# Digital Speech Processing Homework #1

Implementing Discrete Hidden Markov Model

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## Outline

- 1. HMM in Speech Recognition
- 2. Homework of HMM
  - 2.1 Training
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  - 3.1 File Format
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HMM in Speech Recognition

## Speech Recognition 1/2

In acoustic model,

- · each word consists of syllables
- · each syllable consists of phonemes
- each phoneme consists of some (hypothetical) states.

"青色" 
$$\rightarrow$$
 "青 (くーム) 色 (ムさ `)"  $\rightarrow$  "く"  $\rightarrow$   $\{s_1, s_2, \dots\}$ 

Each phoneme can be described by a HMM (acoustic model). Given a sequence of observation (MFCC vectors), each of them can be mapped to a corresponding state.

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## Speech Recognition 2/2

#### Hence, there are

- · state transition probabilities  $(a_{ij})$  and
- observation distribution  $(b_j[o_t])$

in each phoneme acoustic model (HMM).

Usually in speech recognition we restrict the HMM to be a *left-to-right model*, and the observation distribution is assumed to be a continuous Gaussian mixture model.

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#### Review

- Left-to-right
- The observation distribution is a continuous Gaussian mixture model

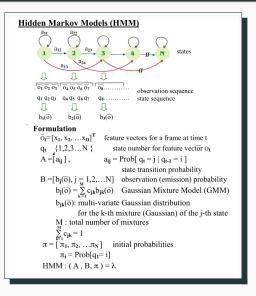


Figure 1: HMM from lecture 2.0

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#### General Discrete HMM

$$a_{ij} = P(q_{t+1} = j \mid q_t = i), \forall t, i, j$$
 (1)

$$b_j(A) = P(o_t = A \mid q_t = j), \forall t, A, j$$
 (2)

Given  $q_t$ , the probability distributions of  $q_{t+1}$  and  $o_t$  are completely determined. (independent of other states or observation)

## HW1 v.s. Speech Recognition

	Homework	Speech Recognition
$\lambda$ set	5 models	initial-final
$\lambda$	model_01-05	" < "
$\{o_t\}$	A, B, C, D, E, F	39-dim MFCC
unit	an alphabet	a time frame
observation	sequence	voice wave

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## Homework of HMM

## **Flowchart**

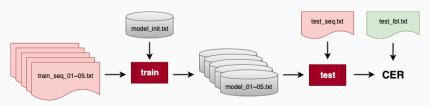


Figure 2: Training and testing models

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#### Problems of HMM

#### Training

- · Basic problem 3 in lecture 4.0
  - Given observations O and an initial model  $\lambda = (A, B, \pi)$ , adjust  $\lambda$  to maximize  $P(O \mid \lambda)$ .

$$A_{ij} = a_{ij}, B_{jt} = b_j[o_t], \pi_i = P(q_1 = i)$$

· Baum-Welch algorithm

### Testing

- · Basic problem 2 in lecture 4.0
  - Given  $\lambda$  and O, find the best state sequences to maximize  $P(O \mid \lambda, q)$ .

· Viterbi algorithm

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## Homework of HMM

Training

## **Training**

- · Basic problem 3
- Baum-Welch algorithm: A generalized expectation-maximization (EM) algorithm<sup>1</sup>
  - Calculate  $\alpha$  (forward probabilities) and  $\beta$  (backward probabilities) given the observations
  - Find temporary variables  $\epsilon$  and  $\gamma$  from  $\alpha$  and  $\beta$
  - Update model parameters  $\lambda' = (A', B', \pi')$

<sup>1</sup>http://en.wikipedia.org/wiki/Baum-Welch algorithm

### Forward Procedure

Forward algorithm: define a forward variable  $\alpha_t(i)$ 

$$\alpha_t(i) = P(o_1, o_2, \dots, o_t, q_t = i \mid \lambda)$$
 (3)

= Prob[ observing 
$$o_1, o_2, \ldots, o_t$$
, state  $i$  at time  $t \mid \lambda$ ] (4)

