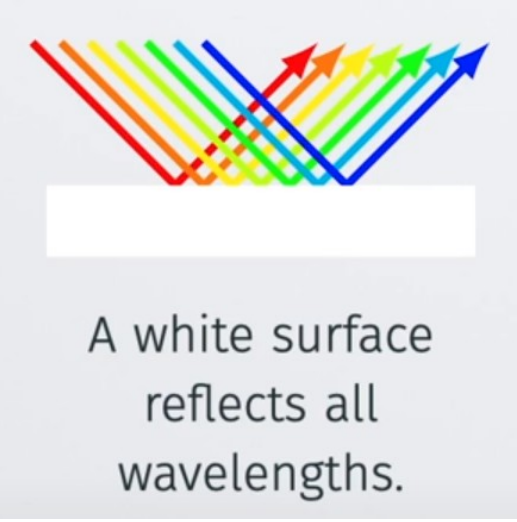
https://en.wikipedia.org/wiki/Incandescent_light_bulb

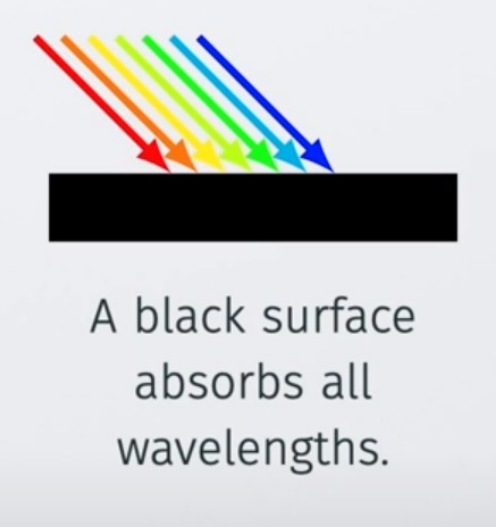


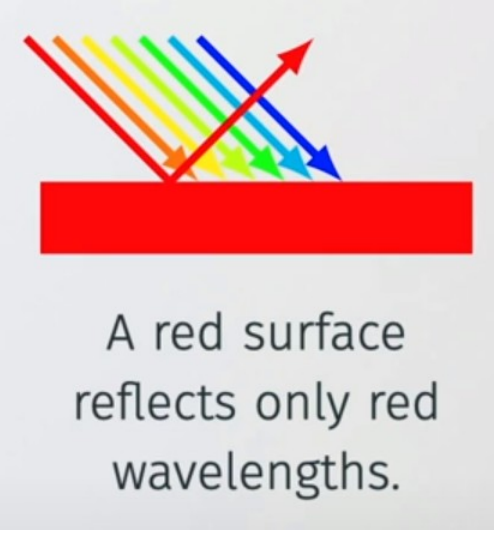
SPD of incandescent light source. Light is perceived as yellow since eye is less sensitive to red.

Material reflectance

- Light falling on opaque surface will reflect and absorb
- **Reflected light is perceived as color of object surface**
- Different materials are characterized with different **spectral reflectance curves**

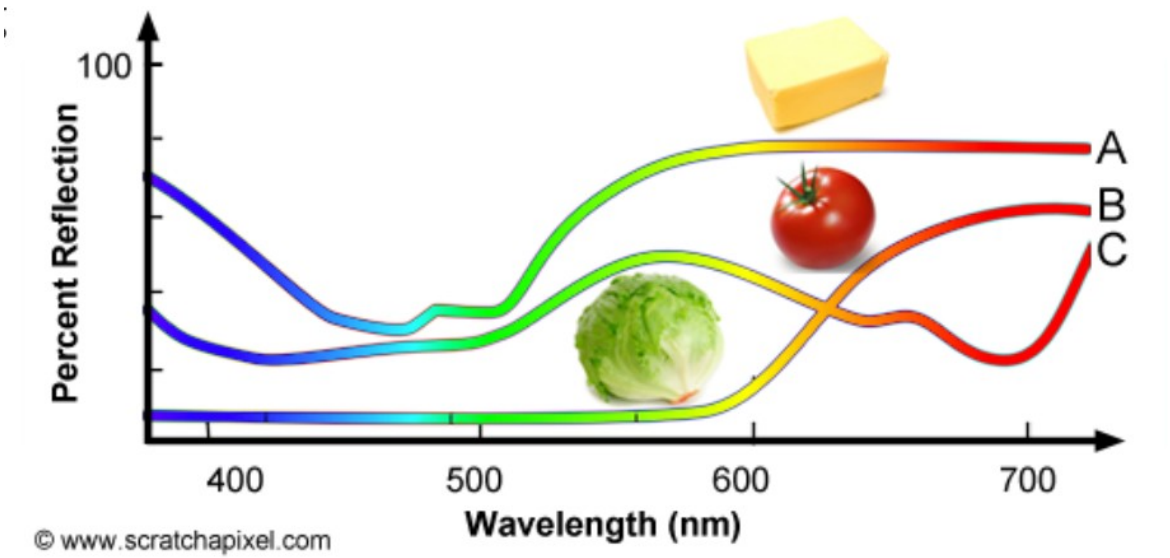






Spectral reflectance curve

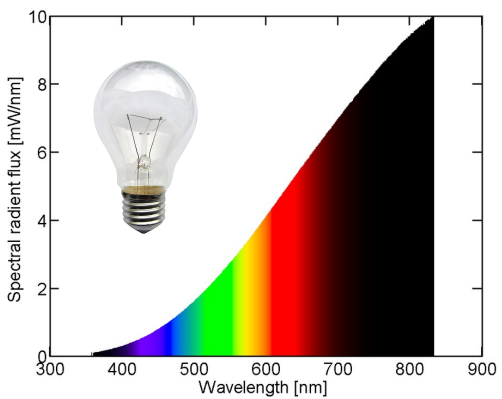
- SPD of light source defines its color and intensity
- **Spectral reflectance curve: SPD describing light reflected from objects**
  - Fraction of the light reflected by the surface of the object over the amount of white light illuminating the object



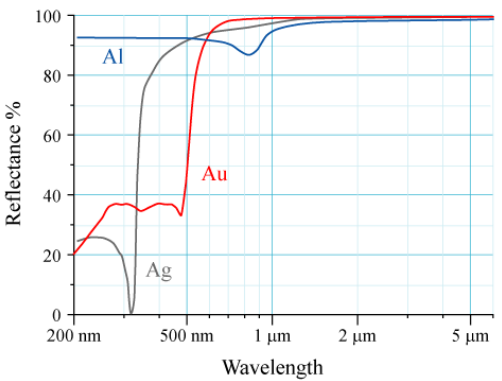
https://www.scratchapixel.com/lessons/digital-imaging/colors

Material reflectance

- Reflected energy depends on:
  - Incoming light energy `(E)`
  - Reflectance `(R)` or absorption `A = 1 - R, A + R = 1`
    - R and A are spectral values, but in graphics we use RGB values

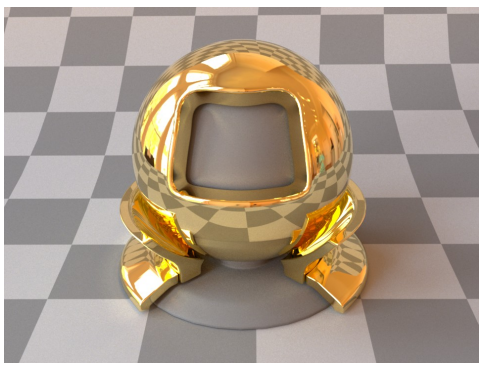


Power spectral distribution of light → incoming light energy `(E)`



Spectral reflectance curve → Material reflectance `(R)`

https://en.wikipedia.org/wiki/Reflectance



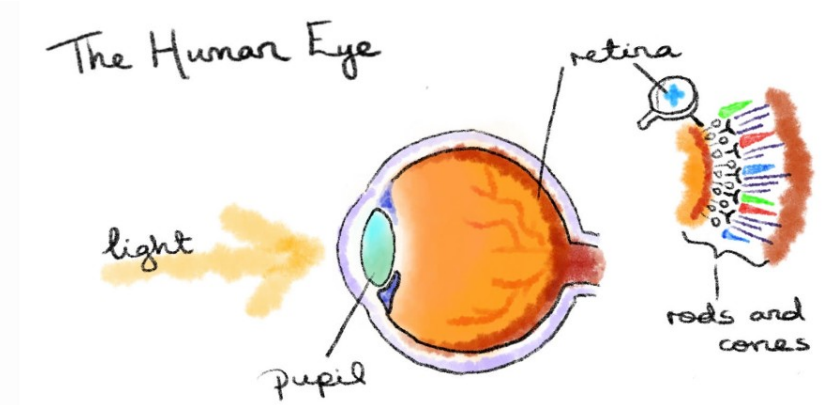
`Reflected = E * R`

Light and human visual system

- Human visual system; back of eye (the retina) is covered with light sensitive receptors – **photo-receptive cells**

- **Cone cells** – responsible for **trichromatic** color vision
  - "Active" in well lit environments (e.g., daylight)
  - Three types sensitive to: **red, green and blue light**

- **Rod cells** – sensitive to smaller amount of light intensity but not reproducing colors
  - "Active" in low lit environments (e.g., night)

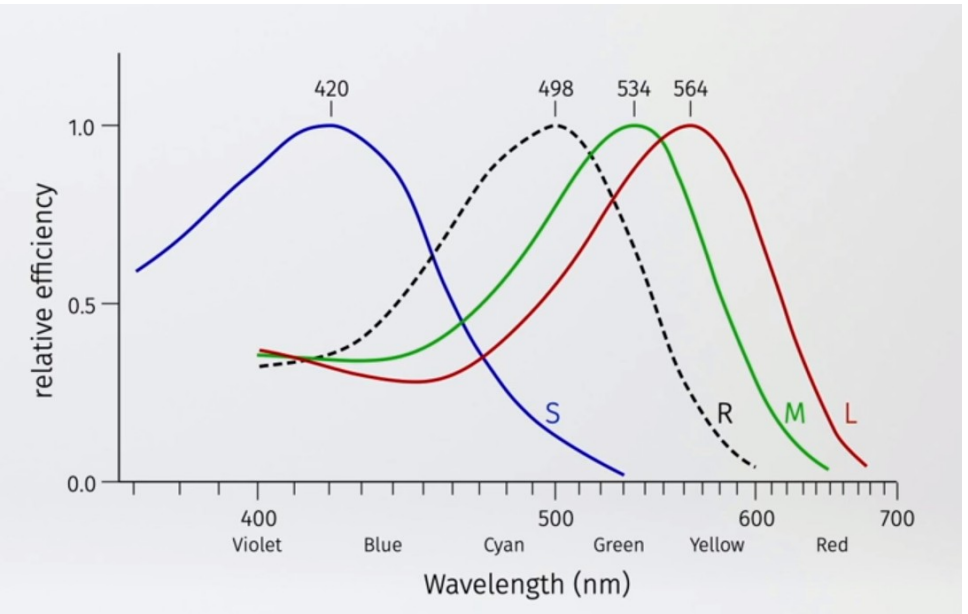


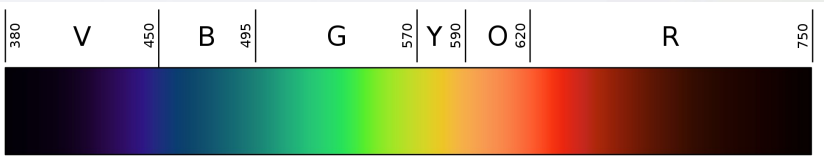
http://daisymolving.github.io/2018/07/30/design-fundamentals-colour.html

Light and human visual system

- **Cone cells**
  - **Trichromatic color vision (RGB)**
  - Well-lit scenes
- Rod cells
  - Intensity
  - Low-lit scenes

Rod cells: intensity Cone cells: RGB





https://www.handprint.com/HP/WCL/color1.html

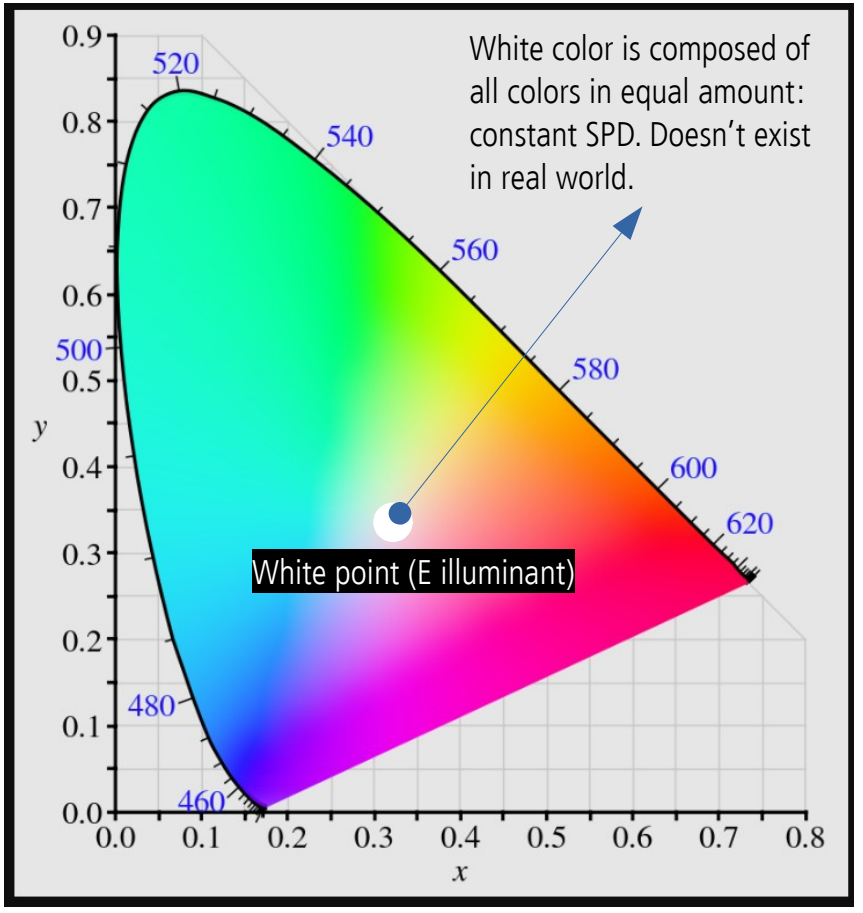
From SPD to color

- **Light from light source** is characterized with spectral power distribution (SPD)
- **Light reflected from object** is defined with SPD; spectral reflectance curve
- **Specifying colors as wavelengths is impractical and in most cases not needed**
  - For rendering we will ignore wave effects such as diffraction, interference and polarization will be ignored
  - Colors must be represented so that they can be visualized to human visual system
- **SPDs must be transformed in color spaces suited for trichormatic vision**
  - SPD is transformed in color hue and color brightness values
  - Light is described with rays which "carry" intensity (brightness) and color (hue)

More on spectral rendering: https://jo.dreggn.org/path-tracing-in-production/2017/talk-jo/

Color space and gamut

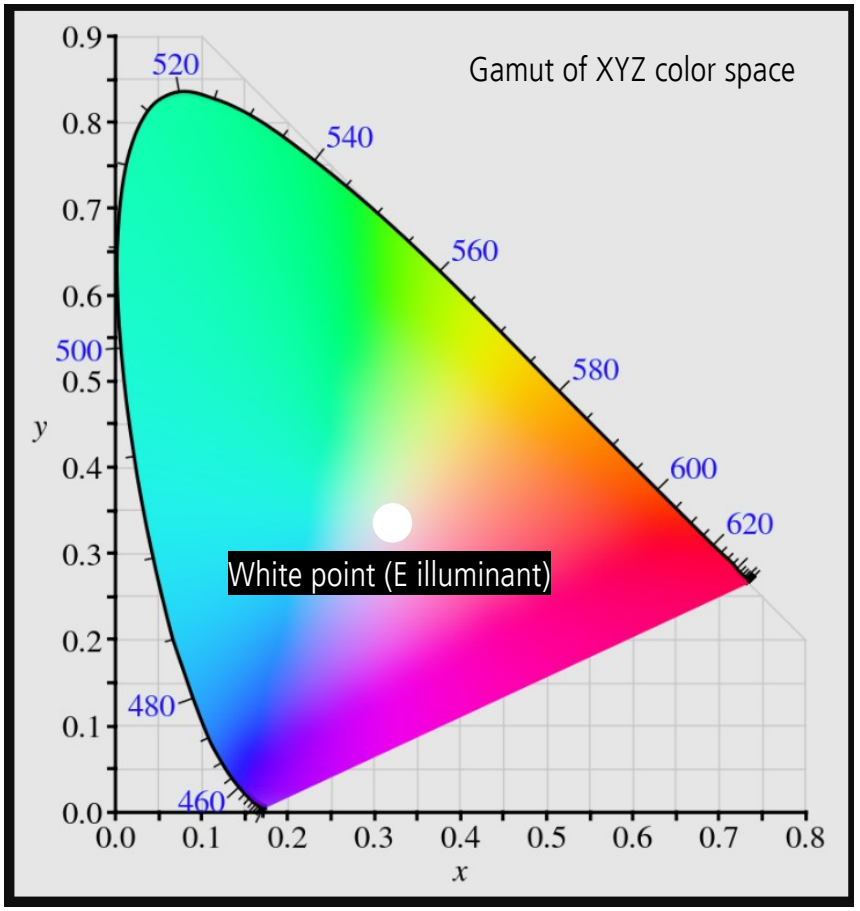
- **Colorspace**
  - Model to represent colors perceived by human visual system
  - Way of representing colors through numerical values (e.g., image pixels or calculation)
  - **CIE XYZ** is foundation for all color spaces
  - **RGB** model is most important for computer graphics
- **Gamut**
  - Range of possible colors that can be represented by particular colorspace



Gamut of XYZ color space:
https://en.wikipedia.org/wiki/CIE_1931_color_space

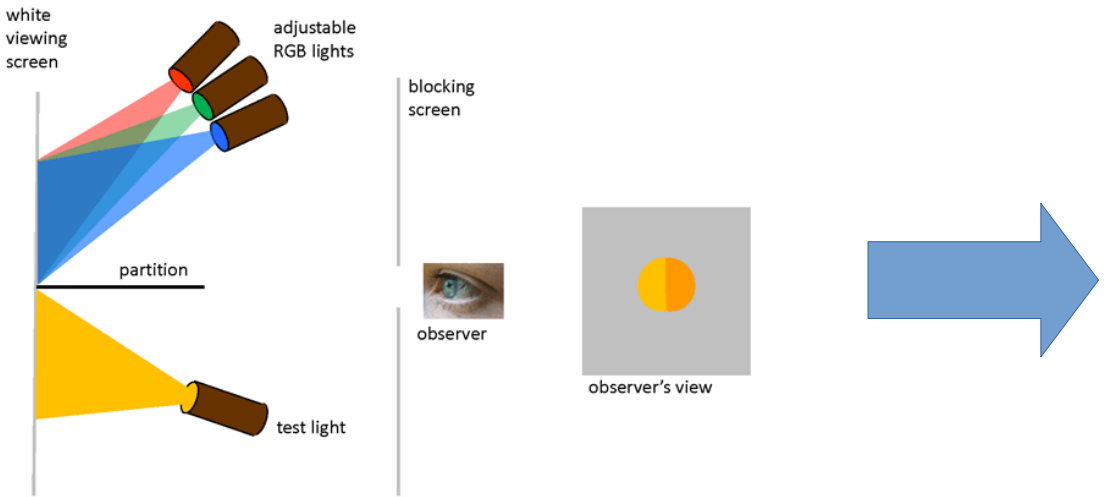
XYZ colorspace

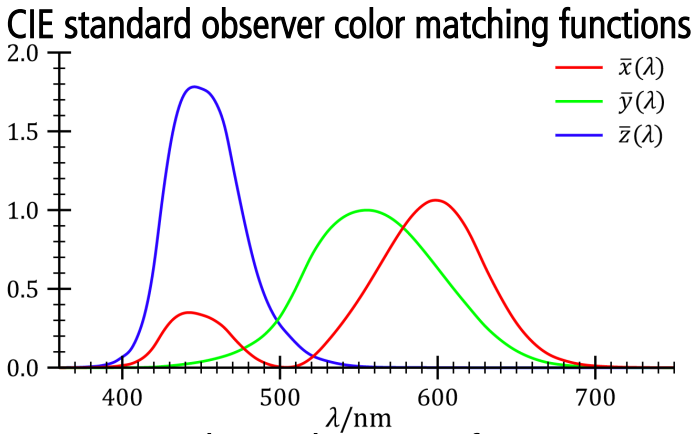
- Trichromatic system motivated idea that any color can be represented by combination of three values
  - **Artificial additive primary colors (X, Y, Z)**
- XYZ values would serve as basis for converting SPD to color spaces visible to human visual system
- **Gamut of XYZ color space** - full range of possible colors visible by human visual system
- To find transfer function from SPD to XYZ colorspace, **color matching experiment** was performed



Color matching experiment

- **Any color perceived by human visual system can be achieved by combining R, G, B signals** (trichromatic theory of color vision)
- Colormatching experiment used trichromatic theory to form **color matching functions**



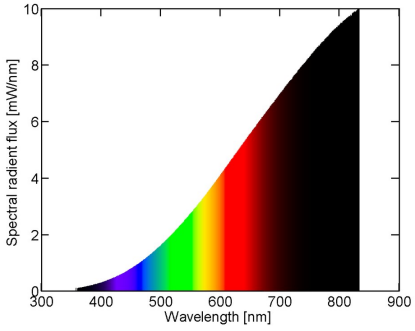


Y curve is close to luminosity function expressing the brightness

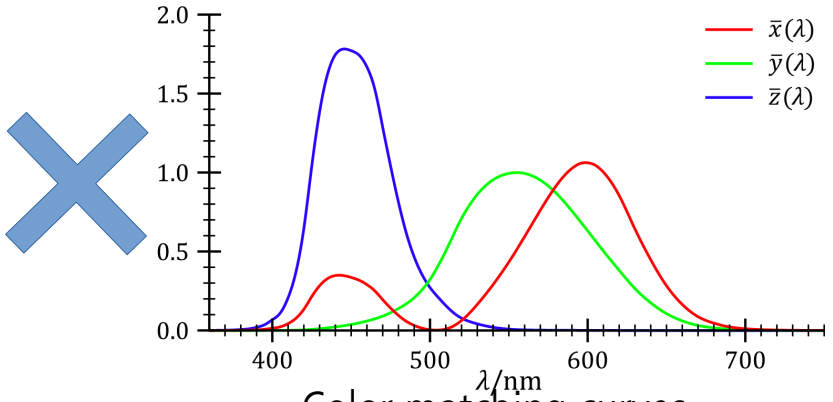
https://www.oceanopticsbook.info/view/photometry-and-visibility/chromaticity

From SPD of light source to XYZ

- **XYZ colorspace is obtained from SPD of light source using color matching functions**
  - SPD and the color-matching functions are in tabular descriptions

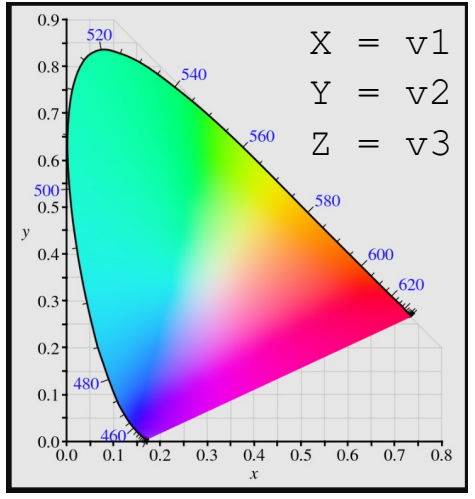


SPD of light source



Color matching curves

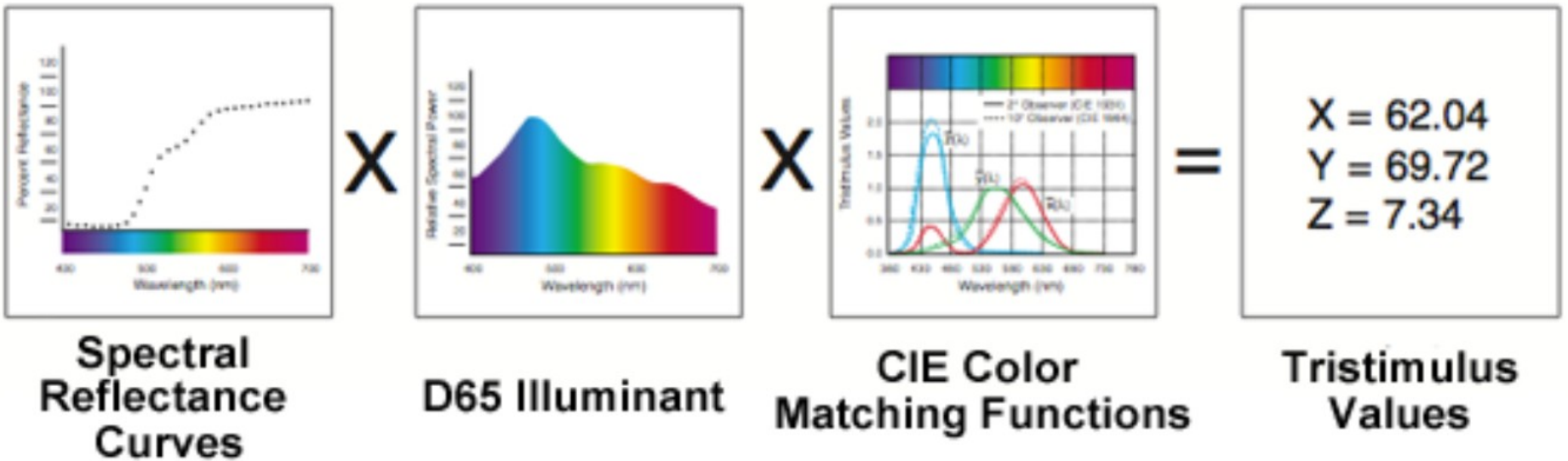
https://en.wikipedia.org/wiki/CIE_1931_color_space



XYZ color space

From SPD of reflected light to XYZ

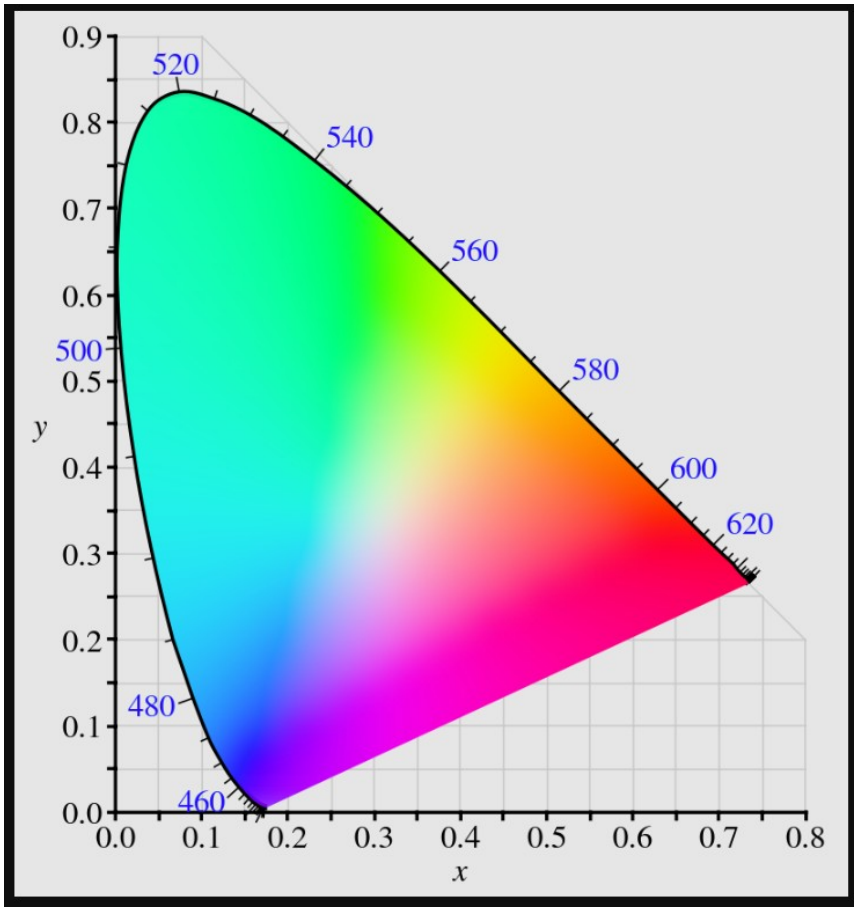
- Light reflected from object is represented as spectral reflectance curve
  - Therefore it must be multiplied by white light which caused the reflection and the standard is D65.



