

# University of Maryland Electron Ring (UMER)

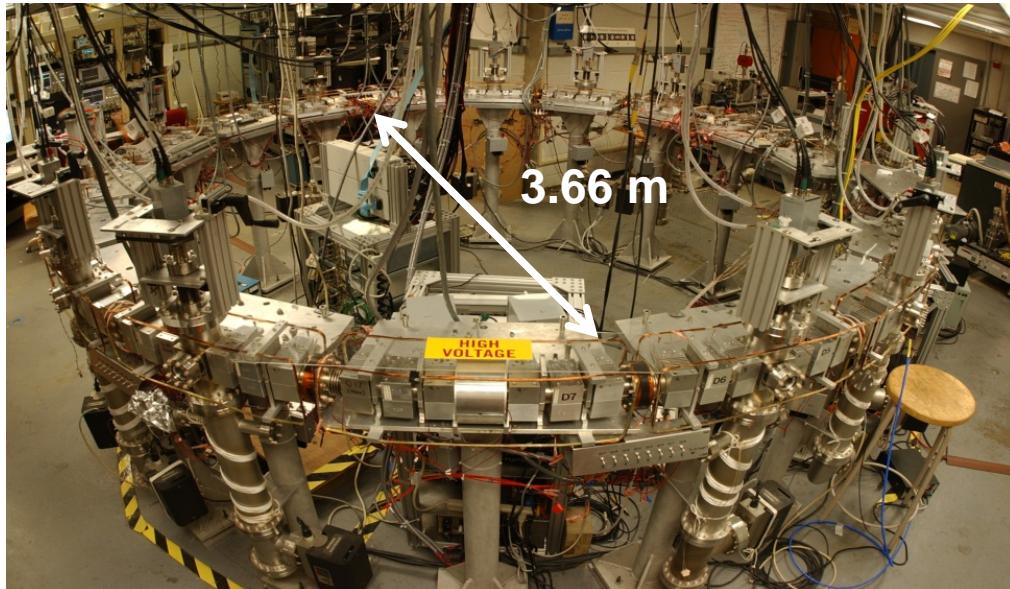
June 23, 2016

Brian L. Beaudoin  
UMER Faculty and Students



**Institute for Research in Electronics & Applied Physics  
Energy Research Facility  
College Park, MD, USA**

# Background on UMER



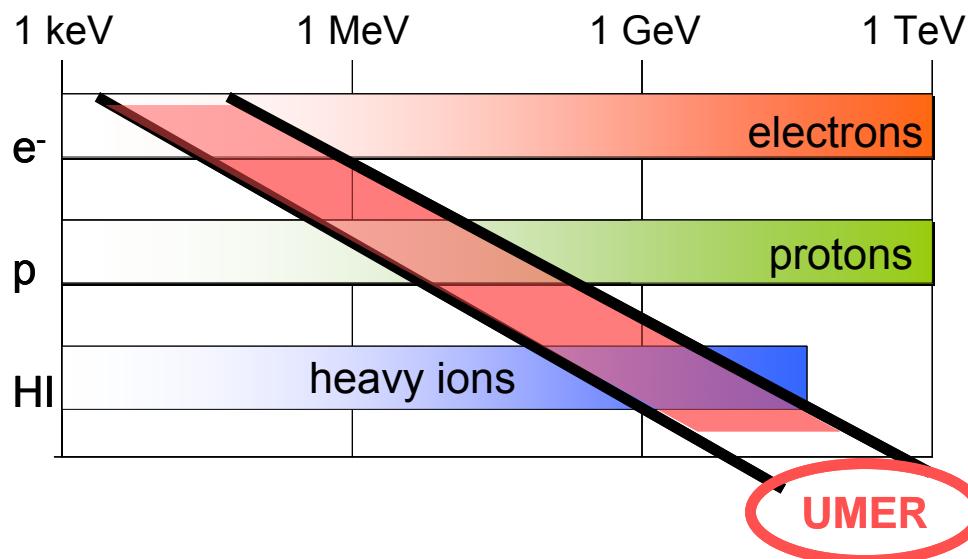
UMER spans a broad range of intensities through the use of the aperture plate

APERTURE PLATE

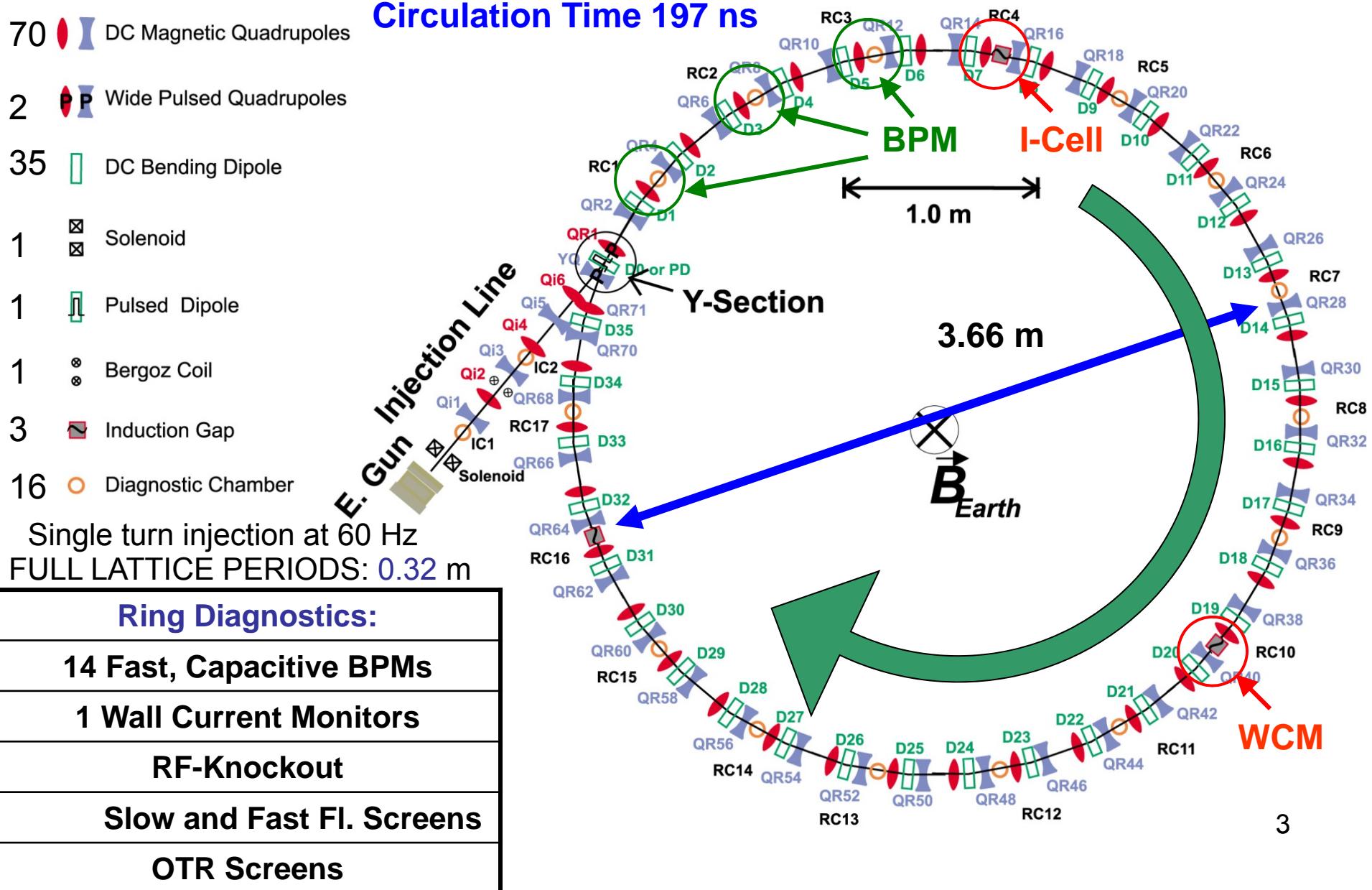


## Parameters

Energy: 10keV  
Rigidity: 3.38E-4T-m  
Current: 0.06-100mA  
Tune: 6.76  
Tune Shift: 0.045-0.96  
Chromaticity: -7.9  
Momentum Compaction Factor: 0.0204  
Size: 1.5-10mm  
Emittance: 7.6-64 mm mr  
Avg Earth Field: 400mG

