



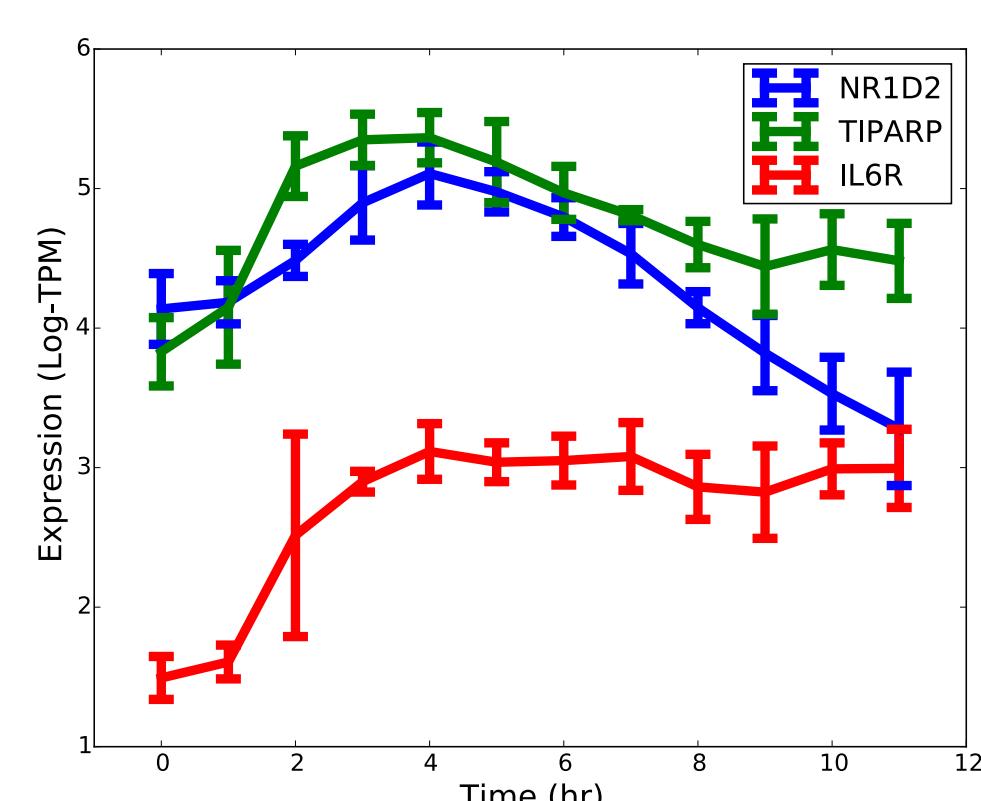
Improved Inference of Causal Networks from Gene Expression Time Series

Jonathan Lu

Advisors: Prof. Barbara Engelhardt, Bianca Dumitrescu and Brian Jo

Background

- Glucocorticoids (GCs) are immunosuppressant drugs that can lead to metabolic disorders such as diabetes and obesity
- How can we disentangle the desired immune effects from the adverse metabolic effects?
- GC binds to the glucocorticoid receptor (GR), which initiates transcription of a variety of genes, leading to a cascade of effects
- Can we infer the triggered causal network to pinpoint the immune and metabolic response?
- Use Gene expression time series from GC-stimulated lung cells
- 2768 differentially expressed genes, 12 timepoints, 4 replicates



Methodological challenges:

- High dimensionality: samples << predictors
- Statistical significance: F-test undefined⁵
- Validation: Ensure biological relevance

Goal

Build comprehensive pipeline for causal network inference that handles high dimensionality, maintains statistical significance, and validates on external biological data.

Prior Approaches

Previous methods either do 1) low-dimensional fit or 2) high-dimensional fit missing an effective statistical null or biological validation

	Mukhopadhyay 2007 ¹ , Tam 2012 ² , ...	Lozano 2009 ³ , Shojai 2010 ⁴ , Yao 2015 ⁵ , ...	Our Work
High-dimensional causal fit	✗	✓	✓
Statistical significance	✓	✗	✓
External validation	✗	✗	✓

Vector Autoregression

Based on Granger Causality⁶ principle:
 $X \rightarrow Y$ if including past values of X helps to predict Y

