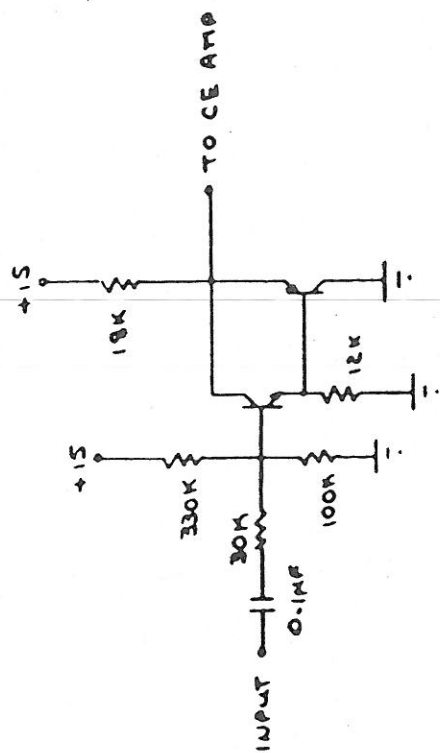


WILLIS ALE 203904
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ALTERNATE FOLLOWER

LAB 2

4/15

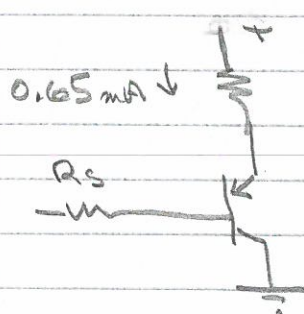
Discussion of my lab 2.

What do the specs imply for the design?

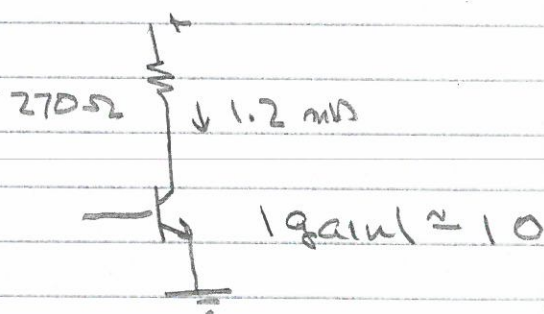
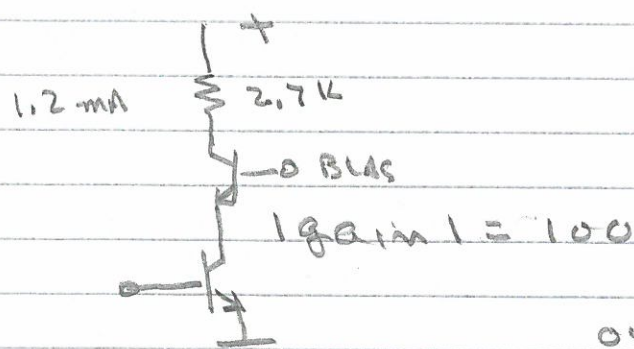
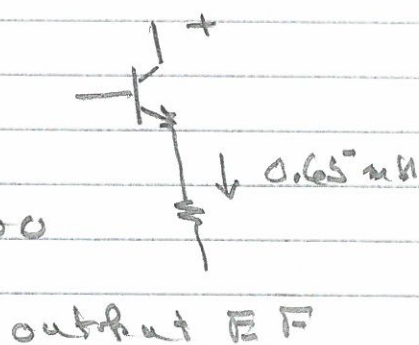
Because of the high source resistance, we need at least a simple emitter follower at the input. The circuit also requires a follower at the output, since the 10 pF capacitor would probably contribute an unacceptable open-circuit time constant otherwise.

The low power requirement is complicated by having only 15-volt supplies available, which are far in excess of what is required for a 2-V peak-to-peak output swing.

I used two voltage gain stages - a CE amp followed by a cascode. My stages are (Describe topology).



Input EF

1st gain stage2nd gain stage

Output EF

The circuit has 4 nodes that have important impact on the bandwidth. One is the input to the first emitter follower. The time constant is $\sim (R_s + r_\pi) C_\pi$. The next is at the input to the 1st voltage gain stage.

$$\left[r_\pi + \frac{(R_s + r_\pi + r_\pi)}{\beta + 1} \right] C_{\pi 1}$$

Input to 2nd voltage gain stage. This is $(R_{L1} + r_\pi) C_{\pi 2}$

Output node of 2nd gain stage $R_{L2} \times 2 C_\mu$.