https://www.scratchapixel.com/lessons/digital-imaging/colors/color-space

XYZ color space

- International, device-independent standard for color specification
- System capable representing all colors human visual system can percieve
- Gold standard for color storage
- **XYZ have to be transformed to, e.g., RGB space to be visualized**

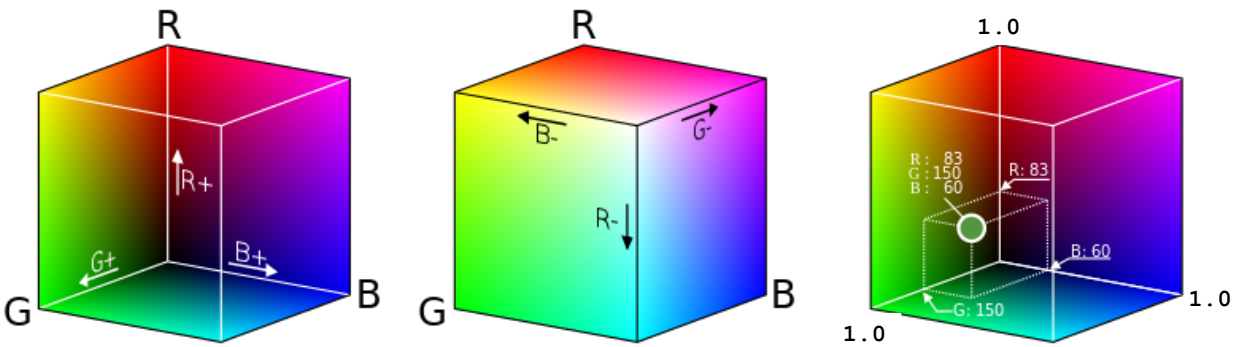


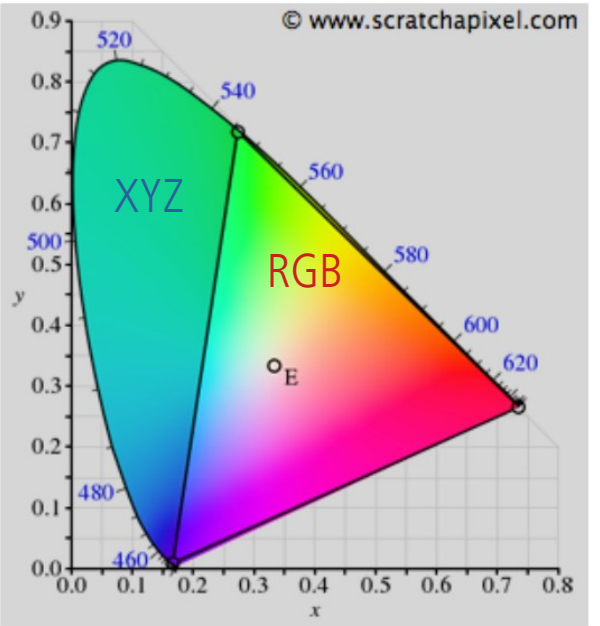
X + Y + Z = 1, gamut can be visualized using:

$$x := \frac{X}{X+Y+Z}, \quad y := \frac{Y}{X+Y+Z}$$

RGB colorspace

- Similar as human visual system: represent colors as simple sum of primary colors `(R, G, B)`
- Visualized as cube where `R, G, B` are placed on axis
- `R,G,B` intensities are in `[0,1]`





XYZ vs RGB gamut

https://www.scratchapixel.com/lessons/digital-imaging/colors/color-space

XYZ to RGB

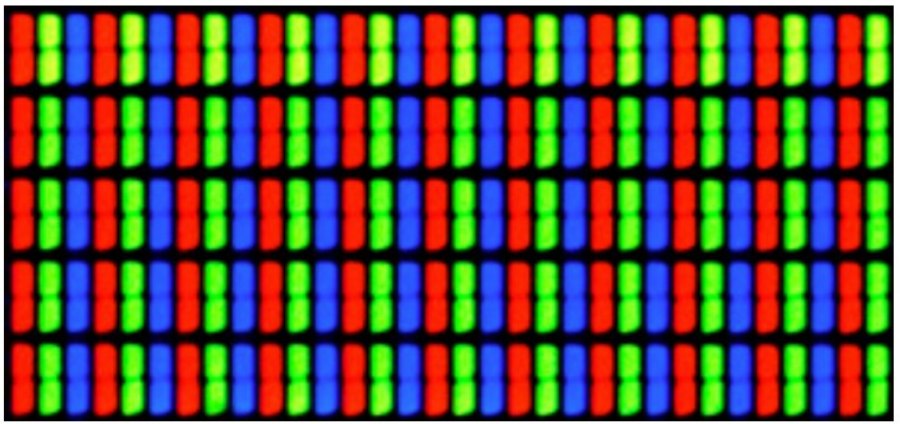
- XYZ and RBG color spaces are defined with three coordinates
  - XYZ and RGB define a 3D space (e.g., cube for RGB)
- Conversion of color from XYZ to RGB can be seen as moving a point from one 3D space to another
  - **Linear transformation** performed using **3x3 matrix**
  - Color is not changed, only expressed in different colorspace

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} 0.4124564 & 0.3575761 & 0.1804375 \\ 0.2126729 & 0.7151522 & 0.0721750 \\ 0.0193339 & 0.1191920 & 0.9503041 \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

http://www.brucelindbloom.com/index.html?Eqn_RGB_XYZ_Matrix.html
http://www.russellcottrell.com/photo/matrixCalculator.htm
https://www.oceanopticsbook.info/view/photometry-and-visibility/from-xyz-to-rgb
https://terathon.com/blog/rgb-xyz-conversion-matrix-accuracy/

RGB colorspace

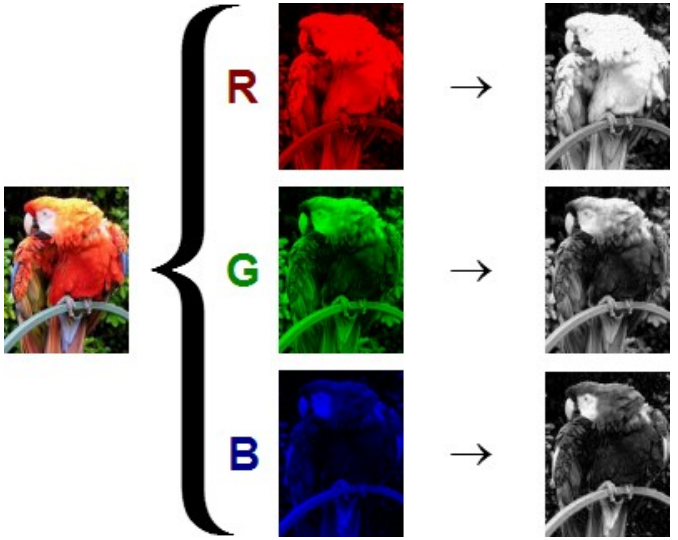
- Most **computer screens technology** is based on systems similar to RGB color model.
  - Additive colorspace: summing all RGB values gives white color
- Most rendering systems work with RGB colorspace
  - RGB and XYZ are **linear** colorspace → linear property is required for correct rendering (shading) computation

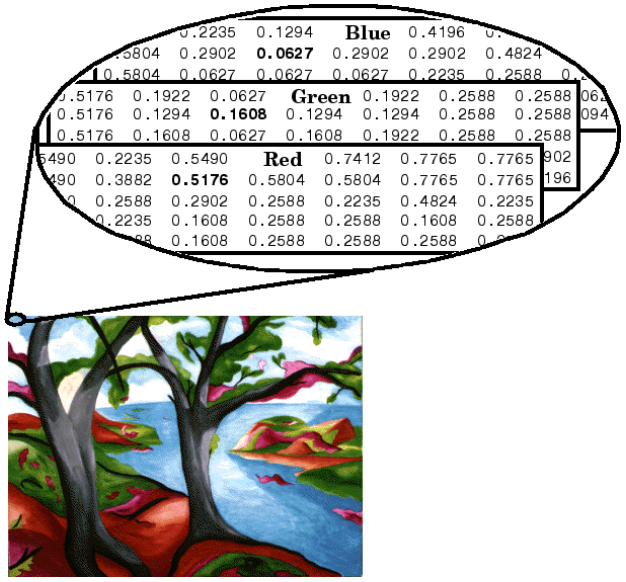


Close-up of LCD screen:
https://jakubmarian.com/the-illusion-of-rgb-screens/

RGB colorspace

- Typical image formats store three intensities in three channels: R, G, B.
  - e.g., standard images: 8 bit per channel [0,255] range
    - $2^{(8x3)} = 16.7$ milion colors (term: true color)
  - e.g., HDR images: 10 or 12 bit per channel

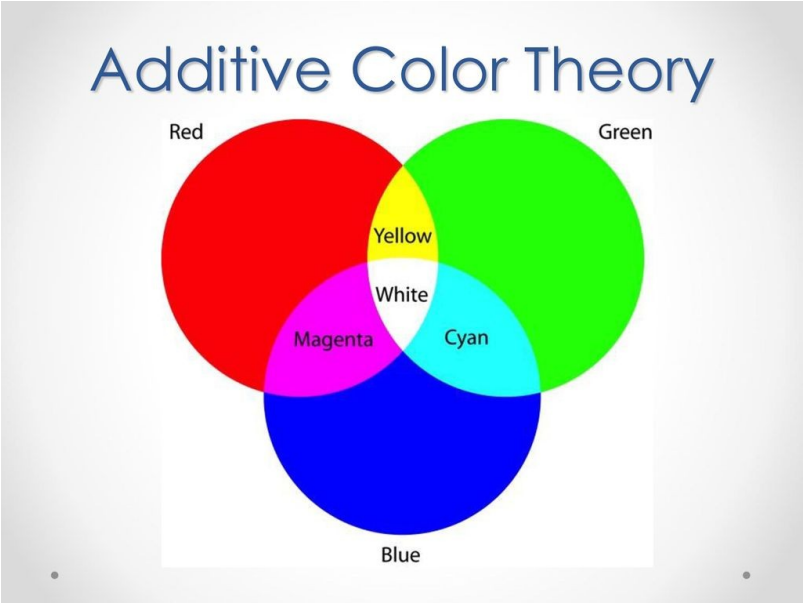




https://www.mathworks.com/help/matlab/creating_plots/image-types.html

Additive colorspaces

- Any color is created by adding **red**, **green** or **blue**
- White color is made of red, green and blue
- Usage: display devices, computer science, lighting technology → **colors are created with light emission**
- Display device (e.g., monitor) can further increase or decrease the overall global image intensity (brightness)



https://carsonparkdesign.com/what-makes-white-on-the-screen/

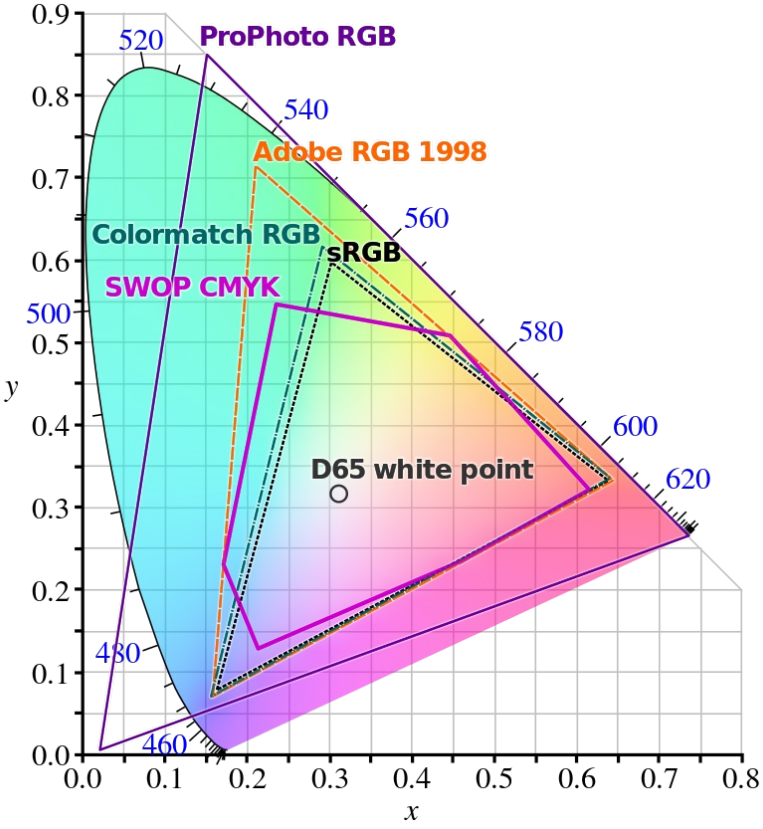
Subtractive colorspaces

- Main colors: **cyan, magenta, yellow** - white light is made by subtracting
- Usage: art, painting, printing
- **Color from canvas is not a result of light emitted from canvas, but light reflected from canvas**
  - When white light hits canvas, what is not absorbed is reflected

https://www.greenleafblueberry.com/blogs/news/modern-primary-colors

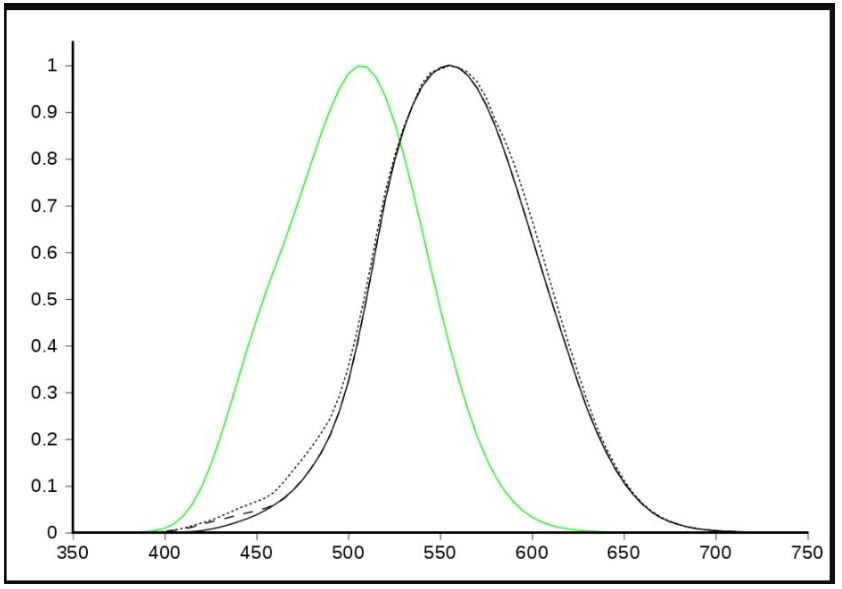
Other colorspaces

- Different colorspaces represent different gamut of colors
- RGB and CMY have small gamut! → device limitations
- RGB and XYZ are linear colorspaces (transformed using `3x3` matrix)
- Not all colorspaces are linear, e.g., **sRGB**, **HSV**, HSL
- Any non-linear colorspace must be converted to linear colorspace before 3x3 matrix transformation



Color brightness

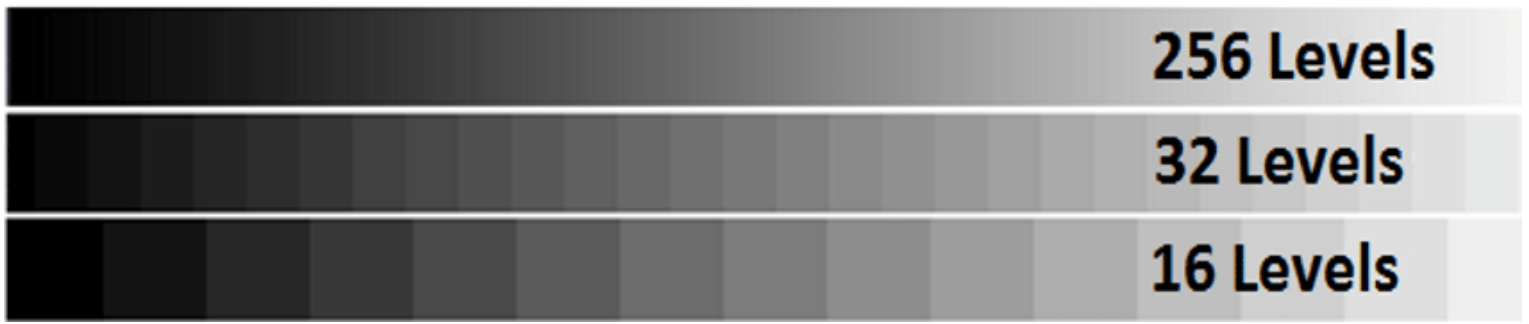
- 555 to 560 nm (green towards yellow) are perceived by the human eye as being the brightest
  - Blue color: the dimmest
  - Green color: the brightest
- How bright color appear to human eye: **luminosity function**
  - Average sensitivity of human eye to different wavelengths for well lit conditions
- Brightness or lightness is present in **HSV and YUV** color models



Luminosity function for photopic – green - (well lit conditions) and scotopic (low lit conditions) – black.
https://en.wikipedia.org/wiki/Luminous_efficiency_function

Brightness (luminance)

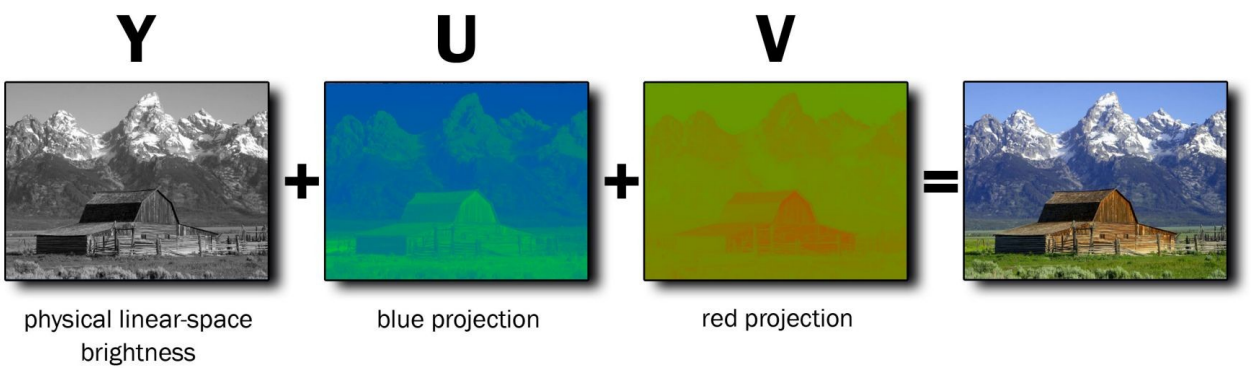
- Human eye can very well see small changes in brightness
- Many levels for brightness is needed to describe it without visual discontinuities
- **Dynamic range**: ratio between image with brightest white level and image with darkest black level
  - Very high ratios are possible in real world → image and display limitations!



https://www.researchgate.net/publication/318818149_Article_title_Graph-Based_Video_Sequence_Matching_Using_Dominant_Colour_Graph_Profile_DCGP

YUV color space

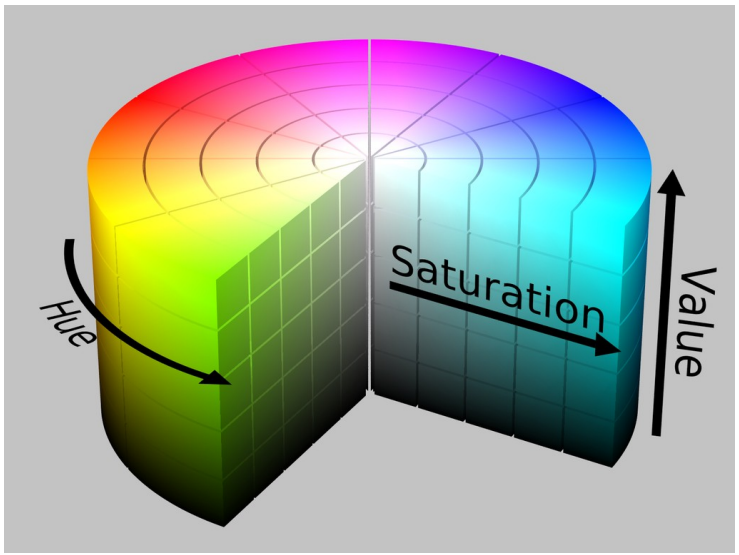
- **Human eye is more sensitive to spatial variations in brightness** (gray scale) than to spatial variations in color
- YUV color space can be particularly useful to **highlight the importance of gray scale brightness**
  - Y – brightness (luminance)
  - U and V – color (chroma)
- YUV can be obtained from RGB using linear transformations
- YUV is useful for compression: Y channel should get the most resolution (e.g., JPEG and H.264/H.265 formats)

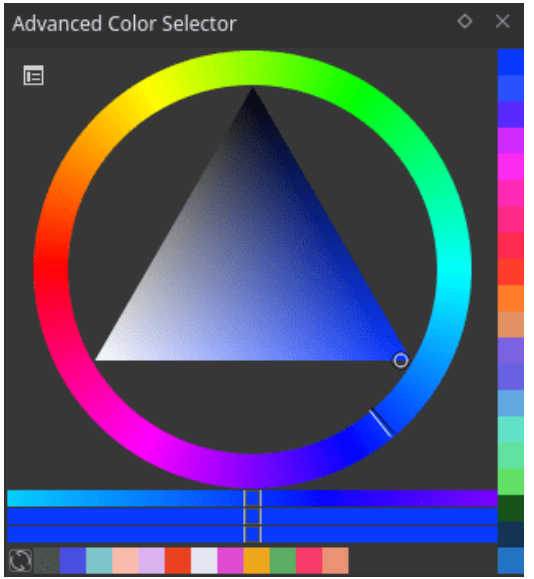


$$\begin{pmatrix} Y \\ U \\ V \end{pmatrix} = \begin{pmatrix} .299 & .587 & .114 \\ -.14713 & -.28886 & .436 \\ .615 & -.51499 & -.10001 \end{pmatrix} \begin{pmatrix} R \\ G \\ B \end{pmatrix}$$

HSV colorspace

- HSV is more intuitve than RGB:
  - H – **Hue** - color (rainbow of colors), wheel, given as angle
  - S – **Saturation** - how white the color is, how much color is mixed with white
  - V – **Value** – brightness of color

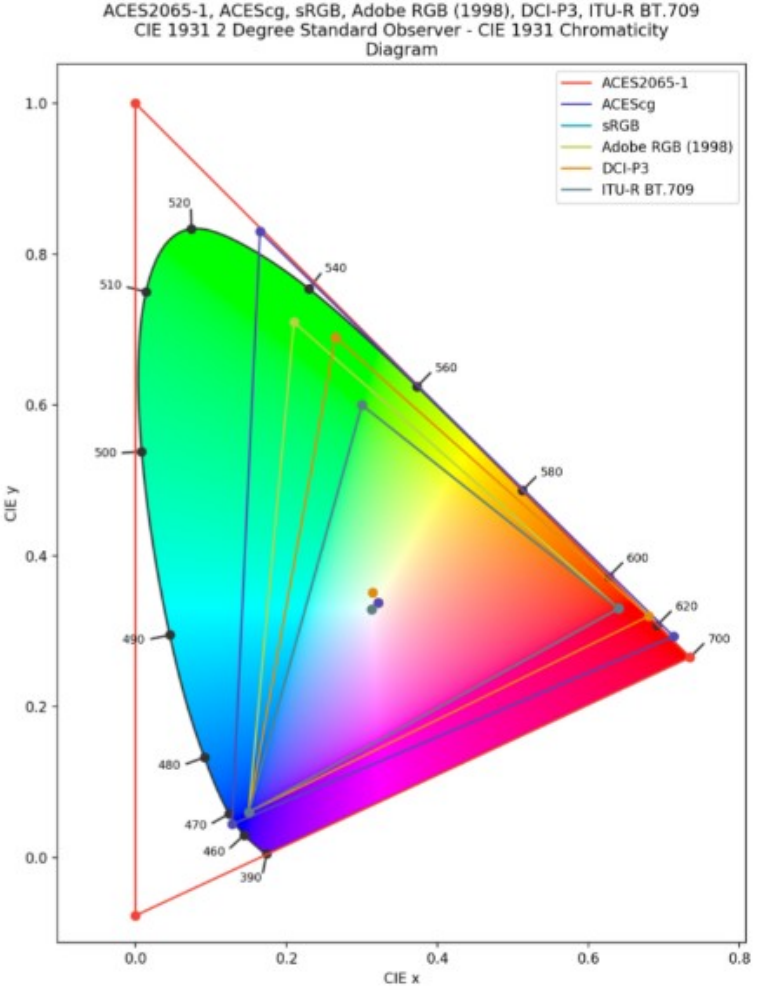




HSV is often used for colorpicking in modeling environments or painting programs:
https://docs.krita.org/en/reference_manual/dockers/advanced_color_selector.html

ACES colorspace

- **Academy Color Encoding Specification (ACES)**
  - Academy of Motion Picture Arts & Science technology committee
- **Designed to cover the full gamut**
- Goal: images should always look the same regardless of used camera and display device.
- Images in ACES color space can't be directly displayed to the screen. Conversion steps:
  - Reference rendering transform: from scene values to display-neutral output space
  - Output device transform: depends on display device (computer monitor, digital projector, etc.)
- Becoming de facto standard for professional production



https://acescolorspace.com/

Color in production

- Digital drawing and image manipulation:
  - Krita: https://docs.krita.org/en/general_concepts/colors/color_models.html
  - Gimp: https://docs.gimp.org/2.10/en/gimp-imaging-color-management.html
- 3D modeling:
  - Blender: https://docs.blender.org/manual/en/latest/render/color_management.html
  - Houdini: https://www.sidefx.com/docs/houdini/render/linear.html
  - Substance painter: https://substance3d.adobe.com/documentation/spdoc/color-management-223053233.html
- Game engines:
  - Godot: https://docs.godotengine.org/en/3.0/tutorials/3d/high_dynamic_range.html
  - Unreal: https://docs.unrealengine.com/4.26/en-US/WorkingWithMedia/OpenColorIO/

Light characterization

- **Radiometry** – measurement of radiation, physical transmission of light
- **Photometry** – like radiometry but related to human visual system
- **Colorimetry** – perception of color

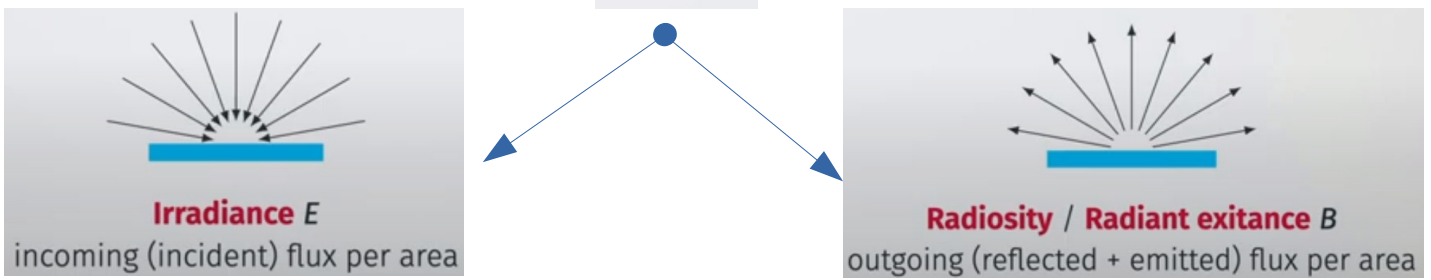
Radiometric quantities

- **Radiant energy (Q) – energy** carried by light (photons) [J]
- **Radiant flux (Φ)** – power carried by light - **energy over time** [W=Js^{-1}]

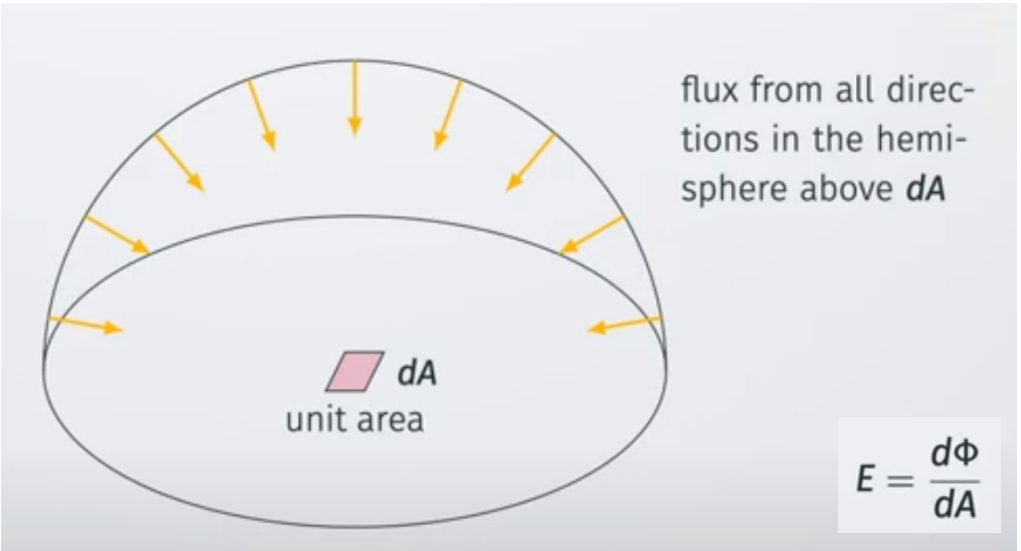
$$\Phi = \frac{dQ}{dt}$$

- **Flux density (E) – radiant flux over area** [Wm^{-2}]

$$E = \frac{d\Phi}{dA}$$

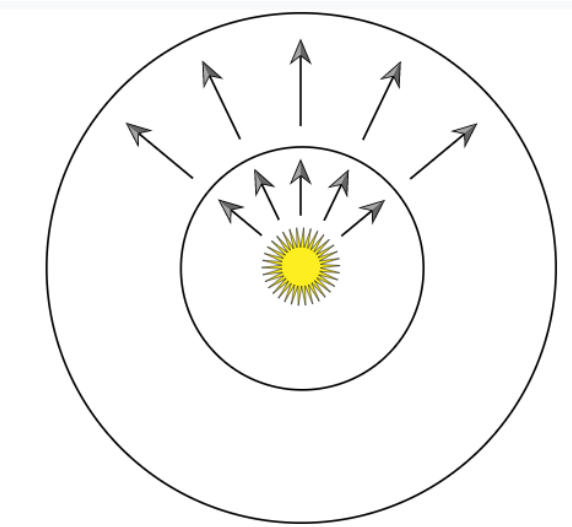


Radiometric quantities



Irradiance – overall radiant flux (light flow) incoming onto surface.

