

Weak lensing shear multipole analysis of galaxy clusters

Constantin Payerne

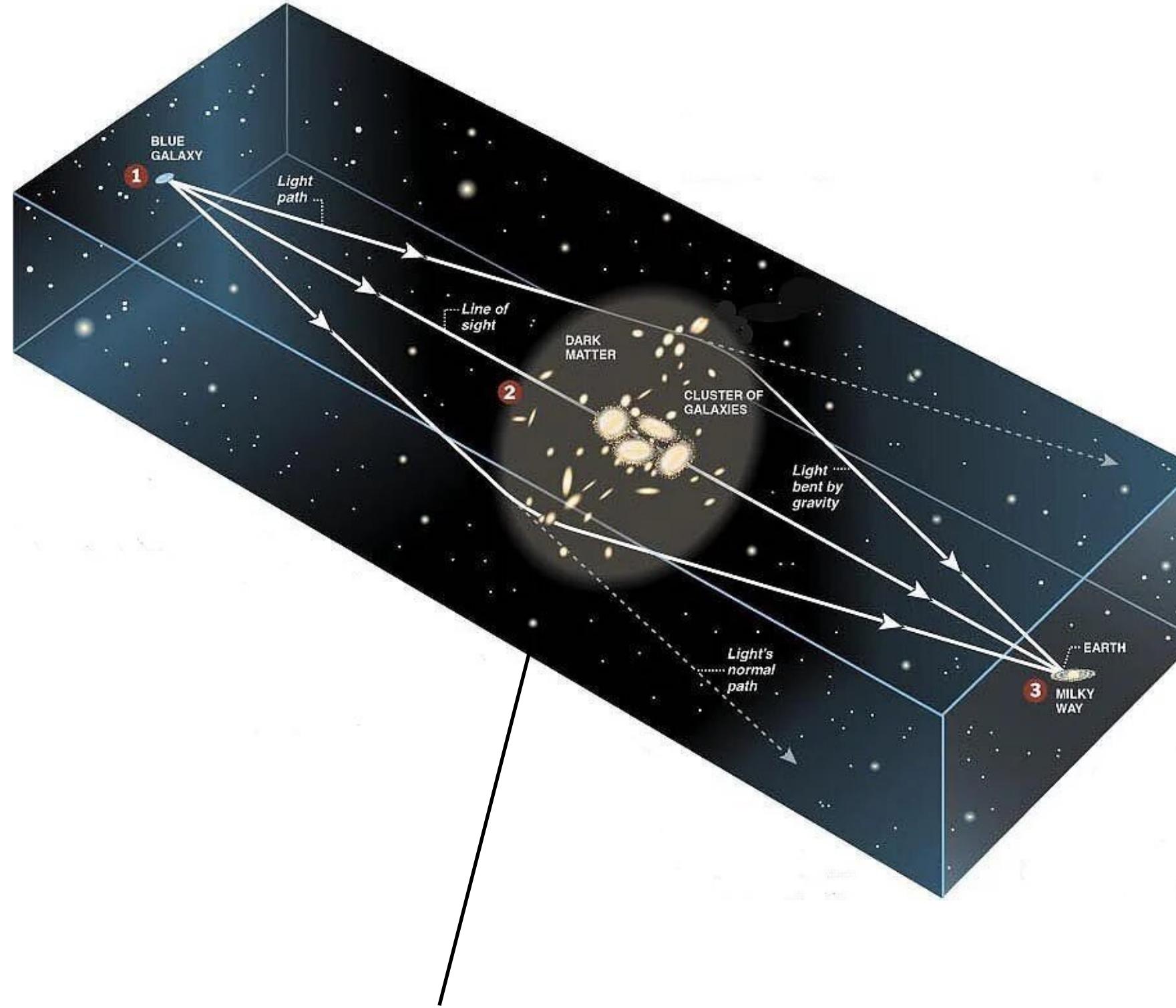
3rd year PhD student

Laboratoire de Physique Subatomique et Cosmologie, Grenoble

Supervisor: Céline Combet

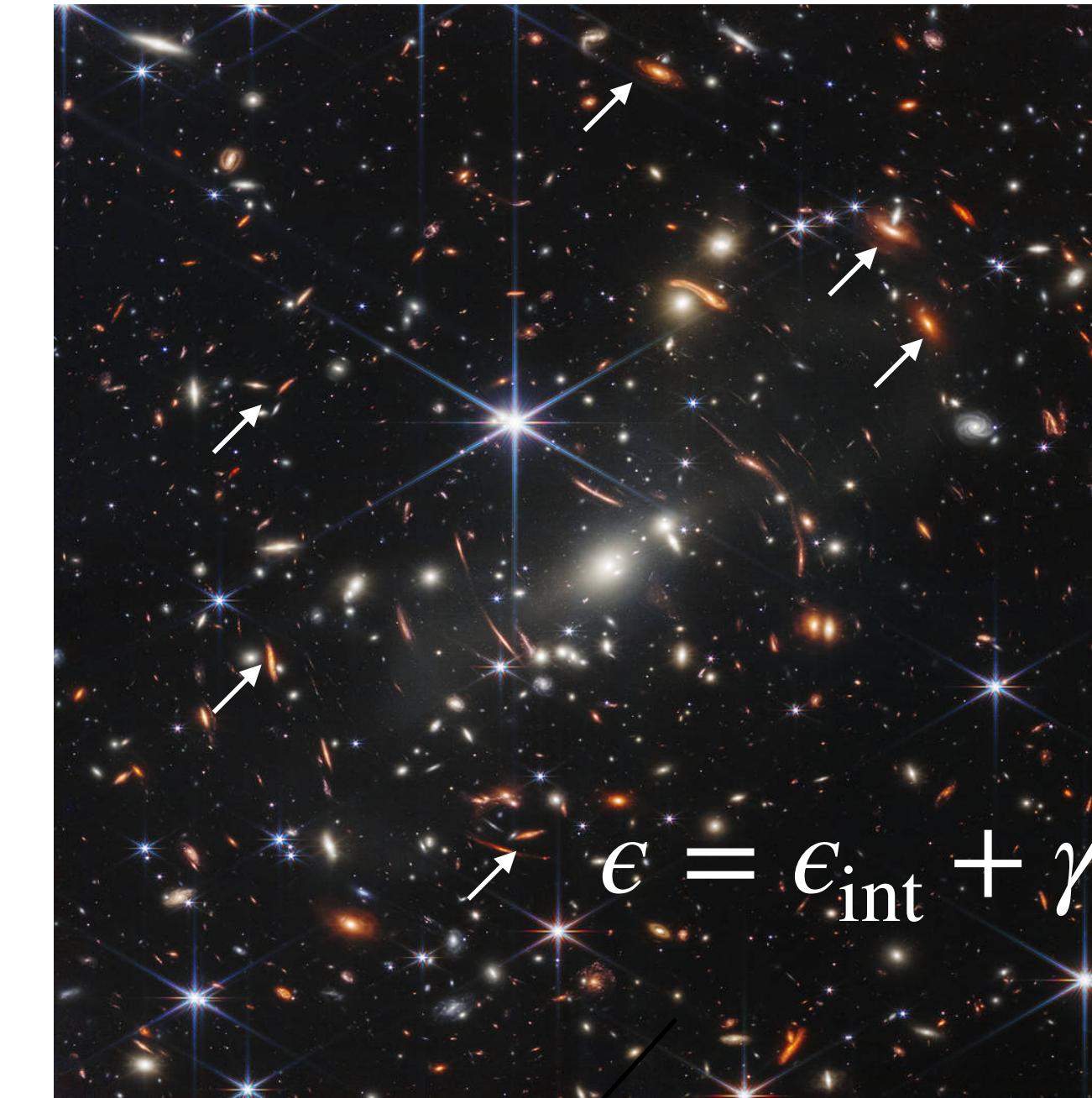


Weak gravitational lensing



Bending of light coming
from distant galaxies

Deformation of galaxy shapes



Inducing a coherent deformation of
observed galaxy shapes

Probe of the local shear field

$$\langle \epsilon \rangle = \langle \epsilon_{\text{int}} \rangle + \gamma$$
$$\approx 0$$

The shear can be deduced locally
by averaging galaxy shapes

Relies on accurate galaxy shape
measurement, see Manon Ramel's
talk

Shear analysis - In practice

Tangential/cross reference frame

$$\gamma_+ + i\gamma_\times = - \gamma e^{-2i\varphi}$$

- Can be fully described by its multipole moments

- Each moment $\gamma_{\pm/\times}^{(m)}$ can be estimated from background galaxies

Observable

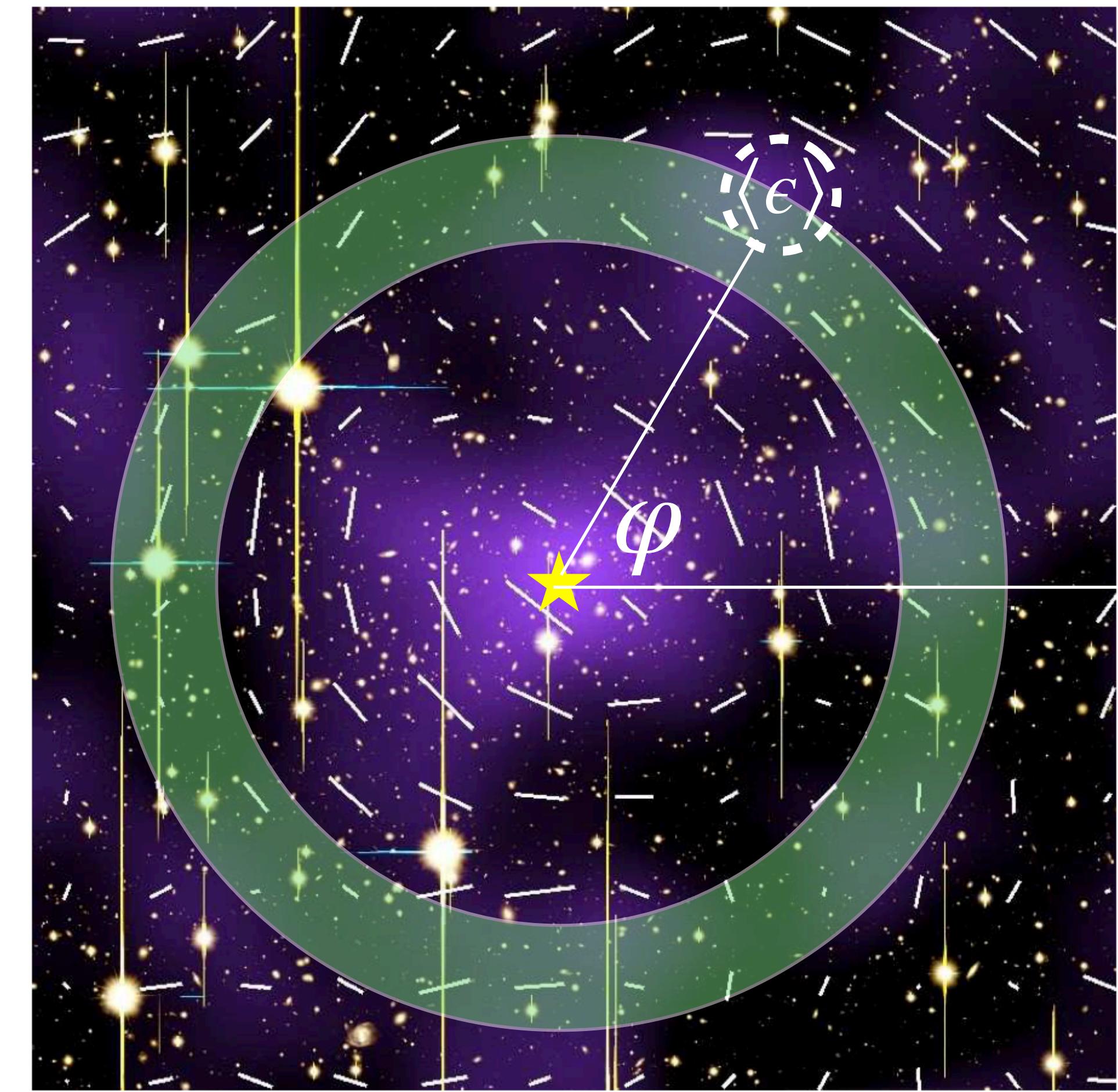
$$\gamma^{(m)} \propto \int_0^{2\pi} \gamma(R, \varphi) e^{-im\varphi} d\varphi$$

