Computational Sociology

Agent-based modeling and programming fundamentals

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Plan

- Course updates
- ► Part I: Agent-based modeling
- ▶ Part II: Programming fundamentals

Course updates

Homework

- ▶ Homework 1 will be released by at the end of class
 - ▶ Due next Friday (2/9) at 5pm Eastern.

Agent-based modeling and quantitative social science

- Most quantitative social science is variable-centered
 - e.g. We study the associations and interactions between variables in a linear regression

Agent-based modeling and quantitative social science

- As a consequence, many sociologists think about the world in terms of what Andrew Abbott calls "general linear reality"
 - ► A social world composed of fixed entities with fixed attributes

Agent-based modeling and quantitative social science

- ▶ Agent-based modeling is the study of "social life as interactions among adaptive agents who influence one another in response to the influence they receive." (Macy and Willer 2002)
 - ► Rather than interactions between *variables*, we consider interactions between *interdependent individuals*

Agent-based modeling and quantitative social science

- Often we are interested in the emergent properties of local interactions between agents and how they aggregate into system-level processes such as diffusion, polarization, and segregation
 - ► These complex system-level patterns can emerge without any centralized coordination
- ► Like historical sociology and ethnography, agent-based modeling is a *relational* approach, focusing on the context-dependent and contingent nature of social interaction

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Key assumptions

- Macy and Willer 2002 outline four key assumptions that underpin many sociological agent-based models
 - Agents are autonomous
 - There is no system-wide coordination
 - Agents are interdependent
 - Agents respond to each other and to their environment
 - Agents follow simple rules
 - Simple local rules can generate global complexity
 - Agents are adaptive and backwards looking
 - Agents can alter their behavior through processes such as imitation and learning

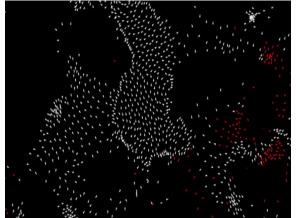
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Advantages of ABMs

- Virtual experiments to test causal mechanisms
 - Particularly useful where real-world experimentation is impractical
- Theory building and testing
 - Bridging between micro and macro levels of analysis
 - Varying the social structure and the agency of individuals

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Craig Reynolds Flocking behavior (1987)



Reynolds, Craig W. 1987. "Flocks, Herds and Schools: A Distributed Behavioral Model." In Proceedings of the 14th
Annual Conference on Computer Graphics and Interactive Techniques. 25–34.

Flocking behavior in NetLogo

```
http://www.netlogoweb.org/launch\#http://ccl.northwestern.edu/netlogo/models/models/Sample%20Models/Biology/Flocking.nlogo
```

Thomas Schelling Homophily and segregation

DYNAMIC MODELS OF SEGREGATION

| | _ | | _ | | - 11 | | | _ | _ | _ | - | | | | |
|---|---|---|---|---|------|---|---|---|---|---|---|---|---|---|---|
| | | # | | # | # | # | | O | O | | O | O | # | # | # |
| # | | # | # | # | # | # | O | 0 | 0 | # | # | 0 | O | # | # |
| # | # | | | # | | | # | 0 | # | # | # | | 0 | # | # |
| # | # | | # | | # | # | | # | # | # | # | | | 0 | # |
| # | 0 | # | | # | | | | | | # | | | O | 0 | 0 |
| 0 | O | # | # | | | # | # | # | # | # | | | | 0 | 0 |
| O | 0 | # | | # | # | | | # | # | # | | # | 0 | 0 | |
| # | # | 0 | # | 0 | 0 | | # | | # | | # | # | | 0 | |
| # | # | # | 0 | 0 | O | 0 | | # | # | # | # | | 0 | 0 | O |
| # | # | # | 0 | 0 | O | # | | | | # | | | # | # | 0 |
| # | | 0 | 0 | 0 | # | | | # | | | # | | | # | |
| | # | # | 0 | 0 | # | # | # | | # | # | | # | # | # | |
| # | # | | O | O | # | # | | # | # | | # | | | | # |

Fig. 13

Schelling, Thomas C. 1971. "Dynamic Models of Segregation." Journal of Mathematical Sociology 1: 143-86.