- Fast, effective, flexible lags

$$Y_t = \sum_{i=1}^k \alpha_i Y_{t-i} + \sum_{i=1}^k \beta_i X_{t-i} + \epsilon_t$$

$$H_0 : \beta_i = 0 \text{ for all } i$$

High-Dimensional Fit

Fit all causes simultaneously and regularize

$$Y_t = \sum_{i=1}^k \alpha_i Y_{t-i} + \sum_{g \in G} \sum_{i=1}^k \beta_i^g X_{t-i}^g + \epsilon_t$$

$$\hat{\beta} = \arg \min_{\beta} \|Y - X\beta\|_2^2 + \lambda f(\beta)$$

$$f_{\text{LASSO}}(\beta) = |\beta|_1$$

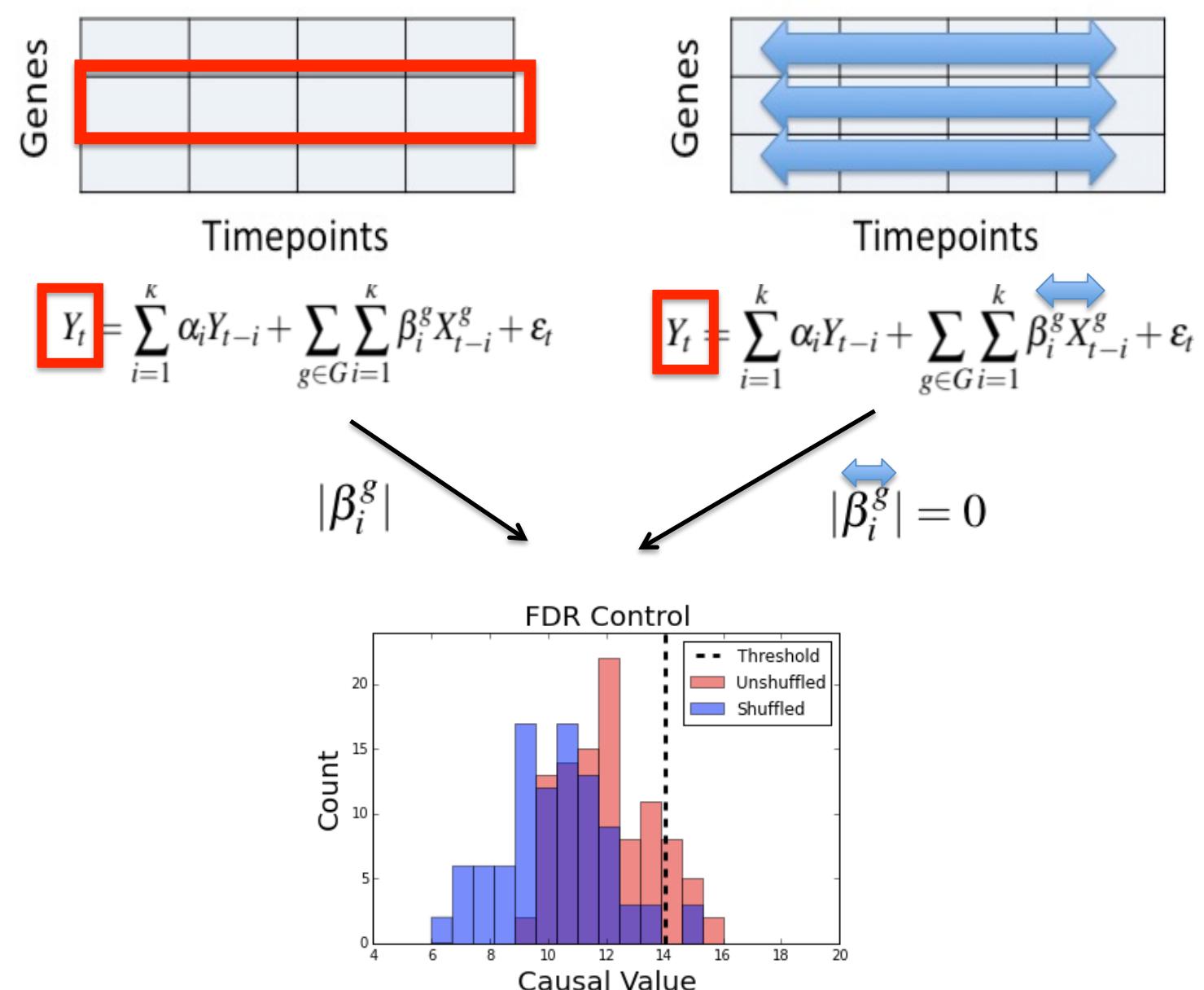
$$f_{\text{RIDGE}}(\beta) = |\beta|_2^2$$