Prediction

Prediction

$\gamma_{+/\times}^{(m)}$ depends on $\kappa^{(m)}$

linked to cluster mass



Oguri et al. 2010, A2390

Standard WL mass reconstruction

- Assume the halo is spherical
 - $\kappa^{(m \neq 0)} = 0 \rightarrow \gamma^{(m \neq 0)} = 0$
- Only the monopole

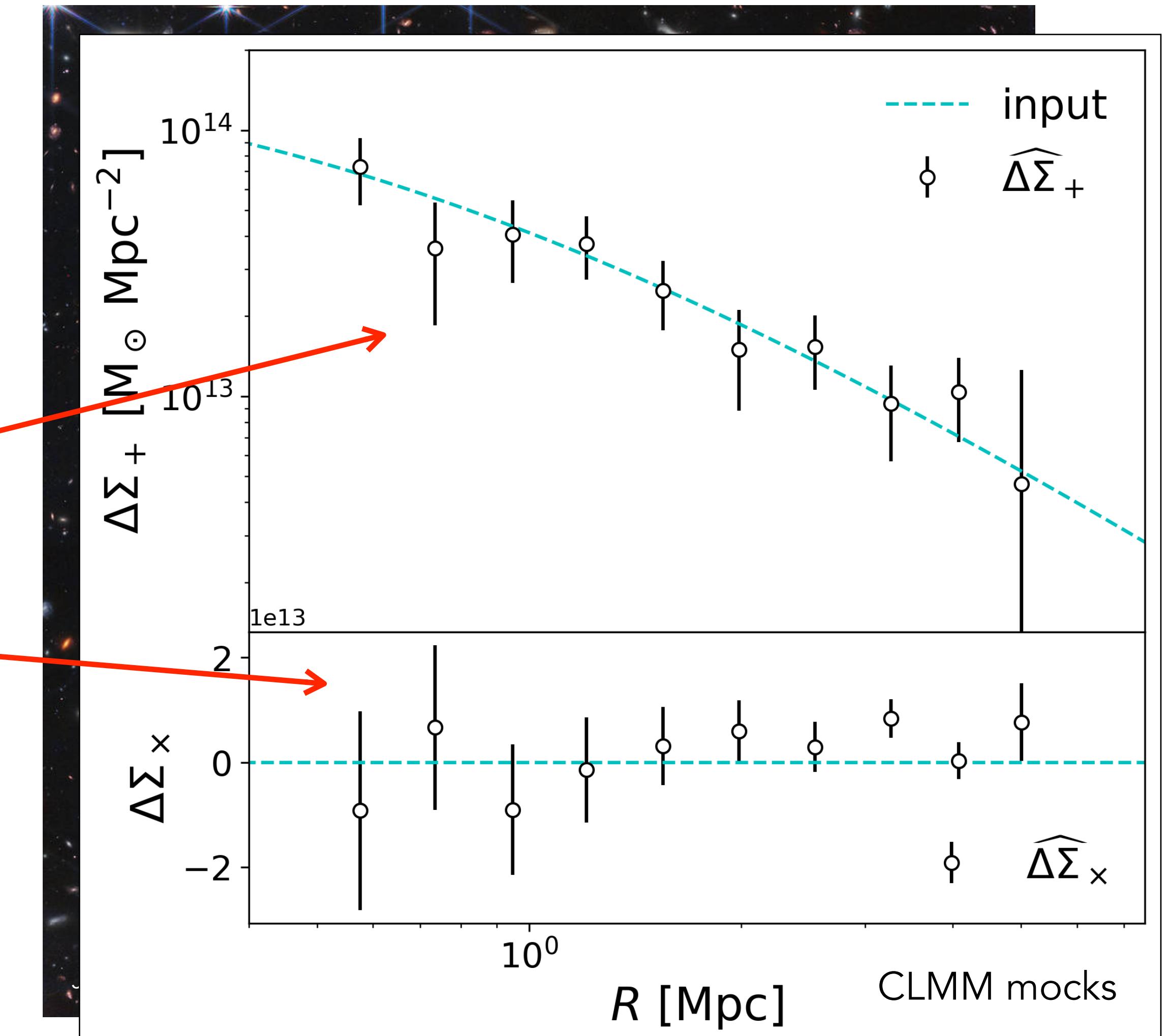
average tangential shear

$$\hat{\gamma}_+^{(0)} = \frac{1}{N} \sum_{s=1} \hat{\epsilon}_{+,s}$$

average cross shear = 0

$$\hat{\gamma}_x^{(0)} = \frac{1}{N} \sum_{s=1} \hat{\epsilon}_{x,s}$$

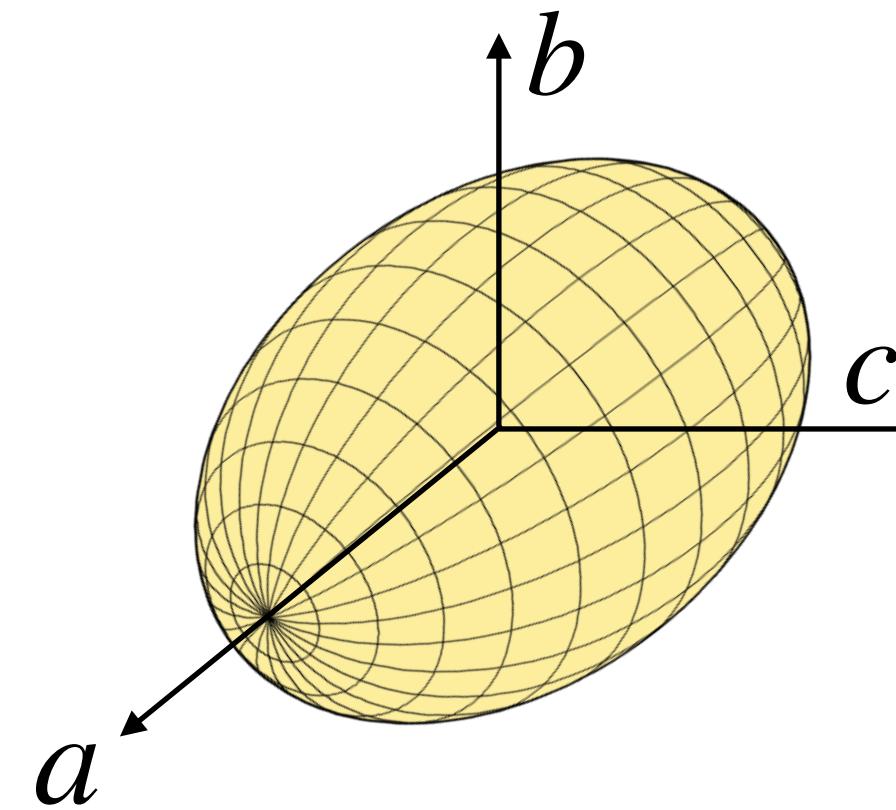
- Halo mass fitted on the average tangential shear profile
- Cross shear = used as a null test (systematic residual)



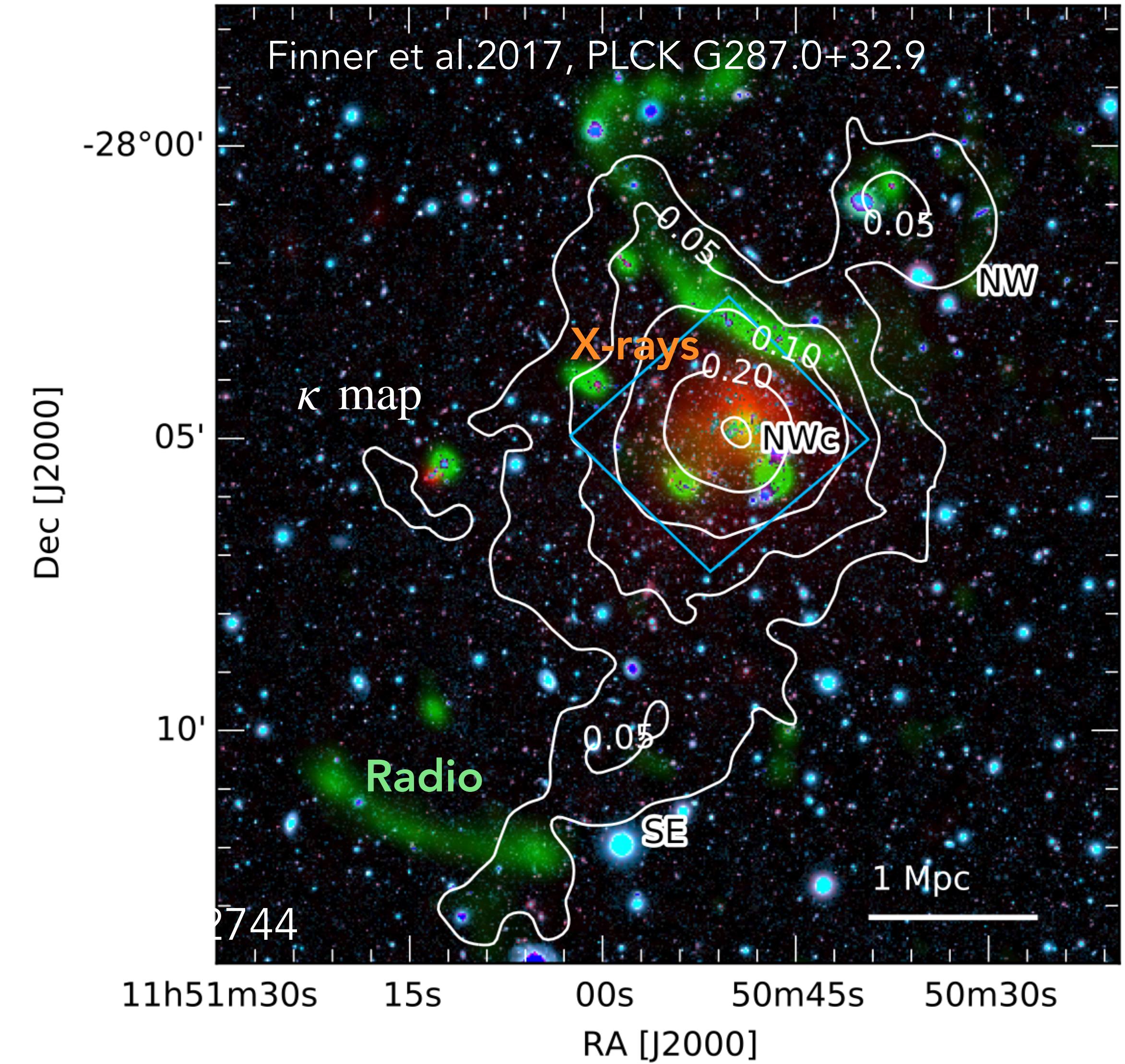
Lensing shear field around real clusters

