

Western University
Department of Computer Science
CS1027b Foundations of Computer Science II
Final Exam
April 24, 2017

Last Name: _____

First Name: _____

Student Number: _____

Section Number (1 - Hughes, 2 - Solis-Oba): _____

PART I	
PART II	
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Total	

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Instructions

- Fill in your name, student number, and section.
- The exam is 3 hours long.
- The exam has 12 pages and 29 questions.
- The first part of the exam consist of multiple choice questions. For each question circle only **one** answer.
- For the second part of the exam, answer each question **only** in the space provided.
- When you are done, raise your hand and one of the TA's will collect your exam.

Part I. Multiple Choice Questions

For each multiple choice question circle **only one** answer.

1. (1 marks) Consider the following three Java classes

```
public class A
public class B extends A
public class C extends A
```

Consider the following statements

```
A varA = new B(); // Line 1
C varC = new C();
varA = varC;      // Line 3
```

Which line(s) generate compilation error(s)? (Line numbers are indicated in the comments).

- (A) Line 1 (B) Line 3 (C) Lines 1 and 3 (D) None

2. (1 mark) Consider the same three classes A, B, and C from the previous question and the following Java statement

```
C varC = (C) new B();
```

Which of the following statements is true?

- (A) The above Java statement generates a compilation error.
(B) The above Java statement generates a runtime error.
(C) The above Java statement does not generate any errors

3. (1 mark) Consider the following Java code

```
int[] a = {3, 1, 2};
int[] b;
b = a;
b[0] = 2; // Line 1
System.out.println(a[0]+", "+b[0]);
```

What does the above code print?

- (A) 3,2 (B) 2,2 (C) Nothing. There will be a runtime error when executing line 1, as b has not yet been allocated memory.

4. (2 marks) Consider the following Java code

```
public class A {
    private int i = 1;
    public A() {
        int j = 0;
        for (int i = 0; i < 3; ++i) j = j + i;
        j = j + i;
        System.out.println("i = "+i+", j = "+j);
    }
}
```

What is printed when the statement

```
A varA = new A();
```

is executed?

- (A) i = 3, j = 6
(B) i = 2, j = 5
(C) i = 1, j = 4
(D) Nothing is printed as the above code throws an exception.

5. (1 mark) Consider the following Java code

```
Integer a = new Integer (2);
Integer b = new Integer (2);
if (a == b) m1(); // Line 1
else m2();
```

Which of the following statements is true?

- (A) When the above code is executed, method `m1()` will be invoked.
- (B) When the above code is executed, method `m2()` will be invoked.
- (C) When the above code is executed, a compilation error will be generated on Line 1 as objects must be compared with the `equals` method.

6. (1 mark) Consider the following Java classes

```
public class A {
    public boolean m() {return true;}
}

public class B extends A {
    public boolean m() {return false;}
}
```

What does the following Java code print?

```
A varA = new B();    // Line 1
if (varA.m()) System.out.println("true");
else System.out.println("false");
```

- (A) true (B) false (C) Nothing. The program has a compilation error in Line 1.

7. (1 mark) The following values are inserted, in the given order, into an initially empty binary search tree: 13, 2, 9, 5, 23, 11.

Which value is stored in a node in level 2 of the tree? (Recall that the root is in level 0, the children of the root are in level 1, and so on.)

- (A) 2 (B) 9 (C) 5 (D) 11

8. (1 mark) Consider a binary search tree `T` in which every node stores an integer value. Which of the following statements is always true?

- (A) A preorder traversal visits the nodes in increasing order of the values stored in them.
- (B) The last node visited by a postorder traversal is the node storing the largest value.
- (C) In an inorder traversal of `T` a node `u` storing value `v` is visited only after all nodes storing values smaller than `v` have been visited.

