## MASSACHUSETTS INSTITUTE OF TECHNOLOGY

Department of Electrical Engineering

## 6.301 Solid State Circuits

Fall Term 2012 Issued : Nov. 16, 2012 Problem Set 9 Due : Friday, Dec. 7, 2012

Suggested Reading: Read as many of the following as you can. All of the recommended references are on reserve at Barker Library.

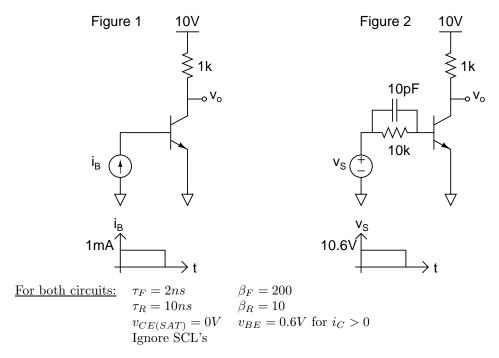
- 1. Lundberg sections 40-44.
- 2. Gray and Searle (in library) chapters 21 and 22.

**Problem 1:** In this problem, a transistor is controlled by supplying a base current drive as seen in Figure 1. Analyze the dynamics of the transistor and sketch  $q_F$ ,  $q_S$ ,  $i_C$  and  $i_B$  versus time. Each sketch should clearly indicate important slopes, final values, time constants, etc. Read this whole problem before starting to solve the first part.

- 1. Assume that the transistor remains in the forward active region. Determine the time constants and final values etc, and sketch the curves.
- 2. Since  $\beta_F i_B > i_{C(SAT)}$ , the device will not remain in the forward active region for all time. Indicate on your graphs the point at which saturation occurs. Find  $q_{BO}$ , the final values (in saturation) for  $i_C$  and  $q_S$  and evaluate the time constant  $\tau_S$ . Continue the sketches. How long does it take to transverse the active region?
- 3. Now consider turning off the device,  $i_B = 0$ . Assume that the transistor remains saturated, that is  $i_C = i_{C(SAT)}$  for all time. Determine the final values for  $q_S$  and sketch the curves.
- 4. Obviously, the transistor does not remain saturated but enters the forward active region when  $q_S$  equals zero. Determine the storage delay time, that is, the time during which the device remains saturated even though  $i_B = 0$ . Determine the time spent crossing the active region. Sketch the curves.
- 5. Compare turn-on times and turn-off times; explain the difference.
- 6. It is observed that the storage delay time decreases if the input pulse duration is reduced. Explain.

## **Problem 2:** Charge Control

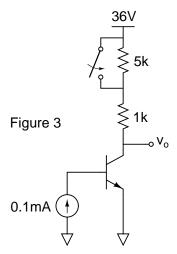
- 1. Sketch  $q_F$ ,  $q_S$ ,  $i_C$  and  $i_B$  versus time for the circuit shown in Figure 2.
- 2. Now assume that you are free to choose the capacitor value. what value should be chosen so that final conditions for both the turn on and the turn off transient are established as quickly as possible?



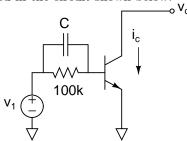
## **Problem 3:** Charge Control

- 1. Initially, the circuit shown in Figure 3 is assumed to be in equilibrium with the switch open. Calculate:  $q_F$ ,  $q_S$ ,  $i_C$ .
- 2. At t=0, the switch is closed, assume instantaneous slosh. Also assume that, after the slosh transition, the circuit is quasistatic. Sketch and dimension graphs of  $q_F(t)$ ,  $q_S(t)$  and  $i_C(t)$ . Be sure to indicate relevant slopes, initial and final values, time constants, etc. Approximately sketch the distribution of charge in the base. Clearly illustrate the slosh transition and the equilibrium distribution.

$$\begin{array}{ll} \underline{\text{Assume:}} & \tau_{BF} = 100ns & \beta_F = 100 \\ & \tau_{BR} = 10ns & \beta_R = 5 \\ & v_{CE(SAT)} = 0V \\ & \text{Ignore SCL's} \end{array}$$



**Problem 4:** A transistor is connected in the circuit shown below.



The voltage  $v_1$  has made a 0 to 10.6V step. The approximate collector current waveform that results is  $i_C(t) = 1mA + 2mA(1 - e^{-t/100ns}), t > 0$ . Determine the parameters  $\tau_F$ ,  $\tau_{BF}$ , and  $\beta$  for the transistor. Also find the value of capacitor C. You may assume that  $v_{BE} = 0.6V$  for any significant value of  $i_C$ .

**Problem 5:** The circuit shown below is driven by a voltage source,  $v_s(t)$ . You may assume that  $v_{BE} = 0.6V$  for any  $I_C$ , when the transistor is in the forward active region. All space charge layer capacitances are zero.

- 1. Assume that C = 0. Sketch and dimension  $v_o(t)$  and  $q_B(t)$ . Note that  $q_b(t)$  is the excess minority charge in the base.
- 2. If C = 1pF, sketch and dimension  $v_o(t)$  and  $q_B(t)$ . You may assume that the quasistatic approximation is valid.
- 3. Suppose that when you assembled the circuit, you inadvertently inserted the transistor upside down. The emitter and collector leads are now reversed. Recalculate parts 1 and 2 for  $v_o(t)$  and  $q_R(t)$ .

 $\begin{array}{ll} \underline{\text{Assume:}} & \tau_F = 1ns & \beta_F = 100 \\ & \tau_R = 20ns & \beta_R = 5 \end{array}$ 

