

## Practice Assignment 6

Problem 1) variables: the following variables will represent the necessary transports

$x_1$  = # of shnupells Mexico  $\rightarrow$  New York

$x_2$  = # of shnupells Mexico  $\rightarrow$  California

$x_3$  = # of shnupells Kansas  $\rightarrow$  New York

$x_4$  = # of shnupells Kansas  $\rightarrow$  New York

objective:  $\min 4x_1 + x_2 + 2x_3 + 3x_4$

s.t.  $x_1 + x_2 \leq 8$  (Mexico production)

$x_3 + x_4 \leq 15$  (Kansas production)

$x_1 + x_3 \leq 10$  (New York consumption)

$x_2 + x_4 \leq 13$  (California consumption)

$x_1, x_2, x_3, x_4 \geq 0$

Problem 2)  $n$  actors, actor  $i$  charges  $s_i$  dollars

$m$  investors, investor  $j$  will invest  $p_j$  dollars if certain actors chosen

variables:  $x_i$  is some actor

$y_j$  is some investor

objective:  $\max \sum_i y_i \cdot p_i - \sum_j x_j \cdot s_j$

s.t.  $x_i \geq y_j$  for all  $i$  part of  $L_j$

$0 \leq x_i \leq 1$  for all  $i$

$0 \leq y_j \leq 1$  for all  $j$

This makes it so that if we pick an investor  $y_j$ , we must select all of his actors  $x_i$ . The profit is found after subtracting the actors salaries.



- Problem 3) @ i. false, because  $X$  is not in polynomial time  
ii. true, because  $X$  reduces from an NP complete problem in polynomial time  
⑥ i. true, because  $Y$  reduced from an NP complete problem and is at least as hard as  $X$   
⑦ i. yes, because they can both reduce into each other by the definition of being NP complete.

Problem 4) If a problem can be solved in polynomial time, then it can also be proven in polynomial time. Since it took at least quadratic time to traverse the table, finding the max out of those must have taken up to polynomial time since it is NP. Proving it will take no longer than solving it, therefore  $P = NP$ . This is because in order to prove it, you must prove that there is no better optimal solution.