9. (2 marks) Consider a sorted list implemented using a circular array. Let `first` be the index of the first element in the list and `last` be the index of the last element in the list. Let the list store `n` integer values, where `n` is an odd number. Operation `median()` returns the value of the median or the $\frac{n+1}{2}$ -th smallest element in the list. For example, the median of this sorted list: 1, 4, 5, 8, 9, 12, 15, is 8. What is the time complexity of the best possible implementation of operation `median()`?

- (A) $O(1)$
- (B) $O(\log n)$
- (C) $O(n)$

10. (2 marks) Consider the same previous question, but this time the sorted list is implemented using a doubly linked list. Reference variable `first` points to the first node in the list and `last` points to the last node in the list. What is the time complexity of the best possible implementation of operation `median()`?

- (A) $O(1)$
- (B) $O(\log n)$
- (C) $O(n)$

11. (3 marks) Consider the following algorithm.

```
public void sort(int[] a, int n) {
    ArrayQueue<Integer> q = new ArrayQueue<Integer>();
    for (int i = 0; i < n; ++i) {
        int x = i;
        (**)
        q.enqueue(a[x]);
        a[x] = -1;
    }
    for (int i = 0; i < n; ++i) a[i] = q.dequeue();
}
```

Which code must be inserted at the point marked (**) to sort array **a** in decreasing order? Array **a** stores **n** positive integer values.

- (A) for (int j = i+1; j < n; ++j) if (a[j] < a[x]) x = j;
- (B) for (int j = i+1; j < n; ++j) if (a[j] > a[x]) x = j;
- (C) for (int j = 0; j < n; ++j) if (a[j] > a[x]) x = j;
- (D) for (int j = 0; j < i-1; ++j) if (a[j] > a[x]) x = a[j];

12. (2mark) Consider the following Java code.

```
private static void m(int[] a) throws ArrayIndexOutOfBoundsException {
    try {
        for (int i = 0; i < a.length; ++i) a[i] = 0;
    }
    catch (NullPointerException e) {
        System.out.print("Error 1. ");
    }
}

public static void main (String[] args) {
    int[] b = {1,2};
    try {
        m(b);
    }
    catch (Exception e) {
        System.out.println("Error 2. ");
    }
}
```

When the **main** method is executed what message(s) will be printed?

- (A) Error 1.
 - (B) Error 2.
 - (C) Error 1. Error 2.
 - (D) Nothing will be printed.
13. (1 mark) Consider the following algorithm.

```
private void m(int size) {
    if (size == 1) return;
    else m(size - 1);
}
```

How many activation records (or call frames) are created in the execution stack (or runtime stack, or call stack) for method **m** when the statement

m(3);

is executed?

- (A) 0 (B) 2 (C) 3 (D) 4

14. (1 mark) Consider the following Java code.

```
public class A {  
    private int x;  
    public String s = "";  
    public A (int y) {  
        x = y;  
    }  
}
```

Which of the following statements is correct?

- (A) The empty string referenced by `s` is allocated memory in the heap, while `x`, `s`, and `y` are allocated memory in the execution stack (or runtime stack or call stack).
- (B) The empty string referenced by `s` and `s` are allocated memory in the heap, while `x` and `y` are allocated memory in the execution stack.
- (C) The empty string referenced by `s`, `s`, and `x` are allocated memory in the heap, while `y` is allocated memory in the execution stack.
- (D) `x`, and `s` are allocated memory in the heap; `y` is allocated memory in the execution stack. No memory needs to be allocated for the empty string.

15. (1 mark) Consider the following recursive definition:

```
f(n) = f(n-1) - f(n-2)  
f(1) = 2  
f(0) = 0
```

What is the value of `f(4)`?

- (A) -2 (B) 0 (C) 2 (D) 8

16. (2 marks) Consider the following Java code.

```
public class ClassA<T> { // Line 1  
    public T smaller (T elem1, T elem2) {  
        if (elem1.compareTo(elem2) < 0) return elem1; // Line 3  
        else return elem2;  
    }  
}
```

Which of the following statements is correct?