Initialization

$$\alpha_1(i) = \pi_i b_i(o_1), \ 1 \le i \le N$$
 (5)

Induction

$$\alpha_{t+1}(j) = \left[ \sum_{i=1}^{N} \alpha_{t}(i) a_{ij} \right] \cdot b_{j}(o_{t+1}),$$

$$1 \le t \le T - 1, \ 1 \le j \le N \quad (6$$

**Termination** 

$$P\left(\bar{O}\mid\lambda\right)=\sum_{i=1}^{N}\alpha_{T}(i)\tag{7}$$

#### **Backward Procedure**

Backward algorithm: define a backward variable  $\beta_t(i)$ 

$$\beta_t(i) = P(o_{t+1}, o_{t+2}, \dots, o_T \mid q_t = i, \lambda)$$
 (8)

= Prob[ observing 
$$o_{t+1}, o_{t+2}, \dots, o_T$$
 | state  $i$  at time  $t, \lambda$  ] (9)

Initialization

$$\beta_T(i) = 1, \ 1 \le i \le N \tag{10}$$

Induction

$$\beta_{t}(i) = \sum_{j=1}^{N} a_{ij} \ b_{j}(o_{t+1}) \ \beta_{t+1}(j),$$

$$t = \{T - 1, T - 2, \dots, 1\}, \ 1 \le i \le N \quad (11)$$

## Calculate Y

Define a temporary variable  $\gamma_t(i) = P(q_t = i \mid \bar{O}, \lambda)$ 

$$\gamma_t(i) = \frac{\alpha_t(i)\beta_t(i)}{\sum_{i=1}^N \alpha_t(i)\beta_t(i)} = \frac{P(\bar{O}, q_t = i \mid \lambda)}{P(\bar{O} \mid \lambda)}$$
(12)

It should be a  $N \times T$  matrix!

#### Calculate ε

The probability of transition from state *i* to state *j* given observation and model.

$$\epsilon_t(i,j) = P\left(q_t = i, q_{t+1} = j \mid \bar{O}, \lambda\right) \tag{13}$$

$$= \frac{\alpha_t(i) \ a_{ij} \ b_j(o_{t+1}) \ \beta_{t+1}(j)}{\sum_{i=1}^N \sum_{j=1}^N \alpha_t(i) \ a_{ij} \ b_j(o_{t+1}) \ \beta_{t+1}(j)}$$
(14)

$$=\frac{\operatorname{Prob}\left[\bar{O},\ q_{t}=i,\ q_{t+1}=j\mid\lambda\right]}{P\left(\bar{O}\mid\lambda\right)}\tag{15}$$

In total T-1 matrices (each  $N \times N$ )

## Accumulate $\epsilon$ and $\gamma$

Recall 
$$\gamma_t(i) = P(q_t = i \mid \bar{O}, \lambda)$$

$$\sum_{t=1}^{T-1} \gamma_t(i) = \text{expected number of times that state } i$$
 is visited in  $\bar{O}$  from  $t=1$  to  $t=T-1$  (16) 
$$\sum_{t=1}^{T-1} \epsilon_t(i,j) = \text{expected number of transitions from}$$
 state  $i$  to state  $j$  in  $\bar{O}$  (17)

## Re-estimate Model Parameters

$$\lambda' = (A', B', \pi') \tag{18}$$

$$\pi_i = \frac{\sum \gamma_1(i)}{N}$$
, where N is number of samples (19)

$$a_{ij} = \frac{\sum \epsilon(i,j)}{\sum \gamma(i)} = \frac{\mathbb{E}\left[\text{ Number of transition from } i \text{ to } j\right]}{\mathbb{E}\left[\text{ Number of visiting state } i\right]}$$
(20)

$$b_i(k) = \frac{\sum_{O=k} \gamma(i)}{\sum \gamma(i)} = \frac{\mathbb{E} \left[ \text{ Number of observation } O = k \text{ in state } i \right]}{\mathbb{E} \left[ \text{ Number of visiting state } i \right]}$$
(21)

Accumulate  $\epsilon$  and  $\gamma$  through all samples!!! Not just the observations in one sample!

