

Randomized Optimization, Unsupervised Learning, and Dimensionality Reduction

Writeup for Assignment 02 - CS 6741

Magahet Mendiola

ABSTRACT

An empirical analysis of planning and reinforcement learning algorithms in the context of markov decision processes.

1. PLANNING METRICS

A number of simple metrics were used to evaluate the performance of our planning algorithms. These include the number of iterations and elapsed time required to find the optimal utility values for each state. However, the goal of planning is to find the optimal policy for an MDP, and not the optimal set of utility values. Therefore, we can also compare how long it takes each to find the optimal policy for each state.

There is also the rate at which a policy converges toward the optimum. This can be seen with the hamming distance between the current policy and the optimal policy at each iteration. If a partial plan can be created quickly, it may be good enough for practical use on the MDP.

Another derivation of the hamming distance metric is the time/iterations required to find the policy which will successfully guide a deterministic agent to the goal state. The idea behind this metric is that there may be many states that are never visited. Running value or policy iteration until enough of the states have optimal policies to guide the agent could greatly reduce planning time.

Creating a planning algorithm with this stopping criteria would be similar to q-learning in regards to limiting exploration. It would also be similar to a* path finding, with search areas radiating omni-directionally from non-zero reward states.

2. GRID WORLDS

Each algorithm was tested against contrived gridworld type MDPs. These worlds were setup to accentuate the strengths and weaknesses of each algorithm. They also illustrate the impact of rewards, discounts, and and to point out opportunities for modifications to each.

2.1 Discount Grid

This grid world, titled Discount Grid [1], is useful for illustrating the effects of utility discounting, transition function probabilities, and state rewards on optimal policies. It includes two terminal states with positive rewards (+1 closer, +10 farther) and five negative terminal states at the bottom edge of the grid. This setup allows us to explore what set of problem and solution parameters affect the goals defined by an optimal policy.

Figure 1a shows the resulting values of the MDP after running value iteration with a γ of 0.9 and a reward of 0 in all the non-terminal states. The transition probabilities are 0.8 for desired action and a combined 0.2 for all orthogonal movements. In this case, the policy directs the agent to seek out the farther, higher valued, terminal state. It also avoids the high penalty cliff except when the alternative is moving into the lower reward terminal state.

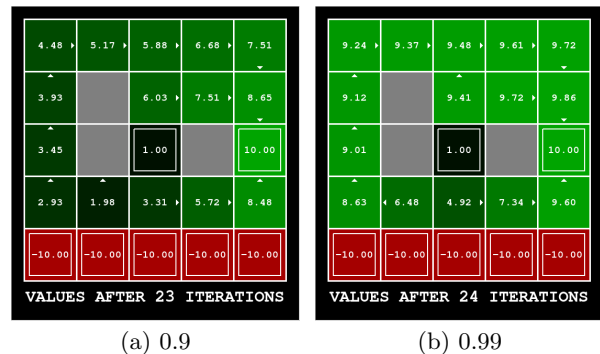


Figure 1: discount grid - various γ settings

Time matters.

With a γ of 0.99, which reduces the effects of discounting, the policy shifts slightly (Figure 1b). The policy in state (2,2) now risks a direct movement to the east, given the higher expected utility of that action. This is due to the higher relative value of state (1,2) due to the reduced discounting. Also, state (3,6) avoids the risk of falling into the lower reward for the same reason. The expected value of attempting a northward movement is now relatively more valuable than with a move east policy, despite the indirect route to the terminal state. This shows the implications of adjusting delayed reward and how an agent could be lead to take greater risks or follow an otherwise sub-optimal route to gain a larger reward farther in the distance.

Rewards matter.

With a shift in rewards, we can affect how the resulting policy directs the agent. Figure 2a shows the result of changing the reward in all non-terminal states to -2. The policy now believes that the closer terminal state is a better alternative at state (3,2). The negative rewards, and risk of falling off the cliff, push the agent toward the closer end point. With the non-terminal rewards set to -3, this early

termination policy extends to the northern path as well (Figure 2b). With a sufficiently negative non-terminal reward, we can even entice the agent to end the process as quickly as possible, by intentionally jumping off the cliff (Figure 2c).

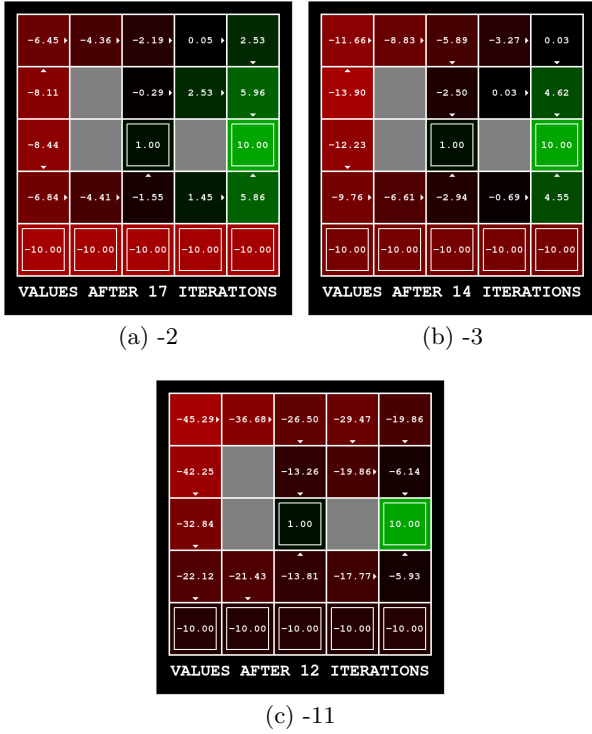


Figure 2: discount grid - various non-terminal reward settings

The problem matters.

