COMP9319 WEB DATA COMPRESSION AND SEARCH

Search on Suffix Array, FM Index, Backward Search, Compressed BWT

SUFFIX ARRAY

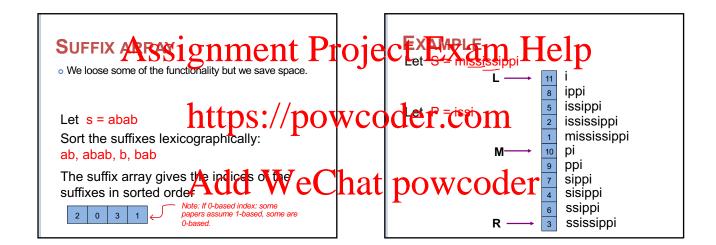
• We loose some of the functionality but we save space.

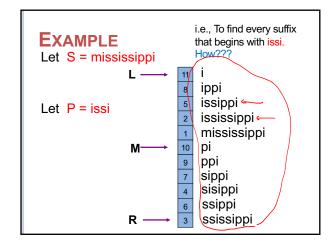
Let s = abab

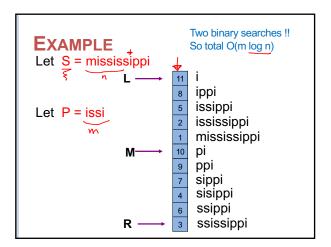
Sort the suffixes lexicographically: ab, abab, b, bab

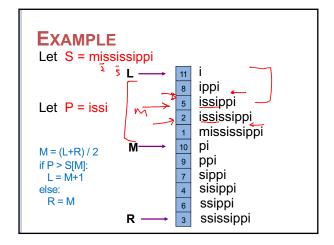
The suffix array gives the indices of the suffixes in sorted order

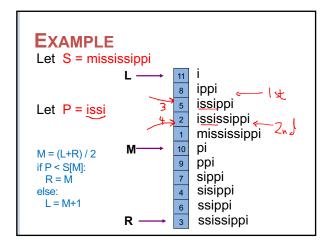
3 1 4 2

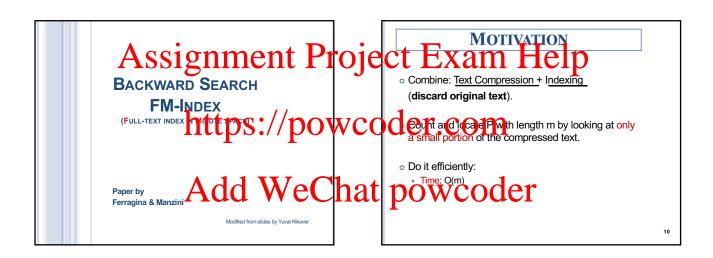




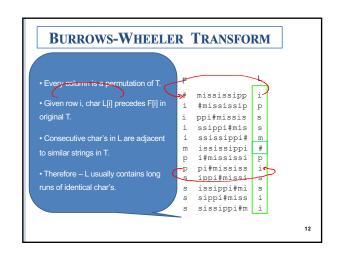


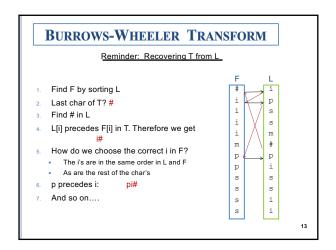


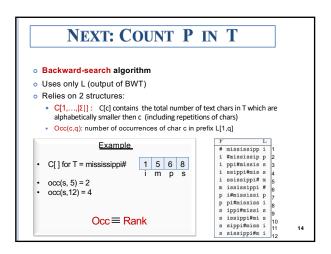


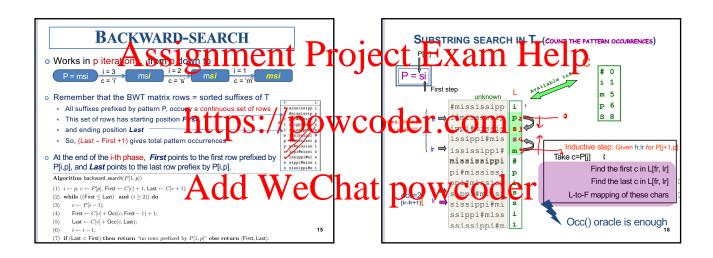


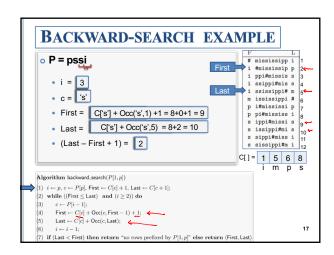
Exploit the relationship between the Burrows-Wheeler Transform and the Suffix Array data structure. Compressed suffix array that encapsulates both the compressed text and the full-text indexing information. Supports two basic operations: Count – return number of occurrences of P in T. Locate – find all positions of P in T.