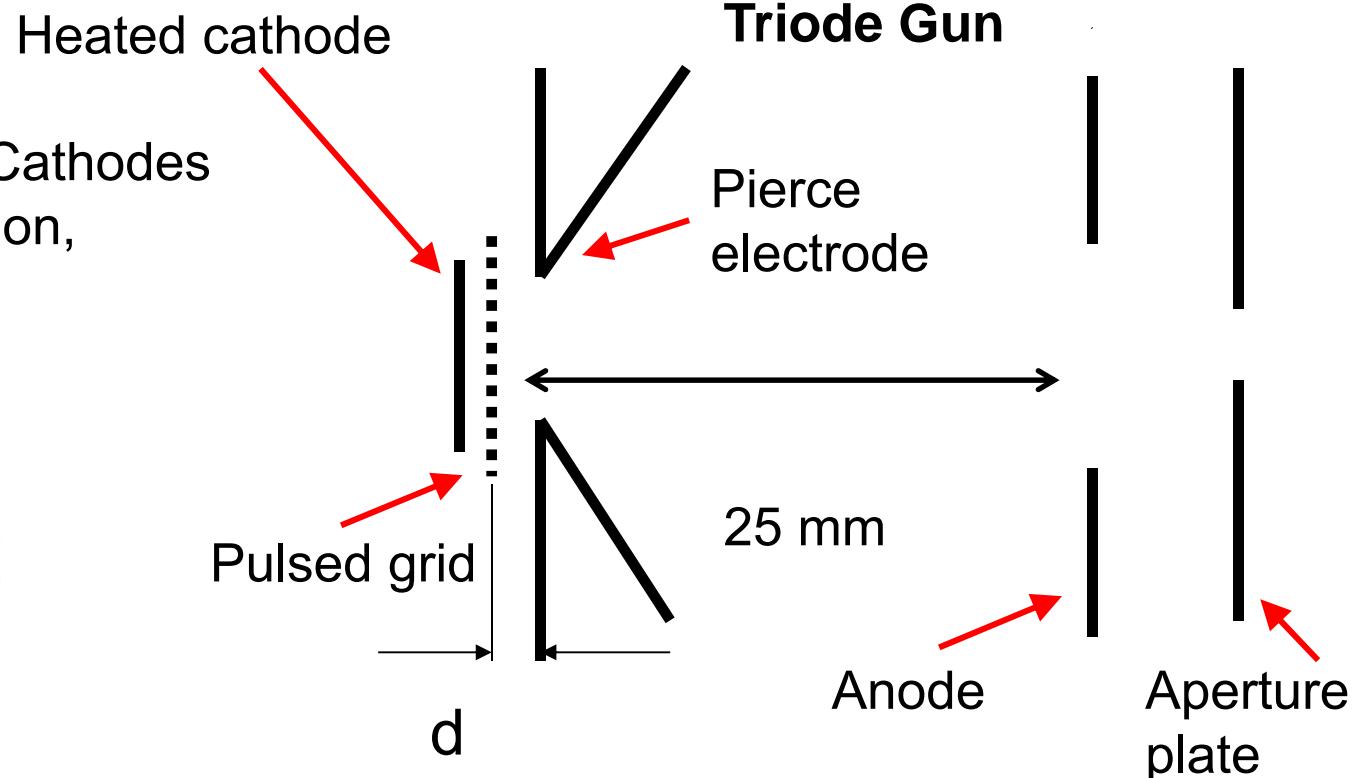


# University of Maryland Electron Ring

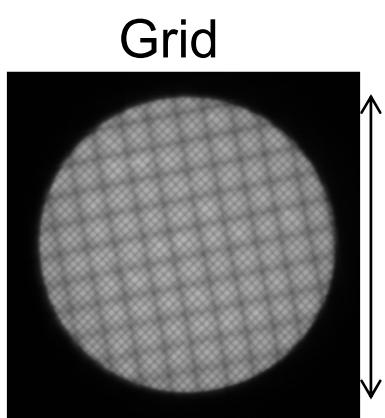
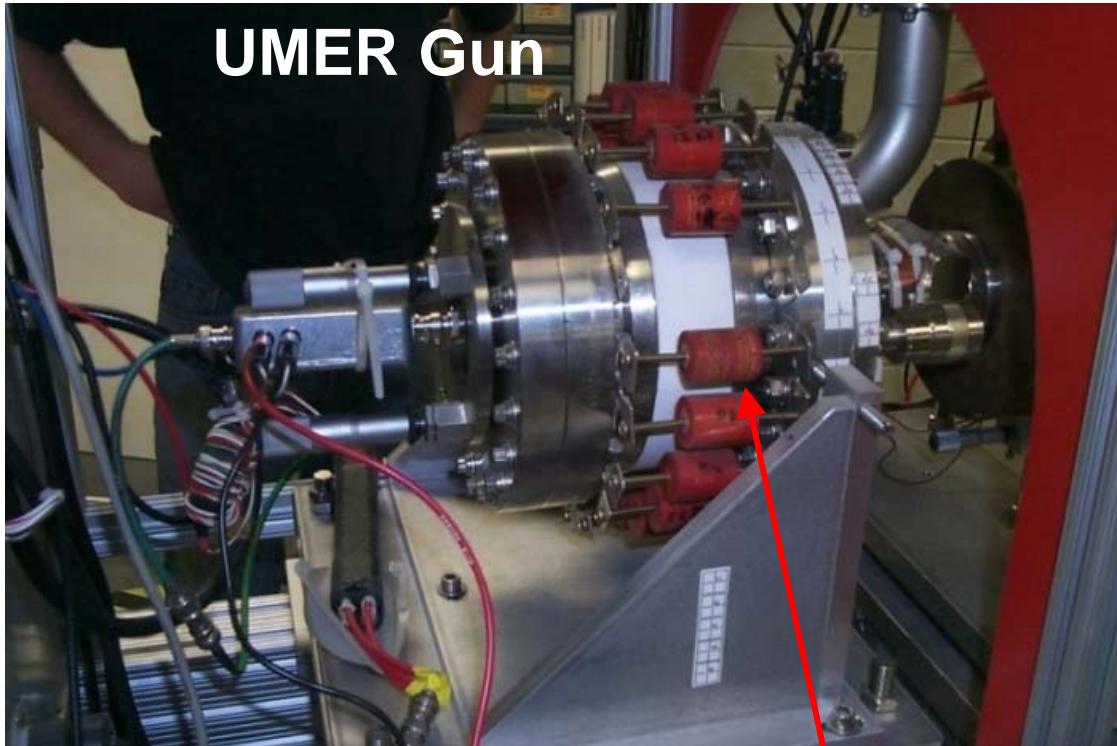


# Thermionic Electron Sources

Standard Dispenser Cathodes  
(3-5A/cm<sup>2</sup> CW emission,  
15A/cm<sup>2</sup> pulsed)



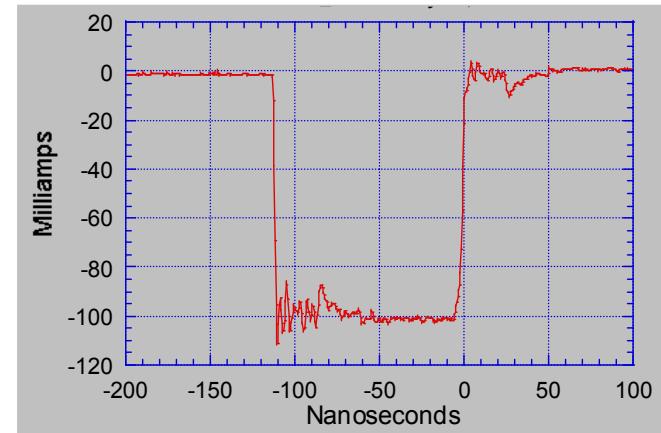
# UMERs Pulsed Electron Gun



Capacitor bank between  
cathode and anode

5 ns laser pulse

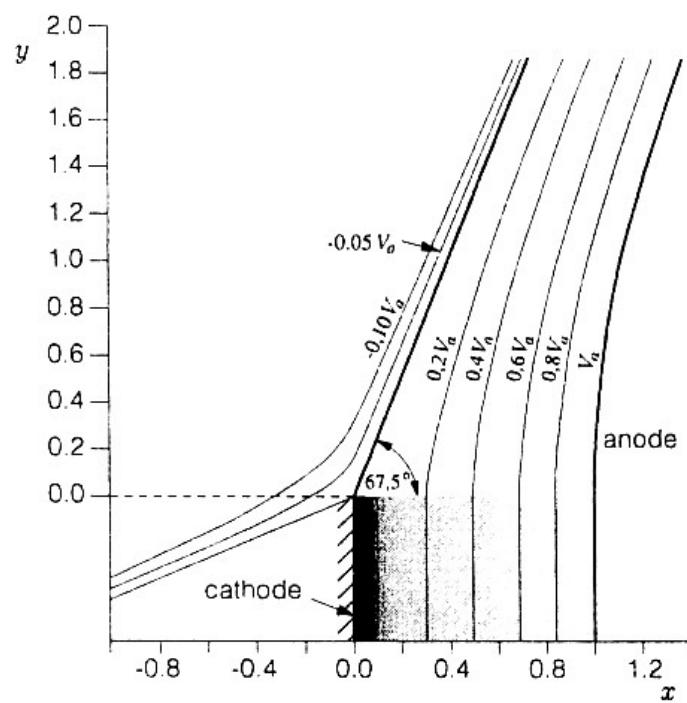
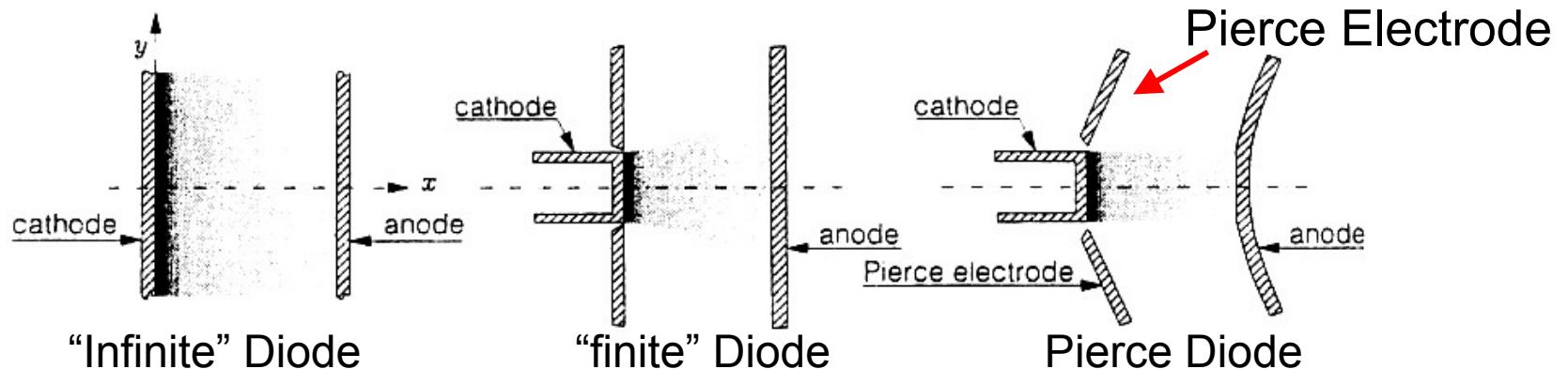
Extracted current pulse with  
a Pulse Forming Line (PFL)



Extracted current pulse with  
a laser and thermionic pulse



# Pierce Electrode Geometry



Assume  $V(x) \propto x^{4/3}$ , outside beam for finite (in  $y$ -direction) diode.

Use complex formalism  $x \rightarrow r e^{i\varphi} = \xi + i\zeta$ ,  $V \rightarrow W = V_R + iV_R$ .

Then  $V_R \propto r^{2/3} \cos[(4/3)\arctan(\zeta/\xi)]$ .

Since cathode is grounded,  $V_R = 0$ , so we need  $(4/3)\arctan(\zeta/\xi) = \pi/2$ , or slope at  $x=0$  is

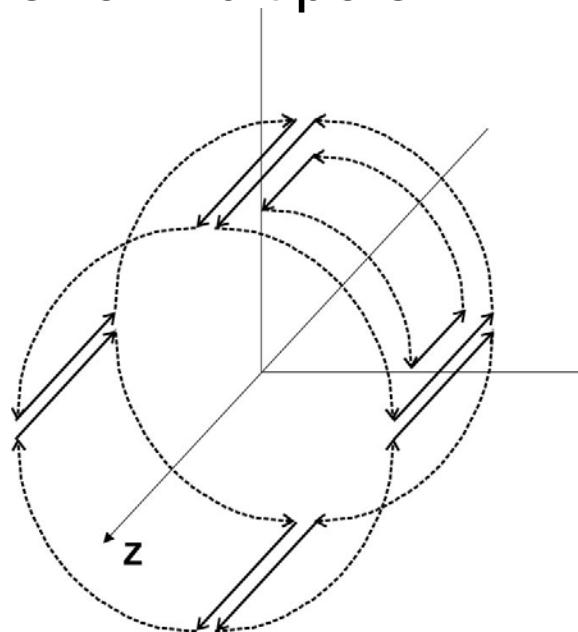
$$(3/4)\pi/2 = 67.5^\circ$$

# Printed Circuit (PC) Dipole and Quadrupole

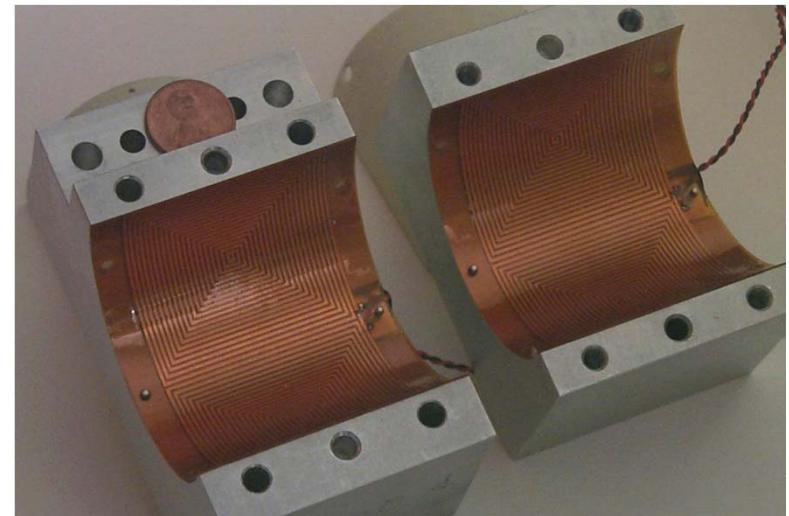
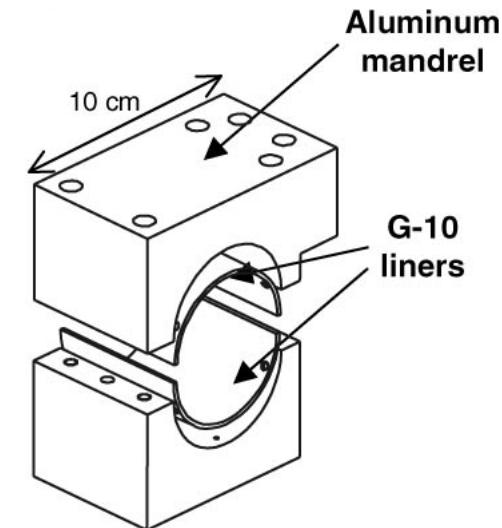
On a circular cylindrical surface,

we want:  $\int K_z dz \propto \cos n\theta$

$n$ =order of multipole.

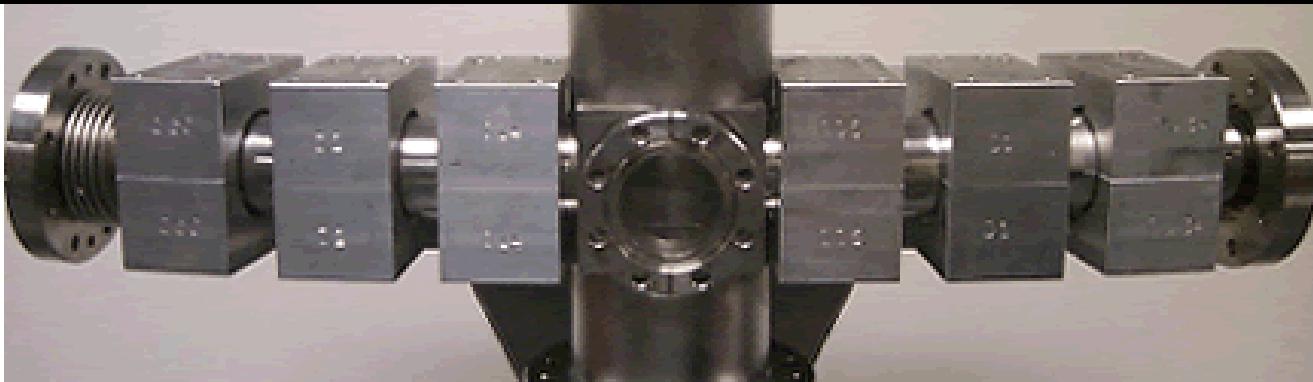


Only conductors parallel to z-axis contribute to integrated  $B$ -field.