Halos are not spherical (at all)

- Complex merging history, non-spherical initial over-densities, connected to neighbouring halos, etc.
- Multi-wavelength probes of the non-sphericity
- Simulations: Triaxial spheroids, halos are found to be prolate shaped ([Schneider et al, 2012](#))



$$b \sim c < a$$



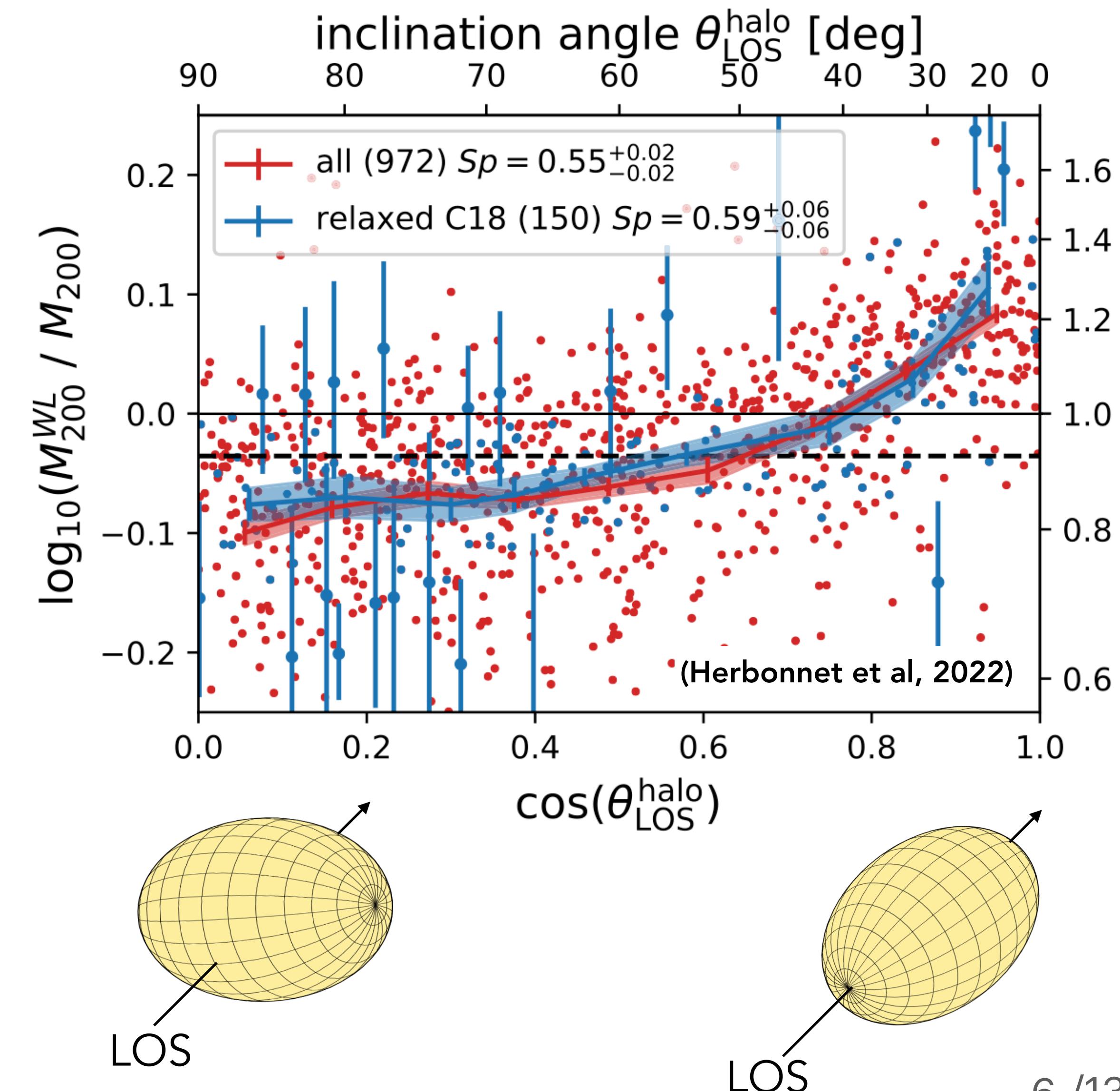
Standard WL mass reconstruction

Spherical halo modeling

- Assuming halos to be spherical may induce a bias
- Trend between WL mass and dark matter halo orientation
= strong effect of projection
- Triaxiality contributes to the scatter in WL mass

Concerns for cosmology

- Stat. power of future large surveys can be not fully exploited if the mass calibration is not accurate
- Issue for optically selected clusters (selection bias, [Wu et al, 2022](#))



Shear multipoles

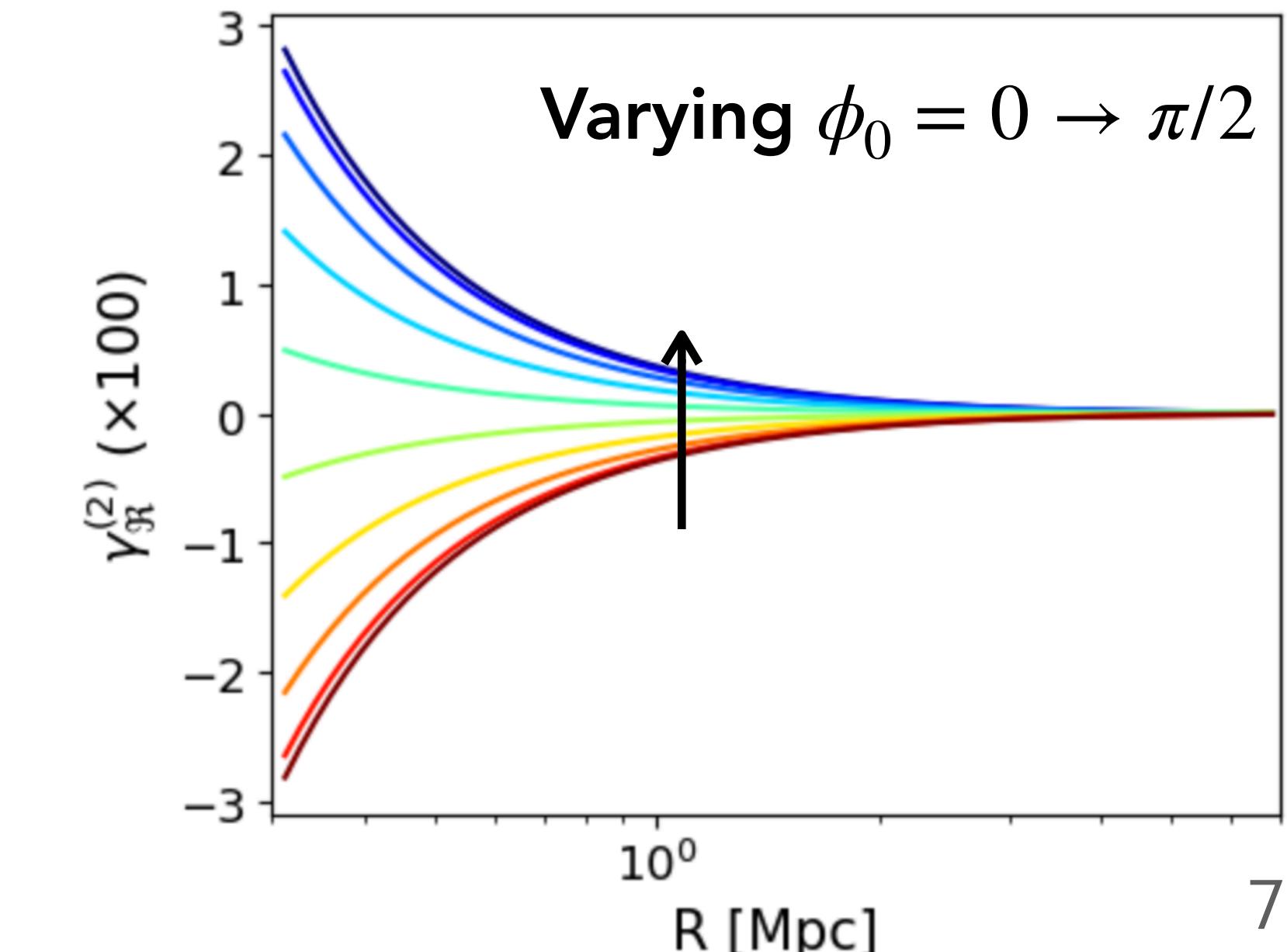
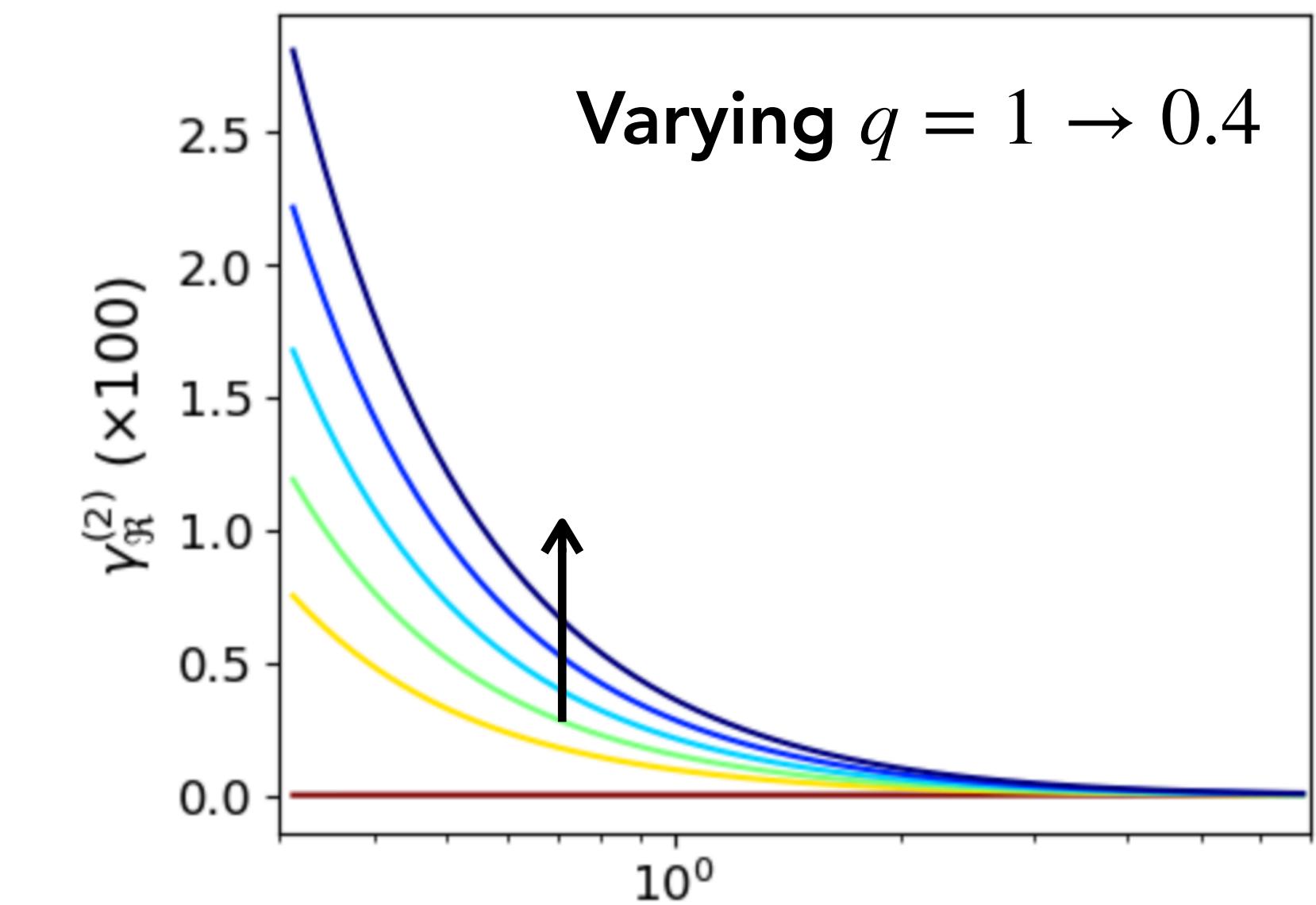
Beyond sphericity

$$\kappa = \kappa_{\text{sph}} \left(R \sqrt{\frac{\cos^2(\phi - \phi_0)}{q^2} + q^2 \sin^2(\phi - \phi_0)} \right) \rightarrow \kappa^{(m \neq 0)}(R) \neq 0$$
$$\rightarrow \gamma^{(m \neq 0)}(R) \neq 0$$

- Shear multipole moments sensitive to halo shape (Adhikari, 2014)
- Use them to probe projected halo ellipticity + orientation
- Does it improve the lensing mass calibration ?