$$f_{\text{ELASTIC}}(\beta) = \alpha|\beta|_1 + (1-\alpha)|\beta|_2^2$$

$$H_0 : \beta_i^g = 0 \text{ for given } g \in G.$$

Statistical Significance

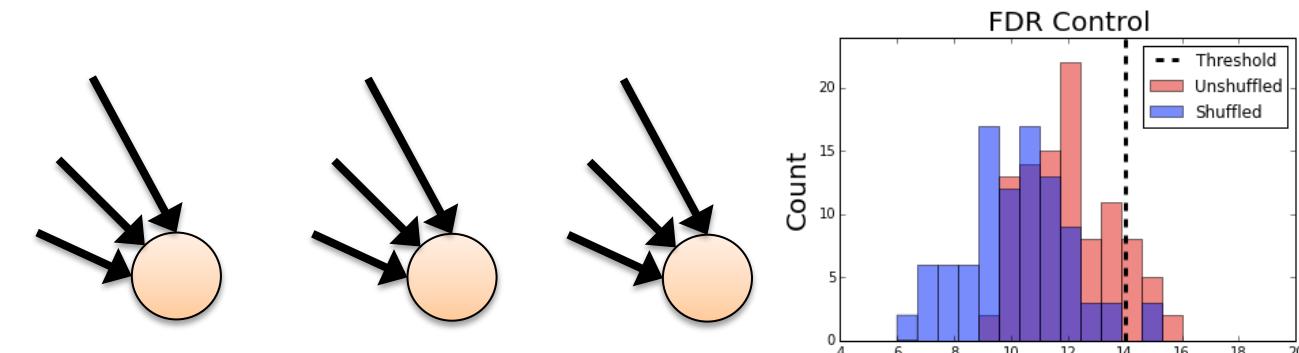
Use coefficients fit over permuted data for null



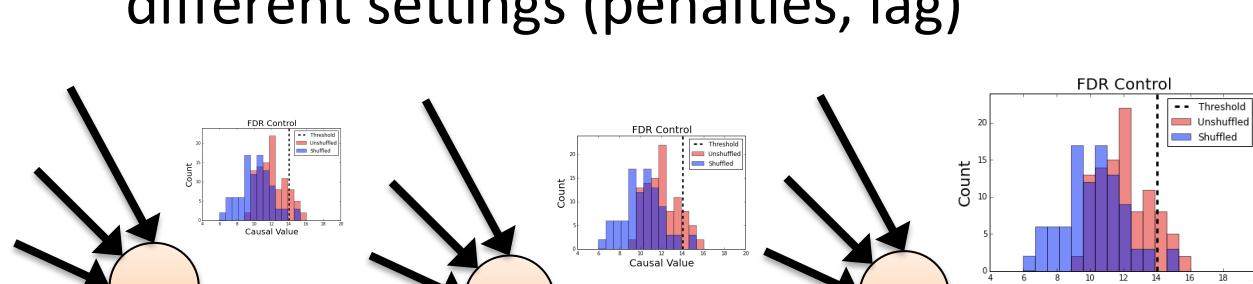
False Discovery Control

2 types of permutation FDR.