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NetLogo and NetLogoWeb

Schelling's segregation model in NetLogo

http://www.netlogoweb.org/launch#http://ccl.northwestern.edu/netlogo/models/IABM%20Textbook/chapter%203/Segregation%20Extensions/Segregation%20Simple.nlogo

Simple diffusion and the S-curve

Complex contagions

- ► A simple diffusion process, like catching the flu, requires a single exposure
- ► Complex contagions require exposures to multiple people
 - Joining a high-risk social movement
 - Avant garde fashions
 - New technologies

Thresholds

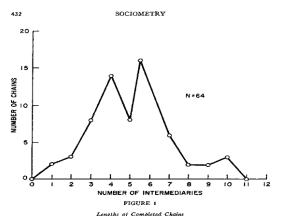
- Thresholds denote the number of exposures
 - Variation across diffusion processes
 - Individual variation
 - Distributions of thresholds in a population*

*See: Granovetter, Mark. 1978. "Threshold Models of Collective Behavior." American Journal of Sociology 83(6):1420–43.

Weak ties as long ties

- ► Granovetter (1971) emphasized the "strength of weak ties"
- Centola and Macy (2007) put emphasis on the "length" of weak ties, noting how the can help to connect different parts of a network

Six degrees of separation and small-worlds



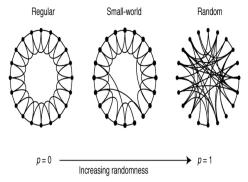
Lengths of Compacted Chains

Travers, Jeffrey, and Stanley Milgram. 1969. "An Experimental Study of the Small World Problem." Sociometry 32(4):425.

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Six degrees of separation and small-worlds

Figure 1: Random rewiring procedure for interpolating between a regular ring lattice and a random network, without altering the number of vertices or edges in the graph.



Watts, Duncan J., and Steven H. Strogatz. 1998. "Collective Dynamics of 'Small-World' Networks." *Nature* 393(6684):440–42.

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Six degrees of separation and small-worlds

| Table 1 Empirical examples of small-world networks | | | | | | | | |
|--|---------|--------------|--------------|--------------|--|--|--|--|
| | Lactual | L_{random} | C_{actual} | C_{random} | | | | |
| Film actors | 3.65 | 2.99 | 0.79 | 0.00027 | | | | |
| Power grid | 18.7 | 12.4 | 0.080 | 0.005 | | | | |
| C. elegans | 2.65 | 2.25 | 0.28 | 0.05 | | | | |

Characteristic path length L and clustering coefficient C for three real networks, compared to random graphs with the same number of vertices (n) and average number of edges per vertex (k). (Actors: n=225,26,k=61. Power grid: n=4,941,k=2.67. C. elegans: n=282,k=14.) The graphs are defined as follows. Two actors are joined by an edge if they have acted in a film together. We restrict attention to the giant connected component of this graph, which includes $\sim 90\%$ of all actors listed in the Internet Movie Database (available at http://us.imdb.com), as of April 1997. For the power grid, vertices represent generators, transformers and substations, and edges represent high-voltage transmission lines between them. For C. elegans, an edge joins two neurons if they are connected by either a synapse or a gap junction. We treat all edges as undirected and unweighted, and all vertices as identical, recognizing that these are crude approximations. All three networks show the small-world phenomenon: $L \geqslant L_{ancomp}$ but $C \gg C_{ancomp}$.

Watts, Duncan J., and Steven H. Strogatz. 1998. "Collective Dynamics of 'Small-World' Networks." *Nature* 393(6684):440–42.

Complex contagions

- While much information flows through weak ties, Centola and Macy (2007) argue that weak ties are often insufficient for social contagions
- ▶ It is not just the presence of ties that "bridge" communities, but the width of the bridge, or the number of ties, that matters

Modeling complex contagions

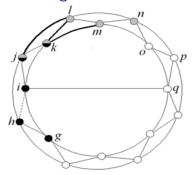


Fig. 1.—A ring lattice with z=4 and one long tie. The figure illustrates the width of the bridge between the neighborhoods of i (black and gray/black nodes) and l (gray and gray/black nodes), showing the two common members (gray/black nodes). The bridge between these two neighborhoods consists of the three ties j_i , kl, and km (shown as bold lines). The long tie from i to q provides a shortcut for a simple contagion but not for one that is complex.