BRDF gives information of reflected light given irradiance.

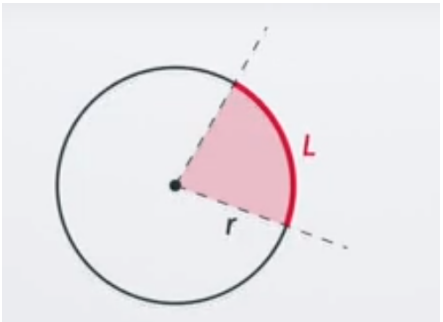


Radiant exitance – radiant flux (light flow) leaving a light source.

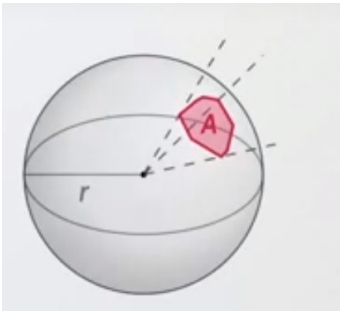
Amount of energy received from a light falls off with the squared distance from the light.

https://www.pbr-book.org/3ed-2018/Color_and_Radiometry/Radiometry

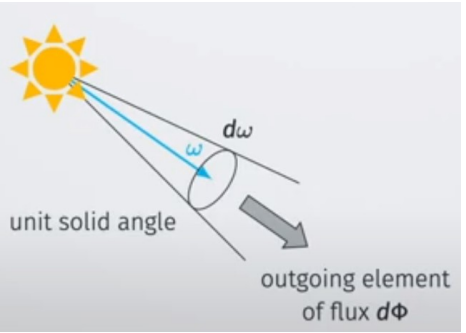
Radiometric quantities



Planar angle: angle of segment of length L on a circle of radius r



Solid angle: area of size A on a sphere of radius r (3D extension of the concept of plane angle)



Radiant intensity (I) – radiant flux with respect to **solid angle** [W / sr]

- Radiant flux of light source in specific direction.
- Radiant flux reaching certain point from some point.

$$\alpha = \frac{L}{r}.$$

Angle of full circle:

$$\alpha = \frac{2\pi r}{r} = 2\pi \text{ [rad = radians]}.$$

$$\Omega = \frac{A}{r^2}.$$

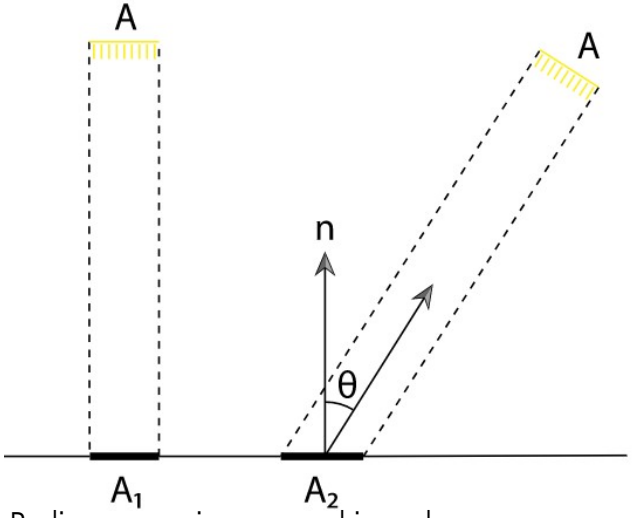
Angle of full sphere:

$$\Omega = \frac{4\pi r^2}{r^2} = 4\pi \text{ [sr = steradians]}.$$

Radiometric quantities

- **Radiance (L)** –radiant flux per unit solid angle, per unit projected area [W / (m^2 sr)]
  - Incident on surface, emerging from surface or passing through surface in certain direction
- L(p, **ω**) – radiance of small area at p along small solid angle d**ω** in direciton **ω**
  - Elementary description of light
  - Electromagnetic radiation in single ray

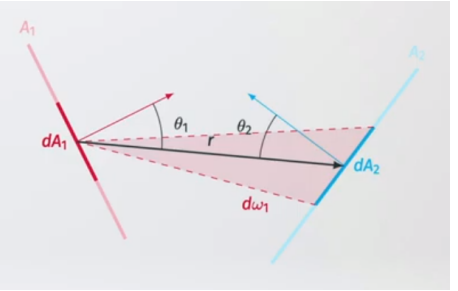
$$L = \frac{d^2\Phi}{d\omega dA_p} = \frac{d^2\Phi}{d\omega dA\cos\theta}$$



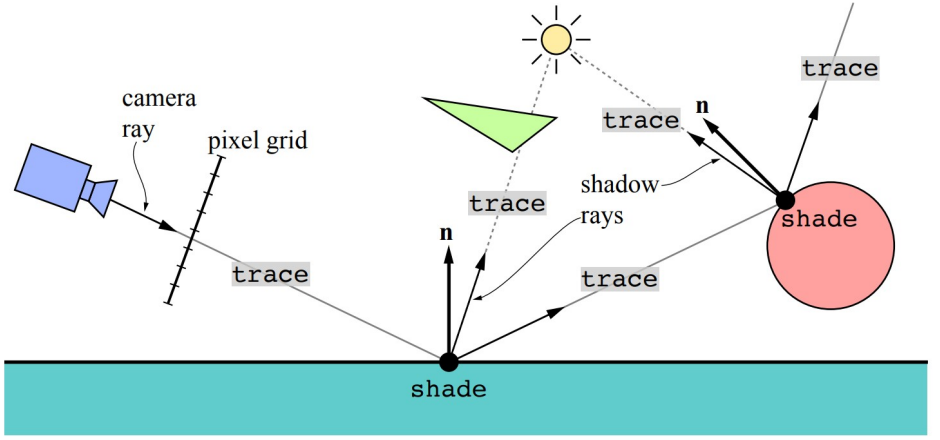
Radiance area is measured in a plane perpendicular to ray, if surface has orientation then cosine correction factor must be used.

* Image-based rendering uses this concept, namely light field technique.

Radiometric quantities

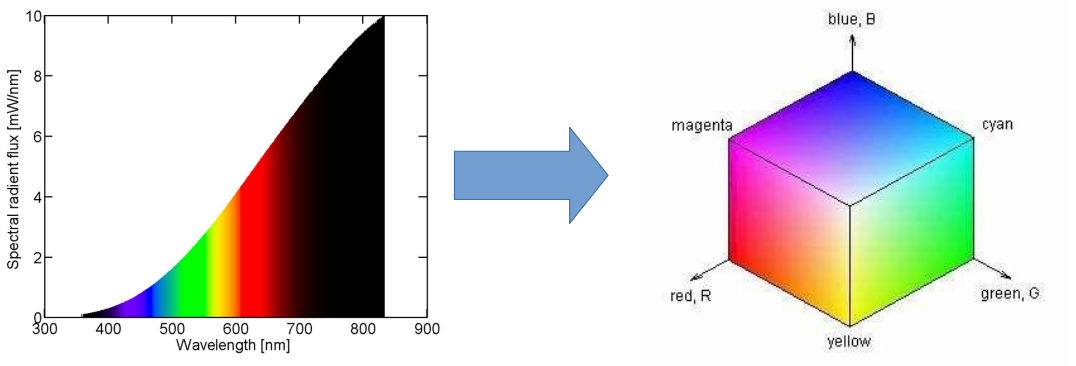


- **Radiance is what cameras measure** – prime importance for rendering
  - Rendering can be seen as evaluating radiance for each camera ray
- The **purpose of shading is to calculate radiance** along a camera ray
  - Radiance is simplified with **color and intensity**
- **Conservation of radiance along rays**
  - If two points on two surfaces can "see each other", then radiance outgoing from one surface and incoming to another surface is same and vice versa → **light can be traced between surfaces until it reaches the sensor**
  - Radiance is not affected by distance if light is traveling in a vacuum
    - Intensity is lower for surfaces which are more distant since light covers less area



Radiometric quantities and SPD

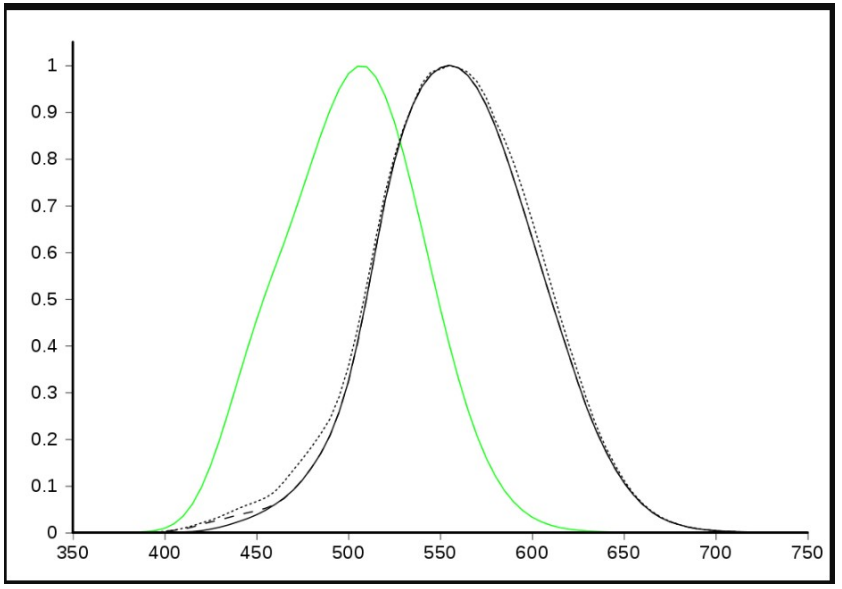
- Most light waves contain mixture of many different wavelengths – **polychromatic** (light with one wavelength is called **monochormatic**).
  - Visualized using spectral power distribution (SPD) – plot showing how light's energy is distributed across wavelengths.
- All radiometric quantities have spectral distributions
  - Using full SPDs for rendering is complex*, often radiometric quantities are represented as RGB triplets.



* Area of research dealing with spectral rendering exists and it is highly active. https://www.fxguide.com/fxfeatured/manuka-weta-digitals-new-renderer/

Photometry

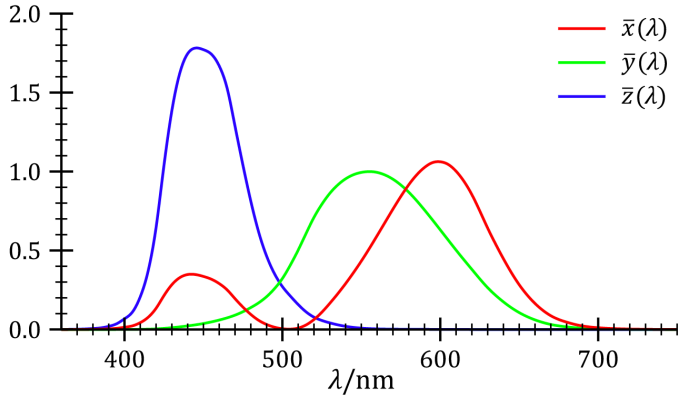
- **Photometry**: science of measuring light (like radiometry) but taking in account human visual system
- Each radiometric quantity has equvivalent photometric quantity
  - Radiant flux → **Luminous flux** (lumen - [lm])
  - Irradiance → **Illuminance** (lux - [lx])
  - Radiant intensity → **Luminous intensity** (candela - [cd])
  - Radiance → **Luminance** ([cd / m^2])
- Radiometric quantities are converted to photometric by using **CIE photopic spectral luminous curve**.
  - Average sensitivity of human eye to different wavelengths for well lit conditions



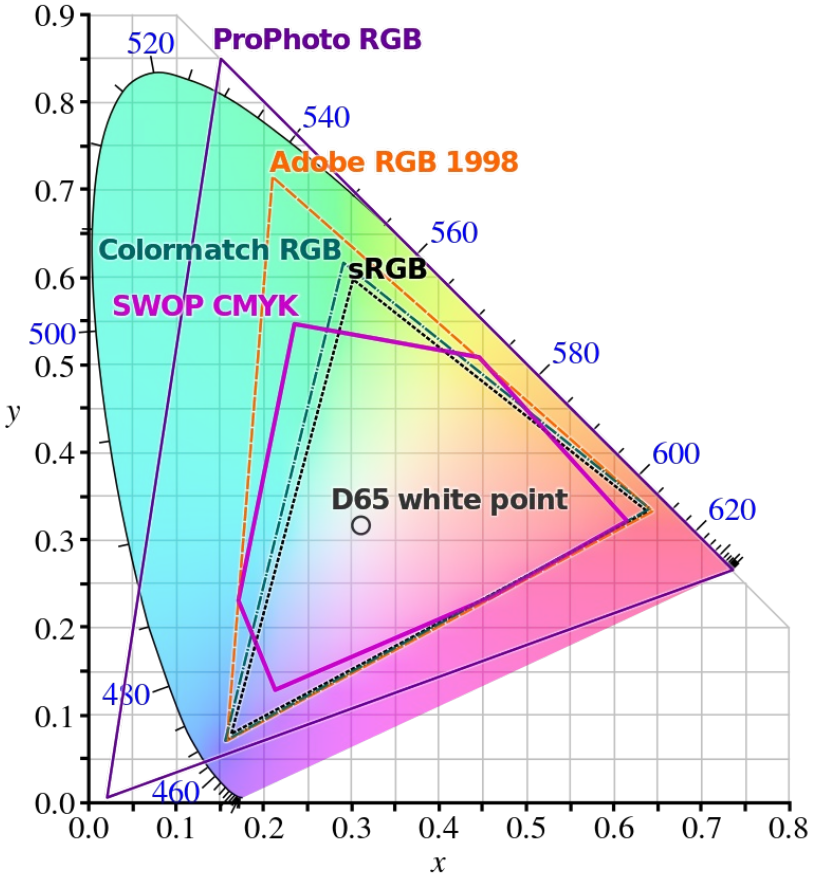
Luminosity function for photopic – green - (well lit) and scotopic (low lit) – black.
https://en.wikipedia.org/wiki/Luminous_efficiency_function

Colorimetry

- Colorimetry: relationship between SPD and perception of color
- **CIE standard observer color matching functions**
  - SPD → XYZ colorspace
- **Define colorspaces and their gamut for visualization**
- RGB color spaces are most interesting for rendering



CIE standard observer color matching functions



Gamut comparison

Rendering and RGB

- For interactive and appearance-based applications (e.g., film) RGB rendering often acceptable.
  - **Object surface reflection is defined using RGB in [0,1]** rather than spectral reflectance curve
  - **Light sources are described with RGB in [0,1] and intensity multiplier** rather than SPD
- RGB is perceptual rather than physical quantity → category error in physically based rendering
  - Correct: use spectral quantities for rendering and RGB conversion for visualization
- For predictive simulations rendering spectral quantities must be used
  - SPD is used in **spectral rendering -** more correct, but expensive
  - https://hal.inria.fr/hal-03331619/document

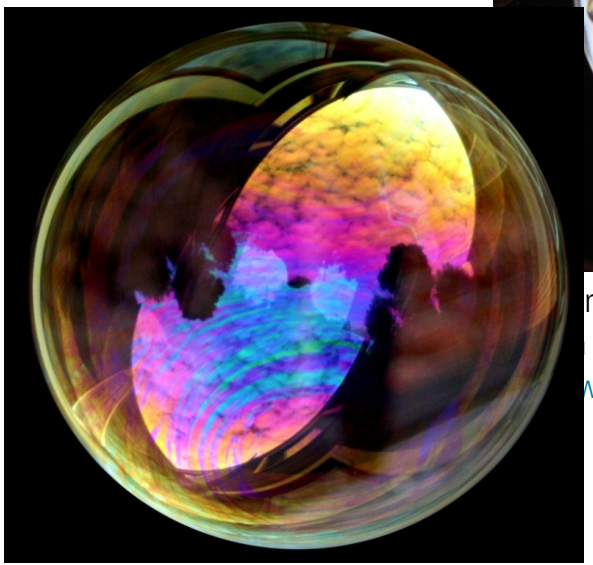
Real world light and sources of light

Light description

- Light can be described both on:
  - Microscopic scale: wave optics and photons
  - Macroscopic scale: **geometric optics**

Light: microscopic level

- Light is quantized – it comes in individual and indivisible packets called **photons**
- At same time light is **wave-like**
- Some effects of light-matter interaction can be only explained (and thus modeled*) using **wave optics**:
  - Interference
  - polarization
  - Diffraction
  - Iridescence
  - Pleochroism and birefringent
  - Etc.
- Also, knowing microscopic background often helps in getting intuition for some shading and light transport methods**



White light interference in a soap bubble – iridescence phenomena (thin-film interference) - https://en.wikipedia.org/wiki/Wave_interference

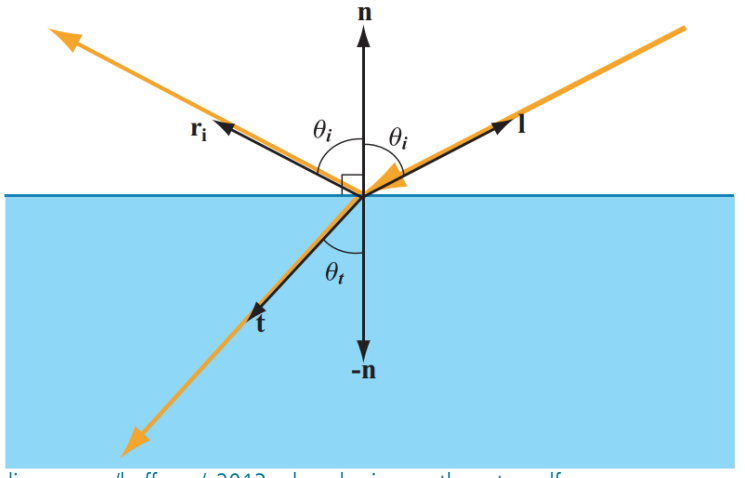
rn of Birefringence effect when a plastic box between two polarizers: wikipedia.org/wiki/Polarization_(waves)

* It is important to note that complexity of model level depends on application. Often, in computer graphics wave effects can be "faked" to achieve desired apperance: https://developer.nvidia.com/gpugems/gpugems/part-i-natural-effects/chapter-8-simulating-diffraction. On the other hand, physically based methods for achieving wave-effects is actively researched area: https://sites.cs.ucsb.edu/~lingqi/publications/202203_practical_plt_paper_lowres.pdf

** For example photon mapping: http://web.cs.wpi.edu/~emmanuel/courses/cs563/write_ups/zackw/photon_mapping/PhotonMapping.html

Light: macroscopic level

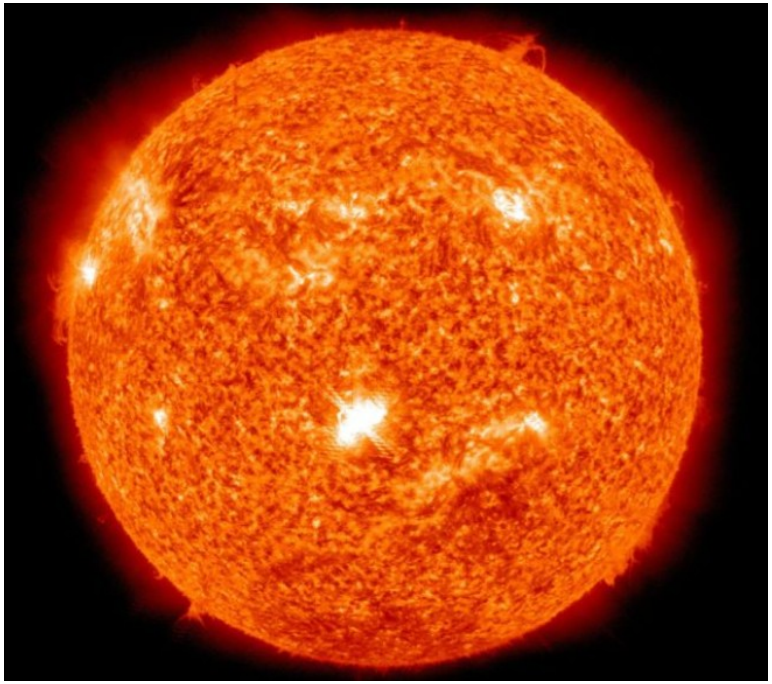
- Light in computer graphics is often modeled at macroscopic level – **geometric optics**.
  - Assumption: features with which light interacts are relative to light wavelength (or larger)
  - Light is described with rays.
  - Microscopic light behavior is described with **index of refraction** (IOR)
- In medium of constant IOR, light energy travels in a straight line
  - It only can get **absorbed**
- Light passing from one to another medium with different IOR changes speed
  - This is described with light **scattering**
  - Interface between media is represented by **surface**
- Scattering of light on surface is described with reflection and refraction described with Snell law (light direction) and Fresnel equations (light energy).



https://blog.selfshadow.com/publications/s2013-shading-course/hoffman/s2013_pbs_physics_math_notes.pdf

Sources of light

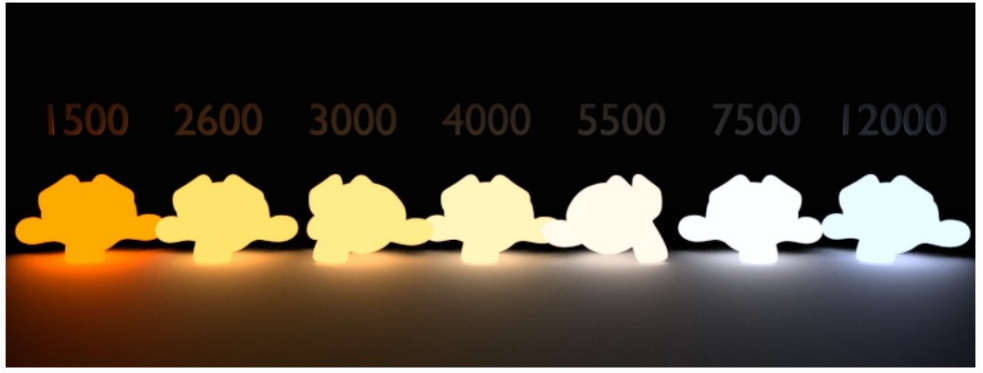
- In a real world, **every light source has a physical shape and size**, e.g., Sun or very hot objects.
- Motion of atomic particles that hold electrical charge causes objects to emit electromagnetic radiation over a range of wavelengths (Maxwell's equations)
- Different way how energy is converted into electromagnetic radiation:
  - **Incandescent (tungsten) lamps**
  - **Halogen lamps**
  - **Gas-discharge lamps**
  - **LED lights**



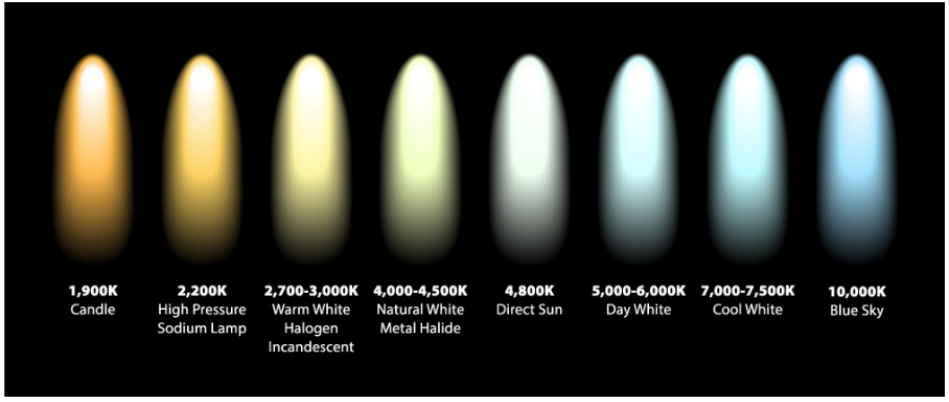
https://education.nationalgeographic.org/resource/sun

Color temperature

- Object which is heated to certain temperature emits light
- Color of emitted light depends on temperature
- Black body radiation

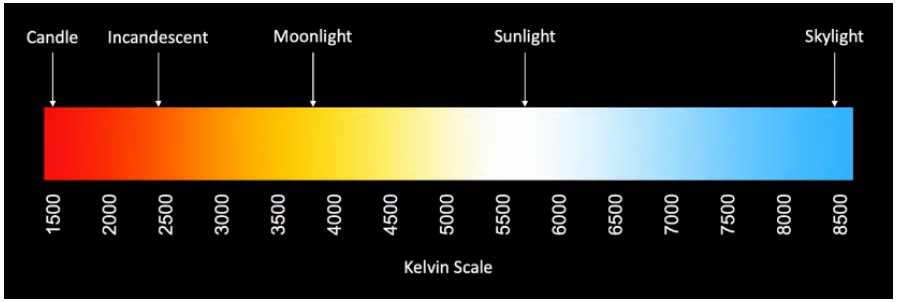


https://docs.blender.org/manual/en/latest/render/shader_nodes/converter/blackbody.html



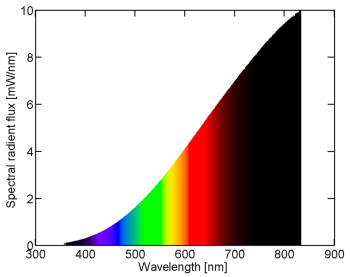
https://www.inlineelectric.com/color_temperature

Color temperature

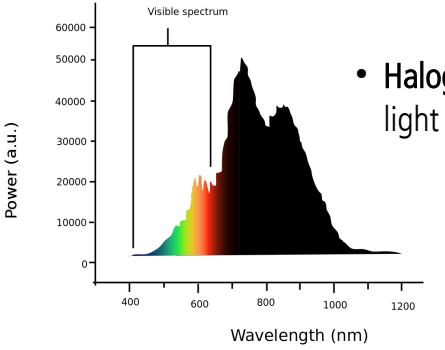


Secrets of photorealism:
https://www.youtube.com/watch?v=Z8AAX-ENWvQ&t=2s&ab_channel=Blender

Sources of light



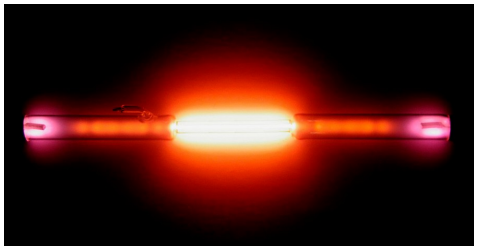
- **Incandescent (tungsten) lamps**:
  - flow of electricity through tungsten filament heats is up and causes to emit electromagnetic radiation with distribution of wavelengths depending on filament temperature.
  - A frosted glass enclosure is often present to absorb some of the wavelengths.