Policies are not only affected by planning algorithm parameters, but also by the problem definition, such as the probabilities in the transition function. If movement in the MDP is deterministic, or the intentional action probabilities are sufficiently high, otherwise risky paths would be considered optimal. Figure 3a shows a policy of cliff-walking given only a 1% change of falling off the ledge. Conversely, the policy in Figure 3b shows how our planning algorithm would approach a high risk environment (inebriated agent). In the later case, the agent will avoid any east-west movement, even at the expense of exiting at the low reward terminal state.

2.2 Tunnel Grid

Tunnel grid is a one dimensional grid with the starting state on one end and the only terminal state on the other. Although this grid is simplistic, it highlights the distinctions between our planning and learning algorithms well.

For example, Figure 1 shows the elapsed time and the number of iterations/episodes each algorithm took to converge. In the case of Q-learning, an episode is determined as a single training run from the starting state until the agent reaches a terminal state. Also, convergence for the Q-learning agent is defined as the state when setting ϵ to zero and following the best q-score at each state would result in the optimal policy.

We see from the first two rows that value iteration requires

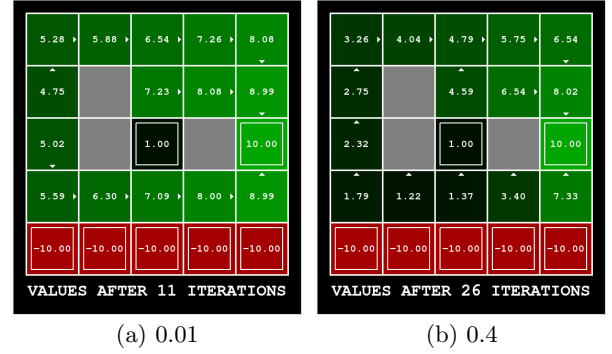


Figure 3: discount grid - various unintentional movement probabilities

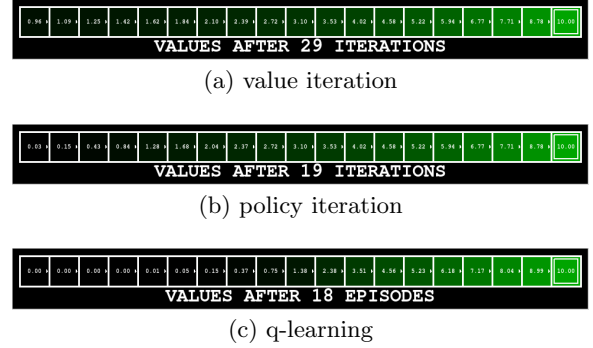


Figure 4: tunnel grid

	Elapsed Time	Iterations/Episodes
Value	0.04	29
Policy	0.04	19
Q-Learning	0.390	18

Table 1: tunnel grid - performance

nearly 50% more training cycles to converge. However, policy iteration and value iteration are identical in terms of elapsed time. This is due to the greater computational requirements of policy evaluation at each interval for policy iteration. Q-learning required a substantially longer amount of time to train.

In the case of the tunnel grid, Q-learning will perform identically to an agent that guesses randomly (random walk) until it eventually reaches a non-zero reward state. Until then, none of the states it visits will produce a meaningful Q-value. This is highly inefficient, as the expected number of states the agent will visit before reaching the end is $n^2 + n$, which is 280 in a 19 state tunnel grid. A more intelligent agent would keep track of previously visited states that resulted in all zero q-scores and place greater action probability on moving to previously unexplored states.

2.3 Simple Grid

To evaluate value and policy iteration performance empirically as the number of states increase, each algorithm was run to convergence on grids ranging from 3 by 3 (9 states) to 30 by 30 (900 states). A single, positive valued, terminal state was set at one corner. Figure /refplanning-performance shows the results of this experiment. Within these grid sizes, iterations seem to grow linearly with respect to the grid edge size, which seems reasonable considering the radiating propagation behavior seen with these algorithms. Elapsed time for each shows greater than linear growth, which can be partially attributed to the polynomial growth of the number of states. Relatively, policy iteration elapsed time seems to grow at a greater rate than value iteration. At 900 states, the difference is as great as 40% slower.

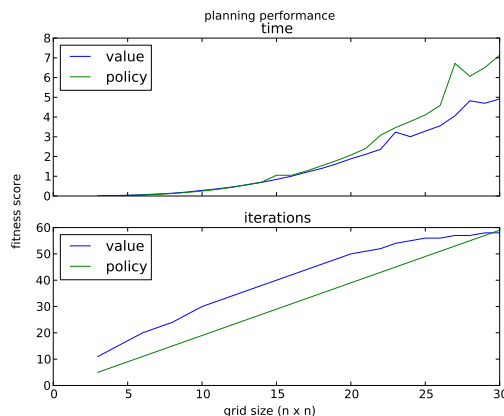


Figure 5: planning performance by grid size

3. VALUE ITERATION

4. POLICY ITERATION

5. Q-LEARNING

metrics elapsed time hamming distance
lazy vs. eager learning.
planning performance

policy iteration implementation issues get's stuck with only policy change check takes too long with epsilon check works well with value update check
q-learning performnace q-learning strategies

6. REFERENCES

- [1] D. Klein. *Project 3: Reinforcement Learning*, 2009 (accessed April, 2014). <http://inst.eecs.berkeley.edu/~cs188/fa09/projects/reinforcement/reinforcement.html>.
- [2] S. J. Russell, P. Norvig, J. F. Candy, J. M. Malik, and D. D. Edwards. *Artificial Intelligence: A Modern Approach*. Prentice-Hall, Inc., Upper Saddle River, NJ, USA, 1996.