Modeling complex contagions

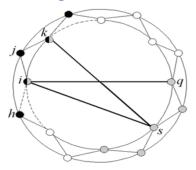
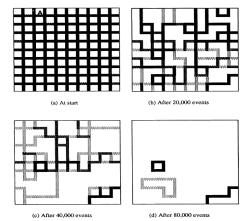


Fig. 2.—A ring lattice with z=4 and three ties. The figure shows the width of the bridge between neighborhood J (black and gray/black nodes, with focal node j) and neighborhood S (gray and gray/black nodes, with focal node s), showing the two common members (gray/black nodes). An increment in the threshold from $\tau = 1/z$ to $\tau = 2/z$ triples the width of the bridge required to create a shortcut (bold lines) between J and S, from one tie to three. The two ties is and ks are sufficient to activate s, and the third tie from i to q is sufficient to activate a, given the tie from s to a.

Robert Axelrod *Local convergence and global polarization* (1987)



Axelrod, Robert. 1997. "The Dissemination of Culture: A Model with Local Convergence and Global Polarization."

Journal of Conflict Resolution 41 (2): 203–26.

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Delia Baldassarri and Peter Bearman (2007)

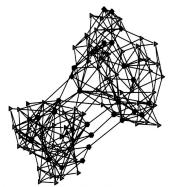


Figure 7. Discussion Network at Time 500 in a Takeoff Case (#963)

Notes: Nodes represent the issue that has been discussed most frequently by each actor. The color distinguishes between
the most popular issue (zery) and all the other issues (oback). Simulation #963, takeoff.

Baldassarri, Delia, and Peter Bearman. 2007. "Dynamics of Political Polarization." American Sociological Review 72(5):784–811.

Politics and lifestyle choices

DellaPosta, Shi, and Macy (2015) suggest a mechanism to explain observed correlations between political attitudes and lifestyle choices

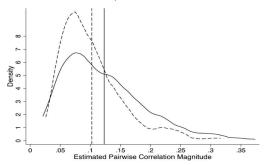
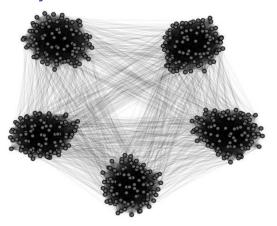


Fig. 2.—Magnitude of zero-order and partial correlation between GSS lifestyle items and ideological identity, Graphs plot Epanechnikov kernel density functions for both zero-order (solid lines) and partial (dashed lines) correlation magnitudes estimated from the mixed-effects model (see table Az in the appendix). One value is plotted for each of the 216 item pairs. Time is set to 2010 to facilitate comparison across item pairs. The solid vertical reference line gives the mean predicted zero-order correlation magnitude across all item pairs in 2010 and the dashed vertical reference line gives the same value for partial correlation magnitude.

Politics and lifestyle choices

- ▶ Dellaposta and colleagues argue that correlation between politics and lifestyle choices explained by network autocorrelation, "the tendency for people to resemble their network neighbors" (p.1488)
- ► Feedback loops between spatial settings, relations, and lifestyle

Politics and lifestyle choices



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Competing explanations: Cognitive mechanisms

Goldberg and Stein (2018) propose an alternative mechanism, arguing that culture does not spread like a virus, but depends on belief structures

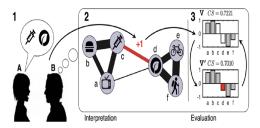


Figure 3. An Illustration of the Agent-Based Model Sequence Note: (1) Agent B observes A express support for vaccinations and organic food (practices c and d); (2) B updates the corresponding element in his associative matrix, B (the edge connecting nodes c and d in the network representation of B); and (3) randomly updates his preference for organic food (practice d, resulting in preference vector V), which is the weaker preference of the pair (c,d) in his preference vector V. Because constraint satisfaction is reduced from .7221 to .7010, this preference update is

Integrating real-world data

DiMaggio and Garip (2011) construct agent with attributes based on the General Social Survey