- Global FDR: global threshold over all coefficients

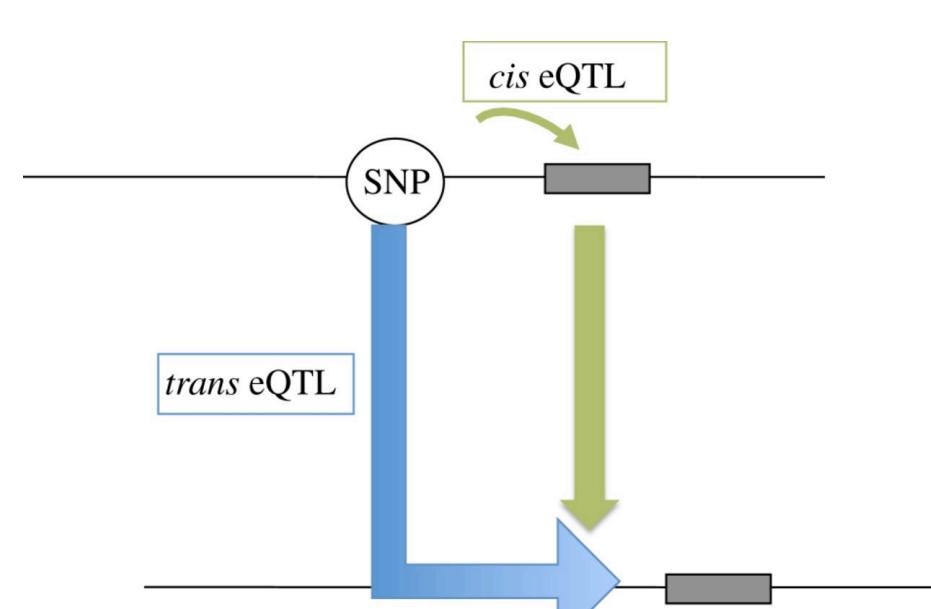


- Local FDR: threshold specific to effect gene
 - Finds networks with more consistent sizes over different settings (penalties, lag)



Validation

- $X \rightarrow Y$ means X, Y not independent
- Use Association test between Y's expression and SNP affecting X's expression in lung Genotype Tissue Expression Data