## Homework of HMM

Testing

## **Testing**

- · Basic problem 2
  - Given  $\lambda$  and O, find the best state sequences to maximize  $P(O \mid \lambda, q)$ .
- Calculate  $P(O \mid \lambda) \approx \max P(O \mid \lambda, q)$  for each of the five models
- The model with the highest probability for the most probable path usually also has the highest probability for all possible paths.

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## Viterbi Algorithm

Complete procedure for Viterbi algorithm<sup>2</sup>

#### Initialization

$$\delta_1(i) = \pi_i b_i(o_1), \ 1 \le i \le N$$
 (22)

Recursion

$$\delta_{t}(j) = \max_{1 \le i \le N} [\delta_{t-1}(i) \ a_{ij} \ ] \cdot b_{j}(o_{t}), \ 2 \le t \le T, \ 1 \le j \le N$$
(23)

**Termination** 

$$P^* = \max_{1 < i < N} [\delta_T(i)]$$
 (24)

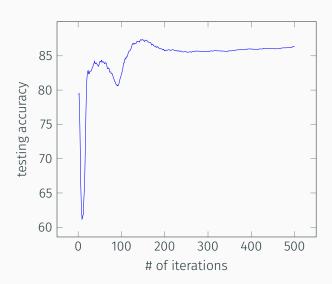
$$\delta_t(i) = \max_{q_1, \dots, q_{t-1}} P[q_1, q_2, \dots, q_{t-1}, q_t = i, o_1, o_2, \dots, o_t \mid \lambda]$$
 (25)

= the highest probability along a certain single path ending at state i at time t for the first t observations, given  $\lambda$  (26)

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<sup>2</sup>http://en.wikipedia.org/wiki/Viterbi\_algorithm

## Test Accuracy v.s. # of Training Iterations



## Requirements

#### **Provided Files**

#### data/train\_seq\_0X.txt

· Training data (10K observation sequences)

#### data/test lbl.txt

Testing labels

#### data/test\_seq.txt

· Testing data (2.5K observation sequences)

#### inc/hmm.h

- · Provided by TA, please work with it!
- · You can load/dump models with functions within.

#### model init.txt

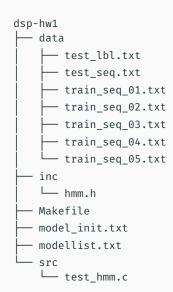
· Initial model parameters

#### modellist.txt

· Paths to model files

#### src/test hmm.c

· A showcase of the usage of hmm.h



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## Input and Output of Your Program

## Training

- **Input** 1. number of iterations
  - initial model (model\_init.txt)
  - 3. observation sequences
     (train\_seq\_01~05.txt)
- Output Five files of parameters for 5 models, each contains  $\lambda = (A, B, \pi)$  (e.g. model 01~05.txt)

## Testing

- - observation sequences (test\_seq.txt)
- **Output** best answer labels and  $P(O \mid \lambda)$  (e.g. result.txt)

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## **Training Details**

```
./train <iter> <model_init_path> <seq_path> <output_model_path>
```

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## **Testing Details**

```
./test <models_list_path> <seq_path> <output_result_path>
```

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## **Program Execution Example**

#### Compiling

```
make # type this in the root directory of the project
```

## Training

```
./train 100 model_init.txt data/train_seq_01.txt model_01.txt
```

### Testing

```
./test modellist.txt data/test seq.txt result.txt
```

#### Notice!

Command-line arguments are not fixed, read them during runtime. (e.g. Use argv in main function to pass the arguments.)

Also the paths in arguments need to be variable path.

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## Requirements

File Format

## **Observation Sequence Format**

The given data/train\_seq\_01~05.txt and data/test\_seq.txt look like this.

- 1 ACCDDDDFFCCCCBCFFFCCCCCEDADCCAEFCCCACDDFFCCDDFFCCD
- 2 CABACCAFCCFFCCCDFFCCCCDFFCDDDDFCDDCCFCCCEFFCCCCBC
- $_3$  ABACCCDDCCCDDDFBCCCCCDDAACFBCCBCCCCCCFFFCCCCCDBF
- 4 AAABBCCFFBDCDDFFACDCDFCDDFFFFCCCDCFFFFCCCCD
- 5 AACCDCCCCCCCCCCBFFFCDCDCDAFBCDCFFCCDCCCEACDBAFFF
- 6 ...