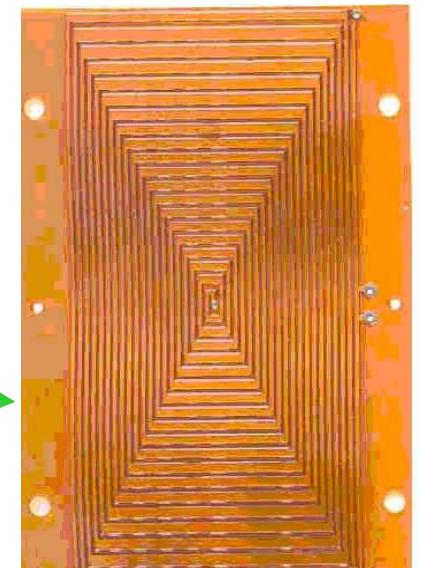
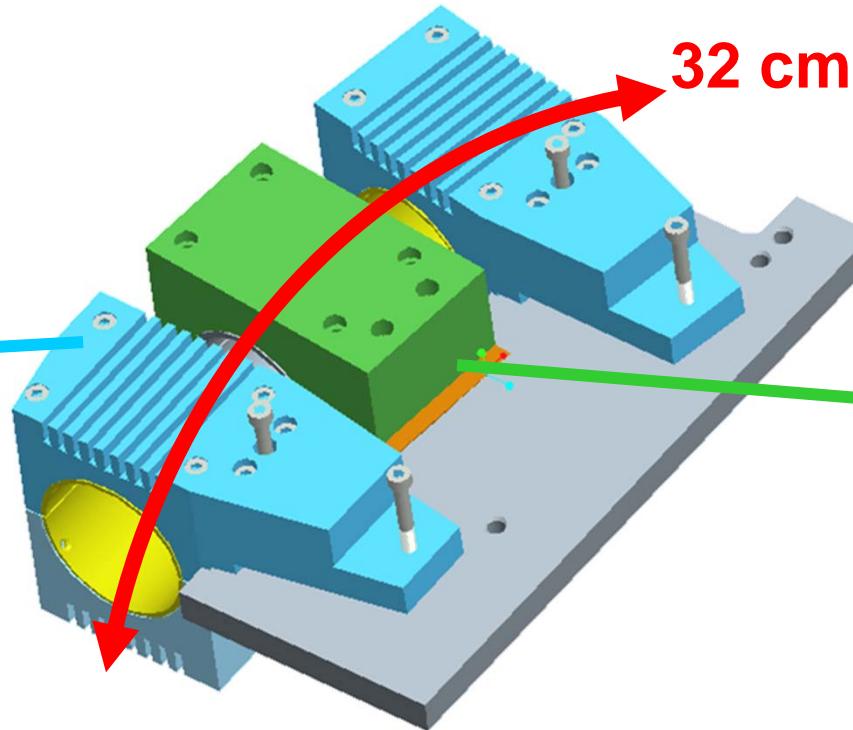
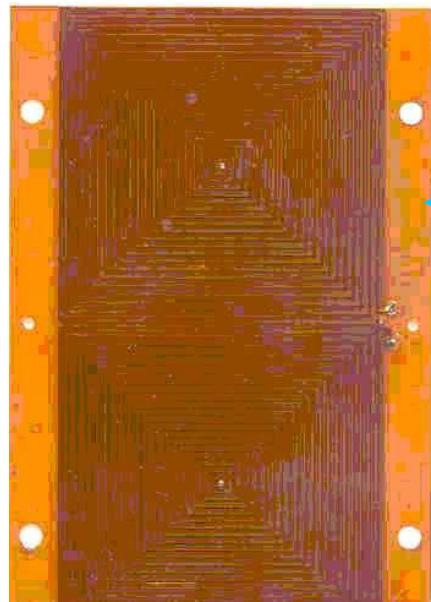


UMER PC quadrupole

# Standard UMER Magnets & Lattice



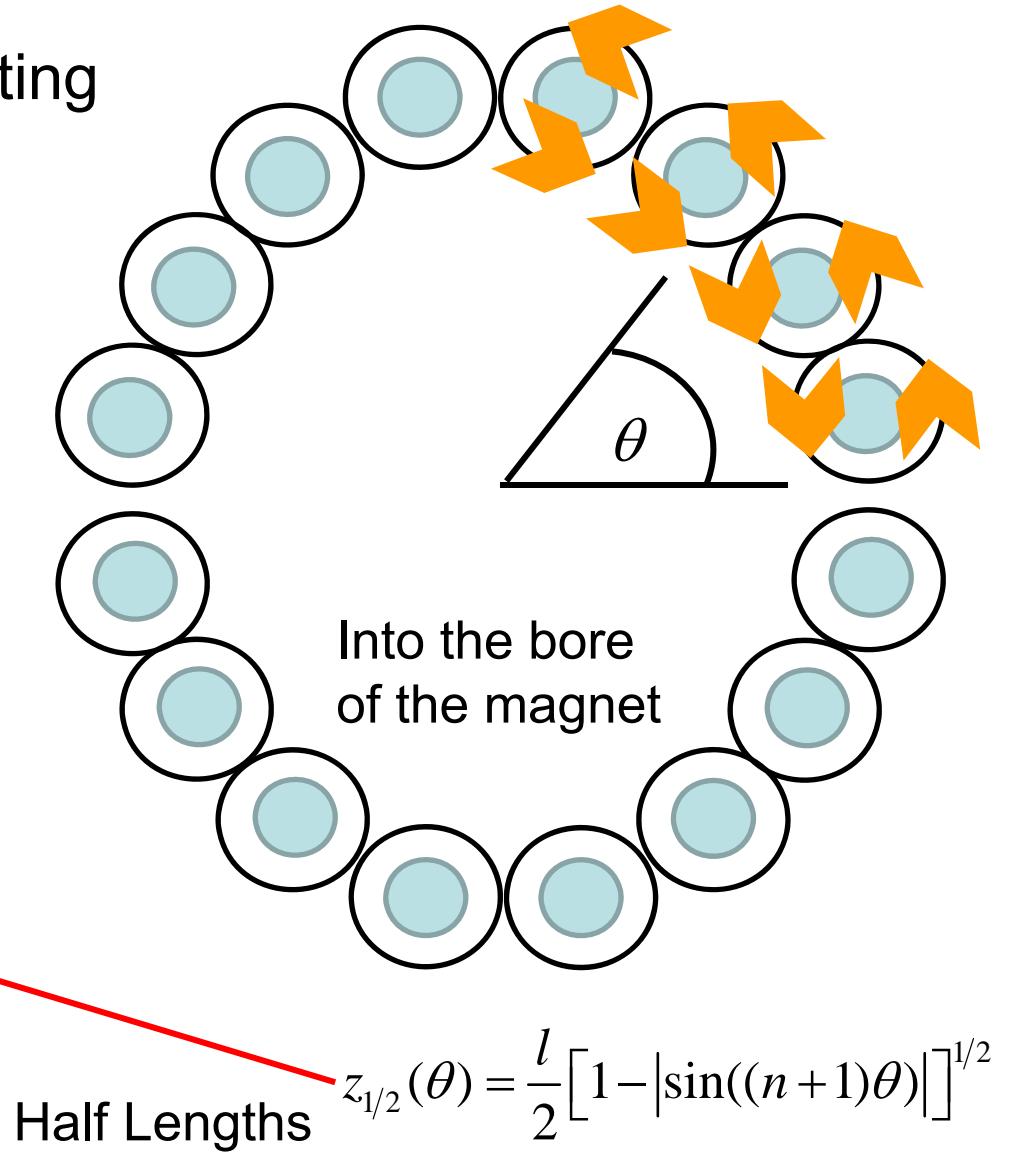
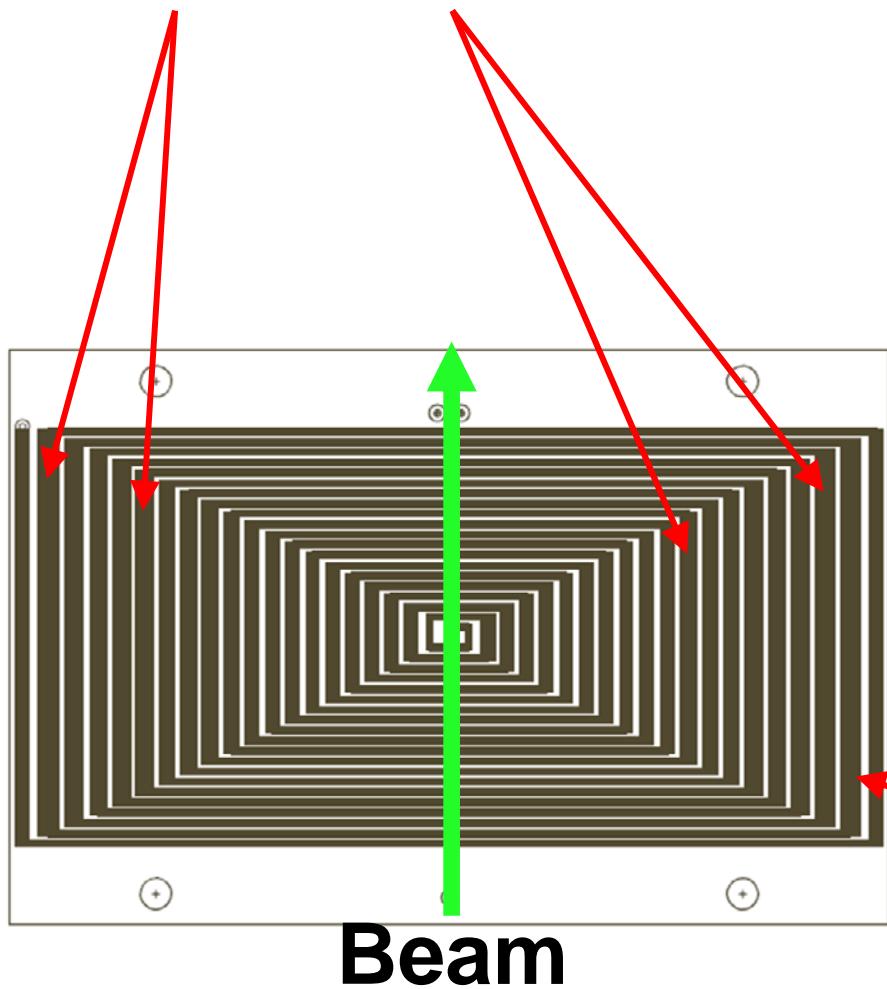
**72 Quads**  
(~ 30 G peak)



**36 Dipoles**  
(~ 15 G peak)

# Multiple Conductors in a PC Dipole

These conductors are contributing most to the total field



# Multipole Expansion

2D Multipole Expansion:

$K_n$  is complex

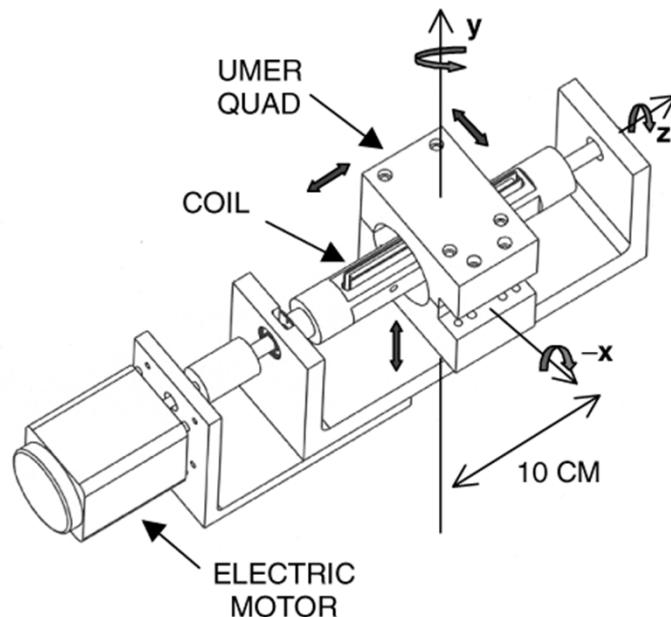
$r$  is real

$$B_y + iB_x = \sum_{n=0}^{\infty} K_n (x + iy)^n = \sum_{n=0}^{\infty} K_n r^n e^{in\theta}$$