- (A) Line 1 has a compilation error.
- (B) Line 3 has a compilation error.
- (C) There are no compilation errors, but the above code will produce a runtime error when executed.
- (D) There are no errors in this code.

Part II. Written Answers

Write your answers **only** in the space provided.

17. (3 marks) Consider the following algorithm.

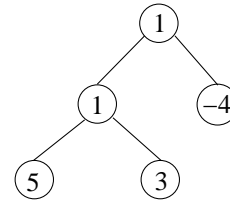
```
public int traverse(BinaryTreeNode r) {  
    if (r == null) return 0;  
    else {  
        int v = traverse(r.getLeftChild()) - traverse(r.getRightChild());  
        if (v > r.getElement()) return v;  
        else return r.getElement();  
    }  
}
```

If the following statement is executed

```
int result = traverse(r);
```

where **r** is the root of the tree on the right.

What value will **result** have? _____



18. (5 marks) Consider the following Java code.

```
public static void main (String[] args) {  
    int[] a = new int[3];  
    int size = 0;  
    init(a,size);  
    for (int i = 1; i < size; ++i) System.out.println(a[i]);  
    System.out.println(a[0]);  
}  
private static void init(int[] a, int size) {  
    for (int i = 0; i < 3; ++i) {  
        ++size;  
        a[i] = (1-i) * size;  
    }  
}
```

Show the output produced by this algorithm. Values must be printed in the same order as the algorithm prints them.

19. Consider the following Java code.

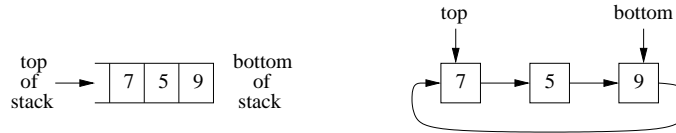
```
public static void main(String[] args) {  
    int[] a = {3, 5, 2};  
    int result = m(a,0,2);  
}  
public static int m(int[] a, int first, int last) {  
    if (first > last) return 1;  
    else {  
        int mid = (int)Math.floor((first+last)/2);  
        return m(a,first,mid-1)+m(a,mid+1,last); // Line 1  
    }  
}
```

where method `Math.floor(x)` rounds the value of the parameter `x` down to the nearest integer. For example, `Math.floor(3.2) = 3`, `Math.floor(3) = 3`.

(3 marks) What value does **result** have at the end? _____

(2 marks) How many recursive calls does the algorithm make (number of calls made in Line 1)? _____

20. (6 marks) Consider the implementation of a stack using a circular linked list. A circular linked list is a singly linked list where the last node of the list points to the first node of the list instead of to null. Each node of the list stores one element of the stack. There is a reference variable called **top** pointing to the node storing the value at the top of the stack and a reference variable called **bottom** pointing to the node storing the value at the bottom of the stack. For example, a stack storing values 9, 5, and 7, with 7 at the top and 9 at the bottom of the stack is represented with the circular linked list below.



Consider the following implementation of the `pop()` operation. Assume that elements stored in the stack are of type `T`; `top` and `bottom` are instance variables. Methods `getElement`, `getNext`, and `setNext` get the data stored in a node, get a reference to the next node in the list, and change the reference to the next node in the list, respectively.

```
private T pop() {
    T element = top.getElement();
    top = top.getNext();
    bottom.setNext(top);
    return element;
}
```

Indicate whether this is a correct implementation of the `pop` operation. If the implementation is incorrect, explain why it is incorrect by giving an example showing that the code will not perform the `pop` operation correctly. If the implementation is correct, explain why it always correctly removes and returns the element at the top of the stack.

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21. (3 marks) Draw a binary tree in which every node stores one of the letters A, B, C, D, E and such that
- a preorder traversal visits the nodes in this order: E A D B C, and
 - an inorder traversal visits the nodes in this order: A E B D C.

