

$$\begin{cases} x'(t) = x - xy^2 \\ y'(t) = x - y \end{cases}$$

$$\begin{cases} x - xy^2 = 0 \\ x - y = 0 \Rightarrow x = y \end{cases} \nearrow \begin{aligned} x - x^3 &= 0 \\ \Rightarrow x(1 - x^2) &= 0 \\ \Rightarrow x = 0 = y \\ \Rightarrow x = 1 = y \\ \Rightarrow x = -1 = y \end{aligned}$$

$(0,0), (1,1), (-1,-1)$ est de équilibre

$$J_f(x,y) = \begin{pmatrix} \frac{\partial f_1}{\partial x}(x,y) & \frac{\partial f_1}{\partial y}(x,y) \\ \frac{\partial f_2}{\partial x}(x,y) & \frac{\partial f_2}{\partial y}(x,y) \end{pmatrix}$$

$$\det(\lambda I_2 - J_f(x,y)) = 0 \Rightarrow \lambda_1, \lambda_2$$