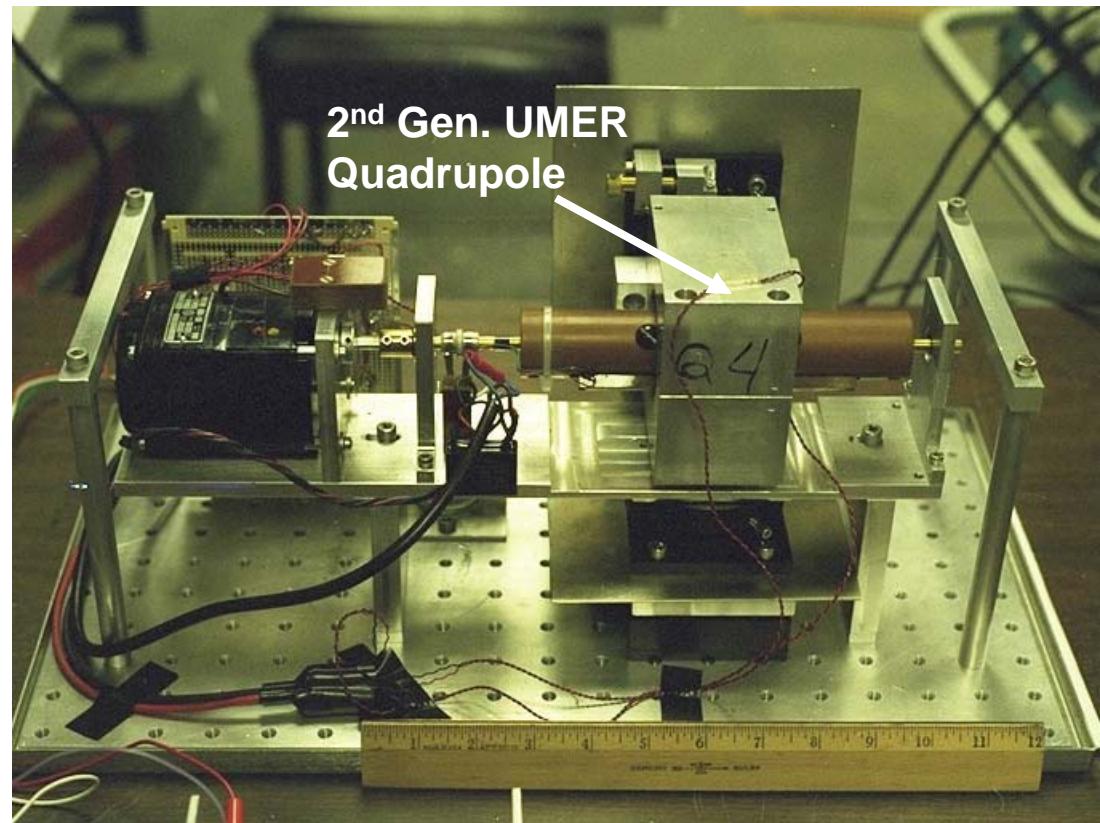
$$= \sum_{n=0}^{\infty} |K_n| e^{i\delta_n} r^n e^{in\theta}$$

$n = 0 \Rightarrow B_x = 0$	$; B_y =  K_0 $	$\equiv$ dipole	$ K_0 $ Amplitude
$n = 1 \Rightarrow B_x(r,0) = 0$	$; B_y(r,0) = r K_1 $	$\equiv$ quadrupole	
	$B_x(r,\pi/2) = r K_1 $	$; B_y(r,\pi/2) = 0$	
		$= -B_{x,y}(r,\theta)$	
$n = 2 \Rightarrow B_x(r,0) = 0$	$; B_y(r,0) = r^2 K_2 $	$\equiv$ sextupole	
	$B_x(r,\pi/4) = r^2 K_2 $	$; B_y(r,\pi/4) = 0$	
		$= -B_{x,y}(r,\theta)$	

# UMER Rotating Coil\*

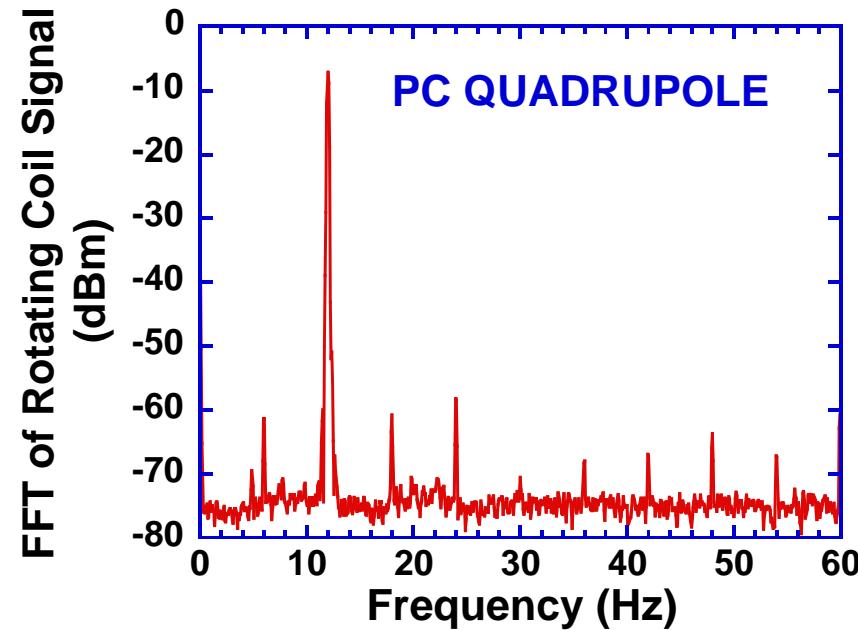
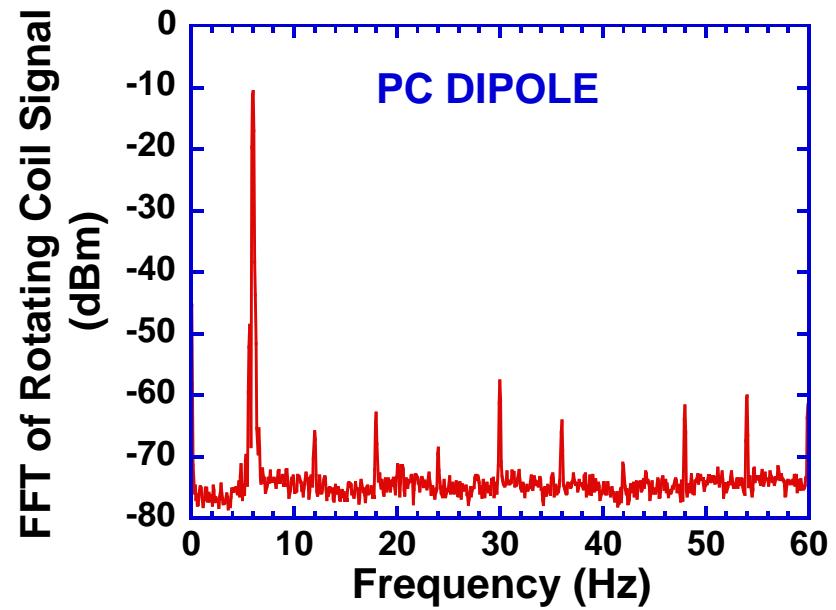
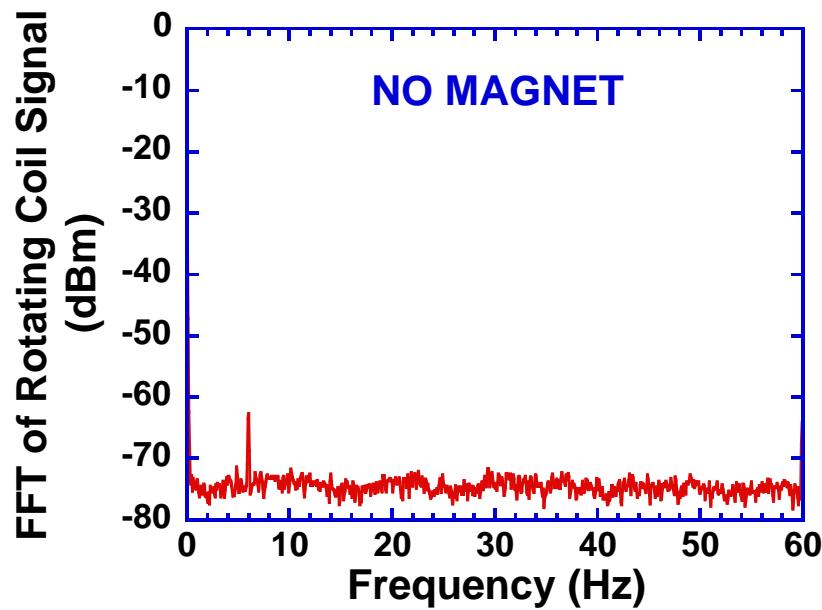


The coil contains  $\sim$ 3000 turns of very fine wire.  
The whole of the rotating coil apparatus is normally enclosed in mu-metal box.



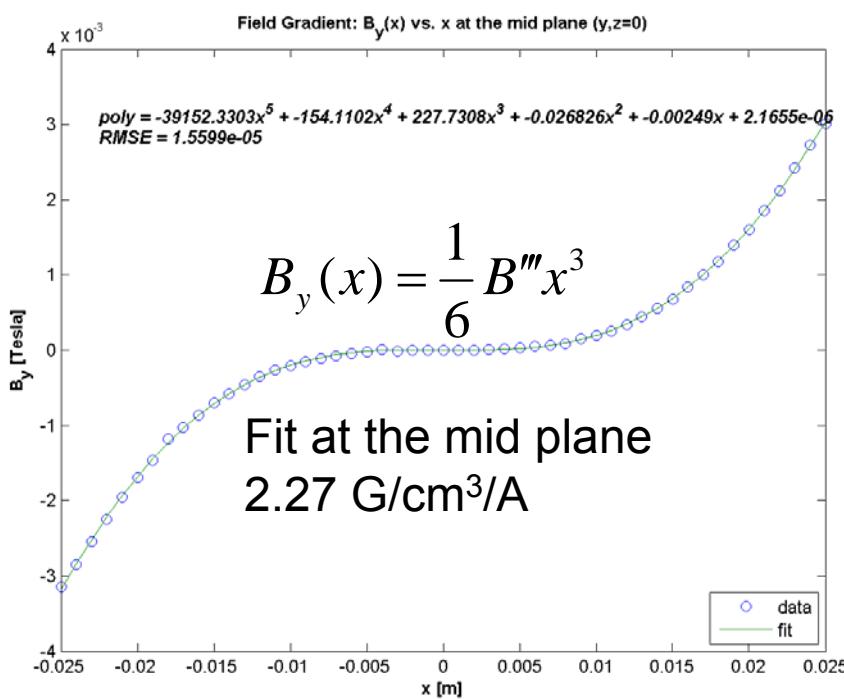
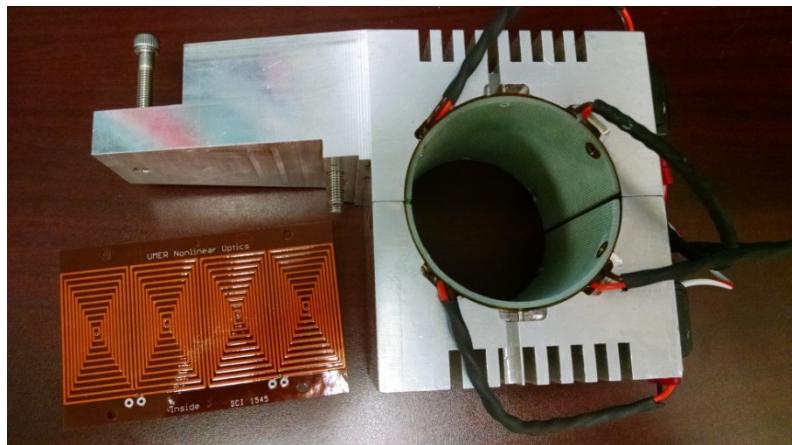
A rectangular rotating coil is positioned along the axis of the magnet. An FFT of the induced voltage details the harmonic content of the magnetic field.