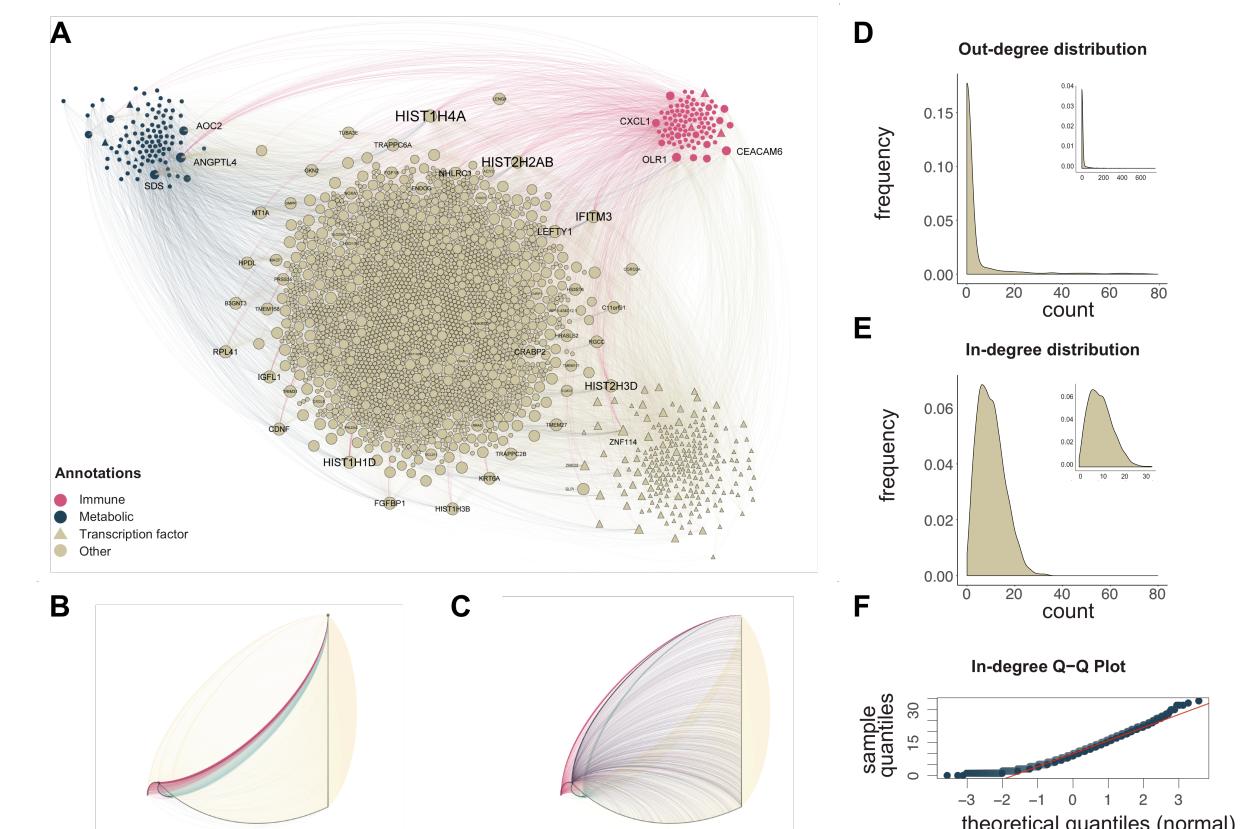


References

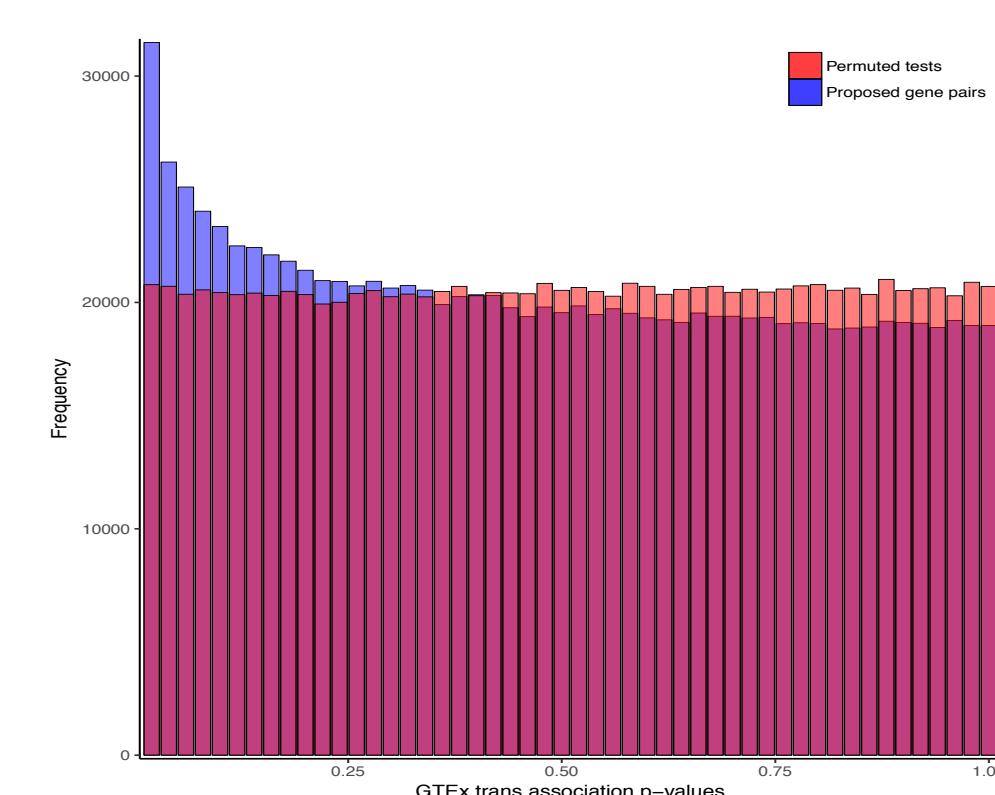
- Nitai D. Mukhopadhyay and Snigdhansu Chatterjee. Causality and pathway search in microarray time series experiment. *Bioinformatics*, 23(4):442, 2007.
- Gary H.F. Tam, Chunqi Chang, and Yeung Sam Hung. Application of granger causality to gene regulatory network discovery. In *IEEE 6th International Conference on Systems Biology (ISB)*, ISB '12, 2012.
- Aurélie C Lozano, Naoki Abe, Yan Liu, and Saharon Rosset. Grouped graphical granger modeling for gene expression regulatory network discovery. *Bioinformatics*, 25(12):i110–i118, 2009.

Results

- 27,781 edge network
- 617 causal genes, 2744 effect genes
- Power-law out-degree distribution
- Normal in-degree distribution