Shear multipole analyses

- Stacked analyses
 - Gonzalez et al. (2020), Shin et al. (2017), Van Uitert et al. (2017)
 - Stack on preferred axis (e.g. BCG, member galaxies)
 - Lower in amplitude, low SNR
- Individual clusters ?
- Feasible in the context of Rubin LSST/Euclid ?



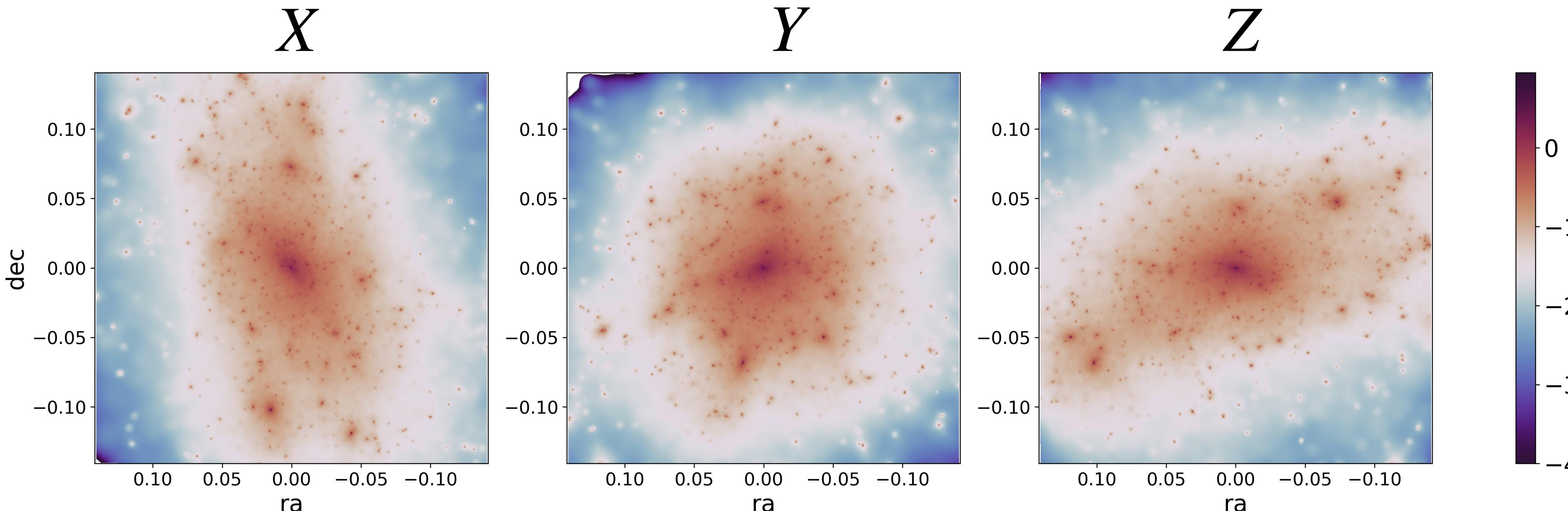
Lensing with the The Three Hundred Project

The Three Hundred (Cui et al., 2018)

- Study galaxy cluster formation history
- High resolution simulations of 300 halos $> 6.4 \times 10^{14} M_{\odot}$ (N-body + hydro.)
- Mock observations in X-rays, SZ, optical
- + Weak lensing maps (Meneghetti et al. 2023 (in prep), Giocoli et al. 2023, and Herbonnet et al. 2022)

"3D" view of matter distribution

- Derived for 3 orthogonal projections along the LOS



THE300:
MODELLING GALAXY CLUSTERS AND
THEIR ENVIRONMENT



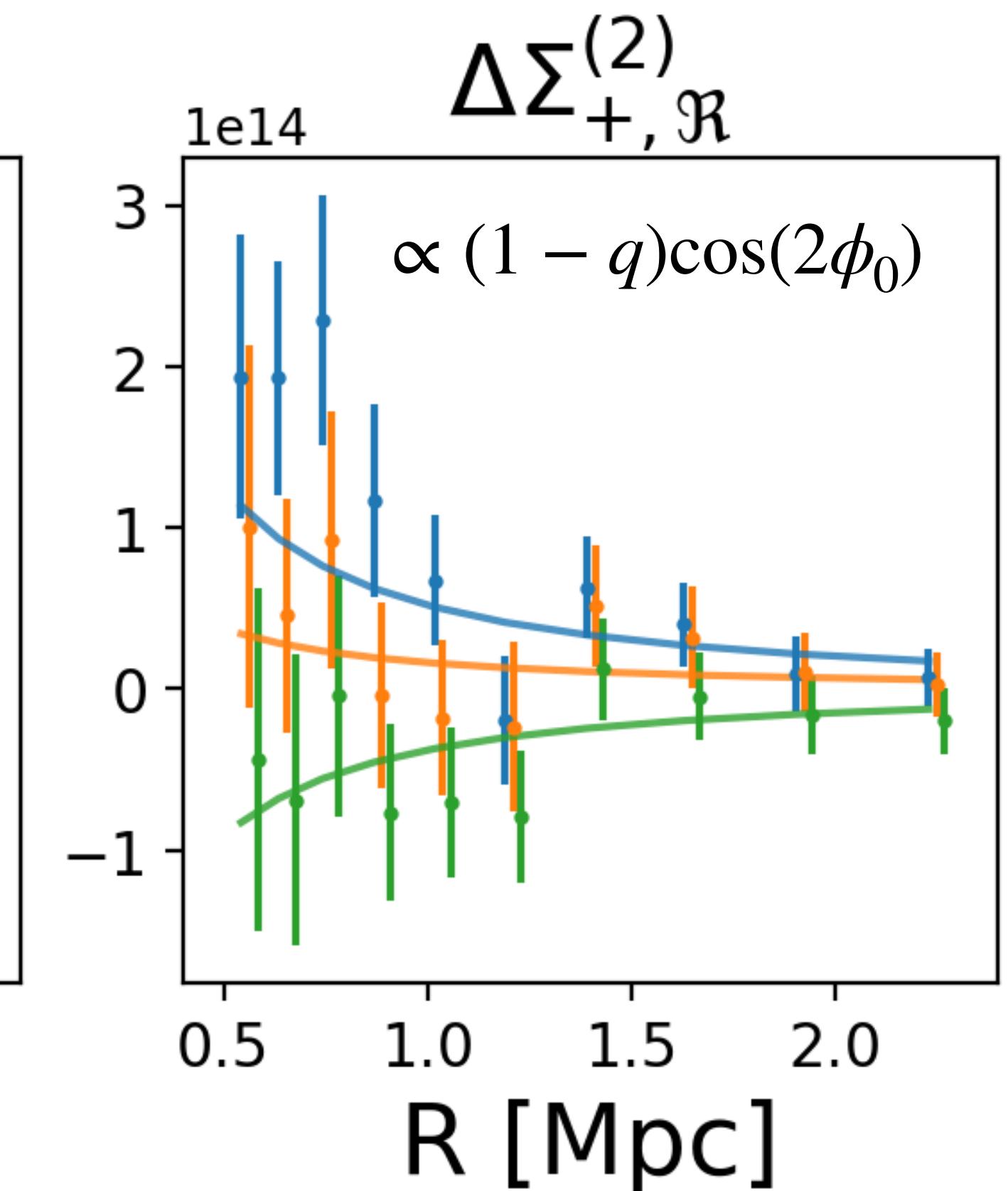
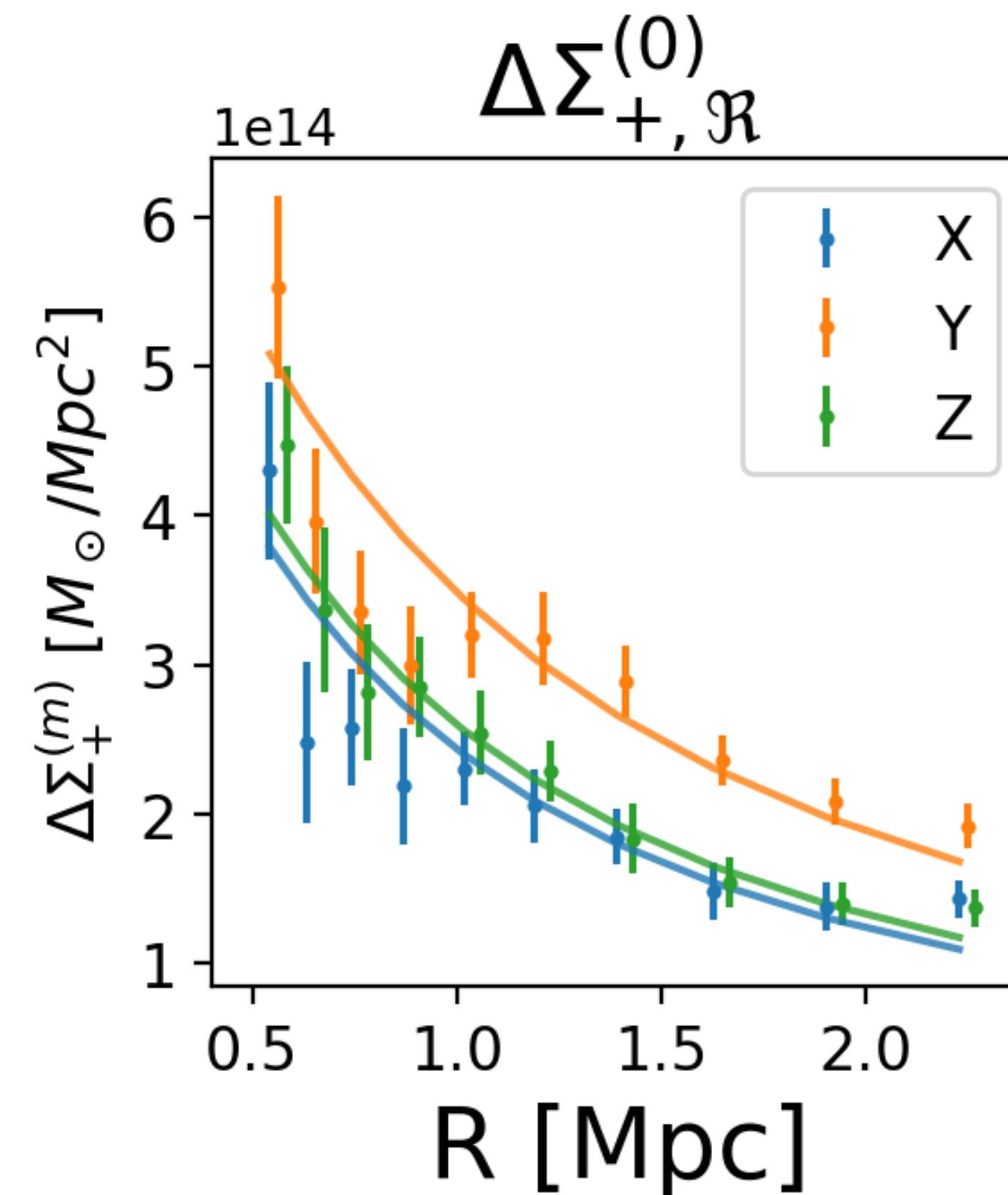
Methodology

Weak lensing analysis per LOS

- Estimate the shear multipoles for each LOS projection (LSST-like source catalog)
- Fit elliptical model to the lensing profiles

Test elliptical mass model

- Compare the recovered lensing masses between them
- Are the masses compatible ?
- Overlap of mass posteriors !