- **Halogen lamps**: tungsten filament is enclosed in halogen gas. Part of the filament in an incandescent light evaporates when it's heated. Halogen causes evaporated tungsten to return to filament

https://en.wikipedia.org/wiki/Halogen_lamp

Sources of light



Helium: https://en.wikipedia.org/wiki/Gas-discharge_lamp

- **Gas-discharge lamps:** passing electrical current through hydrogen, neon, argon, or vaporized metal gas, causes light to be emitted at specific wavelengths that depend on the particular atom in the gas.
- Fluorescent coating on the bulb's interior is often used to transform the emitted frequencies to a wider range.

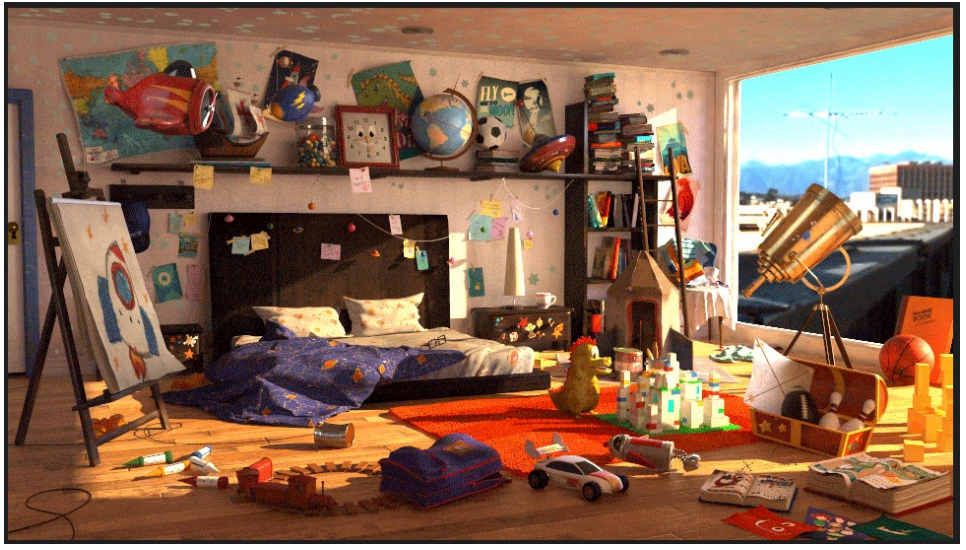
LED lights:
https://en.wikipedia.org/wiki/Light-emitting_diode

- **LED lights** are based on electroluminescence: they use materials that emit photons due to electrical current passing through them.

Light model

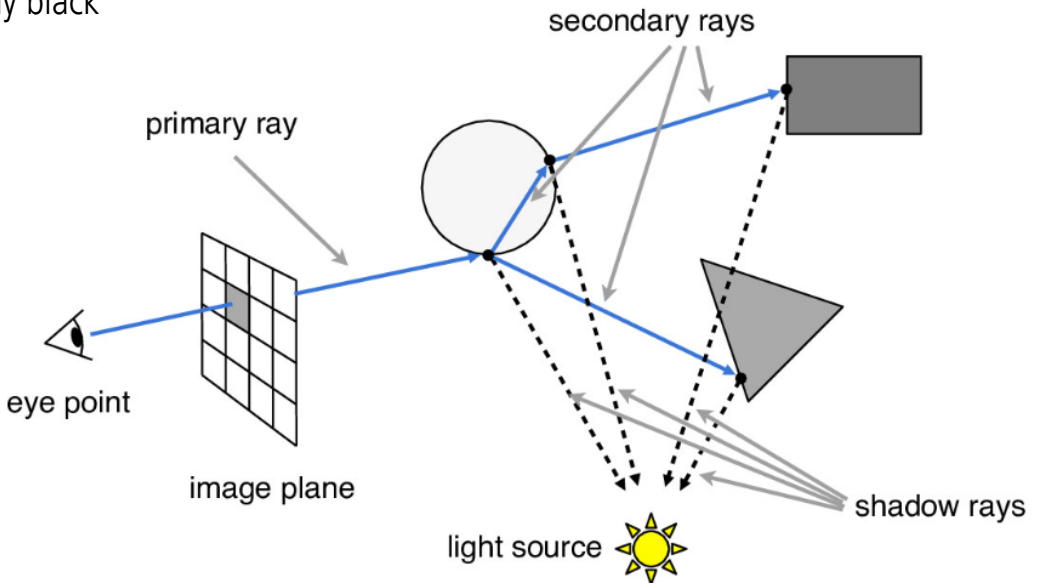
Rendering and light

- **Light is emitted from a light source**,
- **Light propagates through vacuum** (ignore participating media)
- **Light interacts with objects** (e.g., reflection) which depends on object material
- Very small **portion of light enters camera, falls on film producing image**



Rendering and light

- Rendering: calculating colors of pixels on virtual image plane
  - For each pixel, camera ray is generated and tested for intersection with objects in 3D scene → **visibility solving**
  - Color of intersection point (shading point) is calculated in **shading step**
    - Shading takes in account 3D object shape (i.e., normal), object material, viewing direction and incoming light
    - Without light resulting image would be completely black



Rendering and light

- Rendering equation: color (radiance) of shading point p in (view) direction **ω**

$$L_o(p,\omega_o) = L_e(p,\omega_o) + \int_\Omega f(p,\omega_o,\omega_i) L_i(p,\omega_i)(\omega_i \cdot n) d\omega_i$$

BRDF

Incoming light

attenuation

Emission

Reflection

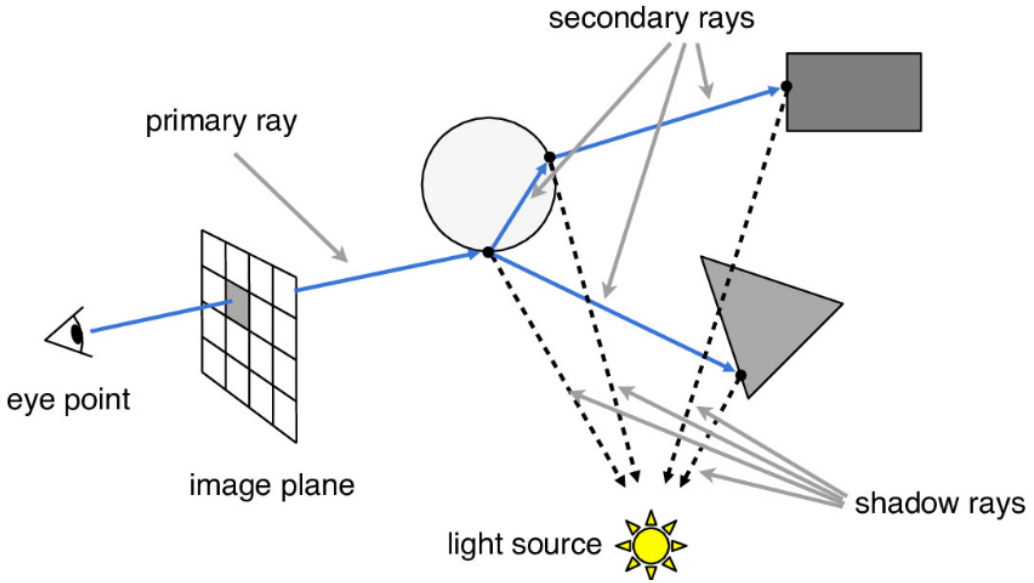
- Foundation of physically-based rendering
- Describes global illumination phenomena – light coming from all directions above object surface
- Recursive equation - not possible to solve analytically: approximation methods are used

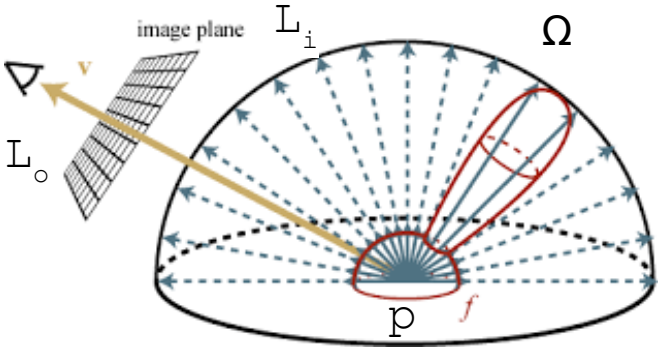
Rendering equation: https://dl.acm.org/doi/10.1145/15886.15902

Global illumination

- **Global illumination**: light can fall on surface from any direction:
  - Light sources
  - Surfaces reflecting light

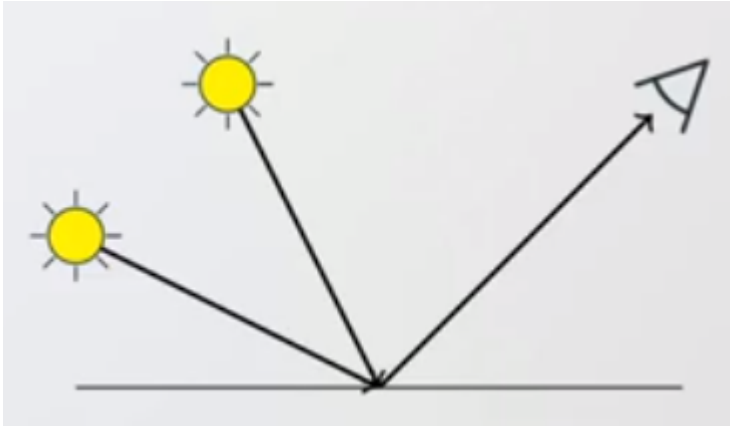
$$L_o(p, \omega_o) = L_e(p, \omega_o) + \int_\Omega f(p, \omega_o, \omega_i) L_i(p, \omega_i)(\omega_i \cdot n) d\omega_i$$





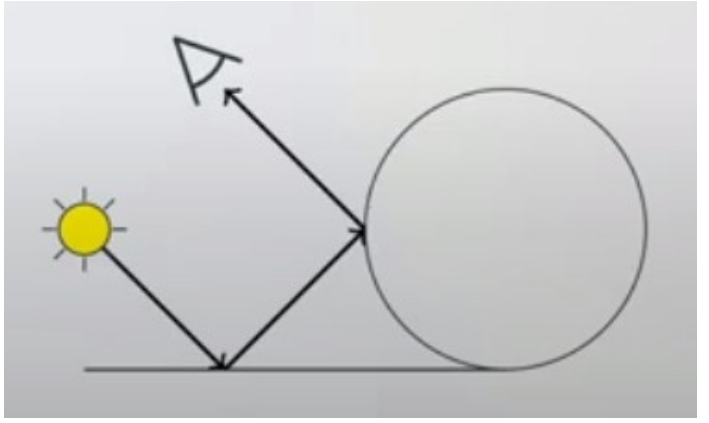
Rendering and light

- Rendering equation is very general equation: different rendering approaches solve different parts of this equation



Direct illumination: takes in account only light from light sources (e.g., non-phyiscal light sources; point lights)

- Often used in rasterization-based rendering
- Problem: additional work needed for shadows, reflections, etc.



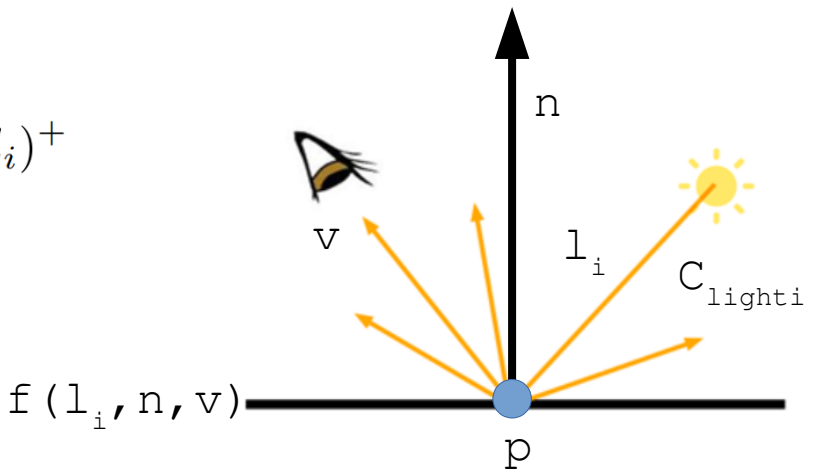
Global illumination: takes in account light from light sources and indirect light: reflections from other surfaces

- Often solved using ray-tracing-based rendering methods
- Multiple reflections, transmissions and shadows can be elegantly incorporated
- More advanced methods, e.g., path tracing, further build on raytracing to solve this problem more correctly

Local (direct) illumination

- **Local illumination**: shading is considering only light coming from light sources (discrete incoming light angles)
  - l_i is given as color and intensity.
  - Direction of light source is given or calculated from its position

$$c_{shaded(p,v)} = \sum_{i=1}^{n} f(l_i, n, v) c_{light_i} (n \cdot l_i)^+$$



https://www.scratchapixel.com/lessons/3d-basic-rendering/global-illumination-path-tracing/introduction-global-illumination-path-tracing.html

Local (direct) illumination

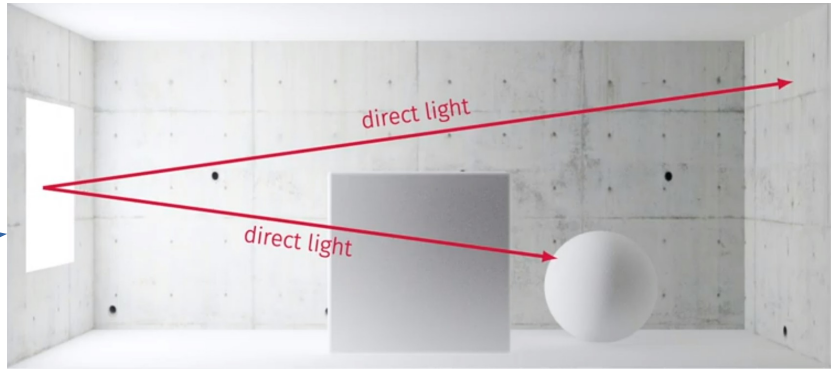
- If multiple light sources are present, they add up linearly
- Different types of light sources differ in light color and intensity and position/direction.

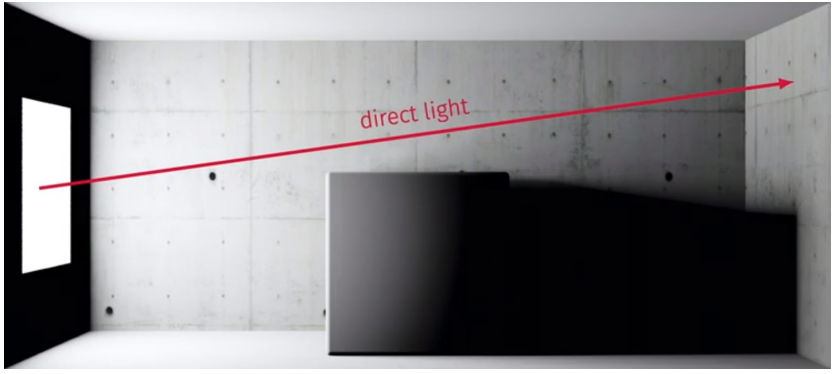
Local and global illumination

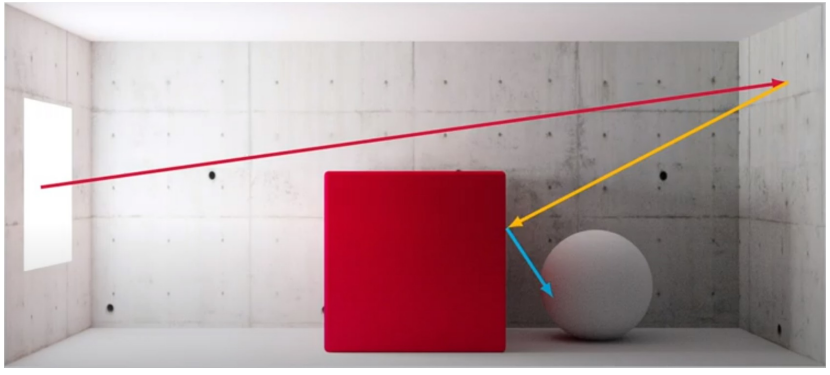
Direct illumination
- No shadows

Direct illumination with shadows
- Areas in shadow are completely black

Global illumination
- Shadows
- Multiple reflections
- Color bleeding

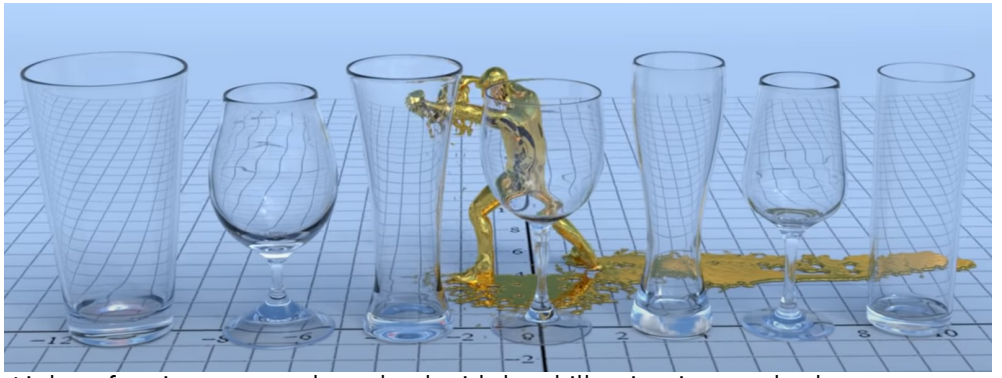






Global illumination

Indirect light causes caustics.
Blender and appleseed:
https://www.blenderdiplom.com/en/tutorials/all-tutorials/649-rendering-caustics-in-blender-with-appleseed.html



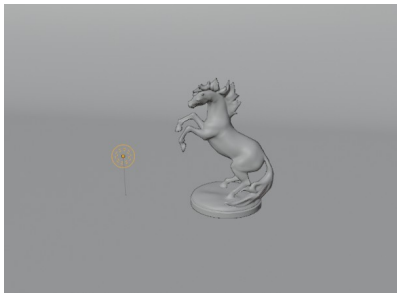
Light refraction can not be solved with local illumination methods:
https://www.youtube.com/watch?v=rJghpp8RVmw&ab_channel=yuichiroyama

Participating media and volumetric objects can not be accurately represented with direct illumination:
https://forums.jangafx.com/t/blender-cycles-test-rendering-of-the-free-vdb-cloud-pack/1273/3

Light and rendering (shading)

- **Light sources** must define
  - **Position** or **direction** of light
  - **Color** and **intensity** of light
- Additionally, light sources can have:
  - **Size**
  - **Shape**

Light models



Representation and modeling of lights **physically,** with shape and size → **geometric area light or physical lights***. Physical lights are computationally expensive.

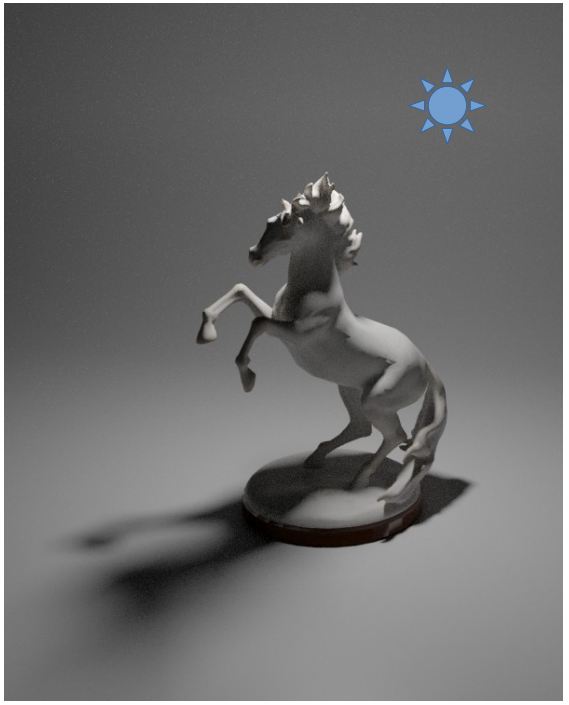
Simplification of lights with no physical size, are called **delta or non-physical lights.**

* When we discussed surface material we mentioned scattering and absorption. Also, materials can be emissive. Therefore, physical lights have 3D shape and material which is emissive. Emissive material is modeled as black body meaning that is absorbs all light falling on it.

Light models parameters

Non-physical lights:

- **Color:** RGB in [0,1]
- **Intensity:** float [0,1] (multiplier)
- **Position ➞ Direction**



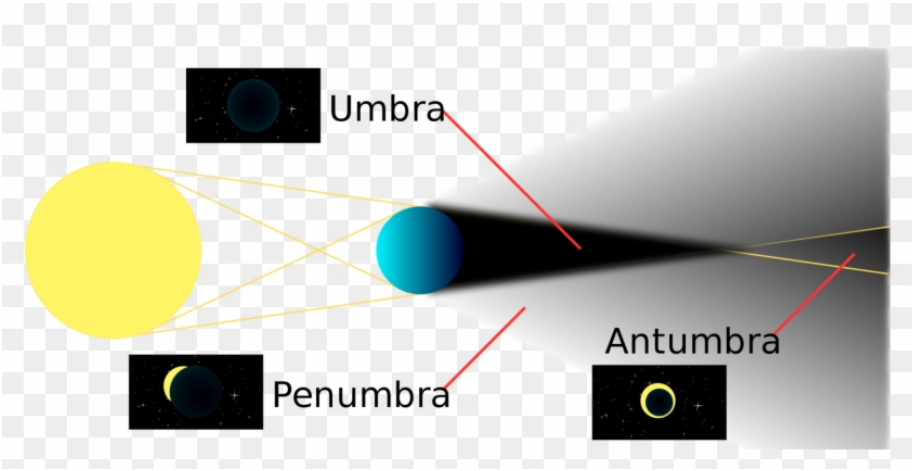
Physical Lights

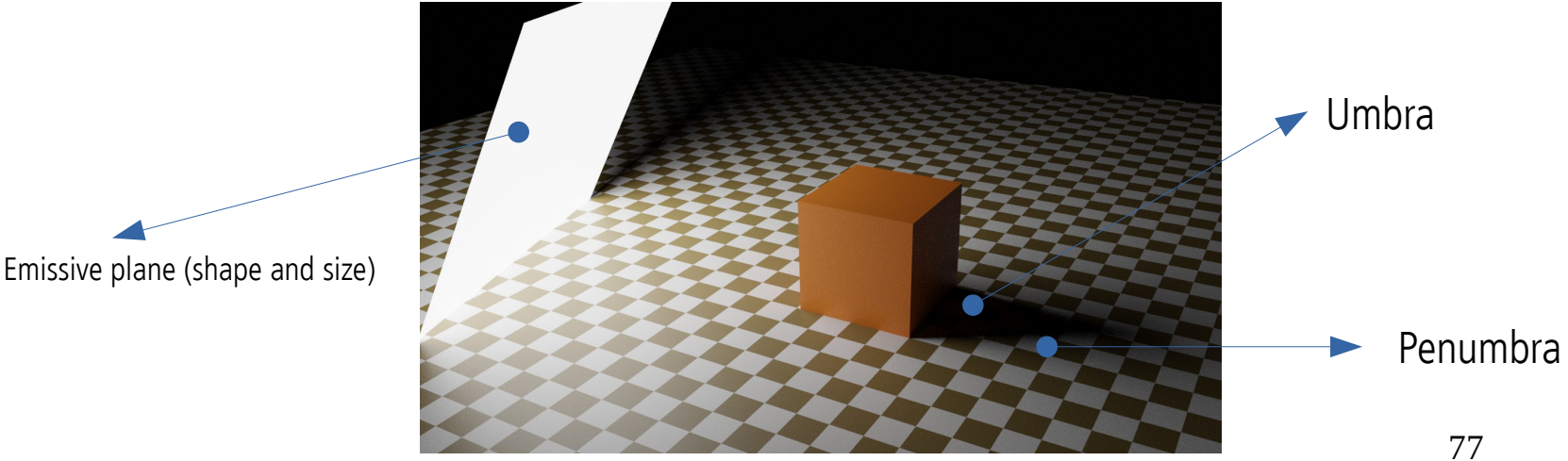
- Color (RGB)
- Intensity (float)
- Position
- Shape
- Size

Physical lights

Physical lights

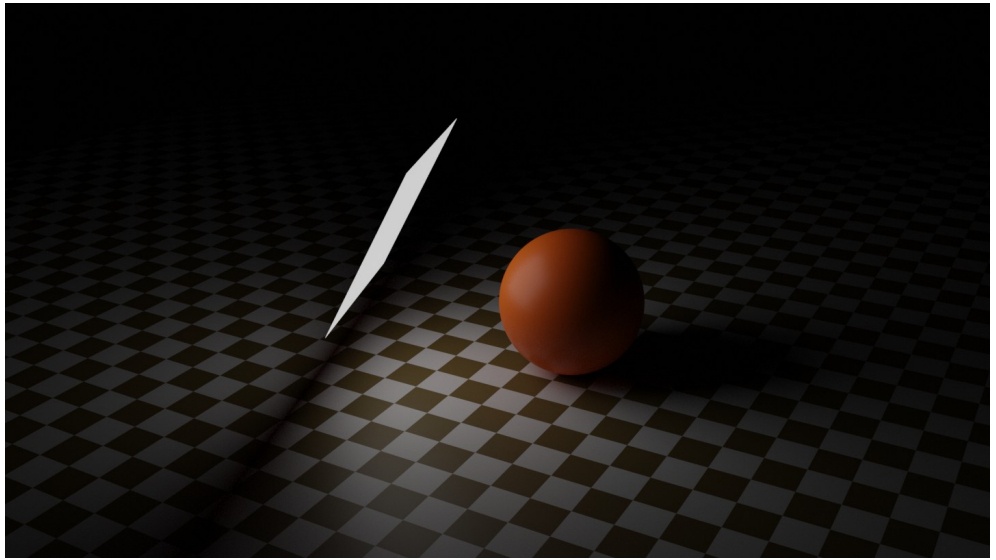
- Shapes that emit light from their surface (emissive material)
  - Color and intensity
  - Position
  - shape and size

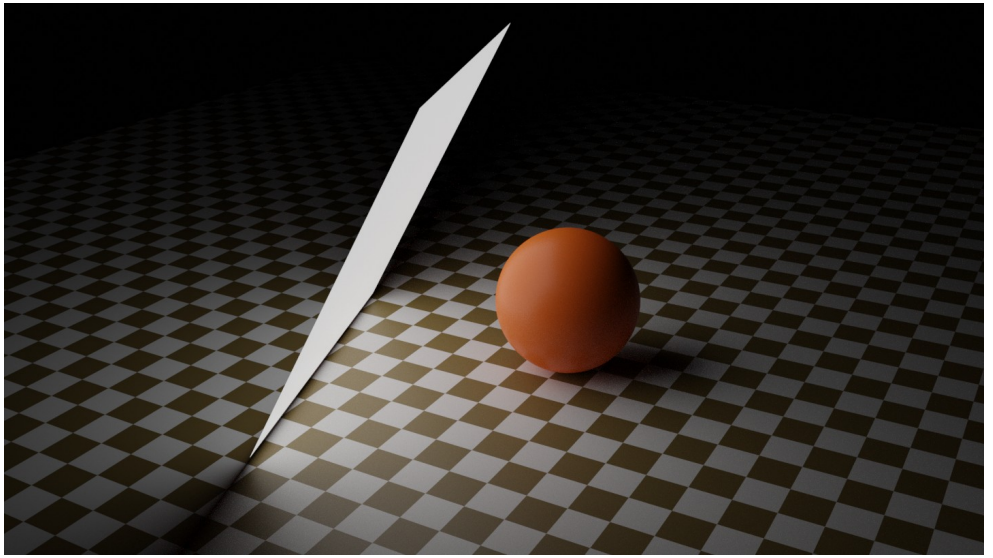




Physical lights

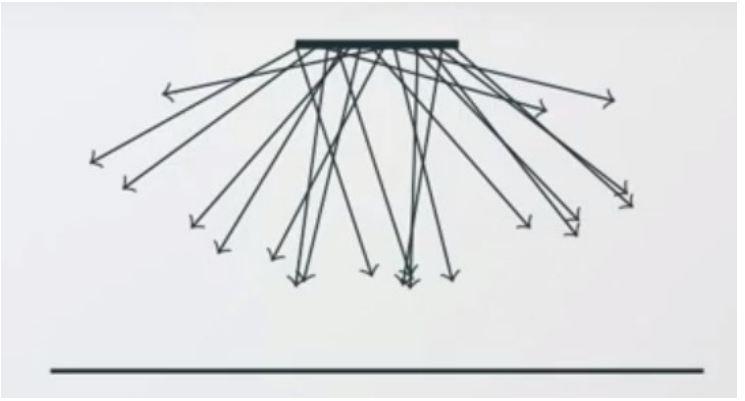
- Shape and size of light matters
  - Amount of brightness
  - Softness and size of shadows





Physical lights

- Intensity and color of emission is given as distribution over emissive surface
- **Diffuse physical light**: uniform spatial and directional intensity and color distribution
  - Light is emitted in direction defined with surface normal
- At each point in the scene, light from physical light source can be incident from many directions → integration over emissive surface is needed*



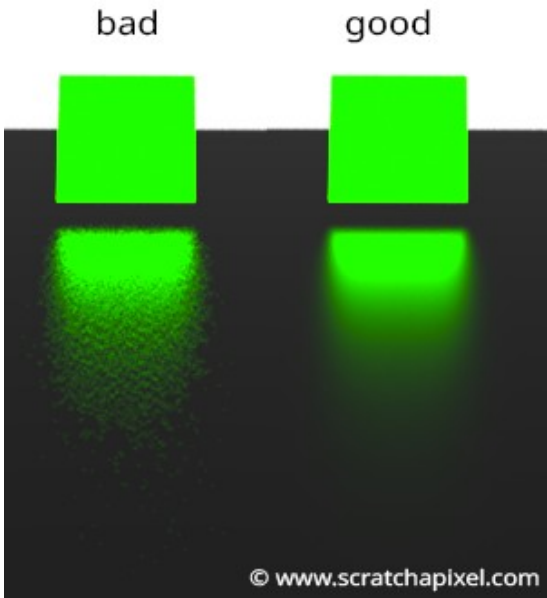
Physical lights

- Computing intensity of physical lights requires computing integrals over emissive surface and often can not be computed in closed form
- Ray-tracing based approaches try to approximate this problem by sampling only smaller number of directions
- Rasterization-based rendering simplifies and approximates effects of physical lights

Physical lights: ray-tracing-based rendering

- Ray-tracing-based rendering simulates physical flow of light, emission from physical lights and their effects on 3D scene (e.g., shadows) can be elegantly solved
- Physical lights have area which has to be sampled
  - Approximation-based methods such as Monte Carlo integration must be used
  - Global illumination methods: path-tracing

$$L_o(p, \omega_o) = L_e(p, \omega_o) + \int_\Omega f(p, \omega_o, \omega_i) L_i(p, \omega_i)(\omega_i \cdot n) d\omega_i$$



https://www.scratchapixel.com/lessons/3d-basic-rendering/global-illumination-path-tracing/introduction-global-illumination-path-tracing.htm

Light Sampling and Shadow/Direct Specular Noise

AA_Samples = 1. Light samples = 2 (4 samples).