Each of the former has 10000 sequences and the latter has 2500 sequences.

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## Model Format 1/2

initial: 6

$$\pi = [ \pi_1, \ \pi_2, \ \pi_3, \ \pi_4, \ \pi_5, \ \pi_6 ]$$

transition: 6

$$A = \begin{bmatrix} a_{11} & \dots & a_{16} \\ \vdots & \ddots & \vdots \\ a_{61} & \dots & a_{66} \end{bmatrix}$$

observation: 63

$$B = \begin{bmatrix} b_1(o_1) & \dots & b_6(o_1) \\ \vdots & \ddots & \vdots \\ b_1(o_6) & \dots & b_6(o_6) \end{bmatrix}$$

Requirements | File Format

<sup>&</sup>lt;sup>3</sup>The sum of column is 1 here.

## Model Format 2/2

A model file (e.g. model\_0X.txt) should look like this.

```
initial: 6
   0.2
          0.1
                 0.2
                       0.2
                              0.2
                                     0.1
2
3
   transition: 6
4
   0.3
          0.3
                       0.1
                              0.1
                                     0.1
                0.1
5
   0.1
       0.3
                0.3
                       0.1
                                     0.1
                              0.1
   0.1
       0.1 0.3
                       0.3
                              0.1
                                     0.1
   0.1
       0.1 0.1
                    0.3 0.3
                                    0.1
   0.1
       0.1 0.1
                       0.1
                              0.3
                                    0.3
                       0.1
                              0.1
                                     0.3
   0.3
       0.1
                 0.1
10
11
   observation: 6
12
   0.2
          0.2
                 0.1
                       0.1
                              0.1
                                     0.1
13
   0.2
       0.2
                0.2
                       0.2
                              0.1
                                     0.1
14
   0.2
       0.2 0.2
                                     0.2
15
                       0.2
                              0.2
   0.2
       0.2 0.2
                    0.2
                              0.2
                                    0.2
16
   0.1
       0.1 0.2
                       0.2
                              0.2
                                     0.2
17
                              0.2
                                     0.2
18
   0.1
       0.1
                0.1
                       0.1
```

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#### **Model List Format**

The given modellist.txt looks like this.

```
model_01.txt
model_02.txt
model_03.txt
model_04.txt
model_05.txt
```

Your testing program should be able to read a list like this and load models from the specified paths for testing. (Don't worry! If you use hmm.h, all of these are done by calling function load\_models(). For more details please refer to hmm.h.)

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## **Output Format**

Your testing program should output these to the specific path (e.g. result.txt) given as a command-line argument while executing the program.

```
model_01.txt 7.822367e-34
model_05.txt 1.094896e-40
model_01.txt 7.928724e-33
model_02.txt 4.262100e-37
model_02.txt 5.914689e-42
...
```

Each line consists of the hypothesis model and its likelihood. They should be separated by a space.

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### Label File Format

The first few lines of the given data/test\_lbl.txt looks like this.

```
model_01.txt
model_05.txt
model_01.txt
model_02.txt
model_02.txt
...
```

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#### Makefile Format

The Makefile you submit should be capable to compile your program using make. The provided one can compile train.c and test.c in directory src into two executables train and test.

```
.PHONY: all clean run
    CC=gcc
    CFLAGS=-std=c99 -02
    LDFLAGS=-lm
    TARGET=train test
6
    all: $(TARGET)
7
8
    train: src/train.c
        $(CC) -o $0 $^ $(CFLAGS) $(LDFLAGS) -Iinc
10
    test: src/test.c
12
        $(CC) -o $0 $^ $(CFLAGS) $(LDFLAGS) -Iinc
13
14
    clean:
1.5
        rm -f $(TARGET)
16
```

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### Report Format

Please write a **one-page** report in **PDF** format, name it **report.pdf** and submit with your source code.