For each one of the following 4 questions, compute the time complexity of the given code. You **must explain how you computed the time complexity** and you must give the order (big-Oh) of the time complexity. (**Hint.** Your answer might be like this: “Number of operations performed outside the loops: x; number of operations performed in one iteration of the inner loop: y; number of iterations of the inner loop when i = 0 is z_1 , when i = 1 is z_2, \dots ; total number of operations performed by the loops: w. Total number of operations performed by the algorithm: $x + w$. The order of the time complexity is $O(v)$.”) The following fact might be useful to you: $\sum_{k=1}^m = \frac{m(m+1)}{2}$.

22. (7 marks)

```
int x = 0;
for (int i = 0; i < n; i = i+1)
    for (int j = 0; j < n; j = j+1) {
        if (j < i) j = j + n;
        else x = x+1;
    }
```

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23. (7 marks)

```
int x = 1;
for (int i = 0; i <= n * n; i = i + n)
    for (int j = 0; j < i; j = j + n)
        x = x + 1;
```


24. (7 marks)

```
int j = 1;
int i = 1;
while (i <= n) {
    if (i == n)
        if (j < n) {
            i = 1;
            j = j+1;
        }
    else i = n+1;
    else i = i+1;
}
```

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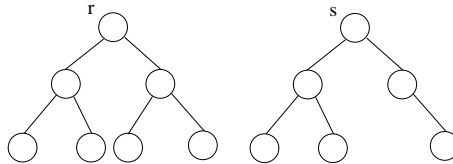
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25. (7 marks) In the following algorithm node r is the root of a binary tree with $n > 0$ nodes.

```
public int traverse(BinaryTreeNode r) {
    int res = 2;
    if (r.getLeftChild() != null) res = res + traverse(r.getLeftChild());
    if (r.getRightChild() != null) res = res + traverse(r.getRightChild());
    return res;
}
```

26. (12 marks) A binary tree is *symmetric* if for every internal node the number of nodes in its left subtree is the same as the number of nodes in its right subtree. Given a node **p**, let **p.size()** return the number of nodes in the subtree with root **p**, and **p.getLeftChild()** and **p.getRightChild()** return the left and right children of **p**, respectively. Write a recursive algorithm **isSymmetric(r)** that receives as parameter the root **r** of a binary tree and it returns **true** if the tree is symmetric and it returns **false** otherwise. For example for the tree below with root **r** the algorithm must return true, but for the tree with root **s** it must return false.



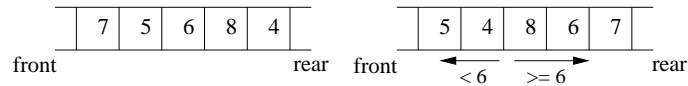
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28. (11 marks) Let `q` be a queue storing `n` integer values. Write an algorithm `partition(q,target)` that receives as parameter `q` and an integer value `target` and it re-arranges the values in the queue so that all the values smaller than `target` appear closer to the front of the queue than any values larger than or equal to `target`. For this algorithm you can use **one** auxiliary stack `s`. You **cannot** use any other auxiliary data structures. You can use the following queue methods: `q.dequeue()`, `q.enqueue(element)`, `q.isEmpty` and `q.size()` (that returns the number of elements in the queue). You can also use the following stack methods: `s.push(element)`, `s.pop()`, and `s.isEmpty()`.

For example, for the following queue on the left side and `target = 6`, your algorithm should produce a queue like the one on the right.



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29. (11 marks) Write an algorithm `remove(target)` to remove the node storing a given value `target` from a sorted singly linked list. If no node in the list stores value `target` then the algorithm must return `null` otherwise it must return `target`. Instance variable `first` is a reference variable pointing to the first node in the list. If `current` is a reference to a node, `current.next()` returns a reference to the next node in the list (or `null` if `current` points to the last node in the list), `current.setNext(succ)` makes the node referenced by `current` point to node `succ`, and `current.getElement()` returns the data item stored in the node pointed by `current`.

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