Single cluster analysis - elliptical modelling

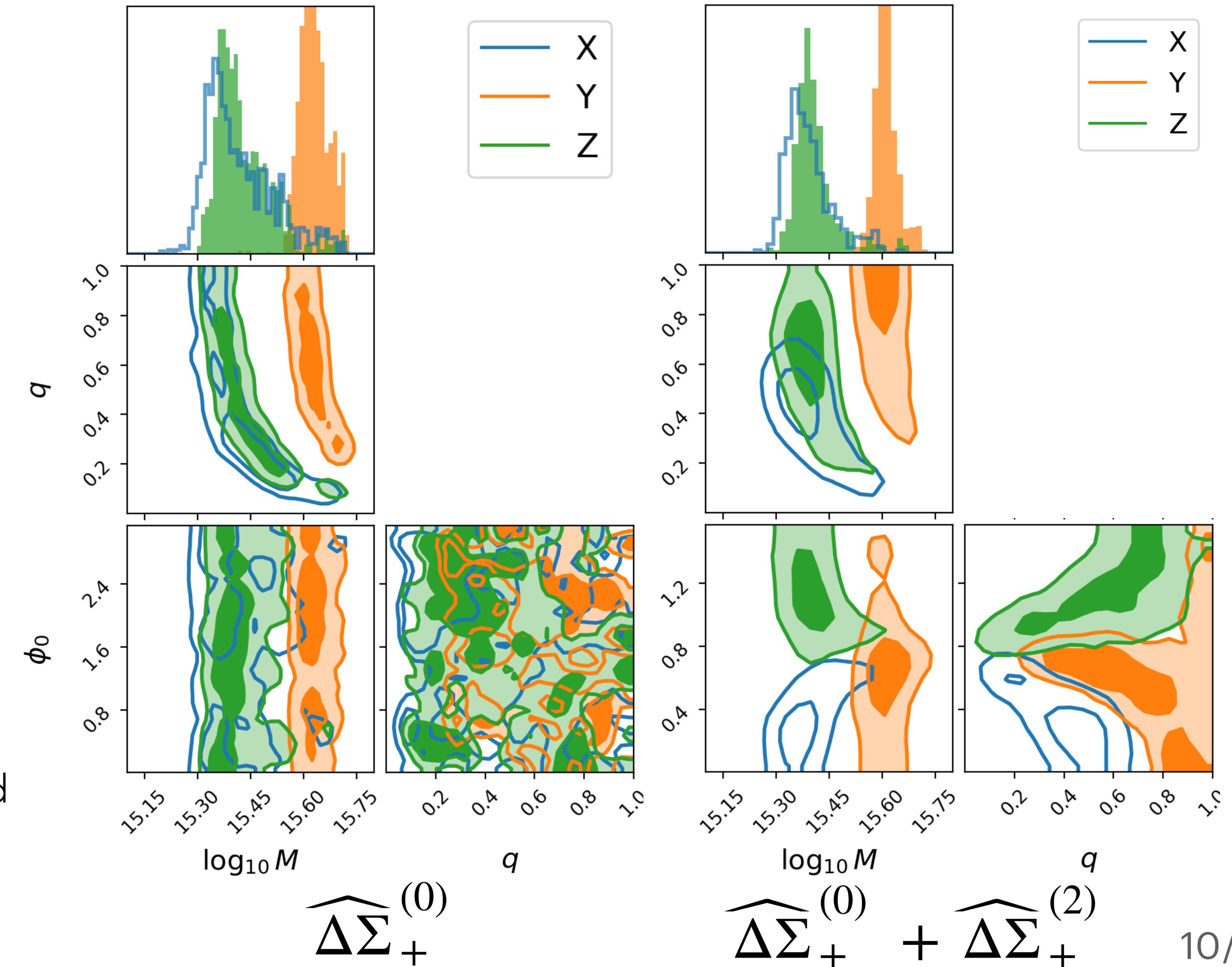
$$\kappa = \kappa_{\text{sph}} \left(R \sqrt{\frac{\cos^2(\phi - \phi_0)}{q^2} + q^2 \sin^2(\phi - \phi_0)} \right)$$

Using only monopole

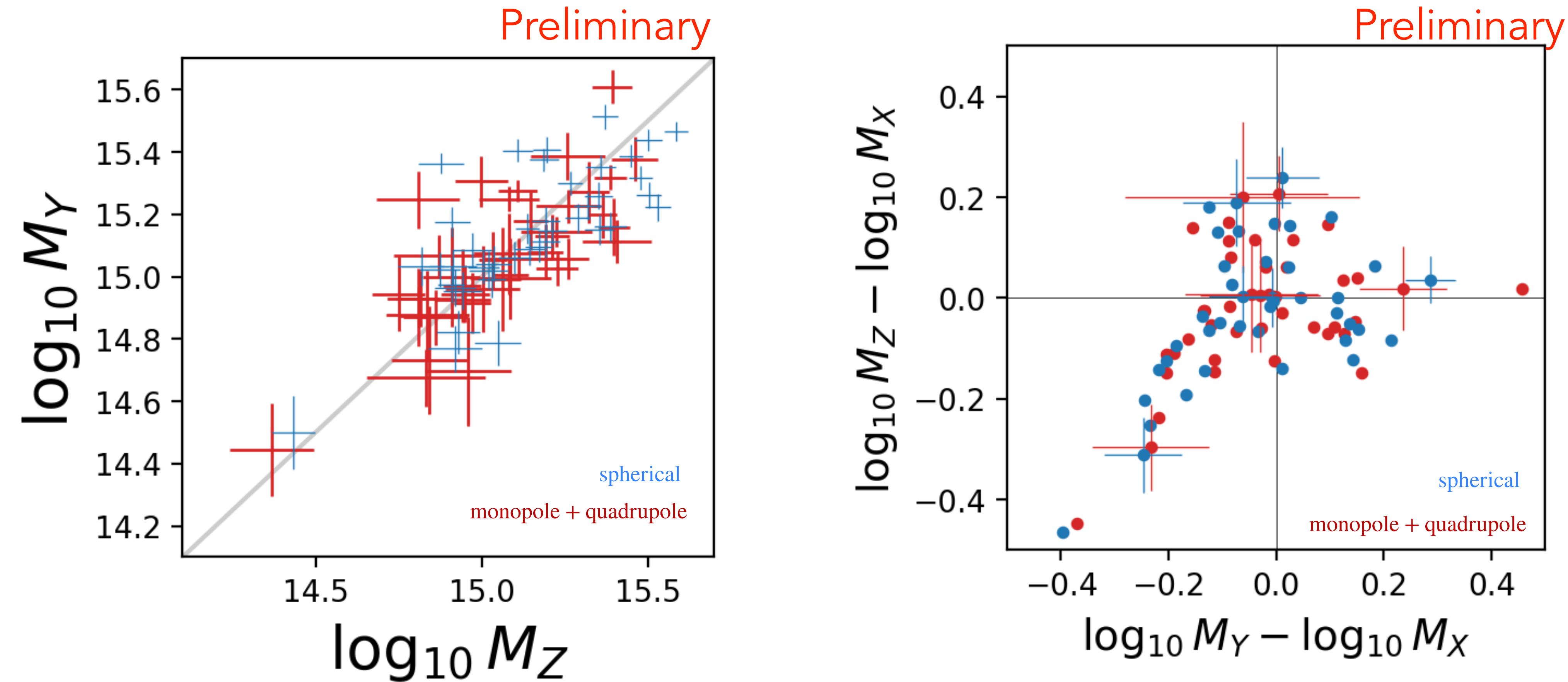
- $\Delta\Sigma_+^{(0)}$ invariant under ϕ_0 , thus difficult to fit axis ratio
- The Y projection gives higher mass

Using monopole + quadrupole

- Probes $\varepsilon \cos(2\phi_0)$
- $q \approx 1$:
- Spherical along LOS, no large quadrupole
- The analysis gives higher mass, which indicates the halo is elongated and aligned along the Y-axis



Impact on cluster mass (40 clusters)



Mass versus Mass

- Ideally, $M_X = M_Y$
- The “quadrupole” masses have larger error bars, more representative to the scatter
- They are compatible at $1-2\sigma$ with spherical masses

Δ Mass versus Δ Mass

- Ideally, $\Delta\text{Mass} \approx 0$
- Monopole + quadrupole = no significant improvement