Network Externalities, Intergroup Inequality

 ${\bf TABLE~2}$ Linear Regression of Adoption Levels on Experimental Conditions

| | | RA | CE | Inc | OME | Education | | |
|---------------------|------------|--------|------------|---------|------------|-----------|--------------------------|--|
| | ALL | Whites | Blacks | High | Low | BA | Less than High School | |
| No network exter- | | | | | | | | |
| nalities | 516** | 536** | 399^{**} | 685** | 238** | 611** | 351** | |
| General network ex- | | | | | | | | |
| ternalities | .030°° | .028** | .043** | .032 | .017°° | .023*** | .030** | |
| Homophily = .25 | 003** | 001 | 012** | .009*** | 014°° | .005*** | 011°° | |
| Homophily = .5 | 005** | 002** | 024** | .017** | 028^{**} | .010** | 024** | |
| Homophily = .75 | 011°° | 006** | 040°° | .024** | 046** | .012** | 043** | |
| Homophily = 1 | 019^{**} | 012** | 061°° | .029** | 067°° | .015** | 068** | |
| Intercept | .618** | .647** | .454** | .925** | .249** | .788** | .392** | |
| R ² | .99 | .99 | .97 | .99 | .96 | .99 | .96 | |

Note.—All independent variables are binary. Both dependent and independent variables are measured on the final period of simulations (t=100). Reference: homophily = 0; N=7,000.

^{*} P < .05.

^{**} P < .01.

Realism and external validity

- Bruch and Atwell (2015) distinguish between two types of realism in ABMs
 - Low-dimensional realism: simple, parsimonious models
 - ► High-dimensional realism: complex, complicated models
- Trade-offs:
 - ► The latter might be more realistic, but involve more parameters and may be less intelligible

Parameters and sensitivity

- Use theory to guide decisions regarding which parameters vary and should be fixed
 - ► Formalizations can be hard to operationalize
- Models can be extremely sensitive to small variations in parameters
 - Be careful to check for coding errors!*
- Timing matters
 - Constant time vs. discrete-time
 - Asynchronous vs. synchronous updating

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^{*} Read these papers and associated exchanges for some cautionary tales: van de Rijt, Arnout, David Siegel, and Michael Macy. 2009. "Neighborhood Chance and Neighborhood Change: A Comment on Bruch and Mare." American Journal of Sociology 114(4):1166–80 & Goldberg, Amir. 2021. "Reply to DellaPosta and Davoodi: Associative Diffusion and the Pitfalls of Structural Reductionism." American Sociological Review 1–6.

Recap

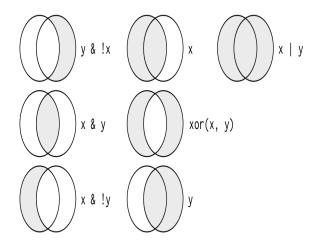
Data structures in R

- ► Basic data types
- Vectors
- Lists
- Matrices

Programming fundamentals

- Boolean logic
- ► If-else statements
- Loops
- Functions
- Pipes

Boolean logic in R



Boolean logic

```
TRUE == TRUE # equals
## [1] TRUE
TRUE != FALSE # not equals
## [1] TRUE
TRUE == !FALSE
## [1] TRUE
!TRUE != FALSE
## [1] FALSE
```

Boolean logic

```
TRUE | FALSE # or

## [1] TRUE

TRUE & FALSE # and

## [1] FALSE

TRUE & FALSE == FALSE

## [1] TRUE
```

Boolean logic

See the documentation for more on logic in R.

```
TRUE | FALSE & FALSE

## [1] TRUE

FALSE | TRUE & FALSE

## [1] FALSE
```

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- ▶ We often encounter situations where we want to make a choice contingent upon the value of some information received.
- ► If-else statements allow us to chain together one or more conditional actions.
 - e.g. If time is between 10:20-11:40am AND day is Monday or Thursday, attend Computational Data Science lecture. Else, do something else.

The basic syntax. The if is followed by a conditional statement in parentheses. If the condition is met, then the code in the braces is executed.

```
x <- TRUE
if (x == TRUE) {
   print("x is true")
```

[1] "x is true"

In this case we have a vector containing five fruits. We use sample to randomly pick one. We can use an if-statement to determine whether we have selected an apple. Complete the conditional.