There are a number of other contributions to ΣOCT , but they are not very important. Examples include those associated with C_π of the two emitter followers, and of the cascode. These are $\sim \frac{1}{\omega_c}$.

We can reduce the sum of the open-circuit time constants by trading off the gains in the two stages subject to the constraint that

$$g_m R_{L1} g_m R_{L2} \sim 1000, \text{ or } R_{L1} \times R_{L2} = 7.5 \times 10^5$$

$$R_{L1} \sim \frac{1000}{g_m^2 R_{L2}}$$

To minimize these contributions to ΣOCT , we want to get all of the parts of the sum that involve R_{L1} and R_{L2} .

For example, one term that includes R_{L1} is

$$(R_i + R_{L1} + g_{m1} R_{L1} R_{L2}) C_{\mu 1}$$

↑

input to 1st gain stage

Term involving $C_{\pi 2}$ is $(R_{L1} + r_{\pi 2}) C_{\pi 2}$.

Another term is

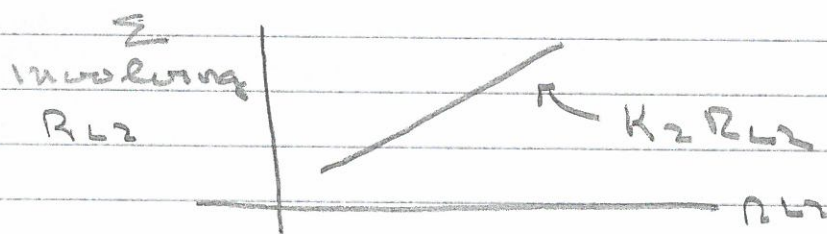
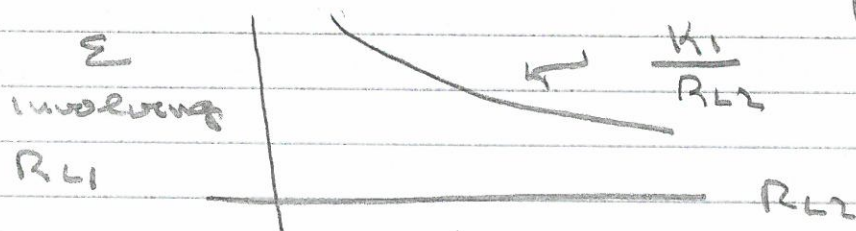
$$\left[R_{L1} + r_{\pi 2} + \left(g_m \times \frac{1}{g_m} \right) (R_{L1} + r_{\pi 2}) + \frac{1}{g_m} \right] C_{\pi 2}$$

We can do the same thing with R_{L2} .

Here we get $2(R_{L2} + r_{\pi 2}) C_{\pi 2}$.

Since R_{L1} and R_{L2} must be reciprocally related to get the correct gain, we can plot

$$R_{L1} = \frac{7.5 \times 10^5}{R_{L2}}$$



Since these are of the form $\frac{K_1}{R_{L2}}$ and $K_2 R_{L2}$,

their contributions to the sum is

$$\frac{K_1}{R_{L2}} + K_2 R_{L2}$$

$$\frac{d}{dR_{L2}} = -\frac{K_1}{R_{L2}^2} + K_2 = 0, \quad R_{L2} = \sqrt{\frac{K_1}{K_2}}$$

This is the value of R_{L2} that makes the two contributions equal. This happens with $R_{L1} \approx 0.1 R_{L2}$ in my design, and with $R_{L1} = 270 \Omega$, $R_{L2} = 2.7 k\Omega$.