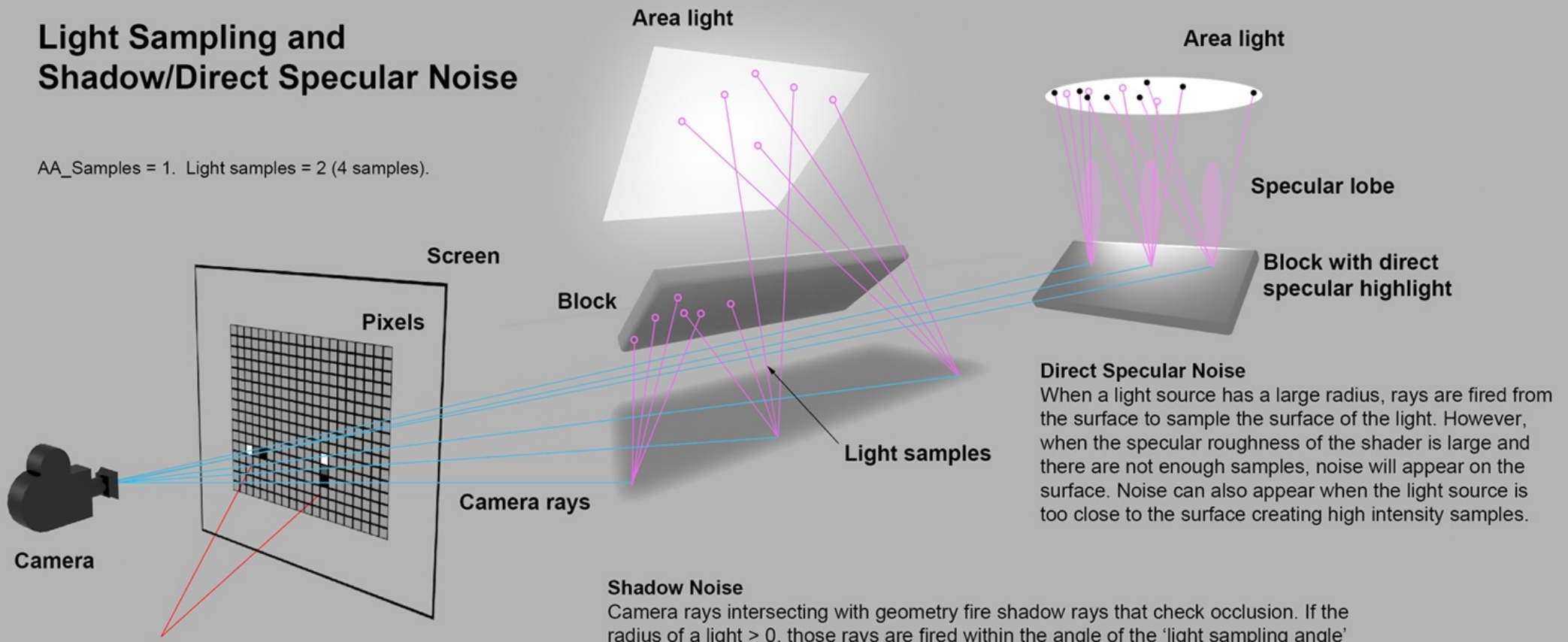


Image noise due to low sampling (pixel value = average subsamples).

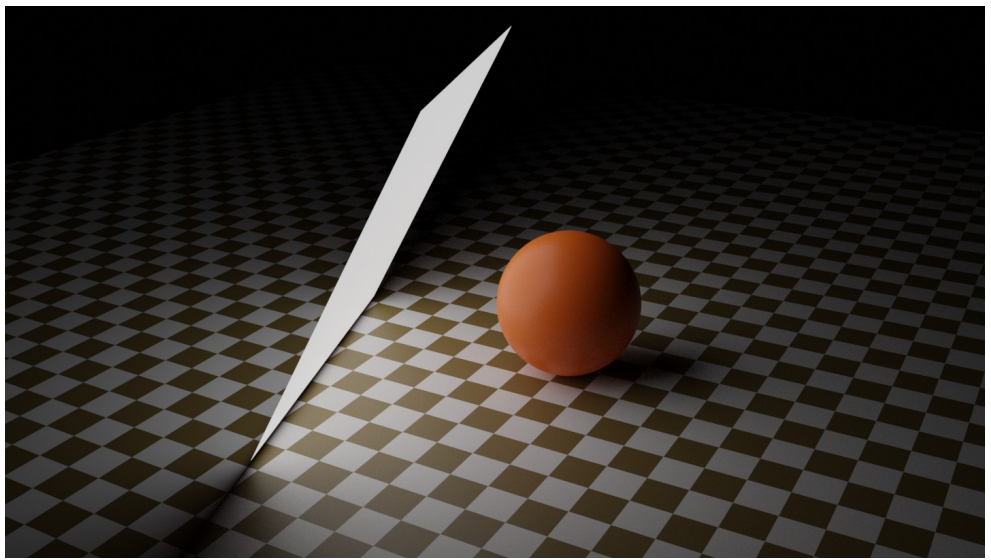
Direct Specular Noise
When a light source has a large radius, rays are fired from the surface to sample the surface of the light. However, when the specular roughness of the shader is large and there are not enough samples, noise will appear on the surface. Noise can also appear when the light source is too close to the surface creating high intensity samples.

Shadow Noise
Camera rays intersecting with geometry fire shadow rays that check occlusion. If the radius of a light > 0, those rays are fired within the angle of the 'light sampling angle' (shaded area with dotted lines); shadows can be noisy as Arnold attempts to resolve the area light with insufficient rays. In this example, the 4 samples fired toward the light randomly hit either the block (resulting in a low value) or the light (resulting in a high value).

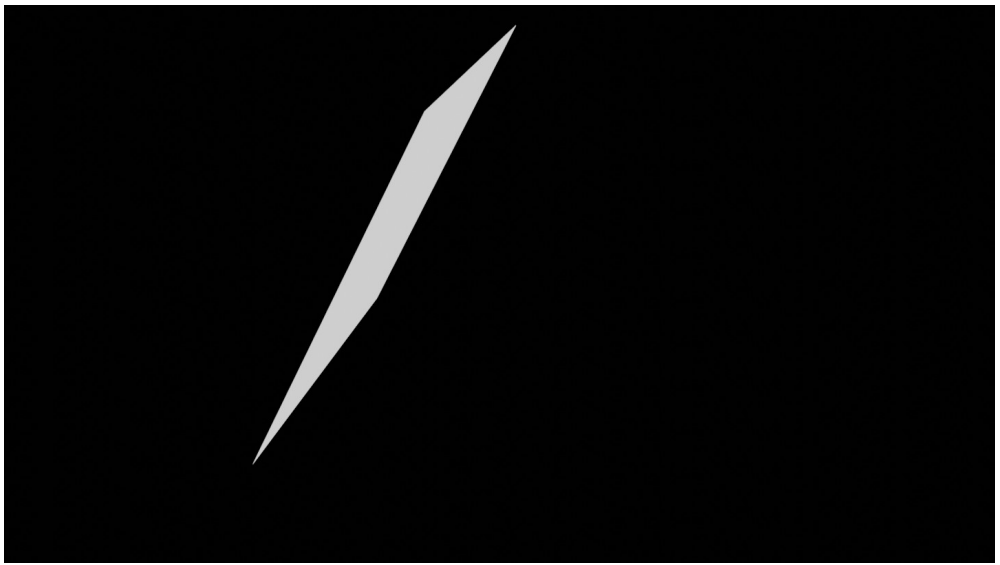
https://help.autodesk.com/view/ARNOL/ENU/?guid=arnold_user_guide_ac_lights_html

Physical lights: rasterization-based rendering

- Rasterization-based rendering is not simulating natural flow of light. Therefore, physical lights and their effects require simplifications and approximations.



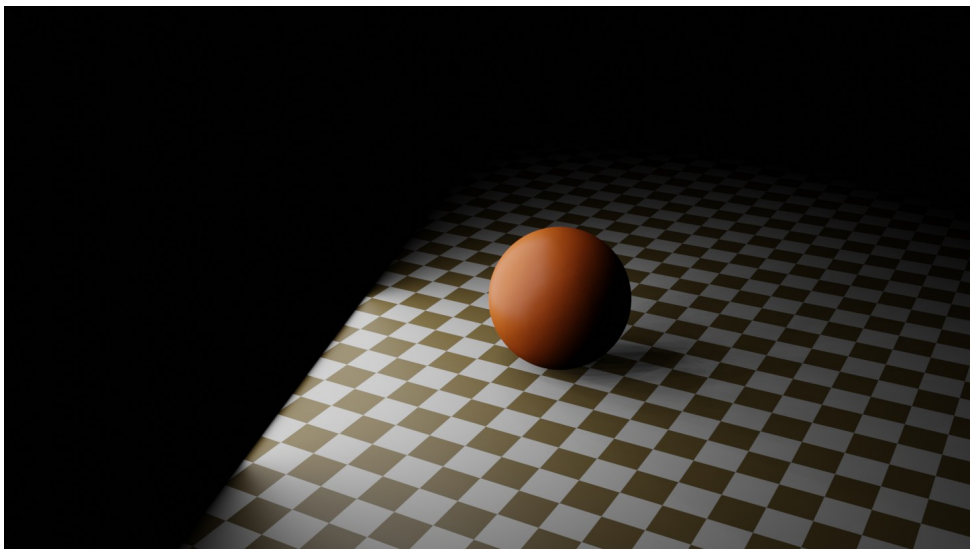
Physical lights in ray-tracing (path-tracing, Blender, Cycles)



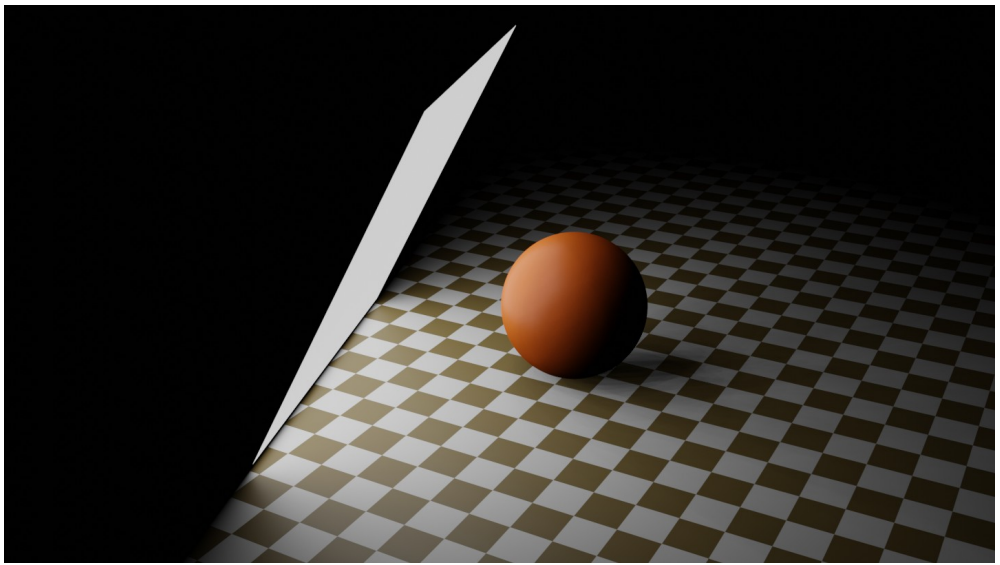
Physical lights in rasterization (Blender, EEVEE)

Physical lights: rasterization-based rendering

- Special cases of phyiscal lights - rectangular planes, can be approximated in rasterization-based renderer*



Rectangular plane emission (Blender, EEVEE):
https://docs.blender.org/manual/en/latest/render/lights/light_object.html#area-light



Emissive plane and rectangular plane emission approximation (Blender, EEVEE)

Physical lights: rasterization-based rendering

- Alternative is to pre-compute effects of physical lights using path-tracing and store it in texture which is then used during shading*
  - https://docs.blender.org/manual/en/latest/render/cycles/baking.html
  - https://catlikecoding.com/unity/tutorials/rendering/part-16/
- **Effects of physical lights can be approximated using non-physical lights**

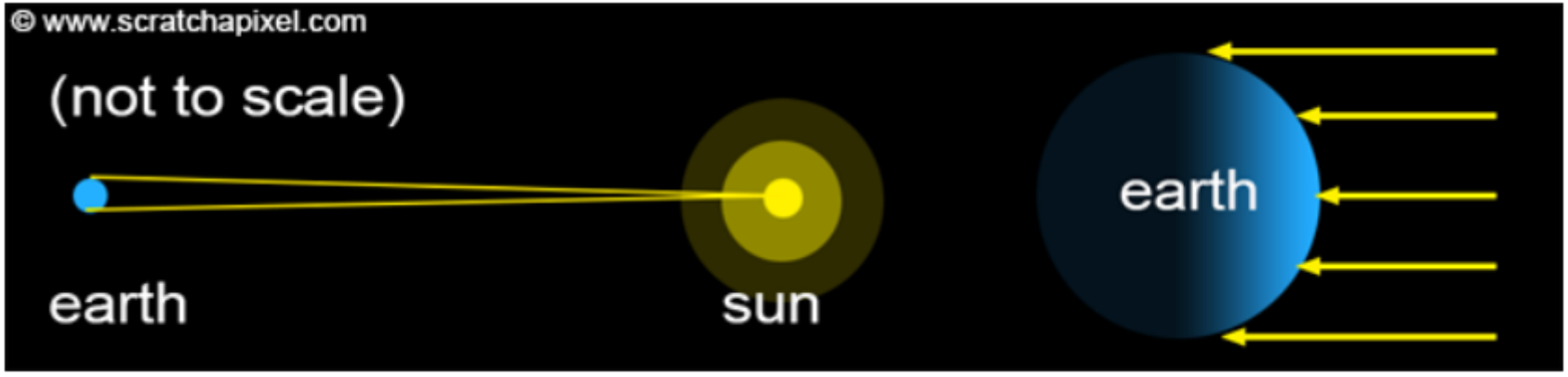
Non-physical lights

Non-Physical lights

- Non-phyiscal lights simulate effects of physical lights: light fall-off with distance, which objects are illuminated, which objects cast shadows, etc.
- Types:
  - **Directional** (distant, parallel) lights
  - **Point** (spherical, omnidirectional) lights
    - Spot lights
    - Other variations

Directional (parallel) lights

- Directional lights are considered so far from the objects in a 3D scene that they can be represented by parallel rays.
  - We only care for the **direction** of those parallel rays



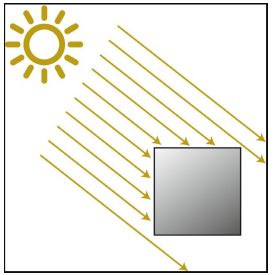
Example of directional light: is Sun light on Earth.

- Sun has spherical shape, but it is so far and Earth is so small compared to it that light rays reaching Earth can be considered parallel (small cone of directions – solid angle).
- For scenes that cover small area of Earth's surface, Sun light can be assumed parallel.

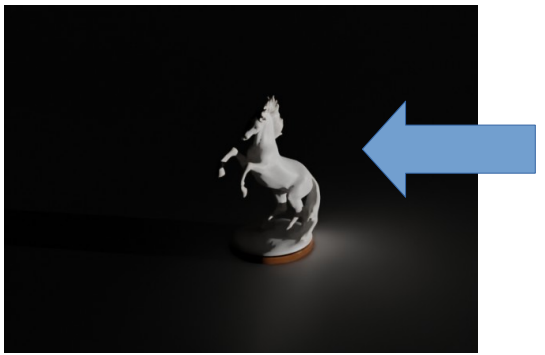
https://www.scratchapixel.com/lessons/3d-basic-rendering/introduction-to-shading/shading-lights

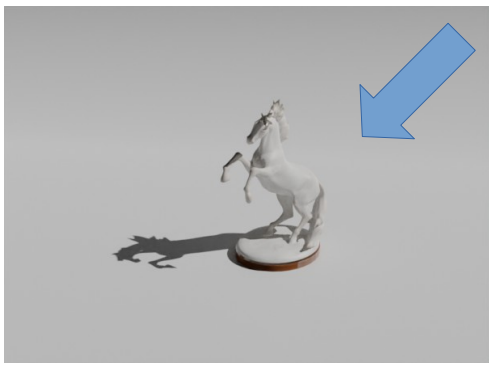
Directional (parallel) lights

- Directional light is simplest model of light source.
  - **Direction (`l`)** – unit vector (not affected by position!)
  - **Color (`c`)** – RGB vector in `[0,1]`
  - **Intensity (`i`)** – float value in `[0,inf]`
  - Direction `(l)`, color `(c)` and intensity `(i)` are constant over 3D scene
- Intensity may be attenuated by shadowing and surface orientation



https://link.springer.com/chapter/10.1007/978-1-4842-4457-9_12



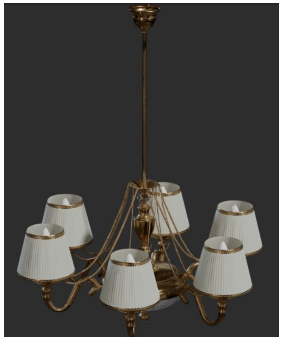


Practical tip: modeling with lights

- Orientation of light greatly determines scene appearance

https://www.youtube.com/watch?v=Ys4793edotw&t=1s&ab_channel=BlenderGuru

Point lights

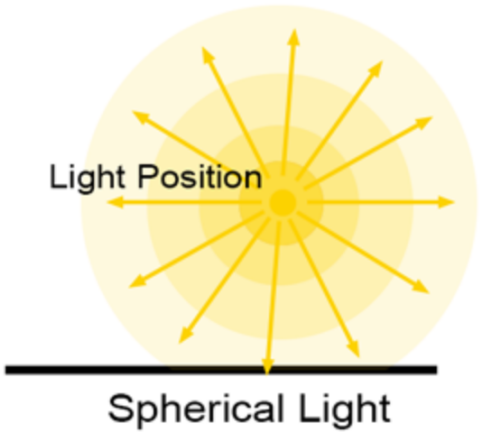


Most common light sources in nature and around us are spherical (e.g., light bulbs) or can be approximated as spherical light sources.

Point light

- **Infinitesimally small in size ➞ no shape**
- **Light is emitted uniformly in all directions** (omnidirectional, isotropic)

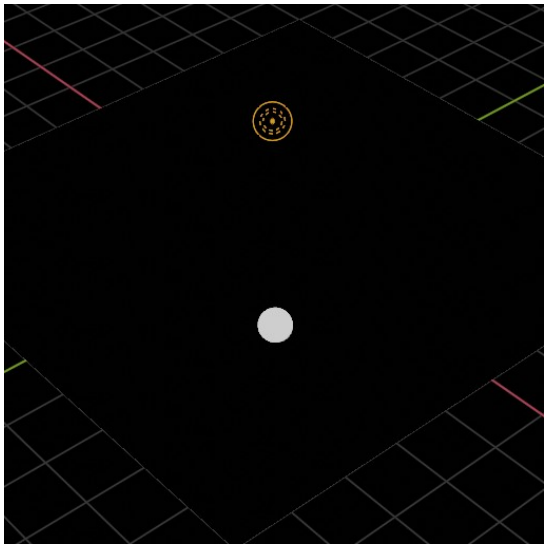
- Parameters
  - **Position** – vector determining position in world space (lights can be also transformed using 4x4 matrices)
  - **Color** – RGB vector in [0,1]
  - **Intensity** – float value in [0,inf]
  - Not affected by scale or rotation.

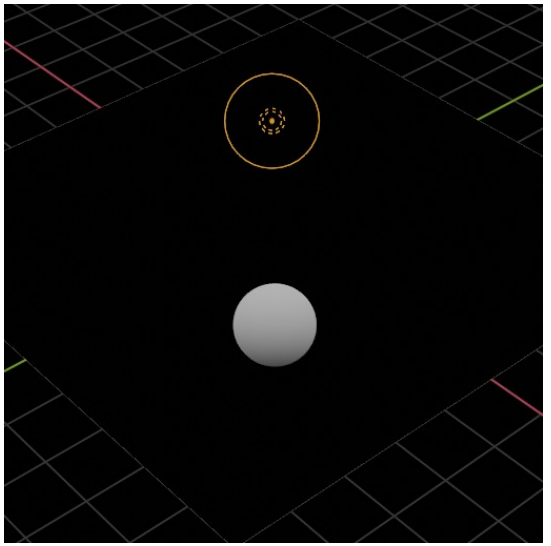


https://www.scratchapixel.com/lessons/3d-basic-rendering/introduction-to-shading/shading-lights

Non-Physical lights: note

- For correct physically-based rendering, non-physical light should be avoided
- Example: size of reflection of object by glossy or mirror-like surface depends on its size and distance to reflective surface. If light source has no shape nor size how reflection should look like? Hack: size parameter which is only used during shading.



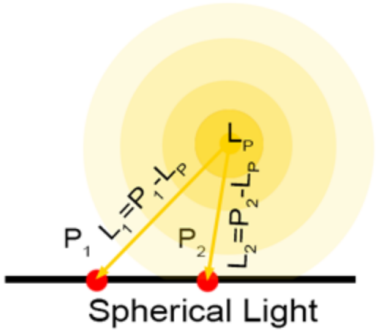


Point lights have parameter "size" which determines light reflection size:
https://docs.blender.org/manual/en/latest/render/lights/light_object.html#point-light

Point lights

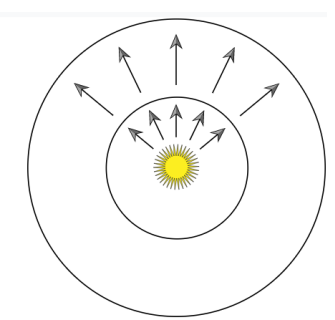
- Point light position determines **direction and distance of incoming light** ray for each surface point of objects in the scene

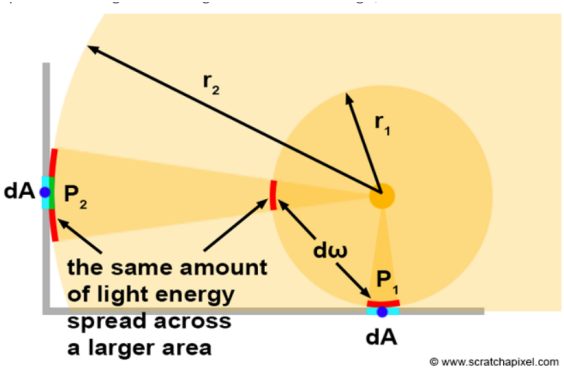
```
PointToLight = P – Lp
LightDistance = length(PointToLight)
LightDirection = normalize(PointToLight)
```

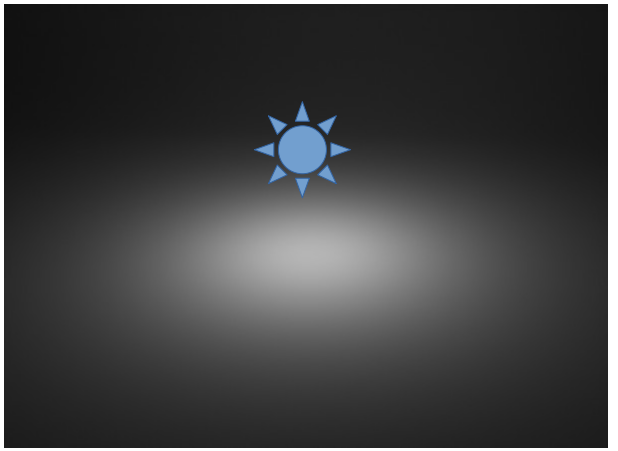


Point lights: direction and light falloff

- **Distance** from point light to surface point determines **light falloff**
- Point light sources emit light radially
  - Energy of light source is redistributed over sphere
  - As the sphere keeps expanding in the space, energy becomes spread across much larger area → more distant objects in the scene receive less light → **light falloff**.
  - Distance of point light to surface point determines how much is that point illuminated → **intensity of point light varies as a function of distance**.