Ellipticities

$$\epsilon_{\text{proj}} = \frac{1 - q}{1 + q}$$

- Fitting monopole and quadrupole
- Per projection

$$\langle \epsilon_{\text{proj},X} \rangle \approx 0.24 \pm 0.08$$

$$\langle \epsilon_{\text{proj},Y} \rangle \approx 0.25 \pm 0.10$$

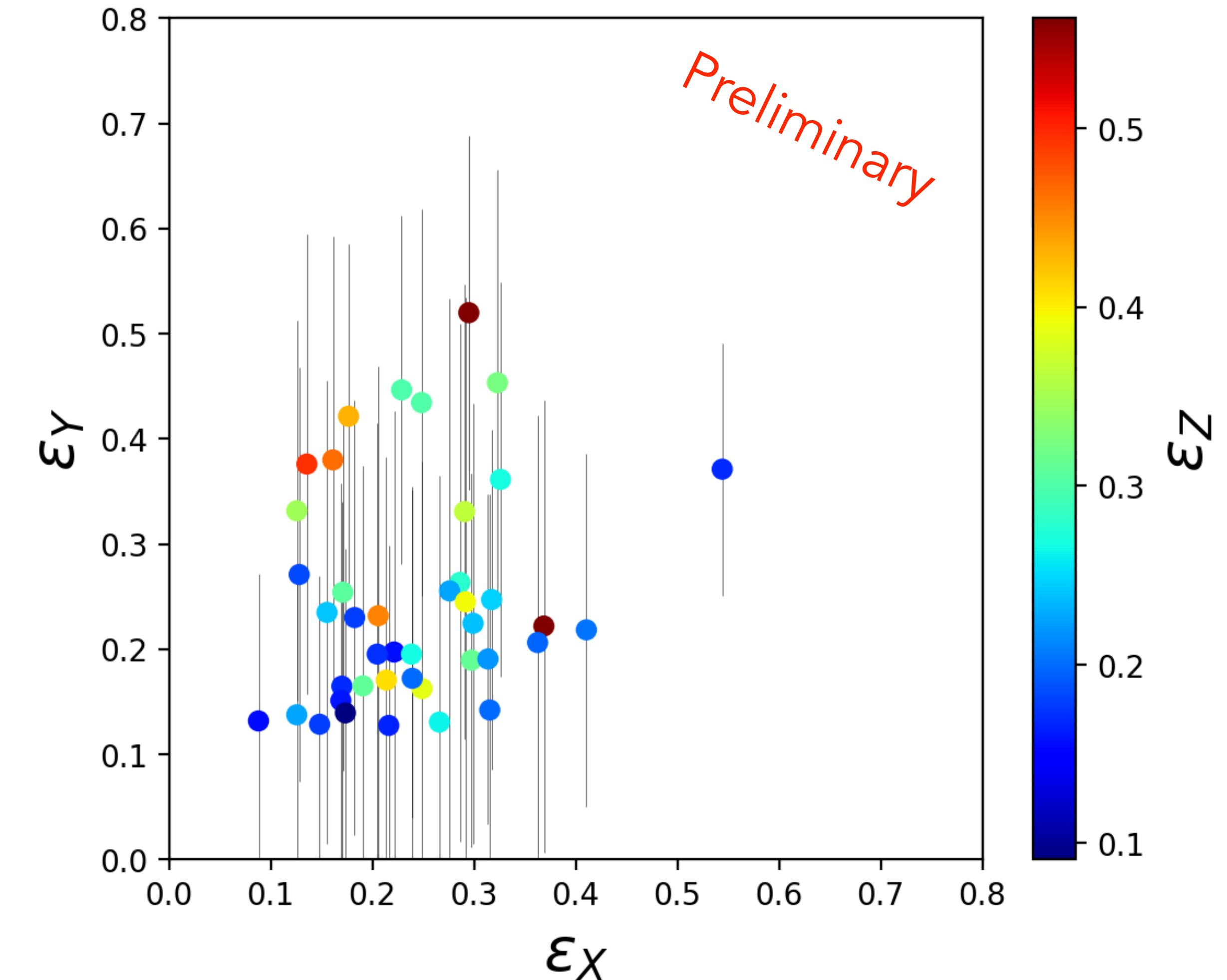
$$\langle \epsilon_{\text{proj},Z} \rangle \approx 0.28 \pm 0.11$$

- Compatible with previous stacked estimates

(Shin et al., 2017) $\langle \epsilon_{\text{proj}} \rangle = 0.21 \pm 0.04$

(Gonzalez et al., 2020) $\langle \epsilon_{\text{proj}} \rangle = 0.27 \pm 0.03$

- Need to check how ellipticity and mass correlate with simulation quantities



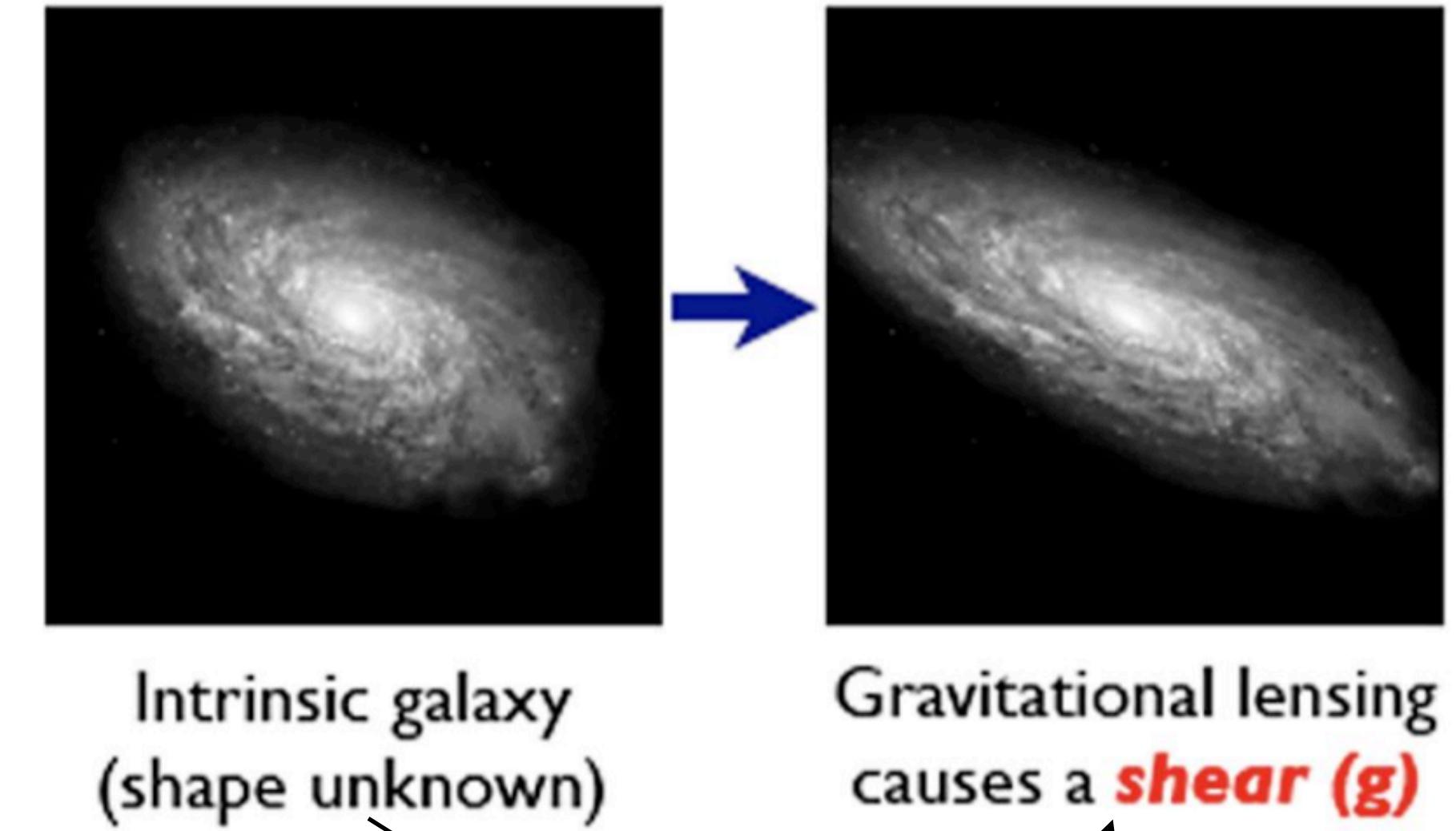
Conclusions

- **Weak lensing study of galaxy clusters**
 - Crucial for precise cosmological constraints
 - The lensing can be used to probe cluster mass density
 - Multipoles are used to trace the halo ellipticity + orientation
- **Methodology**
 - Lensing analyses of the same cluster for several LOS projections
 - Direct test of projection effects
- **The Three Hundred**
 - Multipoles do not correct mass compared to standard spherical approach
 - But increases error bars (need to apply to the full The300 sample)
 - Ongoing:
 - Plan to use higher order multipoles
 - Combining tangential and cross shear (pipeline still under construction)
 - Measuring non-zero multipole moment on individual clusters can be a rapid test for sphericity
 - We find average $\langle \epsilon_{\text{proj}} \rangle$ compatible with other shear multipole studies

Realistic background galaxy sample

Unlensed source sample

- We created source galaxy mocks
- Shape noise/per component $\sigma_{\epsilon_{1,2}} = 0.25$
- Un-lensed source sample $n(z)$ Chang et al. (2013)
- $n_{\text{gal}} = 30 \text{ gal} \cdot \text{arcmin}^{-2}$ (LSST-like density)
- Following the methodology in Herbonnet et al. (2022)