In the previous example we only have an if-statement. If the condition is not met then nothing happens. Here we add an else statement.

```
fruits <- c("apple", "apple", "orange", "orange", "apple")

f <- sample(fruits, 1)

if (f == "apple") {
    print("We selected an apple")
} else {
    print("We selected an orange")
}</pre>
```

[1] "We selected an orange"

Note that R can be quite fussy about the syntax. If else is on the line below then the function throws an error.

What about this case where we have another fruit? If we only care about apples we could modify the output of our else condition.

```
fruits <- c("apple", "apple", "orange", "orange", "apple", "pineapple")

f <- sample(fruits, 1)

if (f == "apple") {
    print("We selected an apple")
} else {
    print("We selected another fruit.")
}</pre>
```

[1] "We selected another fruit."

We could also use else-if statements to have a separate consideration of all three.

```
f <- sample(fruits, 1)

if (f == "apple") {
    print("We selected an apple")
} else if (f == "orange") {
    print("We selected an orange")
} else {
    print("We selected a pineapple")
}</pre>
```

[1] "We selected an apple"

Loops

- Often when we program we need to complete the same operation many times. One of the common approaches is to use a loop.
- ► There are two kinds of loops you will encounter
 - For-loops
 - lterative over an entire sequence
 - While-loops
 - Iterate over a sequence while a condition is met

Here is a simple example where we use a loop to calculate the sum of a sequence of values.

```
s <- 0  # value to store our sum

for (i in 1:100) {
     # for i from 1 to 100
     s <- s + i  # add i to sum
}

print(s)</pre>
```

[1] 5050

```
s = 0
for i in range(1,101):
    s += i
print(s)
```

5050

The syntax varies slightly across programming languages but the basic structure is very similar, as this Python example shows. Note that for-loops and other functions in R tend to use braces around the operations. We will see this again when we look at functions.

Write a loop to print each number.

nums <- 1:10

```
is_orange <- logical(length(fruits)) # a vector of logical objects</pre>
i = 1 # In this case we need to maintain a counter
for (f in fruits) {
    if (f == "orange") {
        is_orange[i] <- TRUE</pre>
    i <- i + 1 # increment counter by 1
}
print(fruits)
## [1] "apple" "apple"
                               "orange"
                                           "orange"
                                                       "apple"
                                                                    "pin
print(is_orange)
```

[1] FALSE FALSE TRUE TRUE FALSE FALSE

Loops can also easily be *nested*. Here we start a second loop within the first one and use it to populate a matrix.

```
M <- matrix(nrow = 5, ncol = 5)

for (i in 1:5) {
    for (j in 1:5) {
        M[i, j] <- i * j
    }
}
print(M)</pre>
```

```
## [,1] [,2] [,3] [,4] [,5]

## [1,] 1 2 3 4 5

## [2,] 2 4 6 8 10

## [3,] 3 6 9 12 15

## [4,] 4 8 12 16 20

## [5,] 5 10 15 20 25
```

While-loops

A while loop runs when a condition is true and ends when it becomes false. Make sure the condition will eventually be false to avoid an infinite loop.

```
i <- 1  # iterator
while (i < 5) {
    print(i)
    i <- i + 1
}</pre>
## [1] 1
```

[1] 1 ## [1] 2

[1] 3

[1] 4

While-loops

In this example we iterate over fruits until we get a pineapple.

```
i <- 1 # iterator
f <- fruits[i] # define initial value</pre>
while (f != "pineapple") {
    print(f)
    i <- i + 1 # increment index
    f <- fruits[i] # get next f</pre>
## [1] "apple"
## [1] "apple"
## [1] "orange"
## [1] "orange"
## [1] "apple"
```

- ▶ A function is a customized sequence of operations
- ▶ We use functions to make our code modular and extendable
- ▶ There are thousands of functions built into R and available for packages, but sometimes it is useful to create our own
 - ► *R4DS* contains the following heuristic:
 - "You should consider writing a function whenever you've copied and pasted a block of code more than twice"

Here is an example of a simple function that returns the mean of a vector of values x.

```
avg <- function(x) {
    return(sum(x)/length(x))
}
avg(c(5, 6, 6, 4, 3))</pre>
```

```
## [1] 4.8
```

We define the function by using the function command and assigning it to the name avg. The content in the parentheses is called the argument of the function. The return statement tells the function what output to produce.