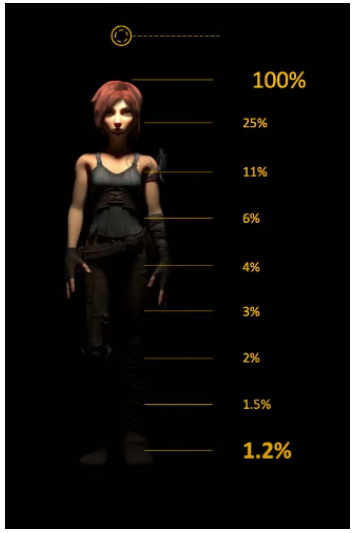




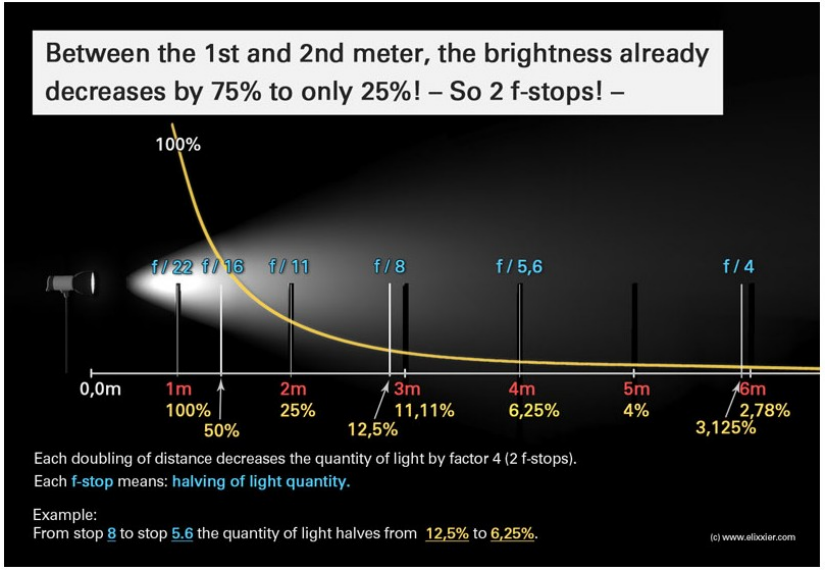
Point light - light falloff

- Point light distributes energy spherically.
- Larger distance → larger sphere → smaller energy
  → attenuated light - **inverse square law falloff**:

$$L_i = \frac{\text{light intensity} * \text{light color}}{4\pi r^2}$$



https://www.youtube.com/watch?v=Z8AAX-ENWvQ&t=2s&ab_channel=Blender



https://petapixel.com/inverse-square-law-light/

Point light - light falloff

https://www.youtube.com/watch?v=Z8AAX-ENWvQ&t=2s&ab_channel=Blender

Point light - light falloff

- Problems:
  - **Small distances**: as r → 0, light intensity → infinity. Fix:

$$L_i = \frac{\text{light intensity * light color}}{4\pi(r + \text{epsilon})^2}$$

  - **Large distance**: for efficient rendering, it is desired to light reach 0 at some point. Otherwise, light calculation should be done no matter how far the camera is from the light
- Notes:
  - Light falloff function can be any other function of distance
  - For stylized appearance different functions may be more interesting

Practical tip: modeling with lights

- Orientation of light greatly determines scene appearance

https://www.youtube.com/watch?v=Ys4793edotw&t=1s&ab_channel=BlenderGuru

Point lights: directional light falloff

- Next to distance light falloff, real-world illumination intensity also **varies by direction,** generally:

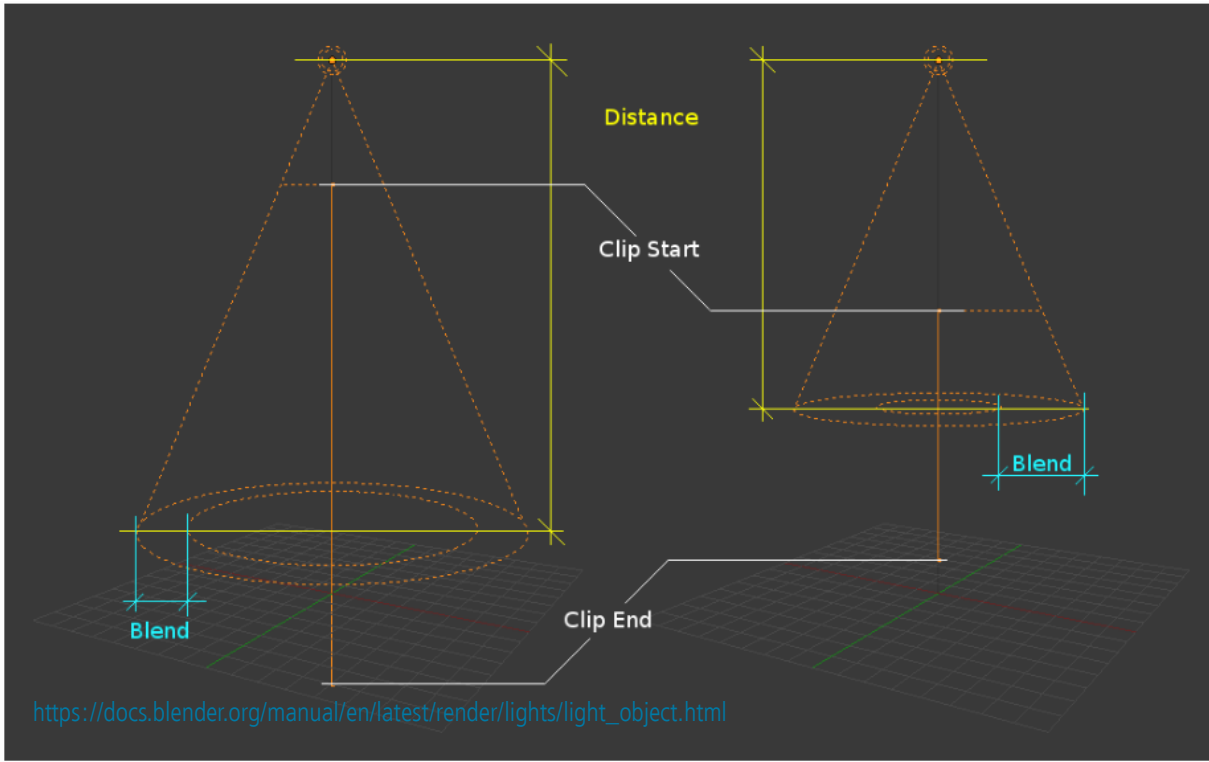
$$L_i = (\text{light intensity} * \text{light color}) f_{distance}(r) f_{direction}(l)$$

- Different choices of distance and directional light falloff functions produce different light sources:
  - **Spotlights** - emit light in a cone of directions from their position

$$L_i = (\text{light intensity} * \text{light color}) f_{distance}(r) f_{direction}(l)$$

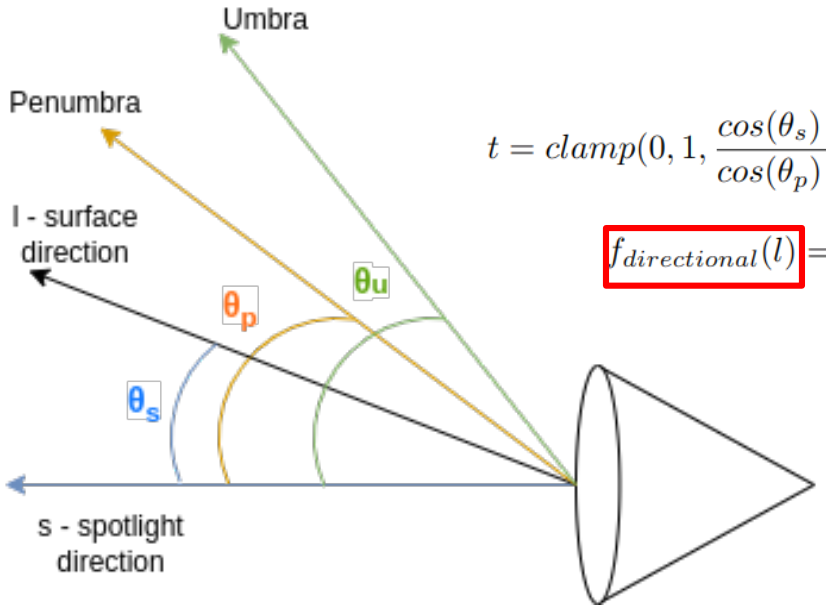
Spotlights

- Projects light in circular cone
- Directional falloff function is rotational symmetric around a spotlight direction



Spotlights

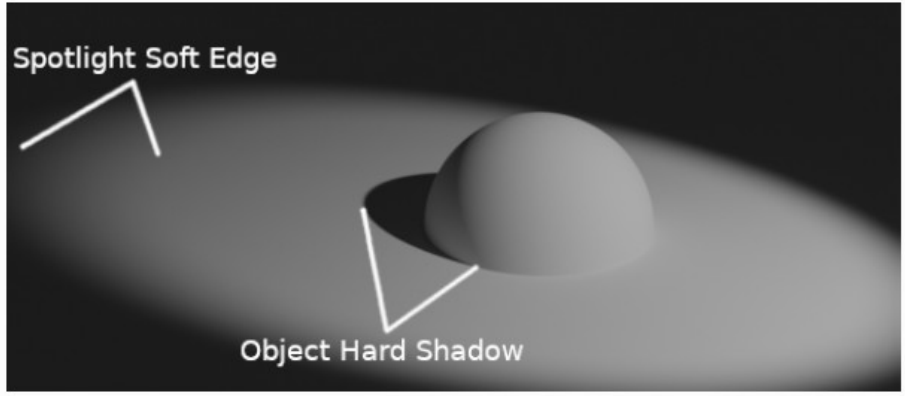
- Parameters:
  - Spotlight direction: `s`
  - Angle of umbra θ_u
    - Outer cone shell
  - Angle of penumbra θ_p
    - Inner cone where the light is at full intensity
  - Color: RGB vector in `[0,1]`
  - Intensity: float in `[0, inf]`



$$t = clamp(0, 1, \frac{cos(\theta_s) - cos(\theta_u)}{cos(\theta_p) - cos(\theta_u)})$$

$$f_{directional}(l) = t^2$$

$$L_i = (\text{light intensity} * \text{light color}) f_{distance}(r) f_{direction}(l)$$



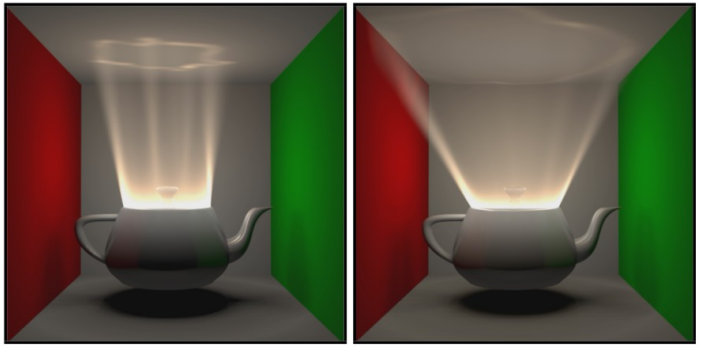
https://seblagarde.files.wordpress.com/2015/07/course_notes_moving_frostbite_to_pbr_v32.pdf

Other distance and directional light falloff functions

- **Textured lights**
  - **Use of texture** for visual richness of light sources: intensity, color and directional/distance variations
  - For **cone-type lights**: projective textures (slide projector effect, gobo/cookie lights)
  - For **omni-directional-type lights**: texture for distance falloff – attenuation maps (e.g., light beams)

$$L_i = (\text{light intensity} * \text{light color}) f_{distance}(r) f_{direction}(l)$$

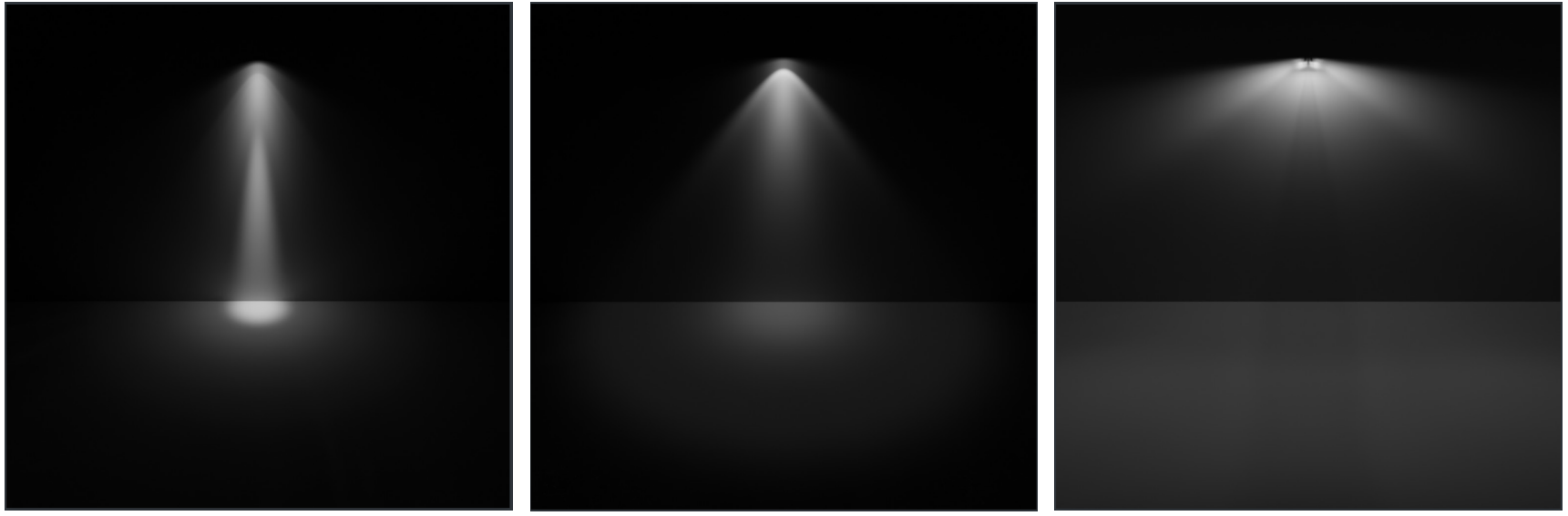
https://developer.valvesoftware.com/wiki/Env_projectedtexture



https://www.researchgate.net/publication/220183756_A_Programmable_System_for_Artistic_Volumetric_Lighting

Other distance and directional light falloff functions

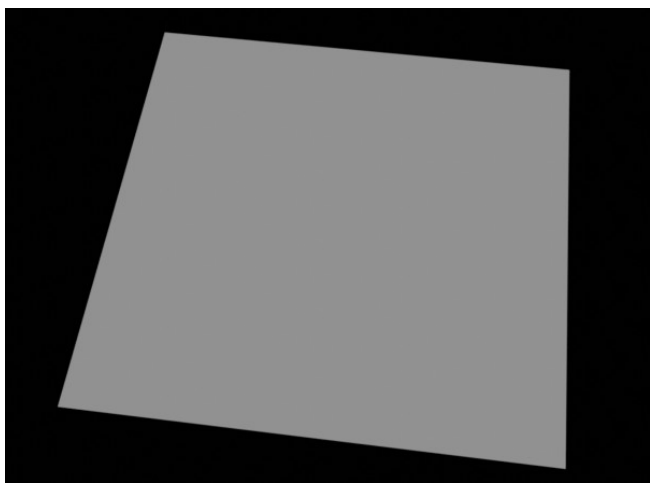
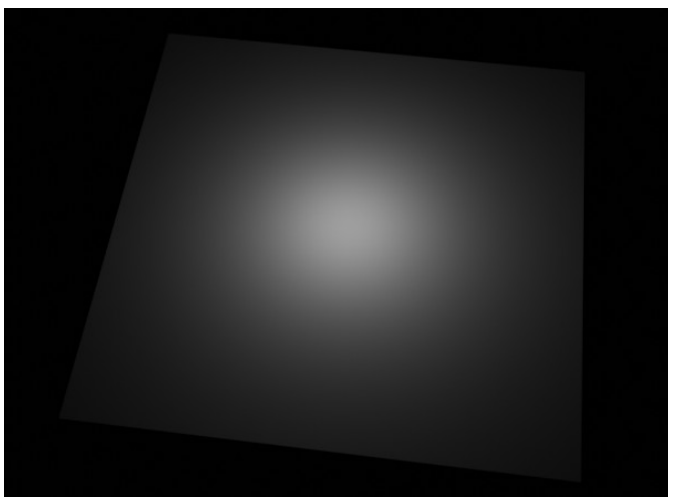
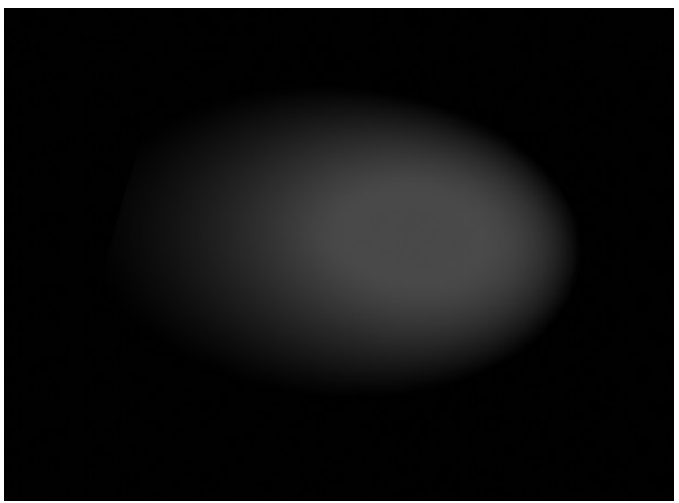
- **Tabulated patterns**
  - Standard: Illuminating Engineering Society (IES profiles)
  - Measured from the real world using: Goniophotometer



IES profiles: https://ieslibrary.com/en/home

Non-physical lights

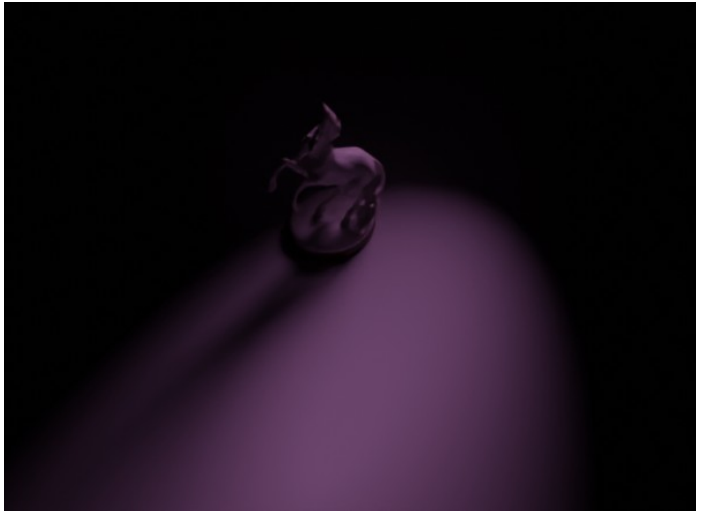
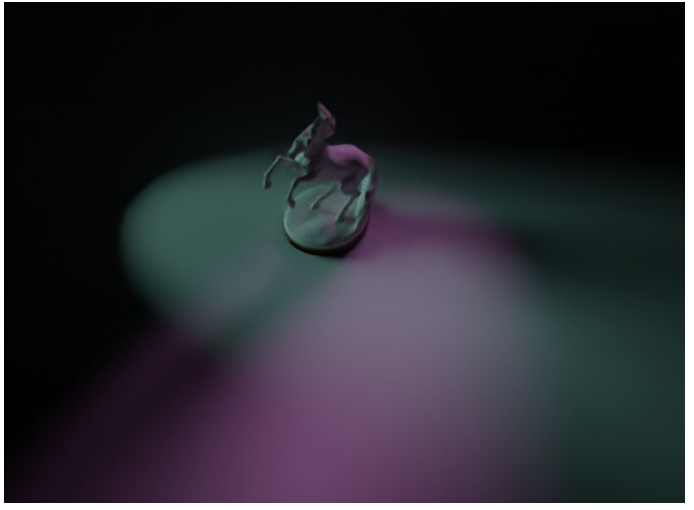
- Directional, point, spot light

Multiple lights

- Contribution of light adds up linearly
  - Basis of photo-realistic rendering where scene contains multiple lights
  - Required for compositing of rendered images: adding multiple rendered images where each has contribution from one light

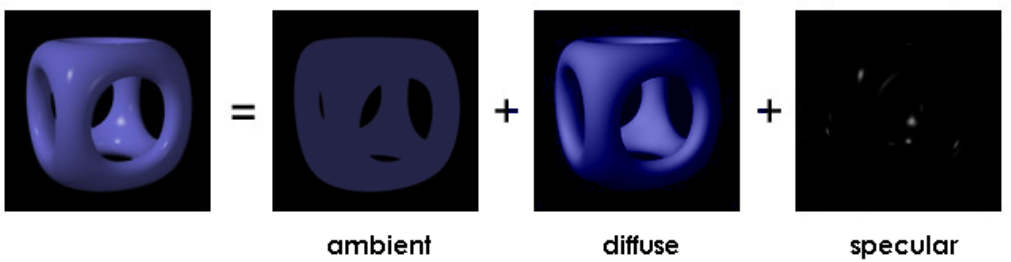
$$L_o(p,v) = \sum_{i=1}^{n} f(l_i,n,v)c_{light_i}(n \cdot l_i) \qquad L_o(p,v) = \int_{l \in \omega} f(l,n,v)L_i(p,l)(n \cdot l)dl$$

Environment illumination

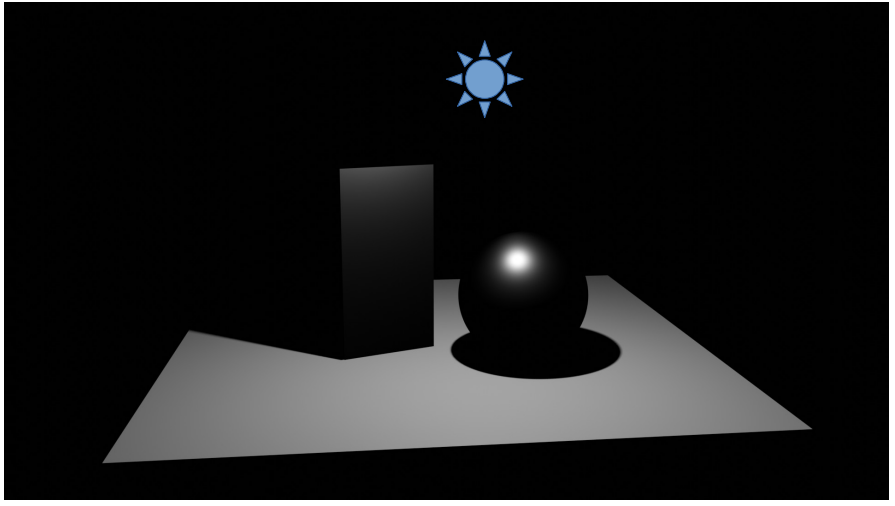
Environment illumination

- Until now, we have considered point and directional lights which limits surfaces to receive light from small number of discrete directions.
- In reality, scenes receive light from all directions otherwise surfaces would appear too dark or completely black if facing away from light sources
  - Example: ambient term in Phong model; constant color added to each point of surface
- To approximate light coming for different directions and large sources of light such as sky and clouds, environment lighting is used.
  - Such emitters solve the problem of objects being too dark

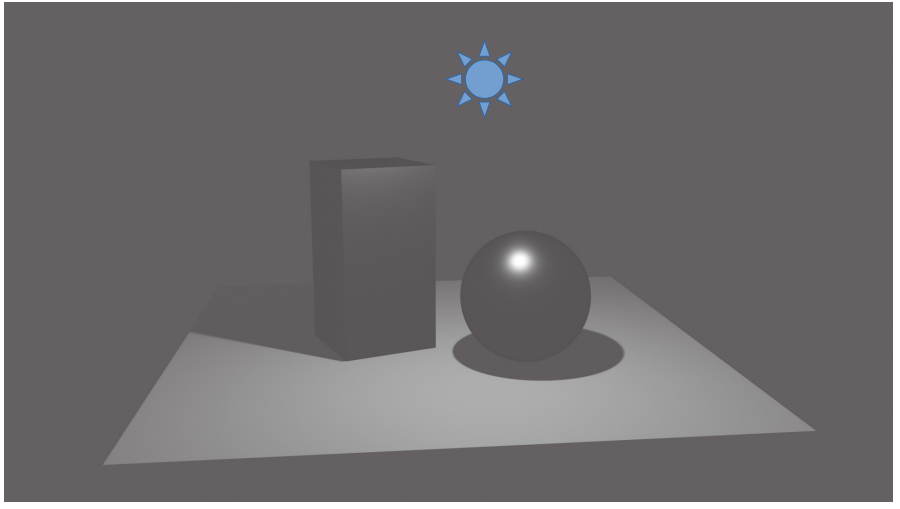


Environment illumination

- Light coming from point or directional light sources can be described with discrete incoming light directions to surface point
- Environment illumination is described with light coming from all directions to surface point



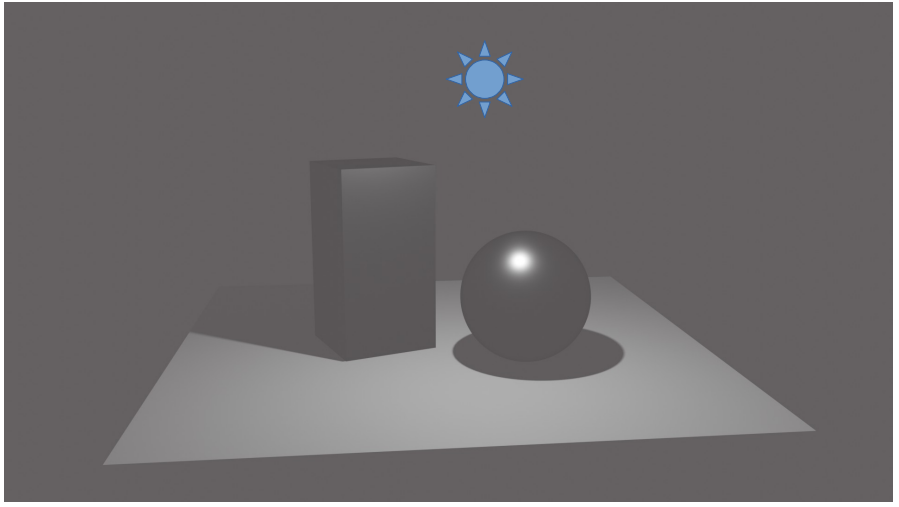
Only point light



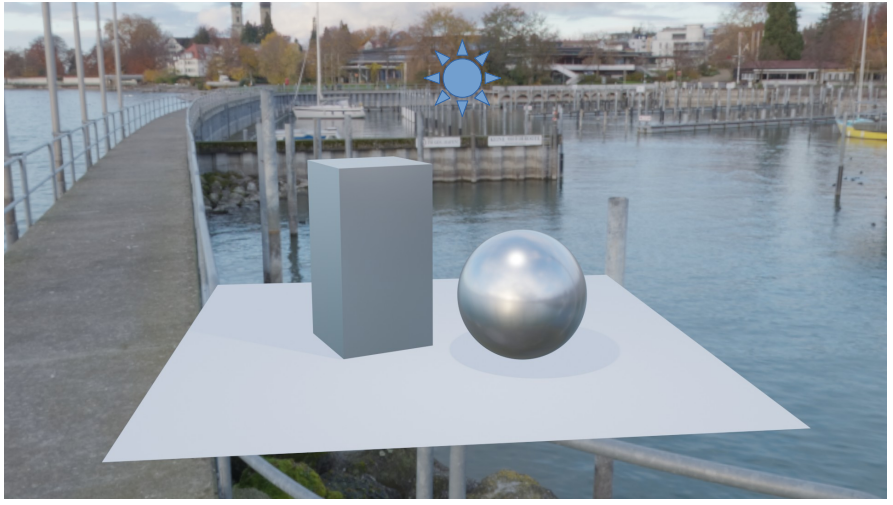
Point light and constant environment

Environment illumination

- Environment illumination is described with light coming from all directions to surface point
- Variation in intensity from different directions can be obtained using texture



Point light and constant environment



Point light and textured environment

Environment illumination

- Note that environment illumination is not global illumination
  - Knowledge of other surfaces which might reflect light is not used
  - Only more directions of light from light emitter are used
- However, this approximation can be used for simulating global illumination effects, that is, indirect light.