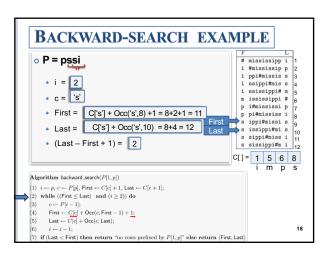


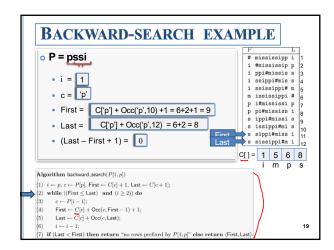




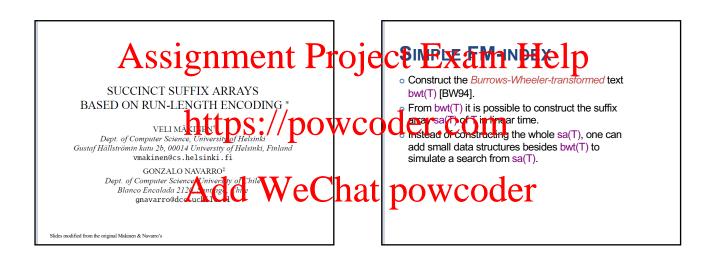








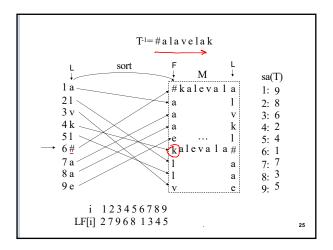
COMPRESSED SUFFIX ARRAY / BWT



BURROWS-WHEELER TRANSFORMATION

- Construct a matrix M that contains as rows all rotations of T.
- o Sort the rows in the lexicographic order.
- Let L be the last column and F be the first column.
- o bwt(T)=L associated with the row number of T in the sorted $\mathsf{M}.$

EXAMPLE pos 123456789 T = kalevala#sa $\stackrel{\mathsf{F}}{\downarrow}$ M $\stackrel{\mathsf{L}}{\downarrow}$ 1:9 #kalevala 2:8 a#kaleval L = alvkl#aae, row 6 3:6 ala#kaley 4:2 alevala#k 5:4 evala#kal Exercise: Given L and the row 6:1 kalevala# number, we know how to compute T. 7:7 la#kaleva What about sa(T)? 8:3 levala#ka 9:5 vala#kale



IMPLICIT LF[I]

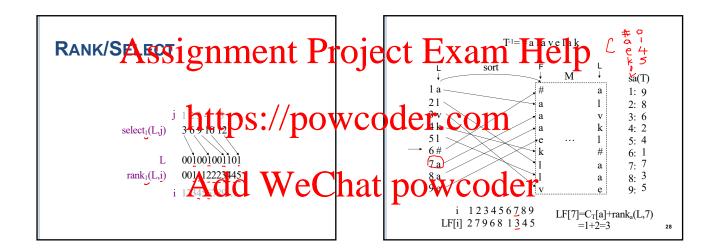
- Ferragina and Manzini (2000) noticed the following connection:
- $\bullet \ \mathsf{LF[i]=C_T[L[i]]+rank_{L[i]}(L,i)}$
- Here

 $C_T[c]$: amount of letters 0,1,...,c-1 in

L=bwt(T)

 $rank_c(L,i)$: amount of letters c in the prefix

L[1,i]



RECALL: BACKWARD SEARCH ON

BWT(T)

 Observation: If [i,j] is the range of rows of M that start with string X, then the range [i',j'] containing cX can be computed as

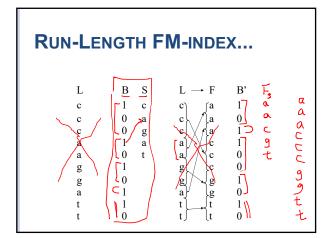
 $F_{\mathbf{V}}$ i' := $C_T[c]$ +rank_c(L,i-1)+1, $L_{\mathbf{V}}$ j' := $C_T[c]$ +rank_c(L,j).

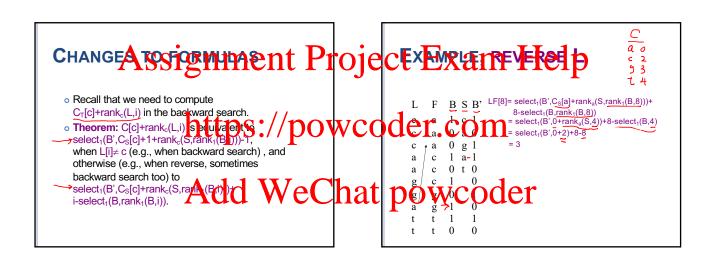
BACKWARD SEARCH ON BWT(T)...