Here is the same function in Python.

```
def avg(x):
    return(sum(x)/len(x))
avg([5,6,6,4,3])
```

4.8

Again you can see that the syntax is slightly different, for example the def command is used to define a function on the left hand side, followed by the name.

Testing

- It is important to test functions to ensure they work as expected
 - Ensure the function will only process valid inputs
 - It is good practice to handle incorrect inputs
 - ► There are many ways a function could behave that would not raise errors in R but could still be problematic
 - Write unit tests to ensure the function works as expected
 - Make sure to handle edge cases, inputs that require special handling

Testing

```
avg(c("a", "b", "c"))
## Error in sum(x): invalid 'type' (character) of argument
```

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Testing

avg(c())

[1] NaN

Testing

The function can be modified to return a message if input is incorrect. Note the use of two return statements within the function.

```
avg <- function(values) {
   if (!is.numeric(values)) {
      return("Input must be numeric.")
   } else {
      return(sum(values)/length(values))
   }
}</pre>
```

Testing

```
# Unit tests
avg(c("a", "b", "c"))
## [1] "Input must be numeric."
avg(c())
## [1] "Input must be numeric."
avg(c(2.6, 2.4))
## [1] 2.5
```

- Pipes are a tool designed to allow you to chain together a sequence of operations
- ► The pipe is designed to improve the readability of complex chains of function
- Implemented in the magrittr package but loaded in tidyverse

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Pipes can be used to chain together sequences of operations. There are two different versions of the syntax:

```
library(tidyverse)
x <- 10

x %>%
    print() # Old style

## [1] 10

x |>
    print() # New style

## [1] 10
```

Note how pipes allow us to chain operations from left to right, rather than nesting them from inner to outer. In this case we take a sequence from 1 to 10, get the square root of each value, sum the roots, then print the sum.

```
print(sum(sqrt(seq(1:10)))) # nested functions

## [1] 22.46828

seq(1:10) %>%
    sqrt() %>%
    sum() %>%
    print() # using pipes

## [1] 22.46828
```

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We can also use pipes to do basic arithmetic using pipes. Note again the difference between the nested operations and the pipe operator.

```
library(magrittr)
((1 + 2) - 10) * 10

## [1] -70

1 %>%
   add(2) %>%
   subtract(10) %>%
   multiply_by(10)
## [1] -70
```

```
## [1] -70
```

Note how magrittr provides aliases for certain mathematical operations as shown in the second line. This

StackOverflow post has some further discussion.

Pipes are particularly useful we're working with tabular data. Here's an example without pipes or nesting. Each line produces an object that is then passed as input to the following line.

```
library(nycflights13)
not_delayed <- filter(flights, !is.na(dep_delay), !is.na(arr_delay))</pre>
grouped <- group_by(not_delayed, year, month, day)</pre>
summary <- summarize(grouped, mean = mean(dep_delay))</pre>
print(summary)
## # A tibble: 365 x 4
## # Groups: year, month [12]
## year month day mean
## <int> <int> <int> <dbl>
## 1 2013 1 1 11.4
   2 2013 1 2 13.7
##
   3 2013 1 3 10.9
```

In this case the expressions have been nested. This is better as we are not unnecessarily storing intermediate objects.

```
summarize(group_by(
 filter(flights, !is.na(dep_delay), !is.na(arr_delay)),
 year, month, day), mean = mean(dep_delay))
## # A tibble: 365 \times 4
## # Groups: year, month [12]
##
      year month
                  day
                       mean
##
     <int> <int> <int> <dbl>
##
   1
      2013
                    1 11.4
##
   2 2013 1 2 13.7
   3 2013 1 3 10.9
##
##
   4 2013
                 4 8.97
                 5 5.73
##
   5 2013
   6 2013
                 6 7.15
##
      2013
                    7 5.42
##
   7
      2013
                    8 2.56
```

Write out this expression using a pipe

Putting it all together: Schelling's segregation model in R

▶ Open the file schelling.R, located inside the code directory

Homework

- Visit the link on Slack for link to Github Classroom
- Clone to your computer (see instructions on website)
- ► Homework due 2/9 (next Friday) at 5pm
- Submit via Github (see instructions on website)

Next week

- ► Application Programming Interfaces for data collection
 - ► Sign up for a Spotify account
- ► Tabular data and visualization