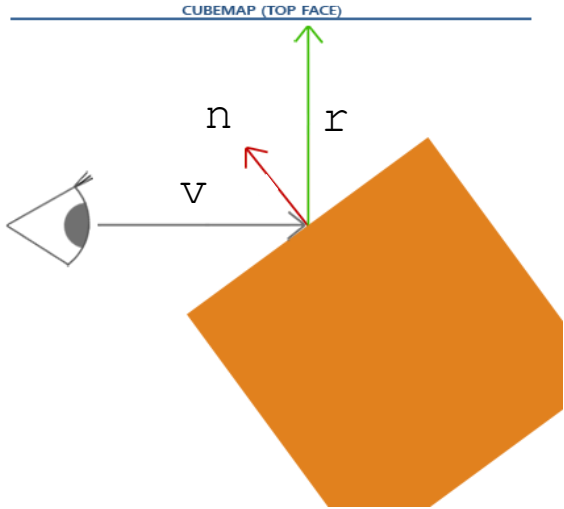
Environment illumination

- **Variation in intensity depends only on incoming direction** and not position
  - Assumption: environment light is infinitely far away.
- **Such illumination can be represented by spherical functions**
  - Defined over surface of unit sphere or space of directions
- Spherical function representations:
  - **Tabulated forms**: discrete points/directions over sphere containing intensity values which are interpolated
  - **Spherical basis**: spherical radial basis functions, spherical harmonics, etc.
  - **Environment mapping**: storing spherical function into texture, e.g., image texture
    - Most widely used, more memory costly but fast compared to other representations

Environment mapping

- Environment illumination is stored into image texture → **environment map**
  - Unlike surface textures, environment textures have color intensities larger than 1 → high dynamic range
- Global spherical function assumption: **light intensity only depends on a direction**
- Basic case of environment mapping: **reflection mapping**
  - For each reflective material, compute normal `(n)` at the location on the surface of the object
  - Compute reflection vector `(r)` from view vector `(v)` and normal vector `(n)`

    `r = 2 (n v) n – v`
  - Use reflected view vector `(r)` to compute environment map texture location
  - Read value from environment map texture and use it as light intensity



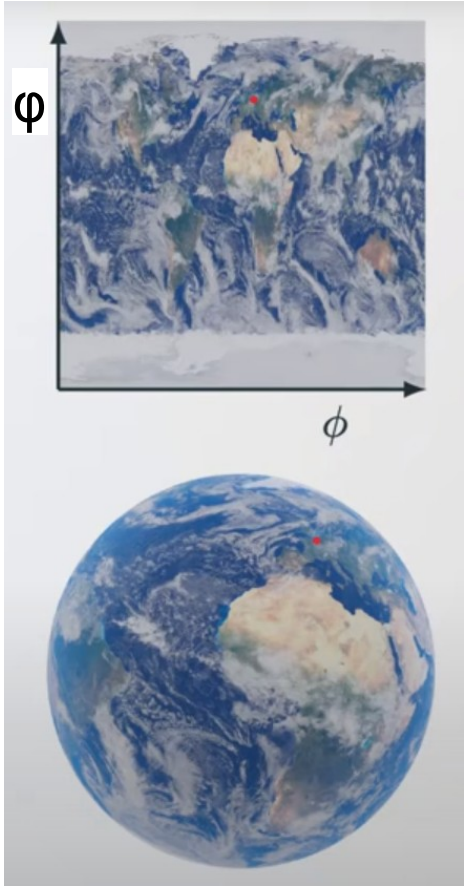
Reflection mapping

- Variety of projector functions mapping from reflected view vector (r) to environment texture location:
  - **Latitude-longitude mapping**
  - Sphere mapping
  - **Cube mapping**

More on environment mapping: http://cg.iit.bme.hu/~szirmay/specstar11.pdf

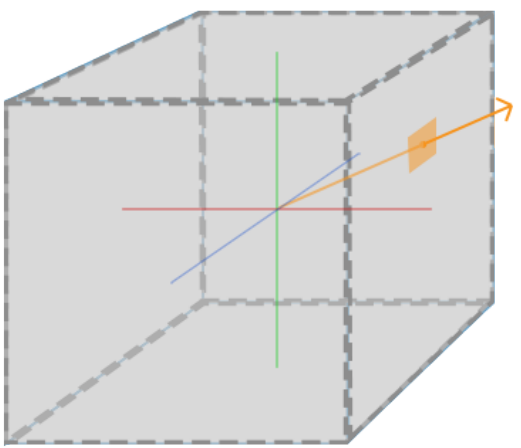
Latitude-longitude mapping

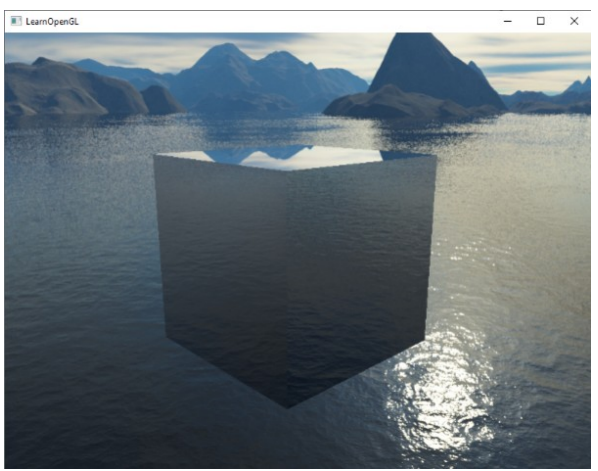
- Blinn and Newell method, first environment mapping method, 1976
  - Environment map idea: imagine that globe is viewed from inside
- Reflected view vector $r\ (r_x, r_y, r_z)$ is converted to spherical coordinates:
  - Longitude Φ in $[0, 2\pi] \rightarrow \Phi = \text{atan2}(r_y, r_x)$
  - Latitude φ in $[0, \pi] \rightarrow \varphi = \arccos(r_z)$
- Spherical coordinates are used to access the environment map



Cube mapping

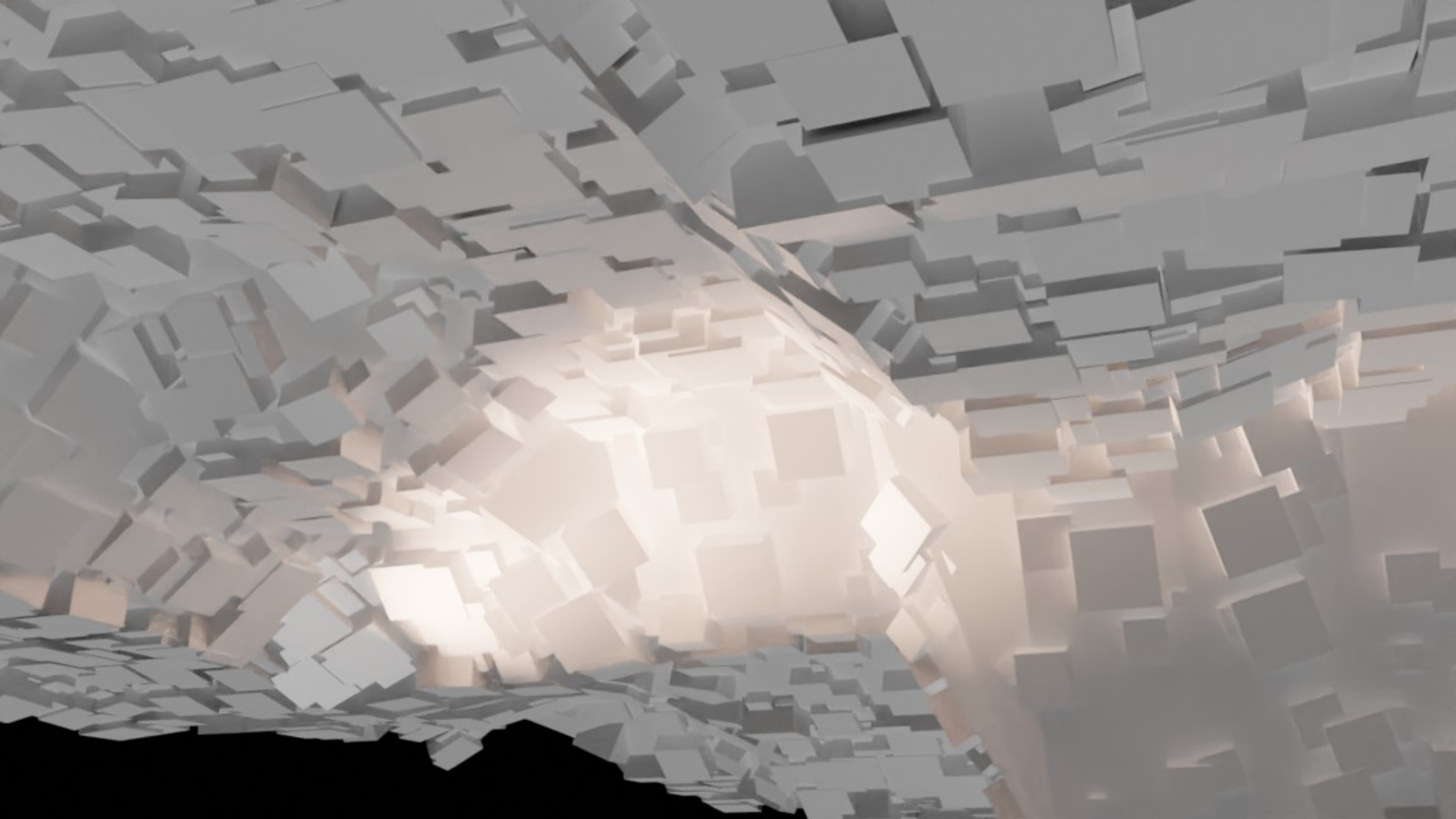
- Most widely used method, Greene 1986
- Cube map is created by projecting environment on the sides of a cube positioned with its center at camera's location
- Visualized as "cross" diagram, stored as six square textures
- Reflected view vector (r) can be directly used as three-component texture coordinate to fetch intensity data stored in cube map

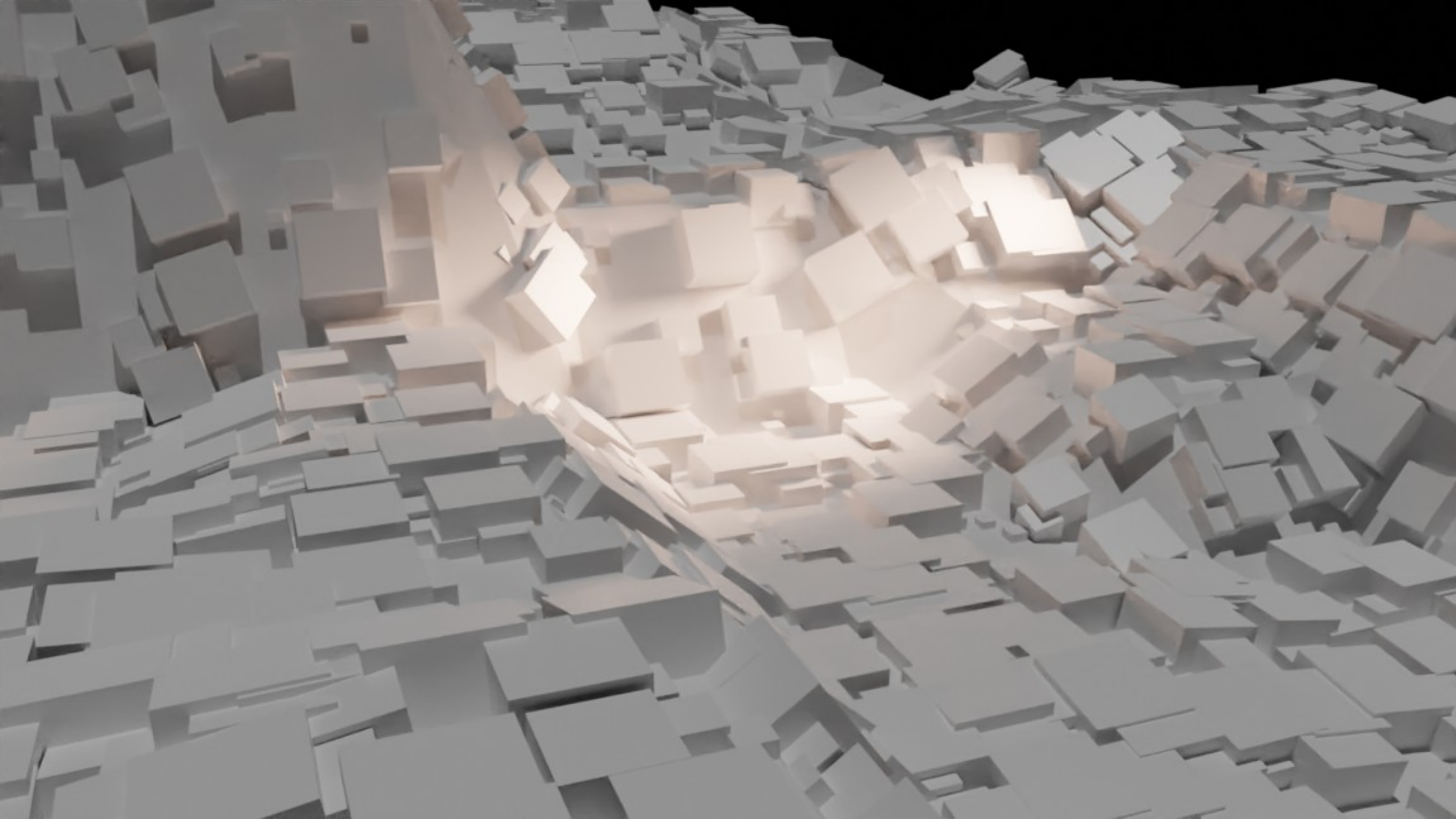




https://learnopengl.com/Advanced-OpenGL/Cubemaps

Shadows






Scene from:
https://casual-effects.com/data/index.html

Shadows

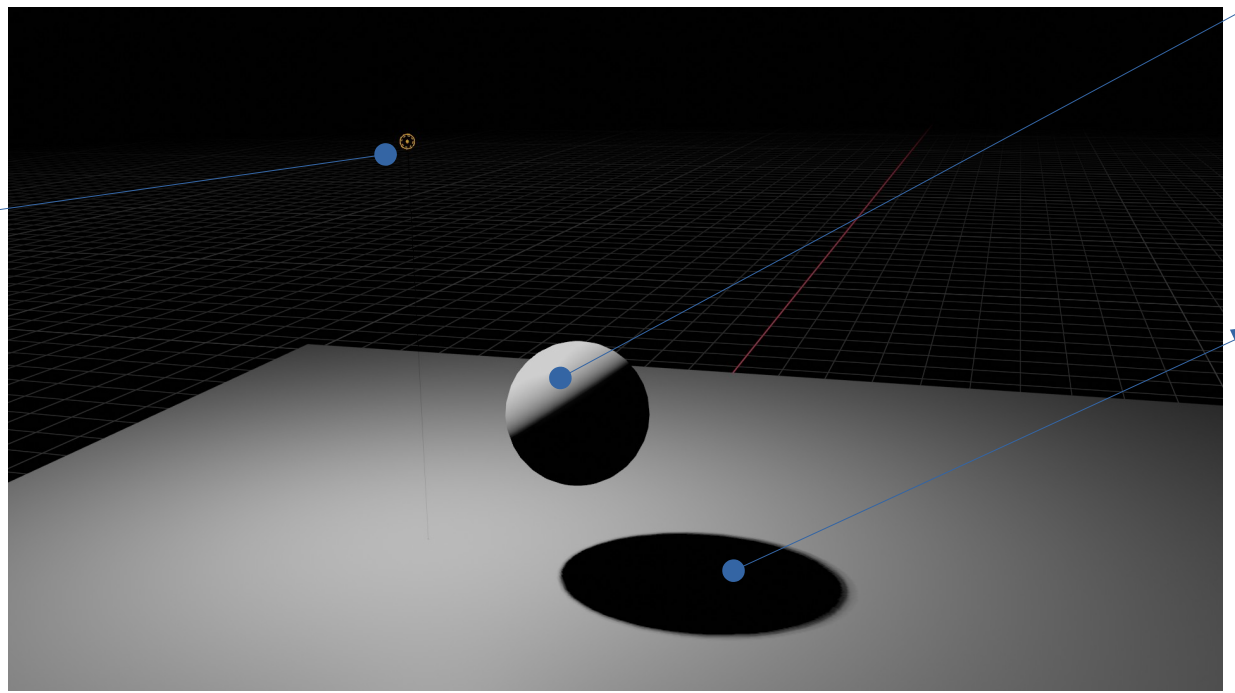
- Shadows are important for:
  - Providing user with visual cues about object placement and relation to other object
  - Realistic image synthesis: needed for understanding details and surface characteristics

https://creativecoding.soe.ucsc.edu/courses/cs488/reportsA/shadows.pdf

https://lumion.com/blog/feature-spotlight-sky-light-soft-shadows-and.html

Light and shadow

- Light falling on object causes object to cast shadow – blocking light to fall on another surface



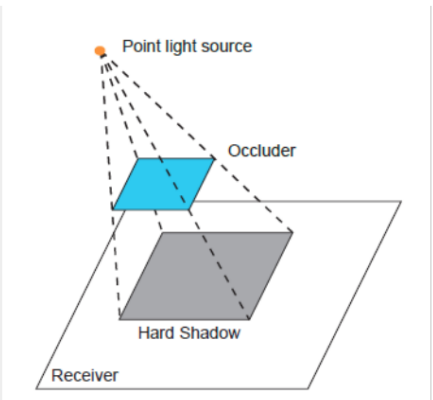
Occluders: objects casting shadow

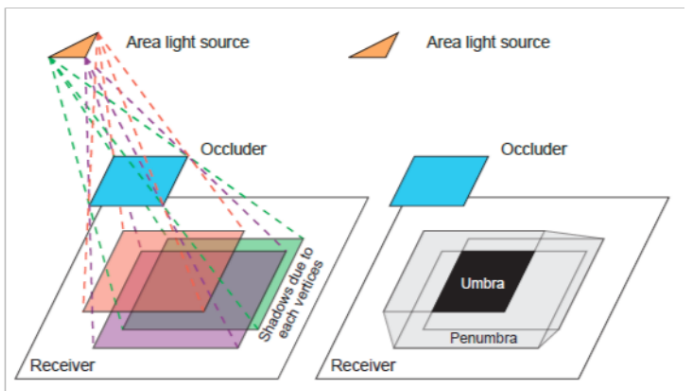
Light source: point light

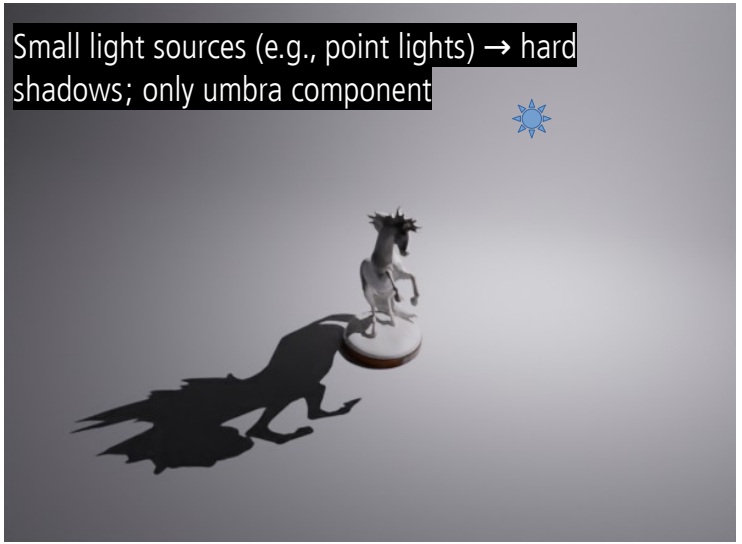
Recievers: objects on which the shadow is cast

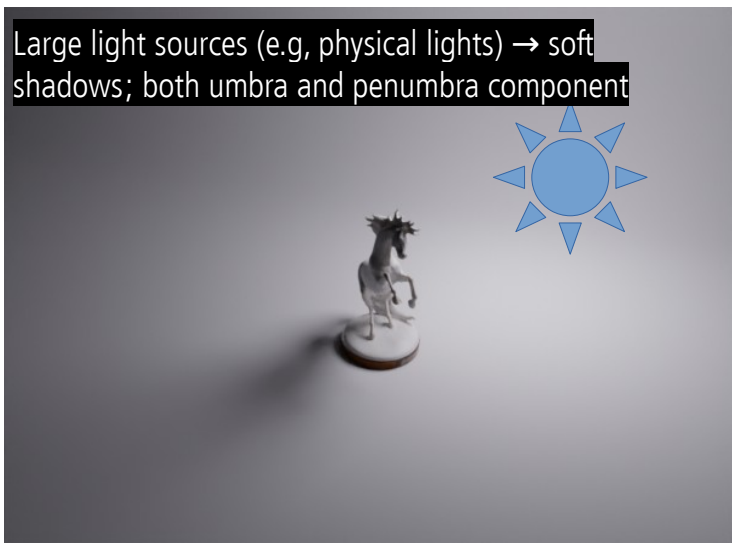
Sharp vs smooth shadows

- Size of light determines shadow smoothness
  - Hard-edge shadows: sharp shadow edges
  - Soft shadows: fuzzy shadow edges
  - Softer shadow edges are more realistic, but more expensive to render





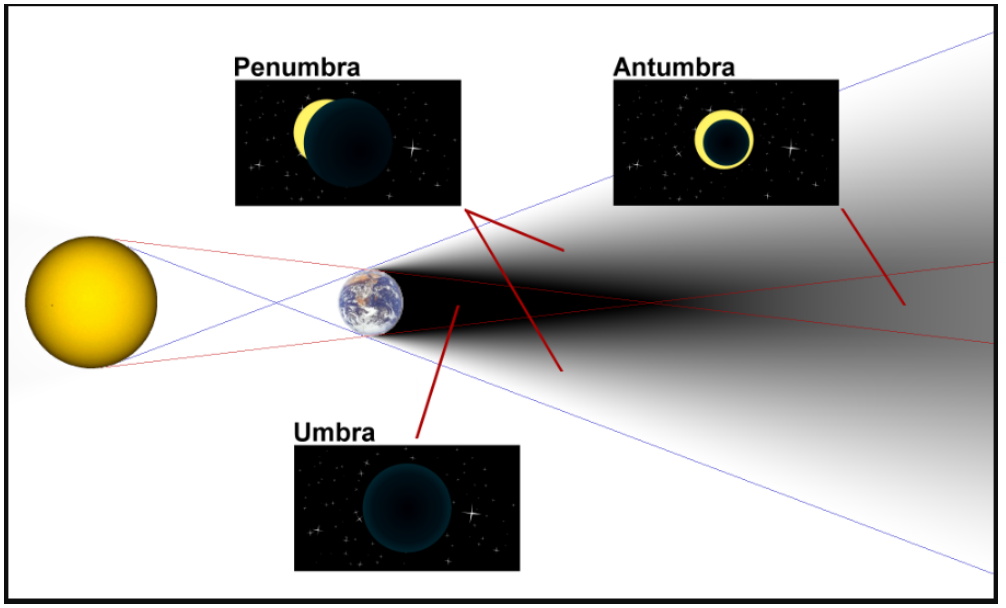




https://creativecoding.soe.ucsc.edu/courses/cs488/reportsA/shadows.pdf

Elements of a shadow

- **Penumbra**
  - Partially shadowed region
- **Umbra**
  - Fully shadowed region
  - Its region decreases in size as the light source gets larger
- NOTE: having any kind of shadow is more important than having soft shadows and penumbra.



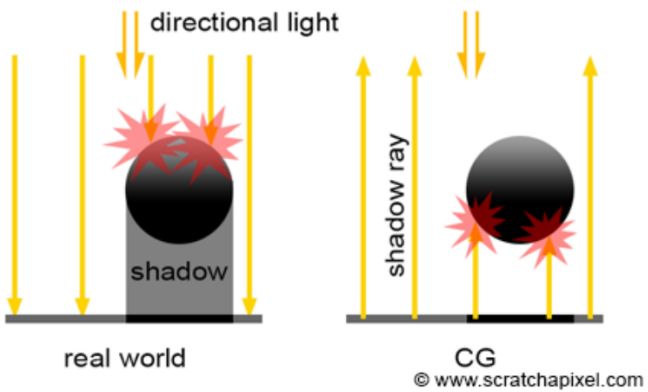
https://en.wikipedia.org/wiki/Umbra,_penumbra_and_antumbra

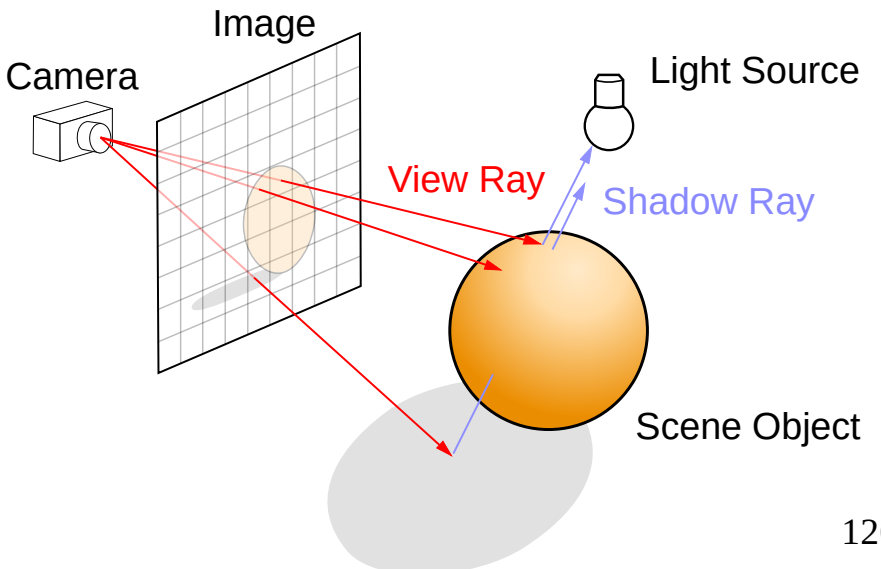
Rendering and shadow

- **Simulating shadow depends on how rendering is solving visibility problem**
- In **ray-tracing based rendering** shadows can be calculated in single pass without complex workarounds
- In **rasterization-based rendering** multi-pass rendering or additional work is required to simulate/approximate shadows

Shadow in ray-tracing

- For each pixel of virtual image plane, a ray is generated and tested for intersection with objects in 3D scene
- For found intersection, color is calculated using shading
- During shading, additional ray is casted towards light source – **shadow ray**
  - If shadow ray intersects object on its way, then shaded surface point is in shadow
  - If object is opaque, shadow is dark
  - If object is transparent, shadow is brighter