# FFT of Rotating Coil Signal

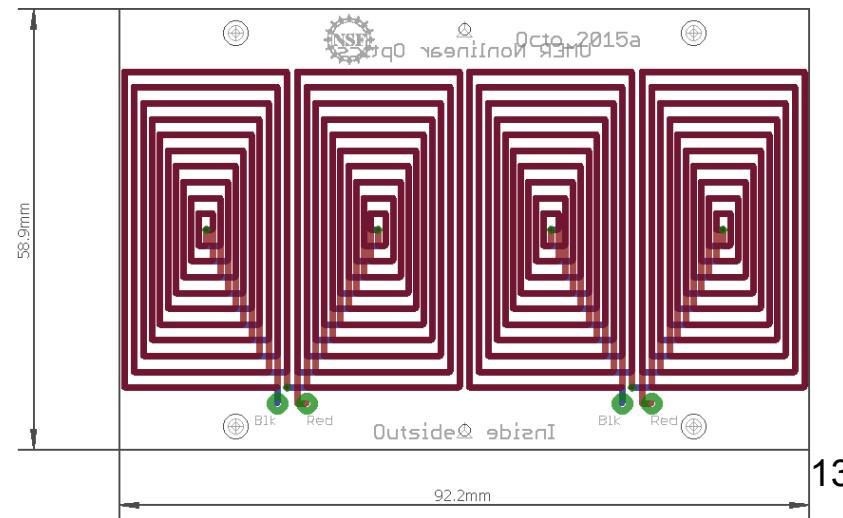
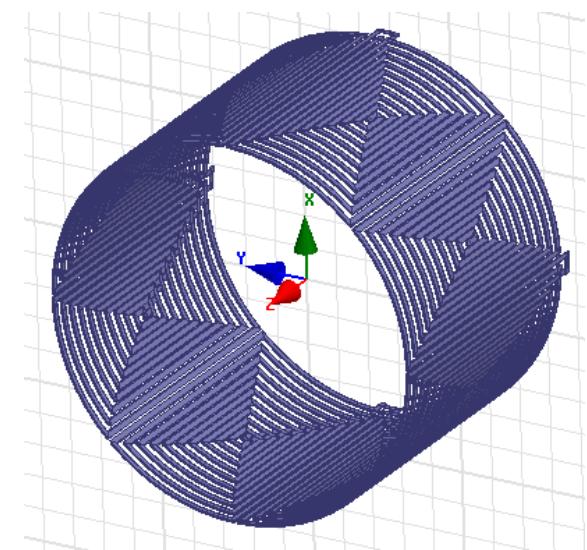


# 1<sup>st</sup> Generation PC Octupoles

Designed by (UG) David Matthew and Kiersten Ruisard

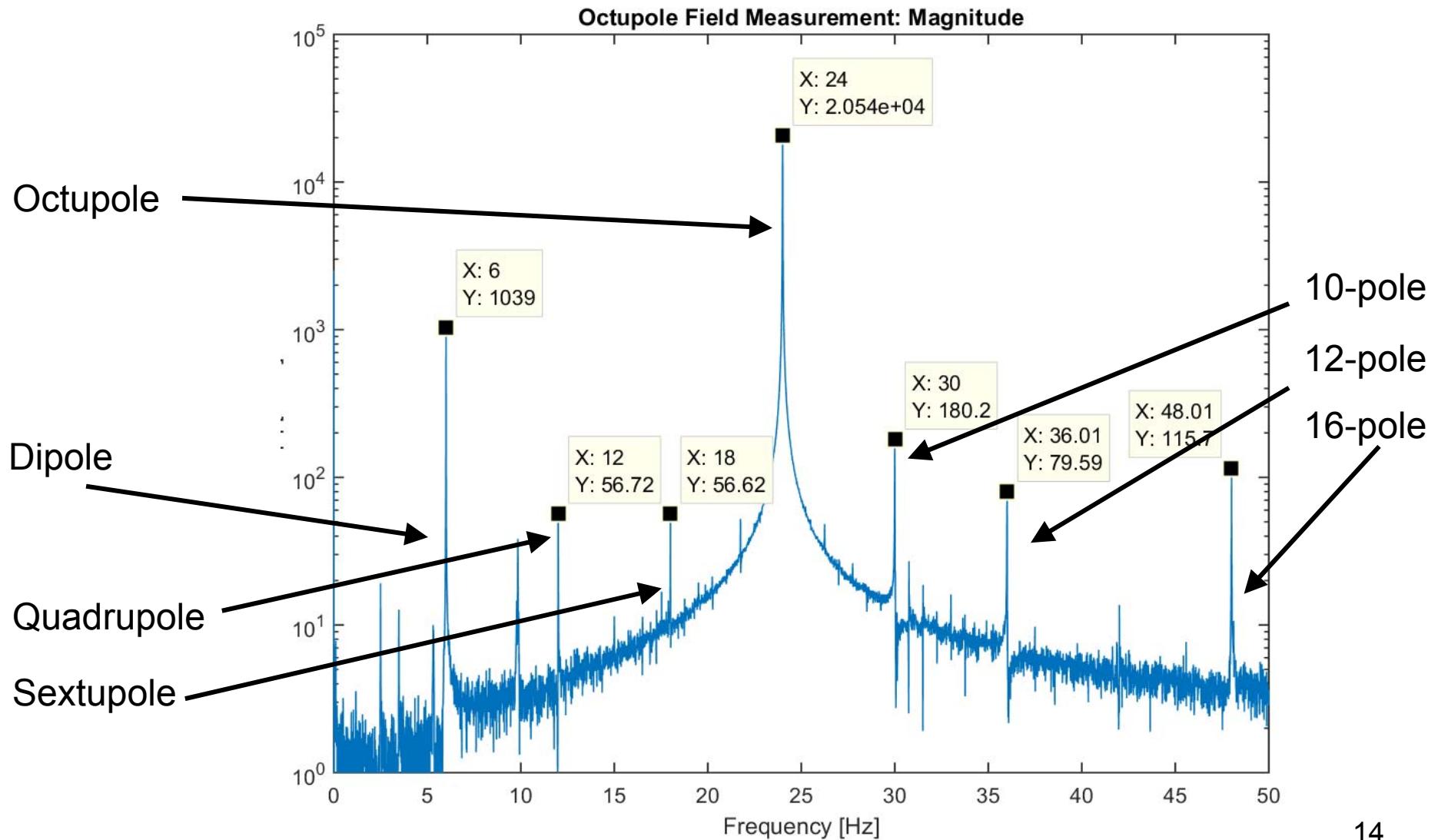


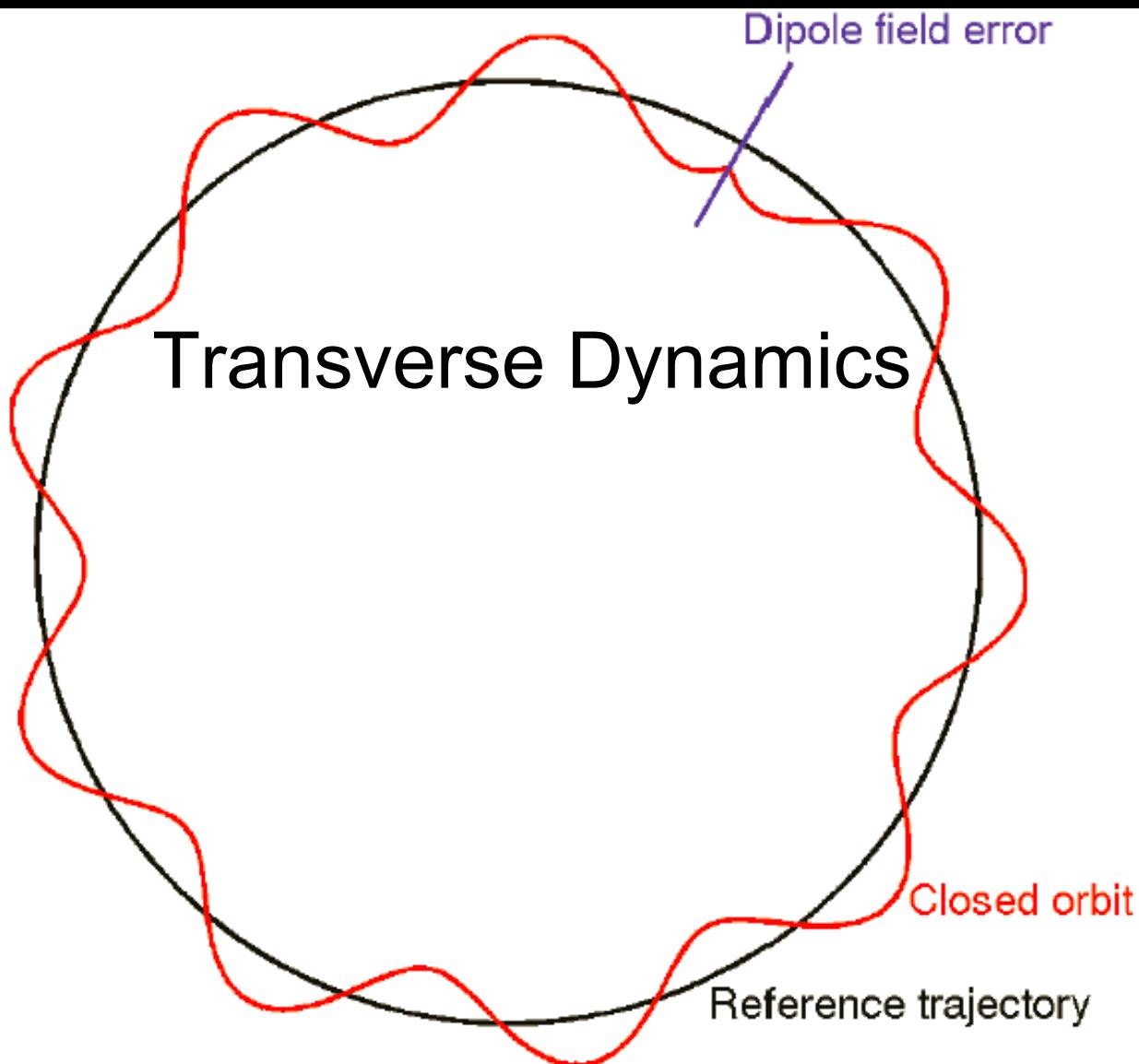
Maxwell model



# Measuring the Multipole Content of the Octupole

FFT Scope Data

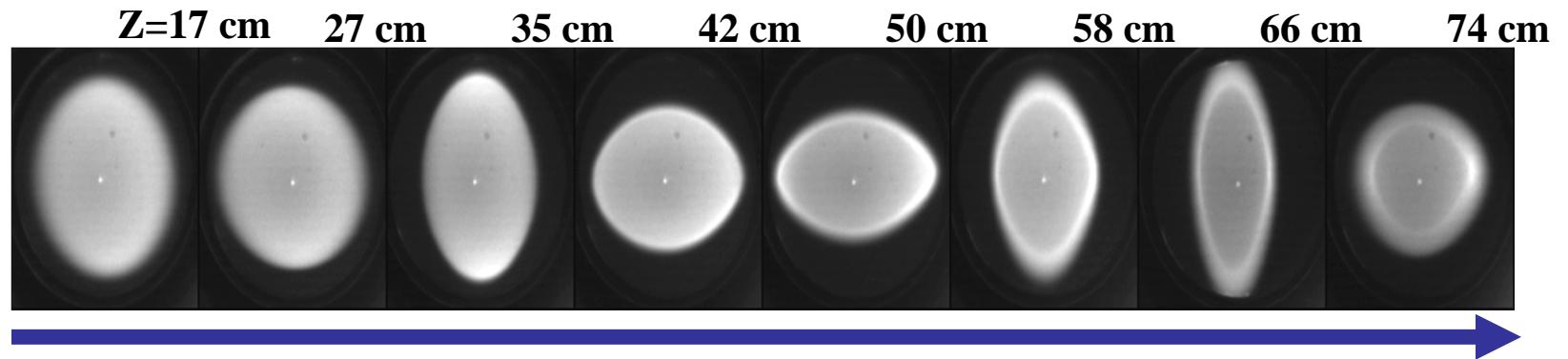




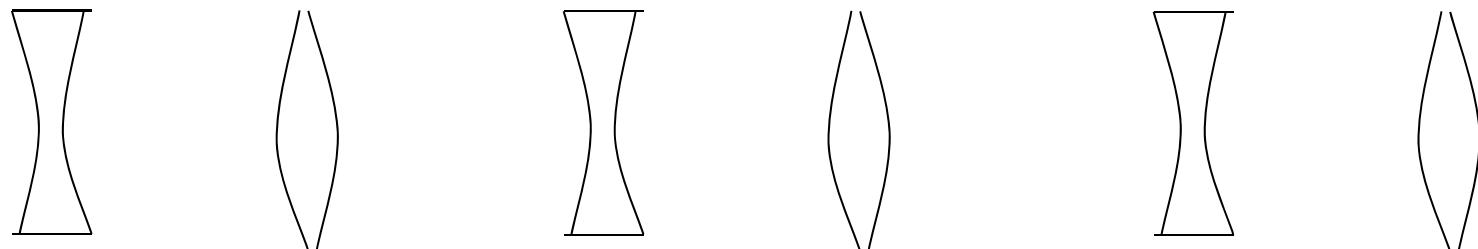
# Beam Transport Down Quadrupole Line

Phosphor screen images of the beam

Gun



$z \sim 0.15 - 1\text{ m}$



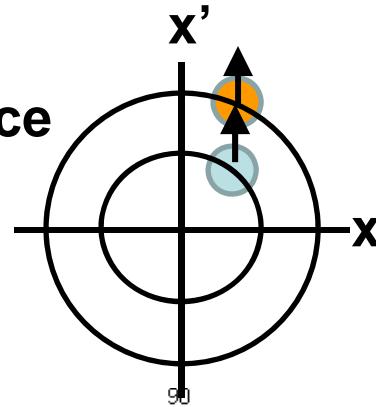
Bernal, Kishek, Haber, and Reiser, PRL, **82**, 4002 (1999).

Kishek, O'Shea, Reiser, PRL, **85**, 4514 (2000).