- \bullet Array $C_T[1,\sigma]$ takes $O(\sigma \ log \ |T|)$ bits.
- L=Bwt(T) takes O(|T| log σ) bits.
- o Assuming $\operatorname{rank}_c(L,i)$ can be computed in constant time for each (c,i), the algorithm takes O(|P|) time to count the occurrences of P in T.

RUN-LENGTH FM-INDEX

- We make the following changes to the previous FMindex variant:
 - L=Bwt(T) is replaced by a sequence S[1,n'] and two bit-vectors B[1,|T|] and B'[1,|T|],
- Cumulative array $C_T[1,c]$ is replaced by $C_S[1,c]$,
- some formulas are changed.

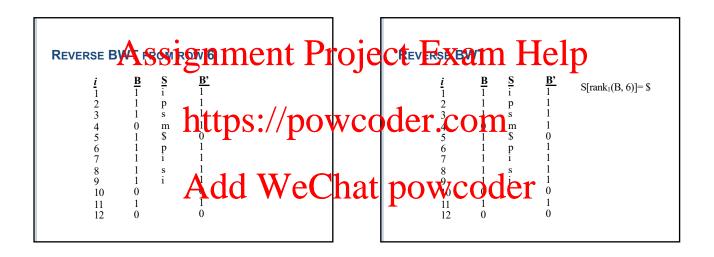




o For more details, read the paper

EXERCISE

- o ipsm\$pisi
- o 111011111010



```
REVERSE BWT
                    S[rank_1(B, 6)] = $
            <u>B'</u>
    B
        \mathbf{S}
                    LF[6]
                    = select_1(B', C_S[\$] + rank_S(S, rank_1(B, 6))) + 6 -
    0
         m
             1
                    select_l(B, rank_l(B, 6))) \\
6
                    = select_1(B', 0 + rank_s(S, 5)) + 6 - select_1(B 5)
                    = 1 + 6 - 6 = 1
8
    1
10
    0
             0
11
12 0
             0
```

```
REVERSE BWT
                         S[rank_1(B, 1)]=i
              <u>B'</u>
     <u>B</u>
          \underline{\mathbf{s}}
                         LF[1]
                         = select<sub>1</sub>(B', C<sub>S</sub>[i] + rank<sub>i</sub>(S, rank<sub>1</sub>(B, 1))) + 1 -
     0
          m
                         select_1(B, rank_1(B, 1)))
6
7
                         = select_1(B', 1 + rank_i(S, 1)) + 1 - select_1(B, 1)
                         =2+1-1=2
8
10
     0
                0
11
    0
               0
```

REVERSE BWT $S[rank_1(B, 1)]=i$ <u>s</u> <u>B</u>' <u>B</u> 1 2 3 4 5 6 7 LF[1] p 1 $= select_1(B', C_S[i] + rank_i(S, rank_1(B, 1))) + 1$ 0 m $-\operatorname{select}_{l}(B,\operatorname{rank}_{l}(B,1)))$ 0 \$ $= select_l(B\texttt{'},\, 1 + rank_i(S,\, 1)) + 1 - select_l(B\, 1)$ p =2+1-1=28 1 You can also construct the SA in this way: 10 0

12,11,8,5,2,1,10,9,7,4,6,3

12, 11,

11

```
      i
      B
      S
      B'
      Suppose search for si:

      1
      1
      1
      1
      c = i, First = 2, Last = 5

      2
      1
      p
      1
      c = i, First = 2, Last = 5

      3
      1
      s
      1
      c = s

      4
      0
      m
      1
      c = s

      4
      0
      m
      1
      c = s

      4
      0
      m
      1
      c = s

      4
      0
      m
      1
      c = s

      4
      0
      m
      1
      c = s

      4
      0
      m
      1
      c = s

      4
      0
      c = s
      c = s

      5
      1
      c = s
      c = s

      6
      1
      p
      c = s

      1
      1
      c = s

      2
      c = s
      c = s

      3
      c = s
      c = s

      4
      c = s
      c = s

      4
      c = s
      c = s

      4
      c = s
      c = s

      5
      c = s
      c = s

    <t
```

```
gnment Project Exam Help
                 c = i, First = 2, Last = 5
    \frac{\mathbf{B}}{1} \quad \frac{\mathbf{S}}{\mathbf{i}} \quad \frac{\mathbf{B'}}{1}
1
2
3
        p
s
                 First = select<sub>1</sub>(halft-prack (S, rank (B2) wcoder.com
   1
           1
    0
       m
           0
                  =select<sub>1</sub>(B',7+1+rank<sub>s</sub>(S,1))
   1
                 =select<sub>1</sub>(B', 8) = 9
                 Last = selecti(BAS) This will be Chat powcoder
10 0
           0
11 1
                 =select<sub>1</sub>(B',7+1+rank<sub>s</sub>(S,4)) - 1
12 0
                 =select<sub>1</sub>(B', 9) -1 = 11 - 1 = 10
```