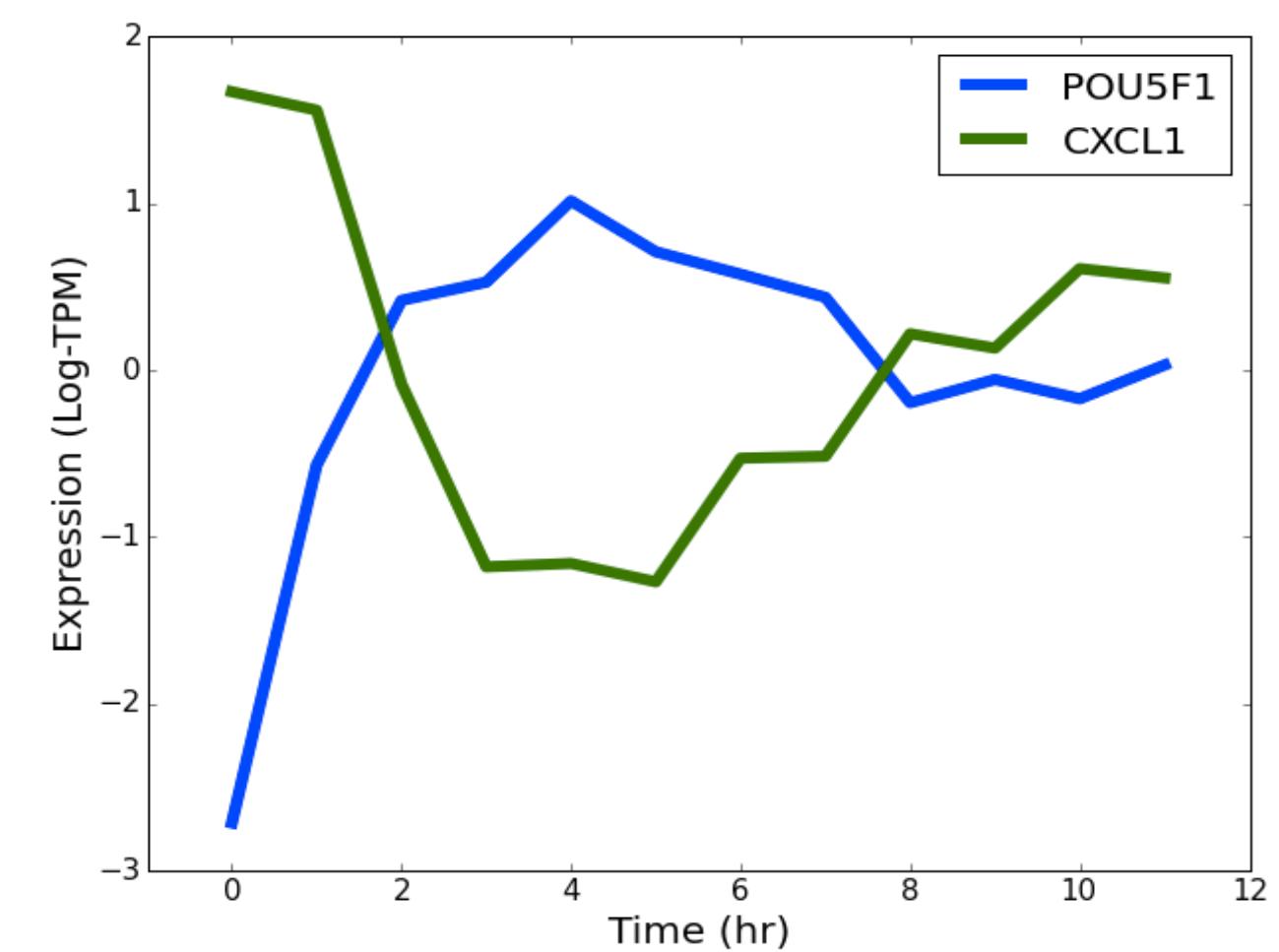
- 280 validated edges (FDR 0.2)
- 81 edges in lung



- Enrichment for Immune-Causal and Metabolic-Causal Edges

Network Edge Statistics			
Edge Type	Total	%	Odds Ratio
TF-Causal	1931	7	0.8
TF-Effect	2393	8.6	1.1
Immune-Causal	2119	7.6	2
Immune-Effect	1047	3.8	1
Metabolic-Causal	2271	8.2	2
Metabolic-Effect	1211	4.4	1

- Strong repressive relation between Transcription Factor POU5F1 and Immune-related gene CXCL2



Conclusion & Future Work

- We have developed an improved pipeline for causal network inference that validates on external data.
- Extension 1: Use the network to suggest genes for perturbation in follow-up experiments
- Extension 2: Extend model to incorporate causal relations learned from data under multiple conditions

4. Ali Shojaie and George Michailidis. Discovering graphical granger causality using the truncating lasso penalty. *Bioinformatics*, 26(18):i517–i523, 09 2010.

5. Shun Yao, Shinjae Yoo, and Dantong Yu. Prior knowledge driven granger causality analysis on gene regulatory network discovery. *BMC Bioinformatics*, 16:273, 2015.

6. C.W.J. Granger. Testing for causality. *Journal of Economic Dynamics and Control*, 2:329 – 352, 1980.