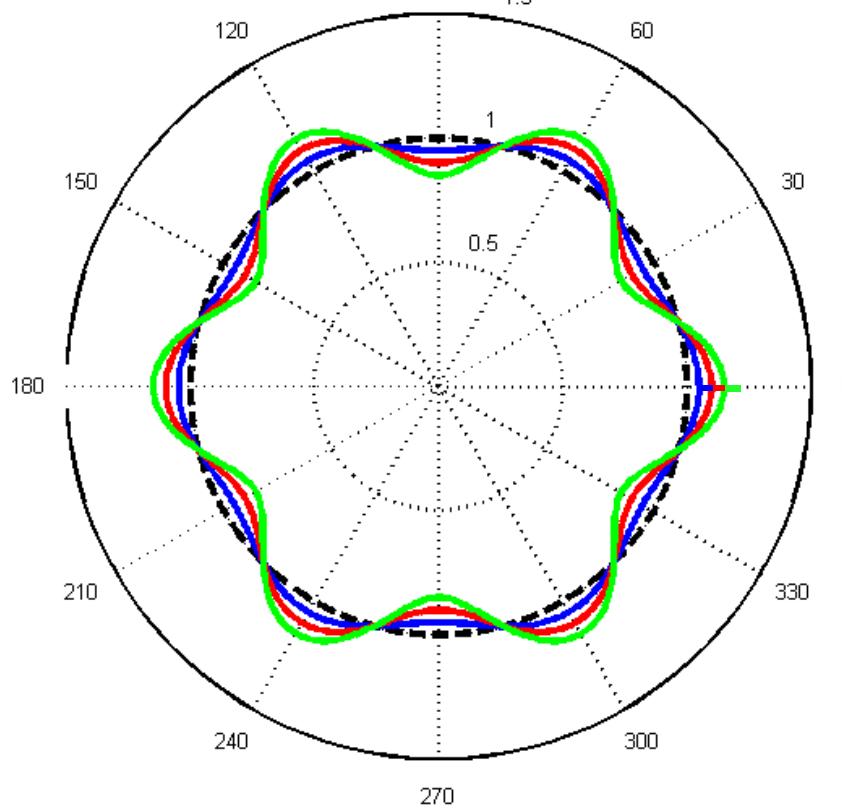
Reiser, Sec. 7.3.5, 7.3.6.1

# Integer and Half-Integer Resonances

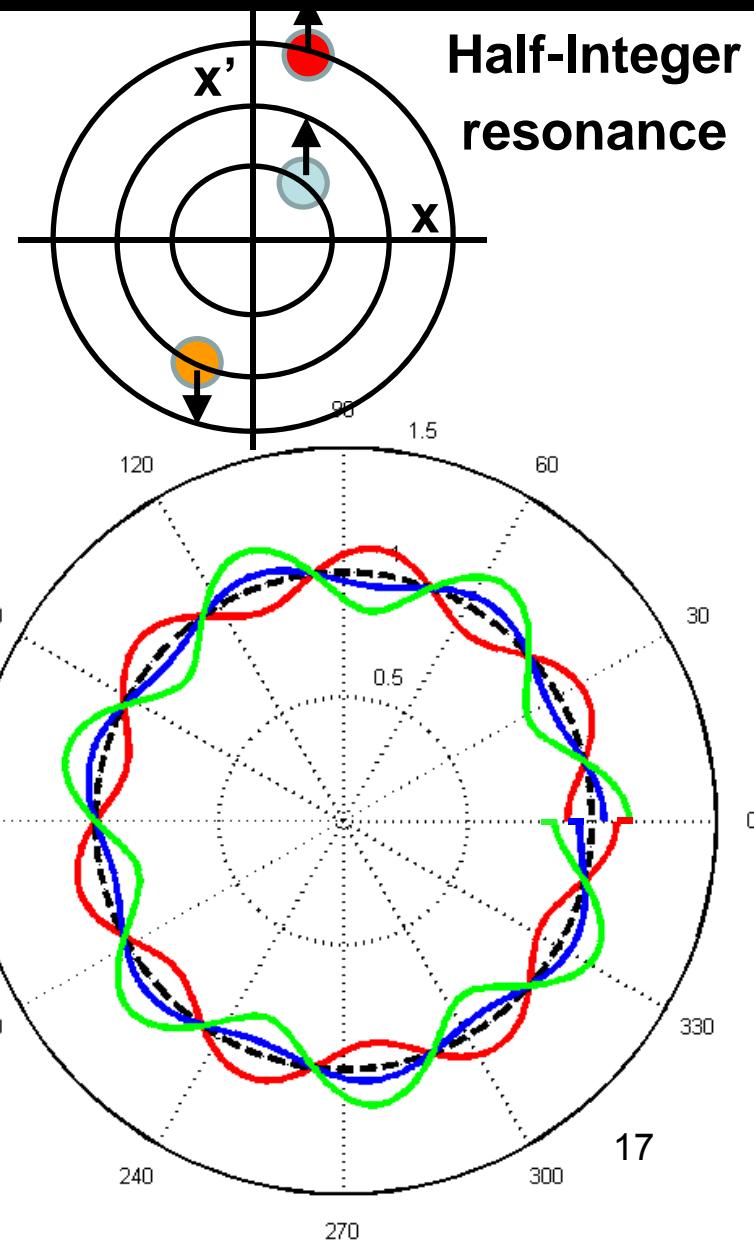
Integer Resonance



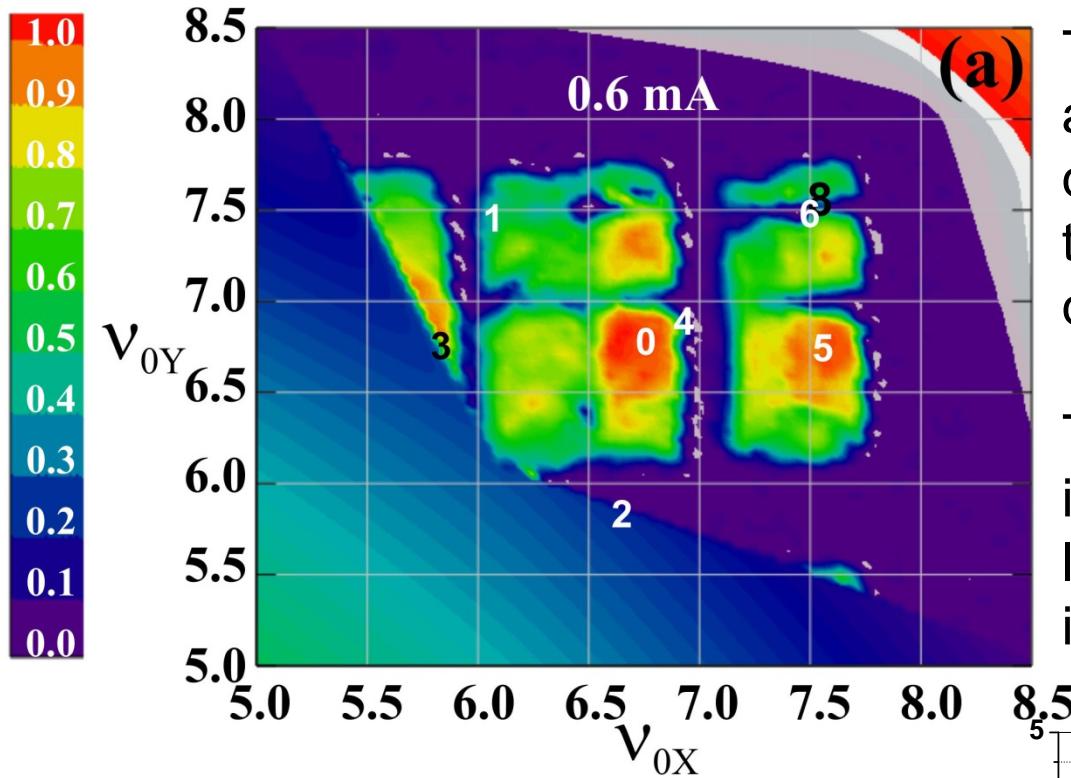
Dipole errors in the accelerator perturbs beam motion



Half-Integer resonance



# Quadrupole Tune Scans

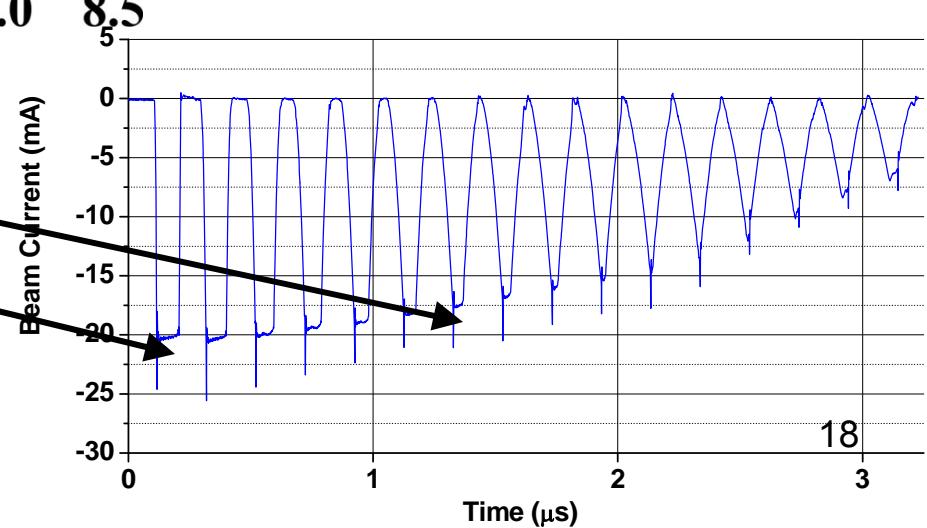


The current traces shown below are taken as a function of the quadrupole currents. We vary both the horizontal and vertical quadrupoles.

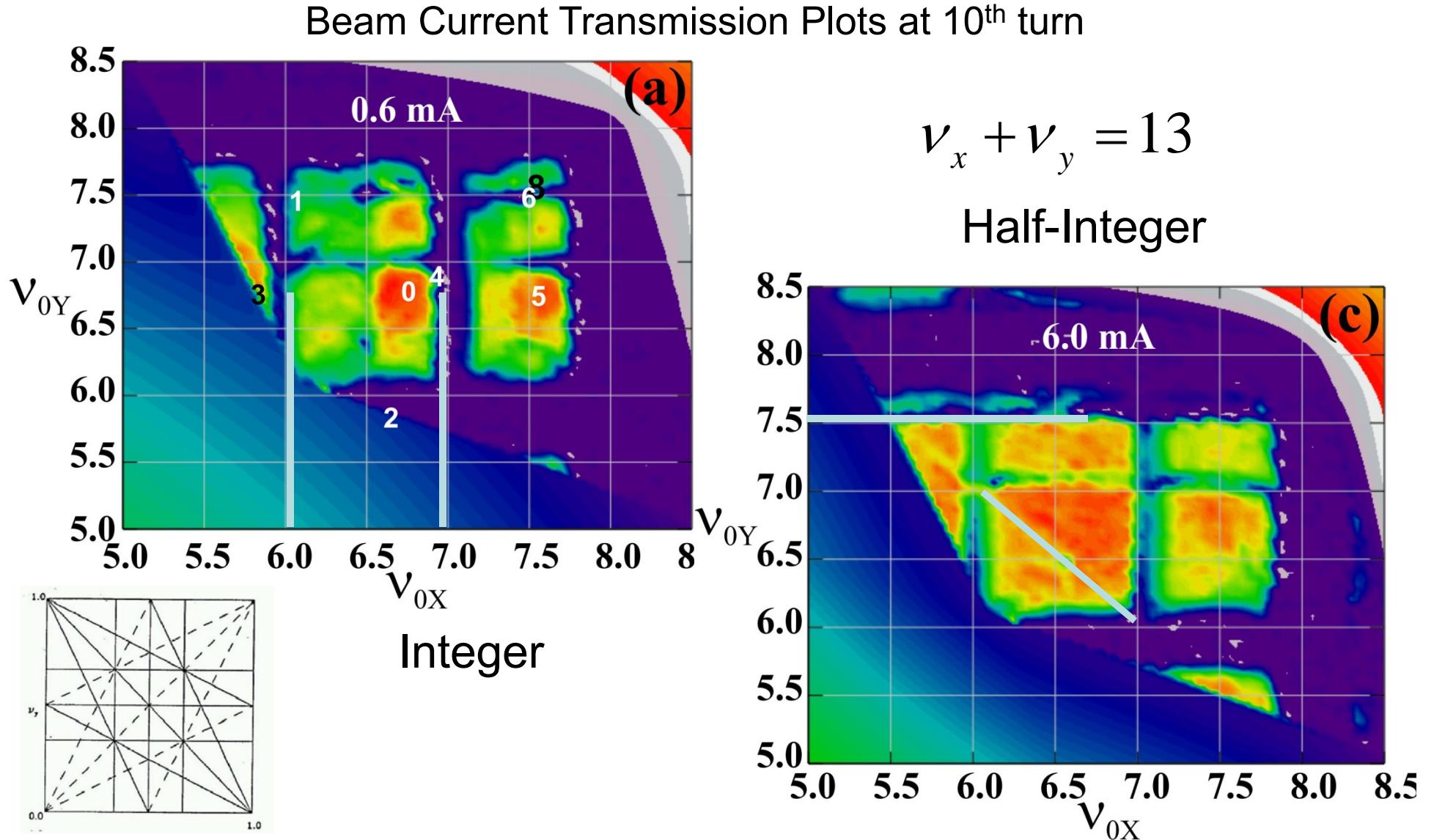
The regions of no transmission indicate current loss at the integer lines, the beam resonantly kicked itself out of the machine.