With this constraint, all 4 of the critical time constants have about the same value $\approx 10 ns$. This would predict

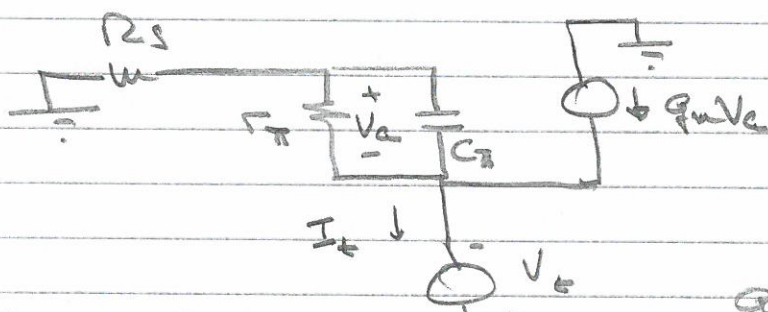
Recitations 4/6 & 4/8 - more circuit examples.

and $\omega_a \approx \frac{1}{40\text{ns}} = 25\text{Mr} \approx 4\text{MHz}$.

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We actually get $\sim 8\text{MHz}$. Most of the reason is the peaking associated with the OCT calculation when we have coincident poles. I showed earlier that with 4 coincident poles, the actual bandwidth is $\sim 1.7\times$ the prediction. There is also at least one pair of complex conjugate poles. Reason is probably that the output impedance of an emitter follower with a large source resistance looks inductive at some frequencies.

We can show this (sort of) as follows.



$$\frac{g_m}{C_{\pi}\omega} \gg 1, \Gamma_{\pi} C_{\pi} \omega \gg 1 \quad \text{or} \quad \frac{g_m}{C_{\pi}} \gg \omega \gg \frac{1}{\Gamma_{\pi} C_{\pi}} = \frac{g_m}{\beta C_{\pi}}$$

$$I_e = \frac{V_e}{R_s + \frac{\Gamma_{\pi}}{\Gamma_{\pi} C_{\pi} s + 1}} + \frac{g_m \frac{\Gamma_{\pi}}{\Gamma_{\pi} C_{\pi} s + 1}}{R_s + \frac{\Gamma_{\pi}}{\Gamma_{\pi} C_{\pi} s + 1}} V_e$$

$$\text{If } R_s \gg \Gamma_{\pi}, \Gamma_{\pi} C_{\pi} \omega \gg 1, \frac{g_m \Gamma_{\pi}}{\Gamma_{\pi} C_{\pi} \omega} = \frac{g_m}{C_{\pi} \omega} \gg 1$$

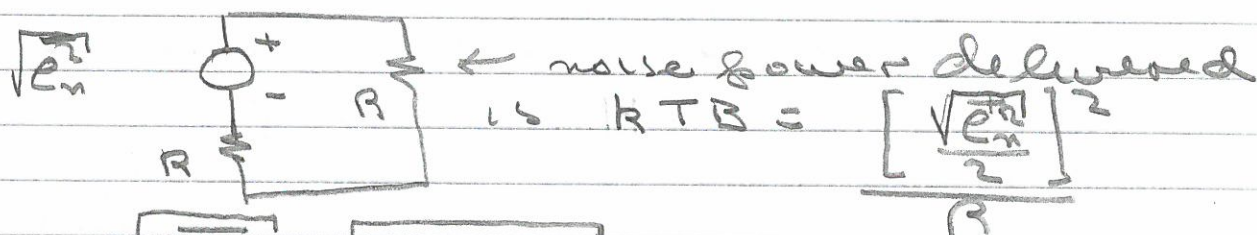
2nd condition is that we are past the β cutoff frequency, 3rd is below ω_t .

$$I_e \approx \frac{g_m}{R_s C_{\pi} s} V_e, \quad \frac{V_e}{I_e} = \frac{R_s C_{\pi} s}{g_m} \text{ (looks like an inductor)}$$

The numbers are reasonable for a transistor (2N3904) with $\beta = 200$, $f_T = 200 \text{ MHz}$.

Alternate with a higher source resistance, bootstrapped emitter follower.

Noise. A resistor has noise associated with it. A model is



or $\sqrt{e_n^2} = \sqrt{4kTB R}$, This is about $1 \text{ nV}/\sqrt{\text{Hz}}$

for 50Ω , we have $5 \text{ k} \Rightarrow 10 \text{ nV}/\sqrt{\text{Hz}}$

and $B = 9 \times 10^6$, $\sqrt{B} = 3 \times 10^3$, so we get 30 nV rms at the input, 30 nV rms at output.