Lensed source sample

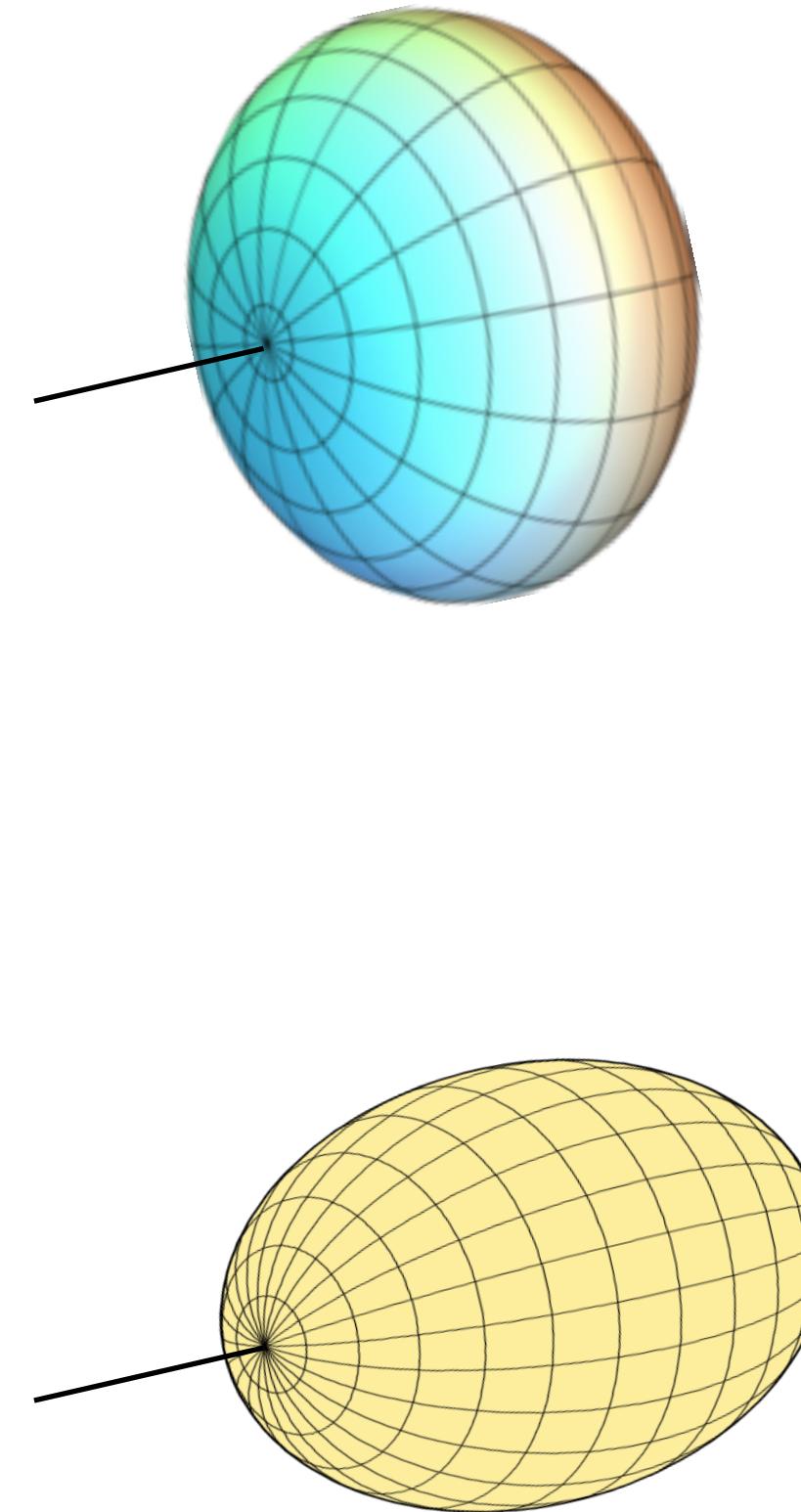
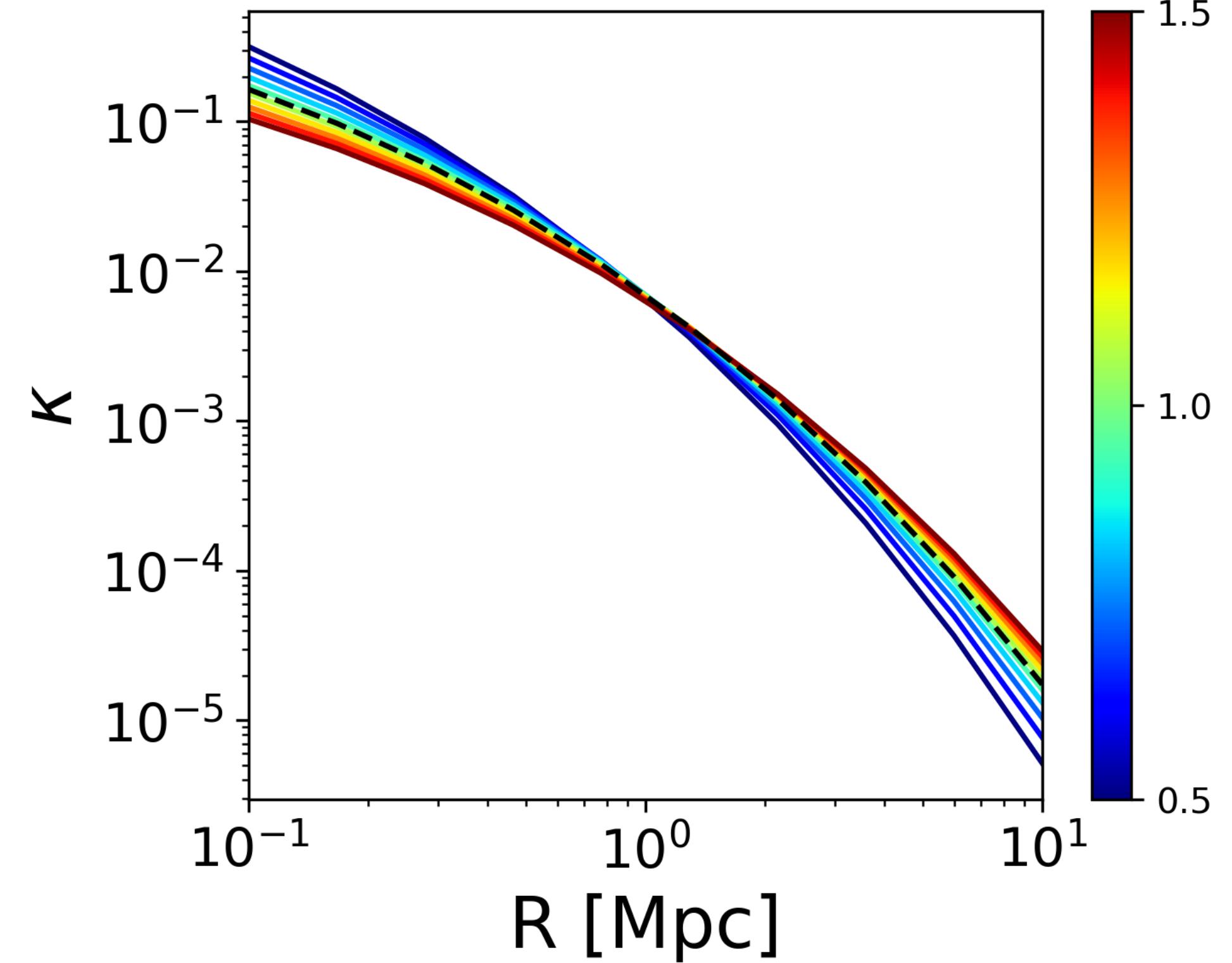
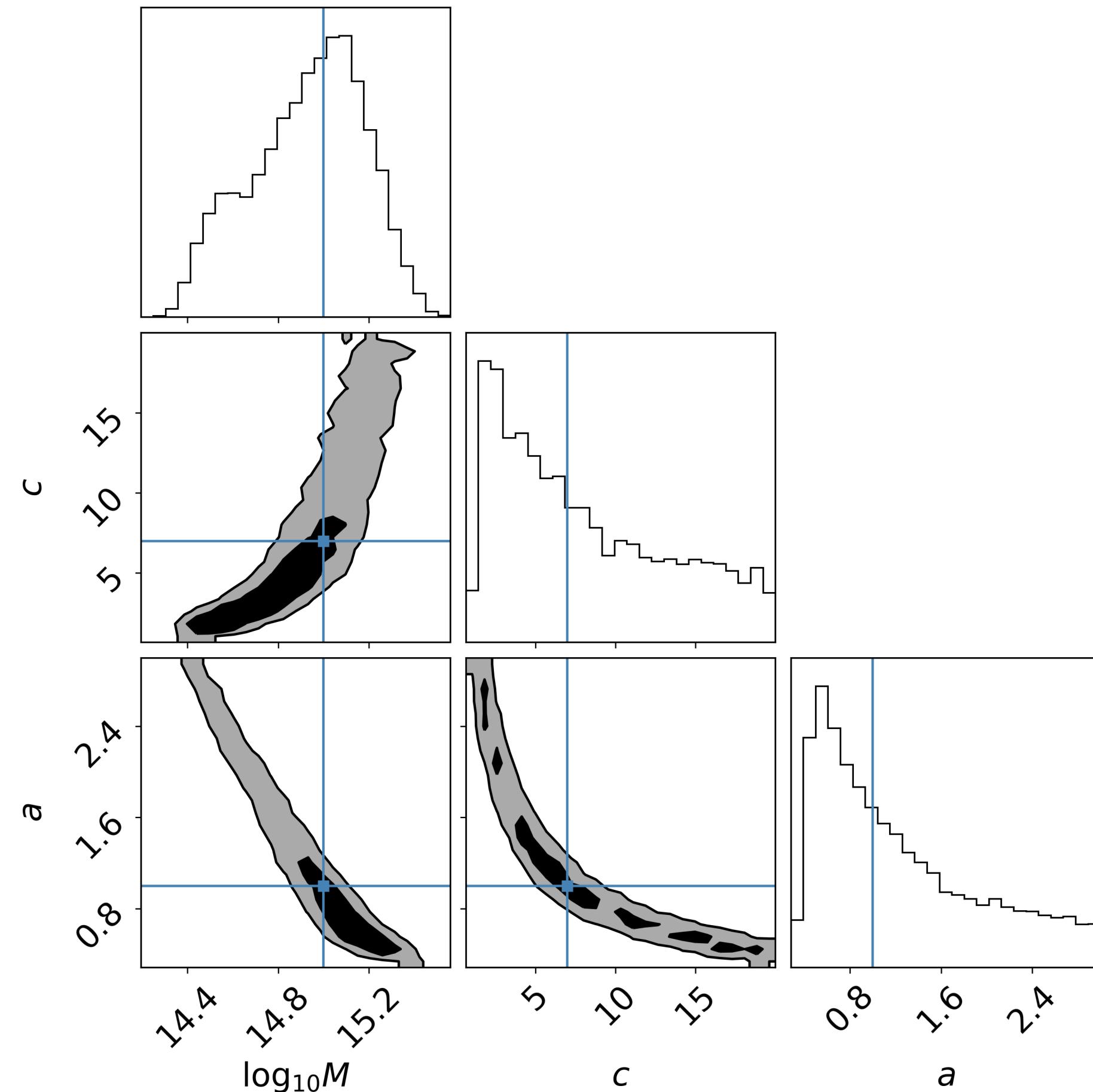
- Create $\kappa(z_{\text{src}})$ and $\gamma(z_{\text{src}})$ maps for each source redshifts (redshift rescaling of the The300 lensing maps)
- Galaxies are individually sheared from the map interpolation
- We do not account for the "shift" of galaxies on the sky plane (magnification)

$$\epsilon^{\text{obs}} = \frac{\epsilon^{\text{int}} + g}{1 + g * \epsilon^{\text{int}}}$$

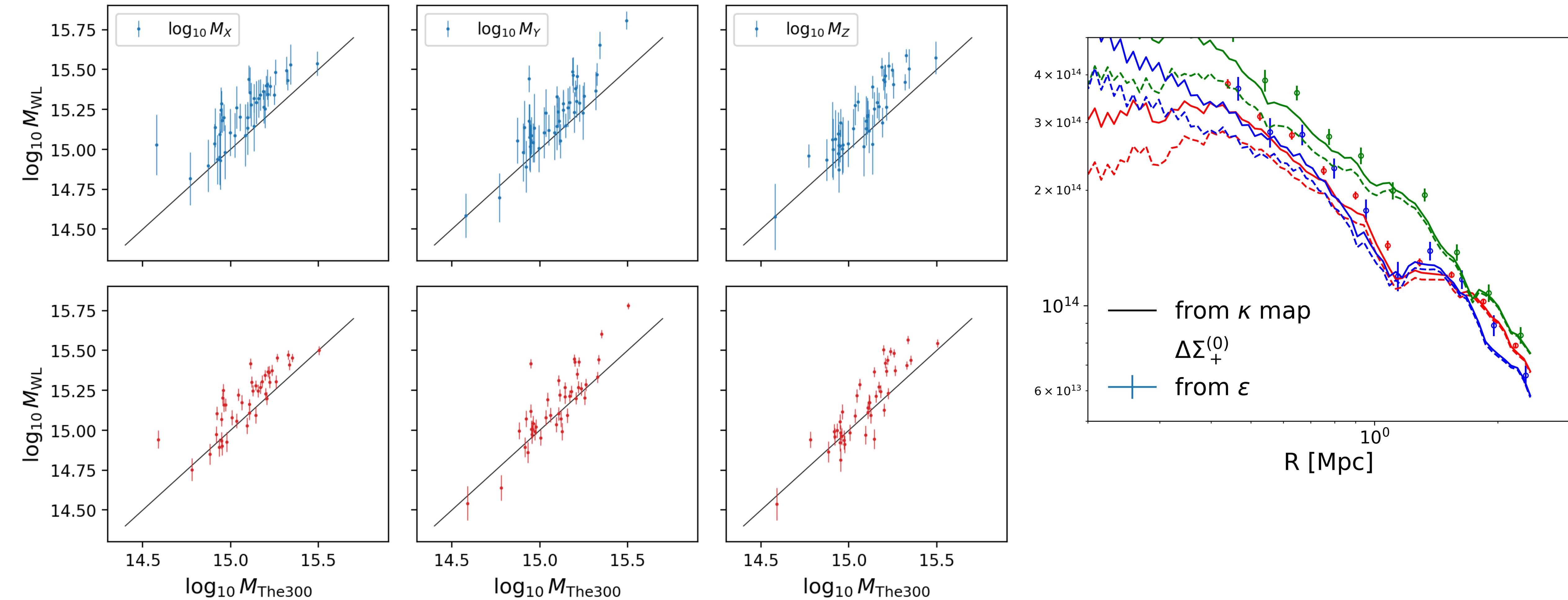
$$g(z_{\text{src}}) = \frac{\gamma(z_{\text{src}})}{1 - \kappa(z_{\text{src}})}$$

Correlation between mass and prolate index

- We consider spherical halo
- Fit prolate/oblate modeling ϵ_{proj}
- Strong correlation between a and mass