$$\text{Intensity}_{\text{Turn}} = \frac{I_{\text{Turn}}}{I_1}$$

Duration the beam survives over multiple turns

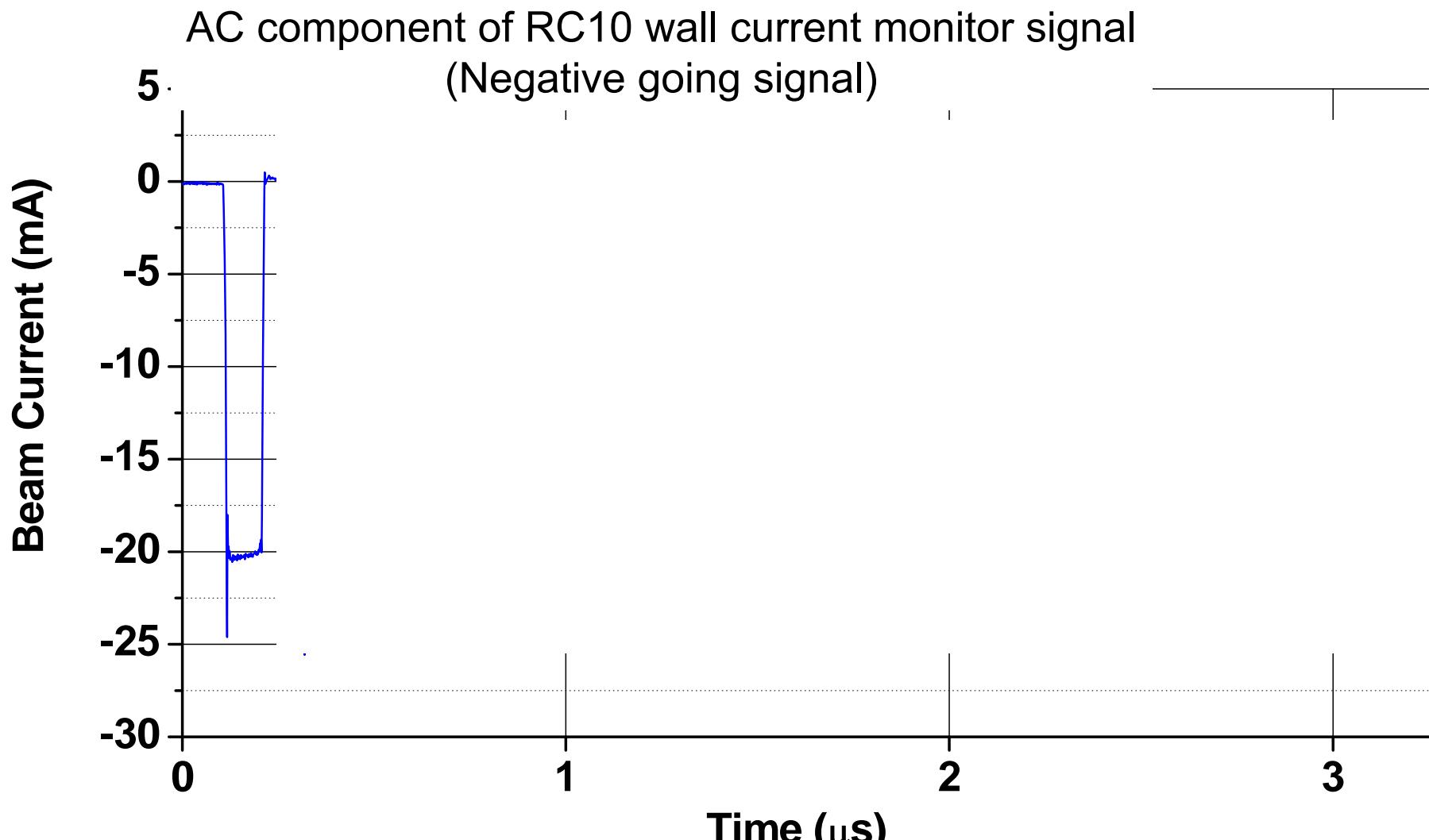


# Quadrupole Tune Scans vs Beam Current



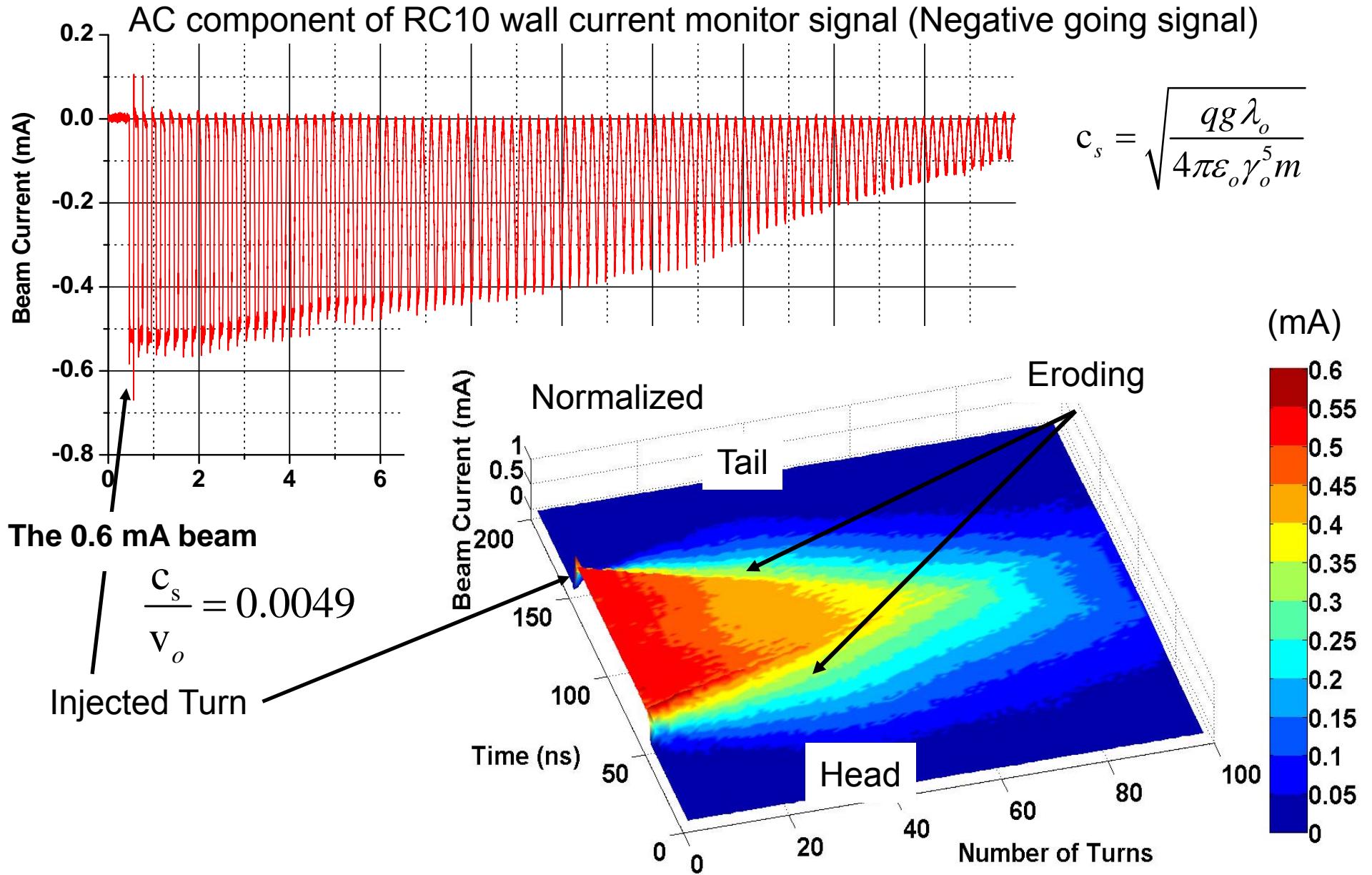
# Longitudinal Dynamics without Barrier Buckets