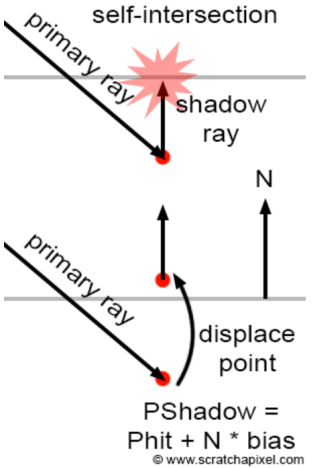




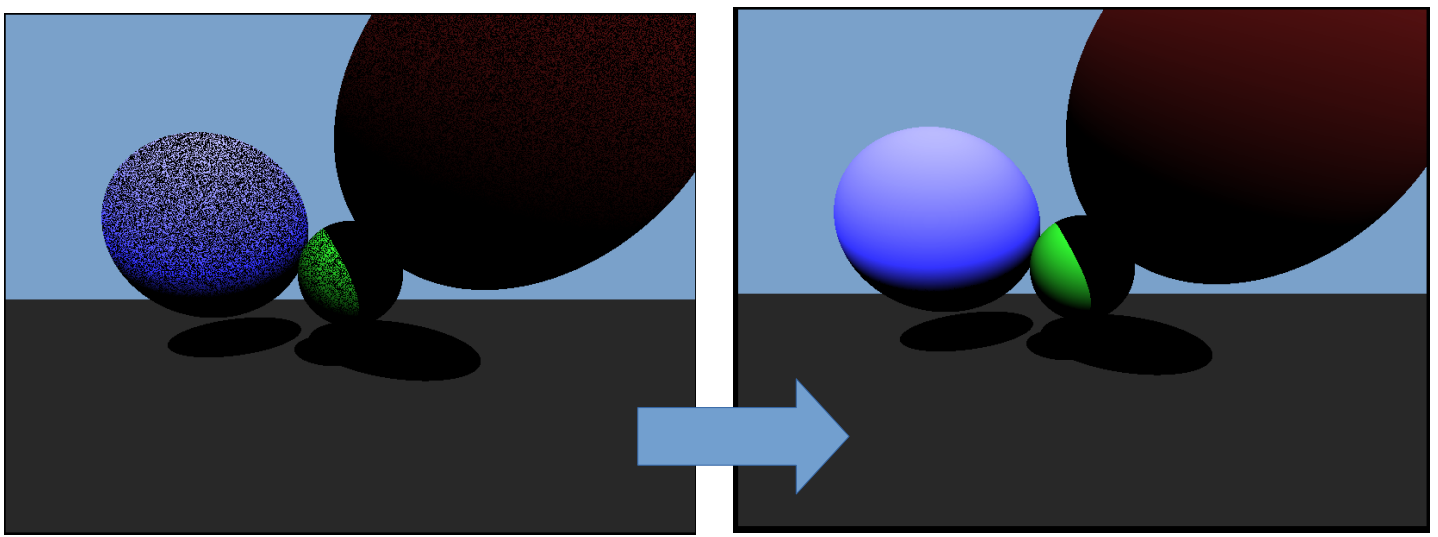
https://en.wikipedia.org/wiki/Ray_tracing_(graphics)

Shadow in ray-tracing: shadow acne

- Due to numerical limits in precision, some intersection point positions might end up under the surface
  - Casting shadow ray from this point causes intersection and thus light obstruction → shadow acne
  - Solutions:
    - Use double float precision
    - Add small displacement to intersection point in direction of normal: **shadow bias** parameter



https://www.scratchapixel.com/lessons/3d-basic-rendering/introduction-to-shading/ligth-and-shadows



https://bheisler.github.io/post/writing-raytracer-in-rust-part-2/

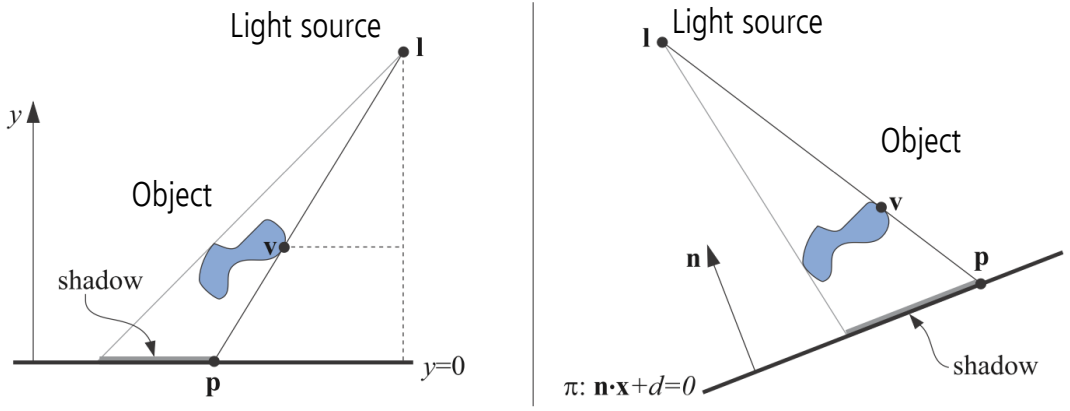
Shadow in rasterization

- Shadow computation in ray-tracing is elegantly solved due to nature of visibility solving which simulates physical light flow
- In rasterization, all objects in 3D scene are projected onto virtual image plane and information of 3D scene is partially lost
- Therefore, various methods are develop to simulate and introduce shadows
  - Different methods solve different special and simplified cases of shadow occurrence
    - **Planar shadows**
    - **Volume shadows**
    - **Shadow mapping**

More about shadows in rasterization-based rendering: https://www.realtimeshadows.com/

Planar shadows

- Simple case of shadowing: object cast shadow onto a planar surface
- Method: **projection shadows**



Projection matrix $\mathtt{M}$ is constructed to project object vertices $\mathtt{v}$ onto plane π with respect to the light source $\mathtt{l}$ giving shadow point $\mathtt{p}$.

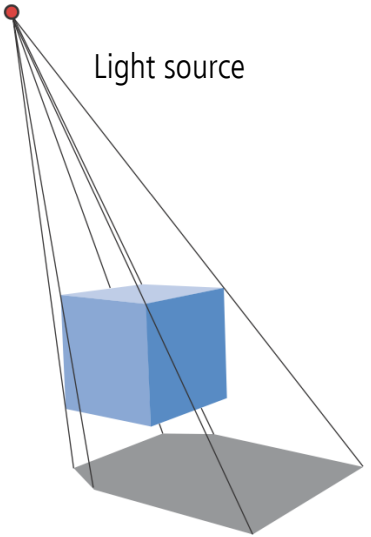
$$\mathbf{M} = \begin{pmatrix} \mathbf{n}\cdot\mathbf{l}+d-l_x n_x & -l_x n_y & -l_x n_z & -l_x d \\ -l_y n_x & \mathbf{n}\cdot\mathbf{l}+d-l_y n_y & -l_y n_z & -l_y d \\ -l_z n_x & -l_z n_y & \mathbf{n}\cdot\mathbf{l}+d-l_z n_z & -l_z d \\ -n_x & -n_y & -n_z & \mathbf{n}\cdot\mathbf{l} \end{pmatrix}.$$

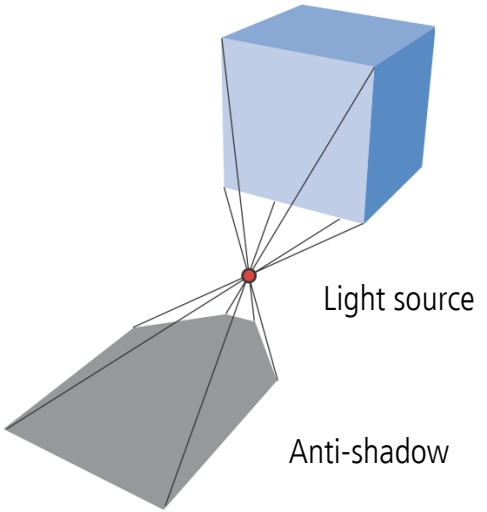
Projection shadows

- To render shadow, projection matrix $\mathtt{M}$ is applied to all objects (their vertices $\mathtt{v}$) which should cast shadow on plane π
- Projected object is obtained which is rendered with darker color and no illumination.

Notes:

- Projected object must be above plane π (introduce bias parameter controlling distance)
- Shadows may fall outside of plane π – this breaks the illusion and clipping must be performed
- Anti-shadow can be generated if light is between object and plane π

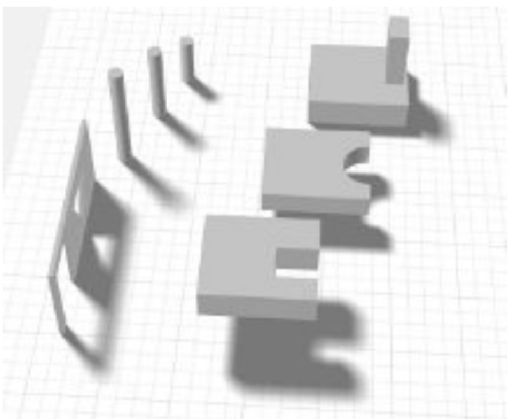




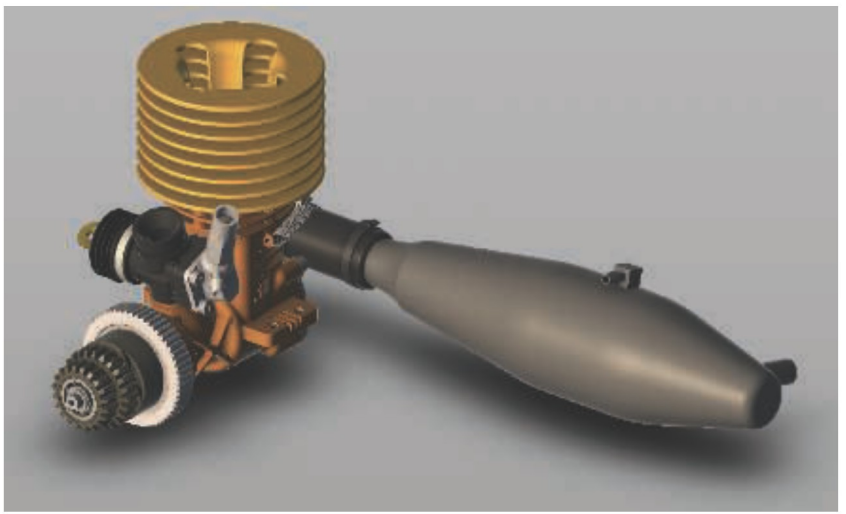
Projection shadows

- Soft shadows can be simulated.

Simulating area light: multiple point lights are placed where area light would be placed, resulting shadows are accumulated and and averaged (Heckbert and Herf's method)

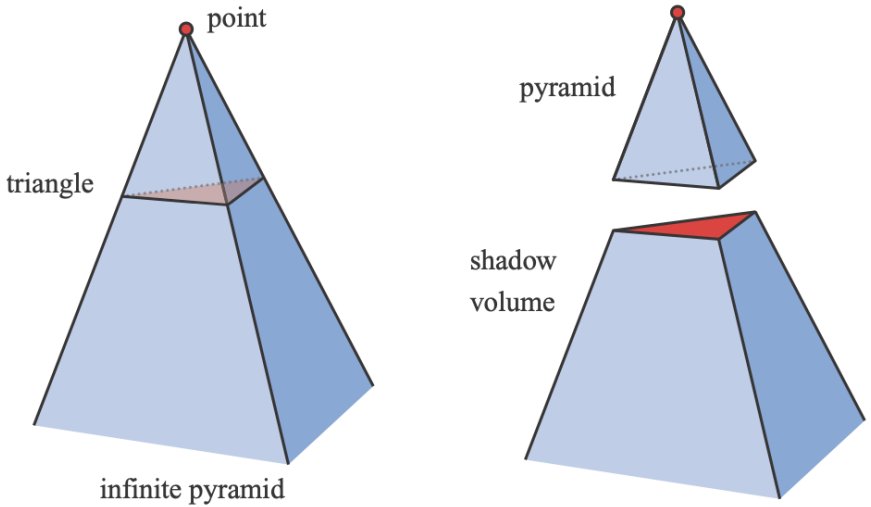


Blurring hard-shadow generated from a single point light.



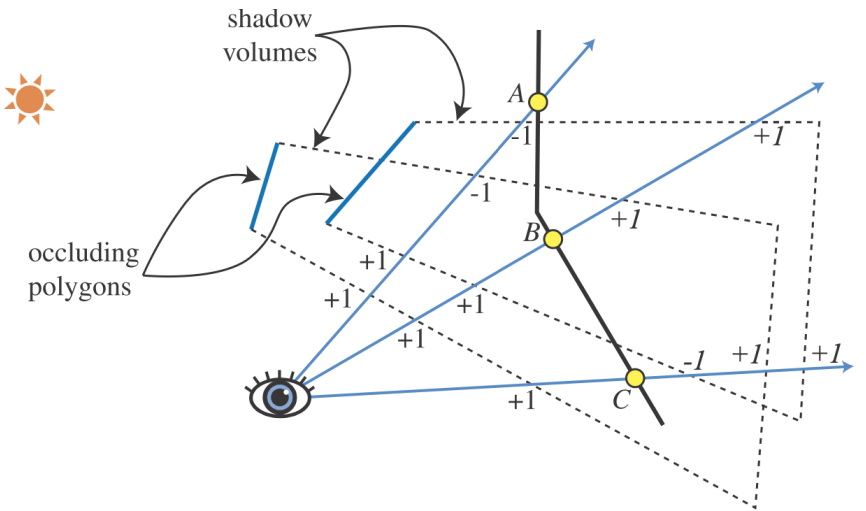
Shadow volumes

- More general approach for receivers of different shapes
- Volume of space is formed by occluder and light source
- Any object inside this volume is in shadow



Shadow volumes

- To determine if object is in shadow, counting method is used.
  - Ray is traced from view to object
  - Every time when ray passes through front-facing triangle of shadow volume the counter is increased
  - Every time when ray passes through back-facing triangle of shadow volume the counter is decreased
  - If counter is equal to zero than object is illuminated (not in shadow)

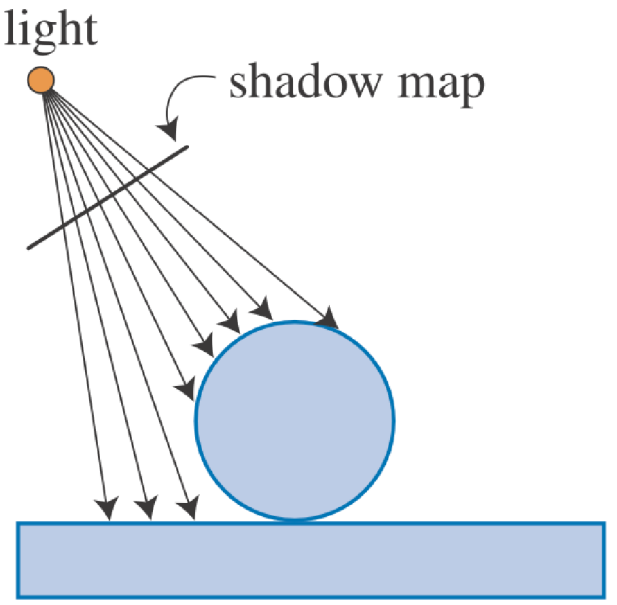


Shadow volumes

- Drawback: extreme variability
  - High difference in computation time depending on camera, object and light position
  - If camera is in shadow volume, the shadow volume fills the whole screen resulting in high computation → slow rendering
  - Consistent frame-rate is not guaranteed
- On GPU rasterization-based rendering counting is performed using depth and stencil buffers*

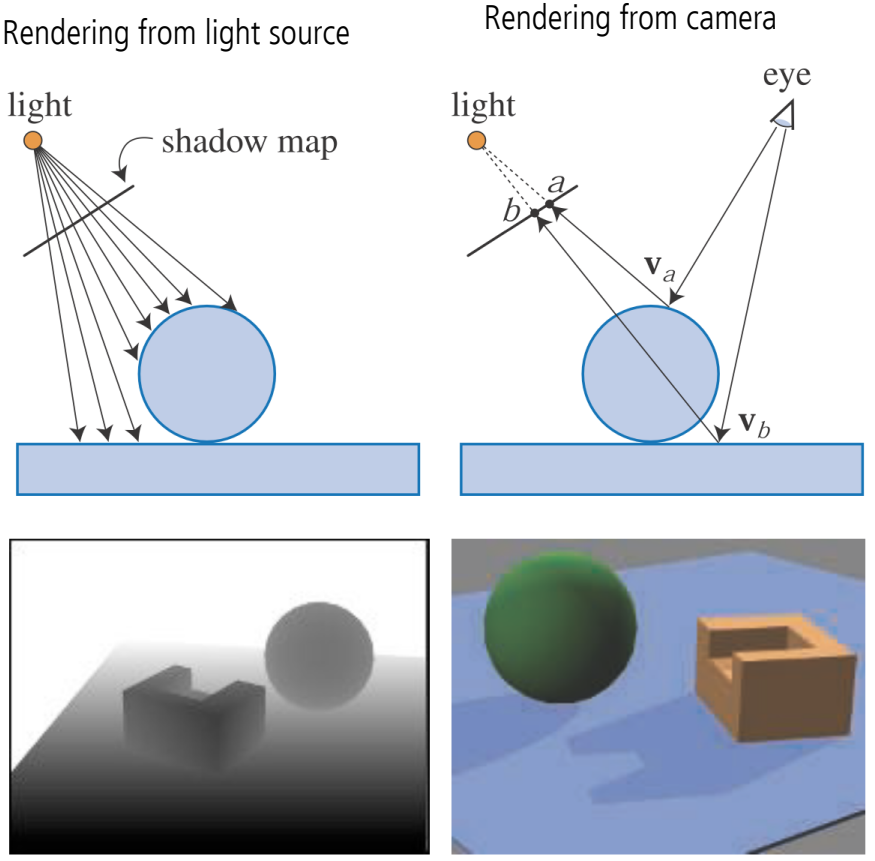
Shadow maps

- Efficient rendering of shadows on various receivers
- Idea: solve shadow casting as **visibility problem**
  - Points visible to light source are illuminated
  - Points invisible to light source are in shadow
- GPU rasterization uses z-buffer to solve visibility and store distance to closest objects in depth buffer*



Shadow maps

- Render the scene from position of light source that is to cast shadows
  - Store distances of visible objects in a texture → **shadow map**
- Render the scene once more, now from camera point of view → **multi-pass rendering**
  - Distance of rendered points to light source are compared to distances stored in shadow map
  - If point is farther from light source than the corresponding value in shadow map, then point is in shadow, otherwise it is not



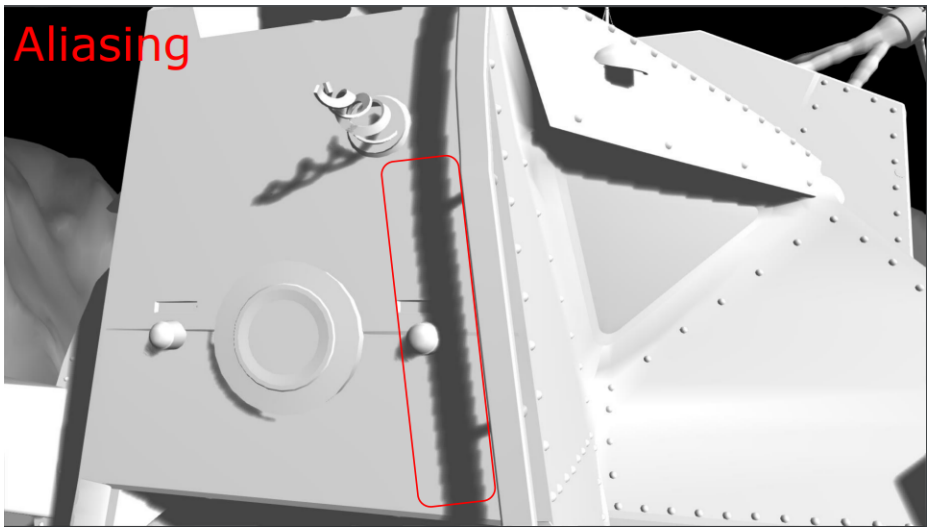
Shadow maps

- **Shadow map creation depends on type of light:**
  - Distant lights: ortographic projection is used since light direction is parallel
  - Spotlight: frustum is defined with spotlight shape
  - Point light: omnidirectional shadow maps – six view cube (similar to environment mapping)
- **Shadow map approach is predictable**
  - Shadow map contains only objects that can can cast shadows – objects inside light frustum
  - Cost of building shadow map is linear with number of triangles
  - Shadow map can be generated once and reused for all frames where light and objects are not moving

Shadow maps

- **Quality of shadows depend on shadow map resolution**
  - Quality of shadows depends on objects distance to light source → more samples for shadow map is needed for better approximation
  - Low shadow map resolution highlights aliasing

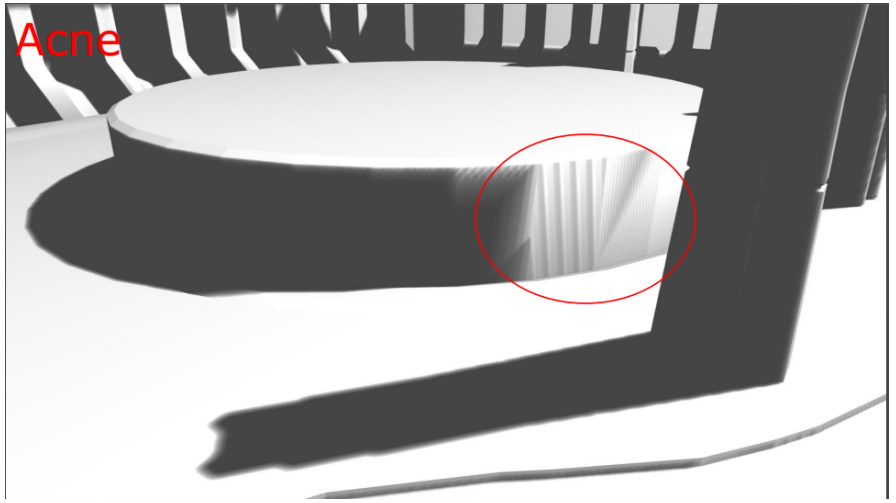
Quality of shadows depend on shadow map resolution



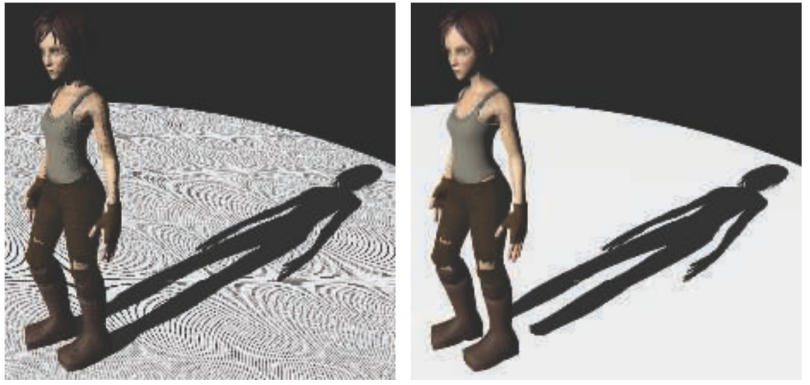
https://developer.download.nvidia.com/assets/events/GDC15/hybrid_ray_traced_GDC_2015.pdf

Shadow maps

- **Self-shadow aliasing and shadow acne** becomes apparent due to numerical limits and slight differences in light and camera view values
  - **Bias parameter** must be introduced which is correcting distances in camera and light view



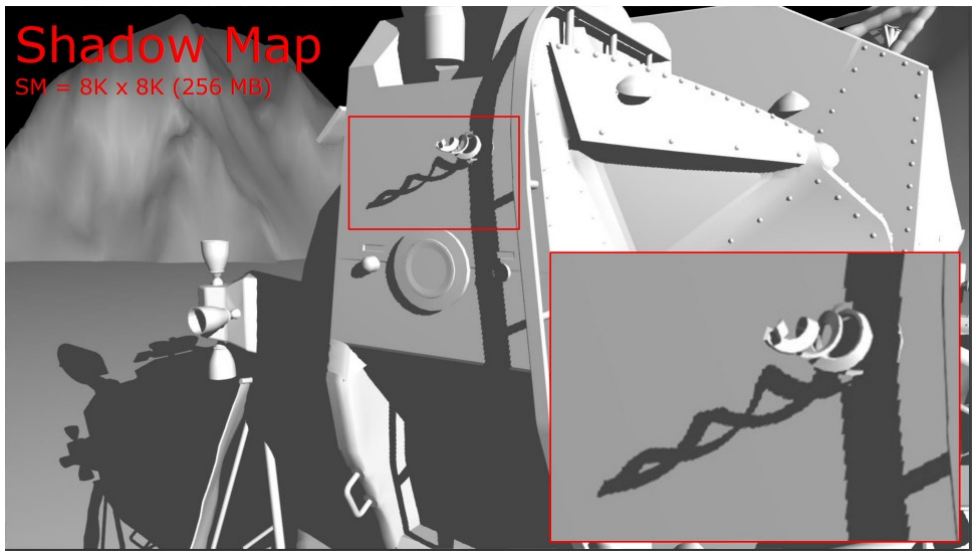
Self-shadowing (shadow acne) → moire pattern

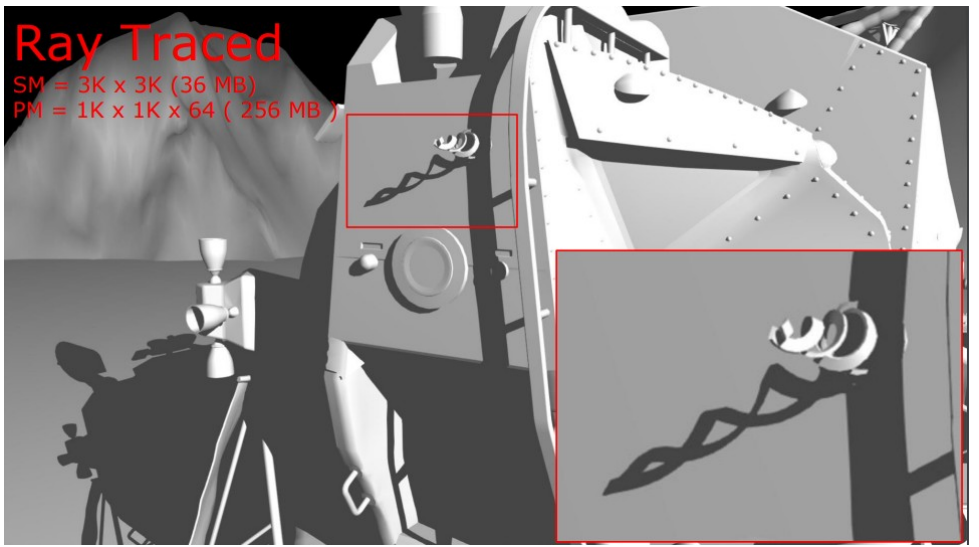


Ground self-shadowing leads to aliasing (Moire pattern)

Hybrid ray-traced shadows*

- Shadow maps are most often used method and still exhibit a lot of problems: aliasing, acne, etc.
- Solution is to combine rasterization-based rendering with ray-tracing for shadow computation





https://developer.nvidia.com/content/hybrid-ray-traced-shadows

Light and Shadow: Tips and Tricks

- Global illumination gives correct light reflection and shadows effects but it is expensive for real-time applications
- Physical lights more correctly describe light color and intensity distribution but are expensive to compute in real-time
- Non-physical light sources and direct illumination can be solved fast and efficiently and can to some extent approximate shadows and global illumination effects but require additional work

Light and Shadow: Tips and Tricks

- When creating 3D scene, artists understand the how the scene should be illuminated. Using this knowledge they place non-physical lights which are rendered with direct illumination to simulate global-illumination effects such as reflections and shadows.

https://80.lv/articles/dishonored-interiors-lighting-props/

More into topic

- Lighting for artists:
  - https://www.artstation.com/channels/lighting
  - https://80.lv/articles/amazing-lighting-for-simple-scenes/
  - https://www.youtube.com/watch?v=Ys4793edotw&ab_channel=BlenderGuru
- Path-tracing lights
  - https://www.pbr-book.org/3ed-2018/Light_Sources/Area_Lights
  - http://graphics.stanford.edu/papers/veach_thesis/
  - https://schuttejoe.github.io/post/arealightsampling/
  - https://www.scratchapixel.com/lessons/3d-basic-rendering/global-illumination-path-tracing/introduction-global-illumination-path-tracing.html
- Area lights approximation in rasterization-based rendering (OpenGL): https://learnopengl.com/Guest-Articles/2022/Area-Lights
- Shadows in rasterization:
  - https://www.realtimeshadows.com/sites/default/files/Playing%20with%20Real-Time%20Shadows_0.pdf
  - https://www.cs.montana.edu/courses/spring2005/525/students/Thiesen2.pdf
  - https://web.cse.ohio-state.edu/~shen.94/781/Site/Slides_files/shadow.pdf
  - https://cg.informatik.uni-freiburg.de/course_notes/graphics_07_shadows.pdf
- Hybrid shadow computation methods (rasterization + ray-tracing):
  - https://gpuopen.com/learn/hybrid-shadows/
  - https://developer.nvidia.com/content/hybrid-ray-traced-shadows

Summary questions

- https://github.com/lorentzo/IntroductionToComputerGraphics/tree/main/lectures/9_light

Literature

- https://github.com/lorentzo/IntroductionToComputerGraphics