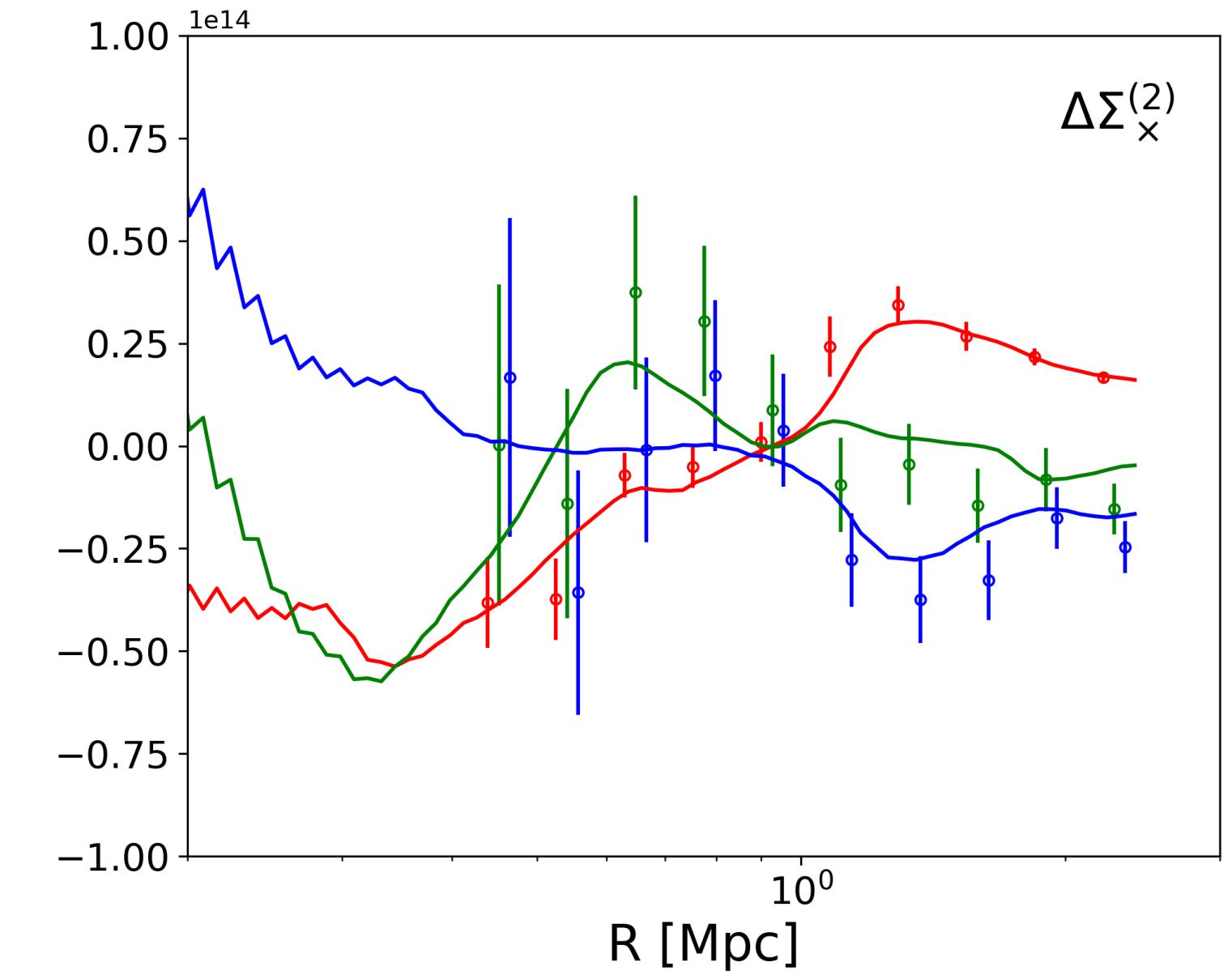
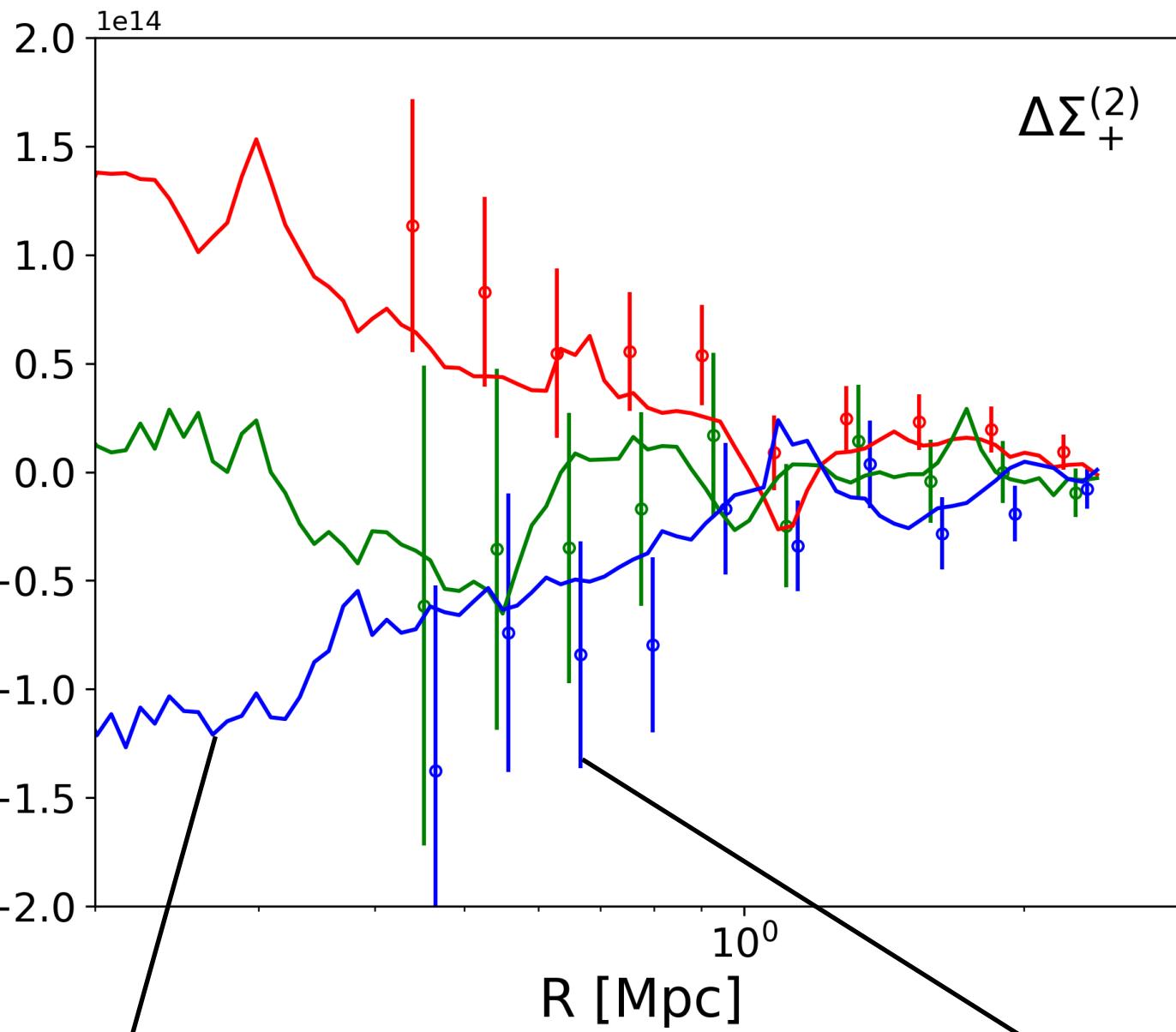
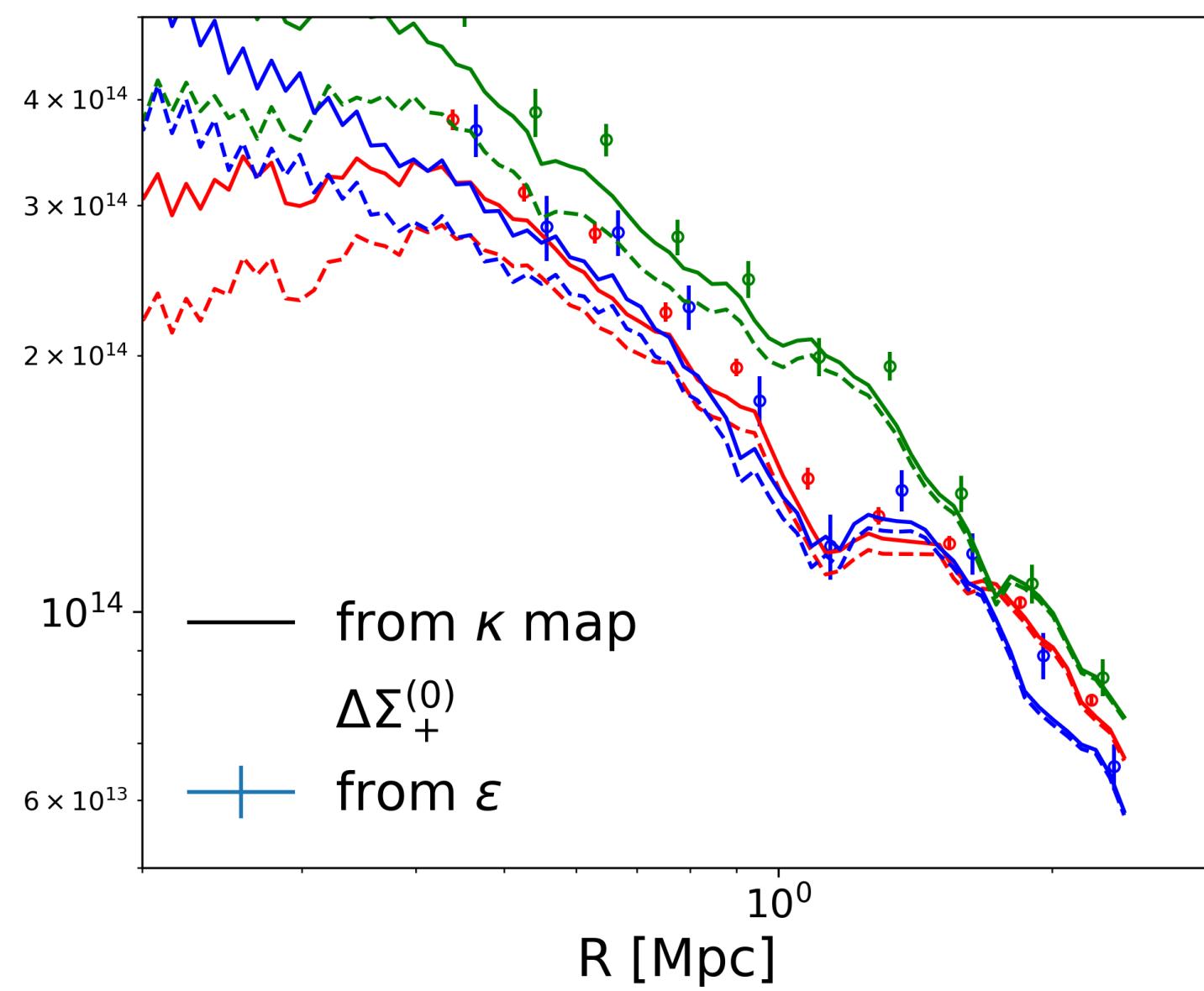


Comparison to The300 masses



- Persistent positive bias (weak lensing corrections, that may be important for massive clusters, not taken in account here)

Data vs maps



$$\gamma_{\text{The300}}^{(m)} = \mathcal{F}(\kappa_{\text{The300}}^{(m)})$$

From the lensing maps

From sheared background sources