State your name, student ID and any challenges you encounter or attempts you try. A good report may grant you bonus of extra 5%.

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#### File Structure

#### All of your source code files must be placed under inc/ and src/.

Let's say you only have two implementation files and use the functions provided in hmm.h. You should put your source code under src/ and leave hmm.h in inc/.

```
inc
inc
hmm.h
lother *.h or *.hpp]
Makefile
model_init.txt
report.pdf
src
test.c
train.c
lother *.c, *.cc or *.cpp]
```

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# Requirements

Submission Requirement

# Submission Requirement 1/2

- 1. Create a directory named hw1\_[STUDENT\_ID].
- 2. Put
  - · inc/
  - · Makefile
  - model\_init.txt
  - · report.pdf
  - · src/

into the directory. 4

- Compress the directory into a ZIP file named hw1\_[STUDENT\_ID].zip.
- 4. Upload this ZIP file to CEIBA.

<sup>&</sup>lt;sup>4</sup>Put every source code files in inc/ and src/.

# Submission Requirement 2/2

Let's say your student ID is r01234567.

```
hw1_r01234567.zip

— hw1_r01234567

— inc

— [*.h or *.hpp]

— Makefile

— model_init.txt

— report.pdf
— src

— [*.c, *.cc or *.cpp]
```

# Grading

# **Grading Method**

Your training and testing program will be tested respectively. We will specify **100** as the number of iterations while testing your training program. And each of your program is allowed to run for 1 min.

Here's TA's environment.

Kernel Linux 5.3.1-arch1-1-ARCH <sup>5</sup>

Processors Intel Core i7-9700K (2 Cores)

**RAM** 4096 MB

GCC Version 9.1.0

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<sup>&</sup>lt;sup>5</sup>You can download the OVA file here if need be: https://ppt.cc/fl7drx. The user is root and its password is ntudsp

# **Grading Policy**

#### File Format 20%

- · ZIP file name
- · directory name
- separated header and implementation files
- · Makefile
- model\_init.txt

#### Program 20%

- compiled and executed without error
- · output files generated after execution

#### Report 10%

and bonus of extra 5% for the impressive ones

#### Accuracy 50%

30% for your training program and 20% for your testing program

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#### Late Submission

You are still allowed to submit after the due date. The penalty for late submission is an exponential decay with decay rate 1.5% of the maximum grade applicable for the assignment, for each hour that the assignment is late.

An assignment submitted more than 3 days after the deadline will have a grade of zero recorded for that assignment.

$$SCORE_{final}(hr) = \begin{cases} SCORE_{original} \times 0.985^{hr} &, hr \leq 72 \\ 0 &, hr > 72 \end{cases}$$

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<sup>&</sup>lt;sup>6</sup>less than 70% after 24 hrs, 48% for 48 hrs and 33% for 72 hrs

#### Please Note...

#### File Frmat

- · All of your source code files should be placed under inc/ and src/.
- model\_init.txt must be submitted, even if it's not needed for your program.

#### Program

- · Make sure your program can be compiled with the Makefile you submit.
- The paths in command-line arguments have to be relative path.
- Each of your program is allowed to run for 1 min.

#### Accuracy

· Make sure your training program saves models within time limit.

Should you have any questions, please read the FAQ<sup>7</sup> first.

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<sup>&</sup>lt;sup>7</sup>http://speech.ee.ntu.edu.tw/DSP2019Autumn/hw1/FAQ.html

#### DO NOT CHEAT

Any form of cheating, lying, or plagiarism will not be tolerated.

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#### **Contact TAs**

Should you have any question or need help,

- · send email to ntudsp\_2019fall\_ta@googlegroups.com
- and use "[HW1]" as the subject line prefix

Or come to EE2 R531, and don't forget to inform us by email, thanks!

林義聖	Tue.	14:00 - 17:00
	Thr.	9:00 - 12:00
林政豪	Mon.	10:00 - 12:00
	Thr.	15:00 - 18:00

Office hours

Contact TAs 39 / 39