# Longitudinal Space-Charge Forces Diminishes the Bunch Shape



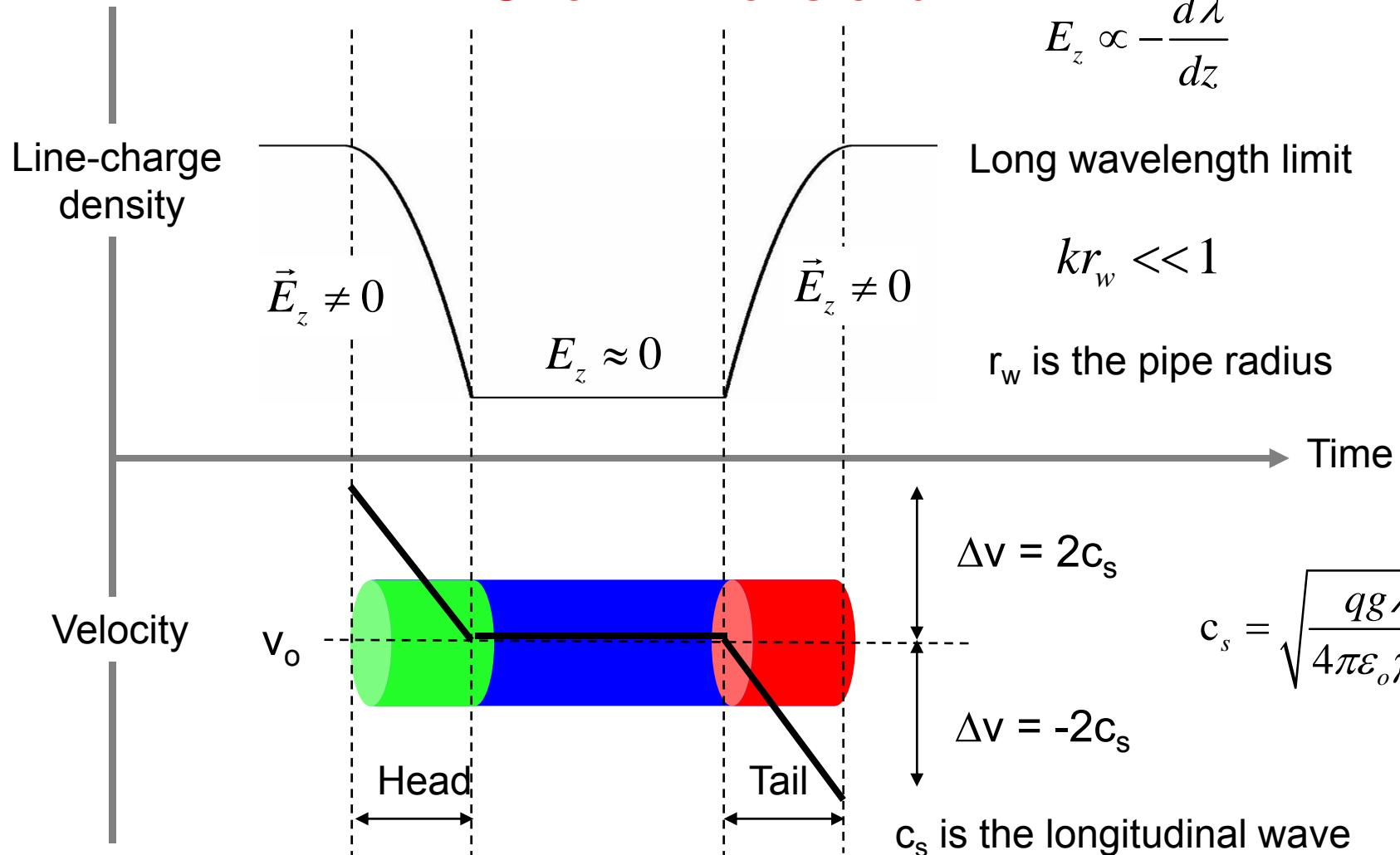
Injected Turn  
21 mA

# Longitudinal Bunch Erosion of Bunch Current



# Longitudinal Space-Charge Physics

## One - Dimensional



-CERN 77-13, 19 July 1977,

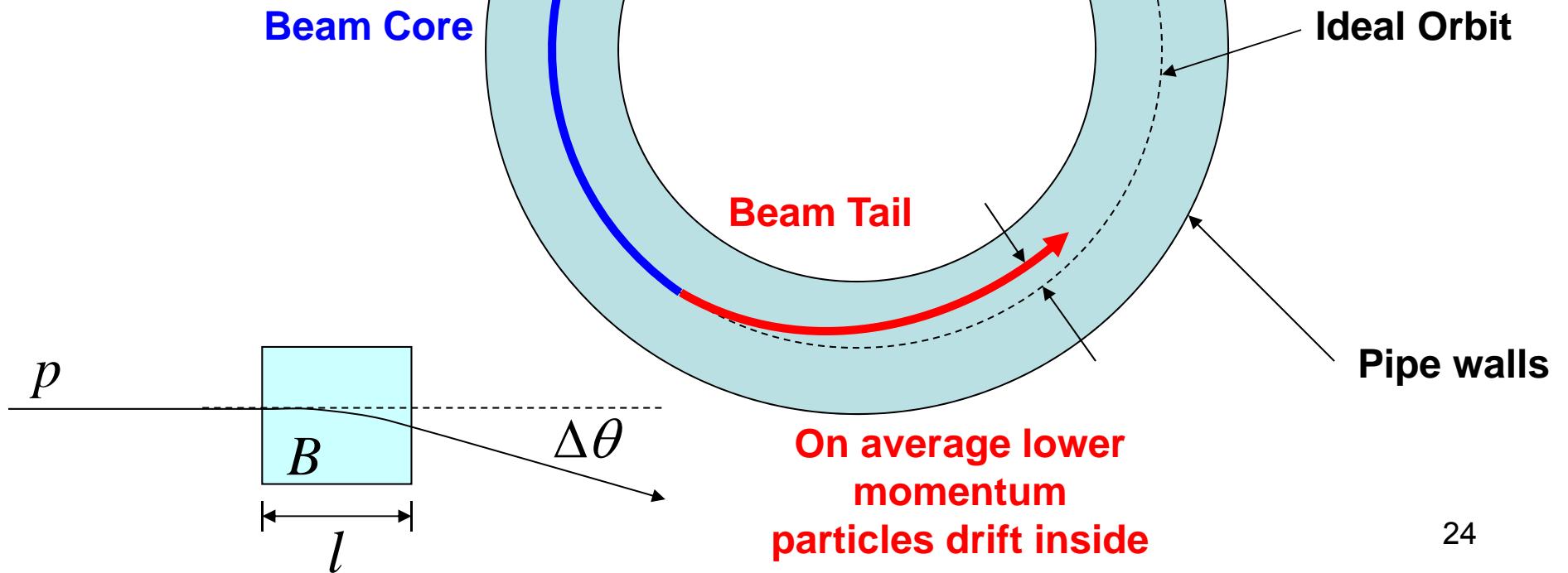
"Theoretical Aspects of the Behavior of Beams in Accelerators and Storage Rings"

-A. Faltens, E.P. Lee, and S.S. Rosenblum, Journal of Applied Physics, 61, 5219, (1987).

# Space-Charge Driven Transverse-Longitudinal Correlation

$$\rho = \frac{p}{eB}$$

$$\Delta\theta \approx \frac{p_\perp}{p} = \frac{Bl}{(B\rho)}$$

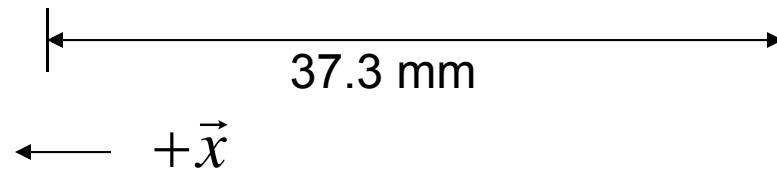
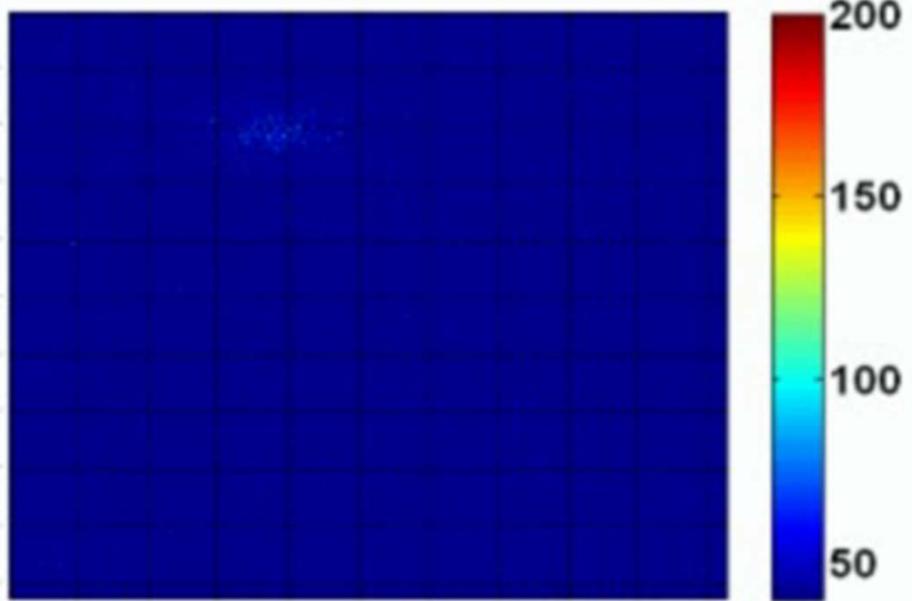
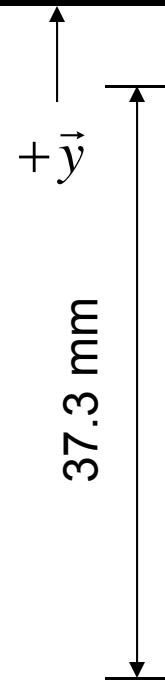
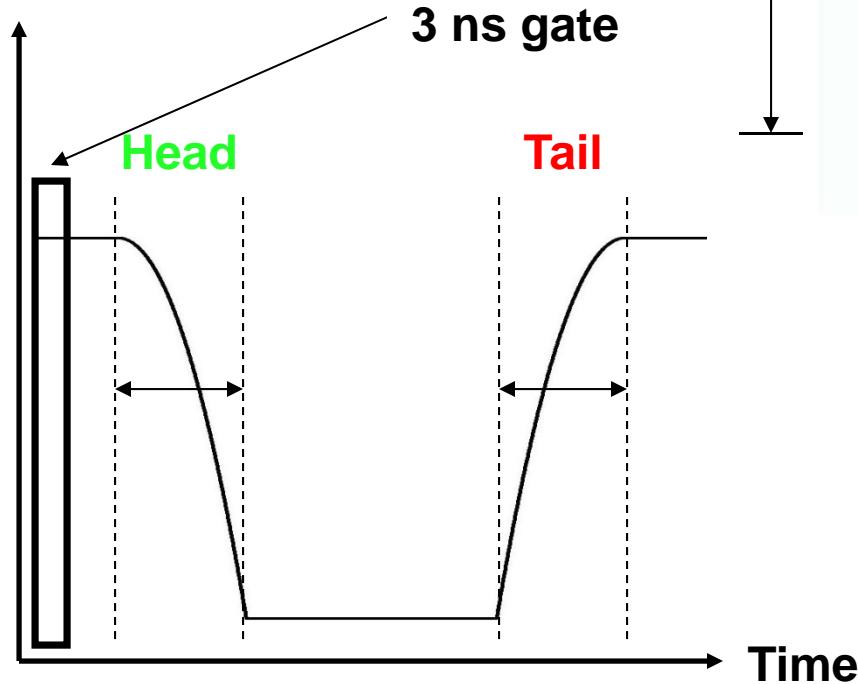


# Time Resolved Measurement of Beam Ends

**21 mA Beam**

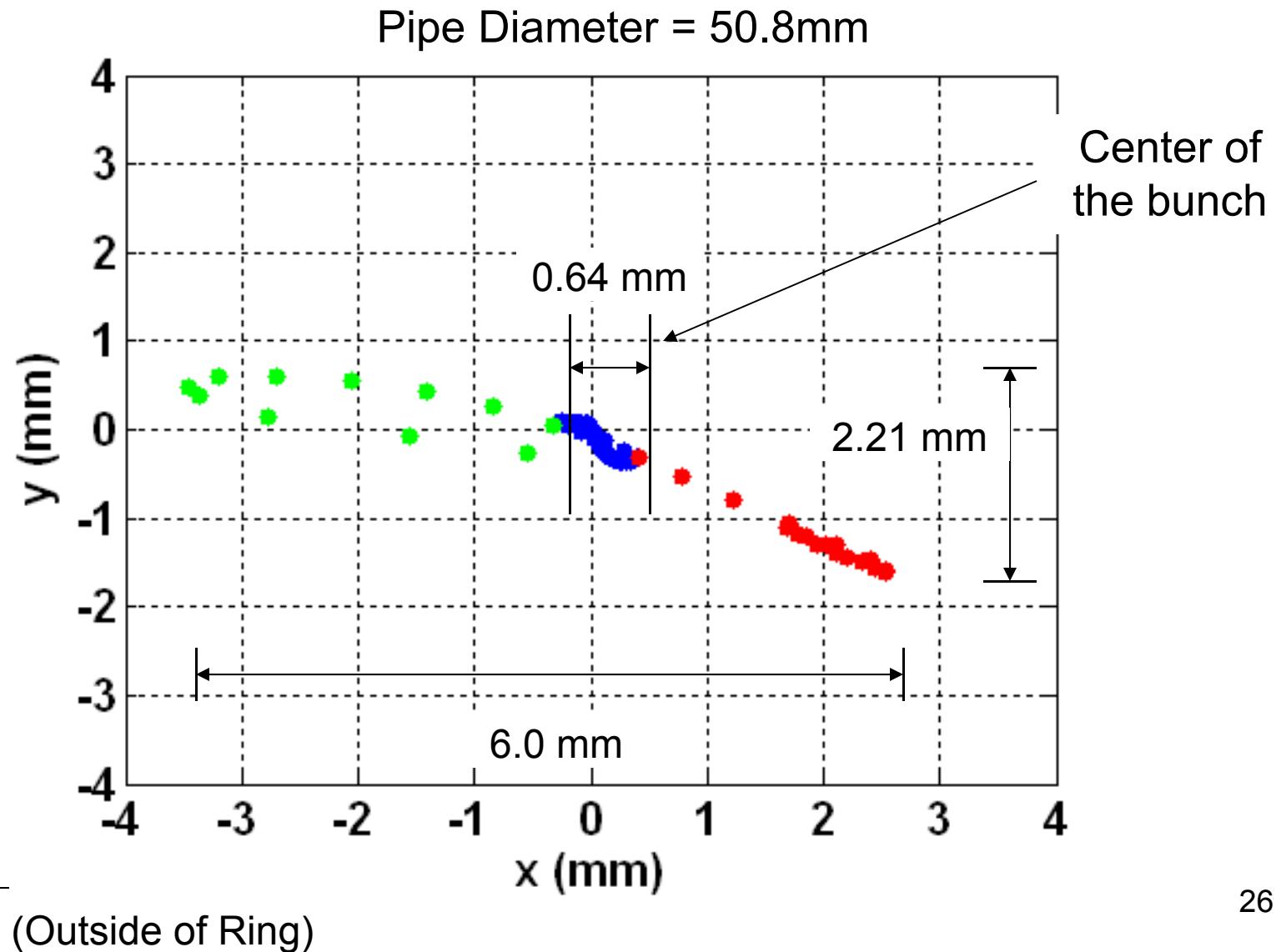
Multiple images are taken every 3 ns along the ~110 ns beam

**Beam Current**

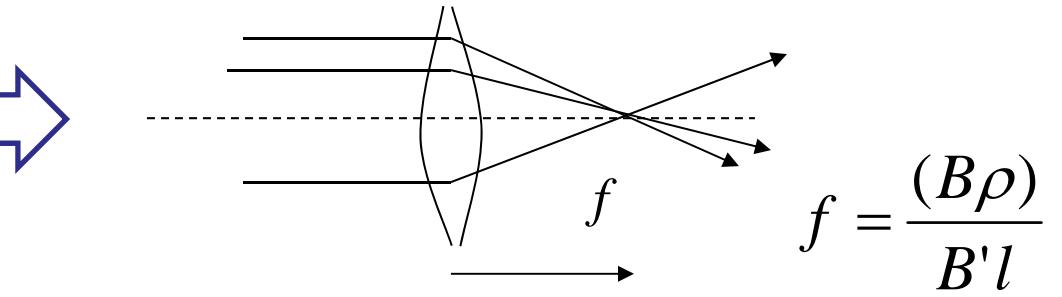
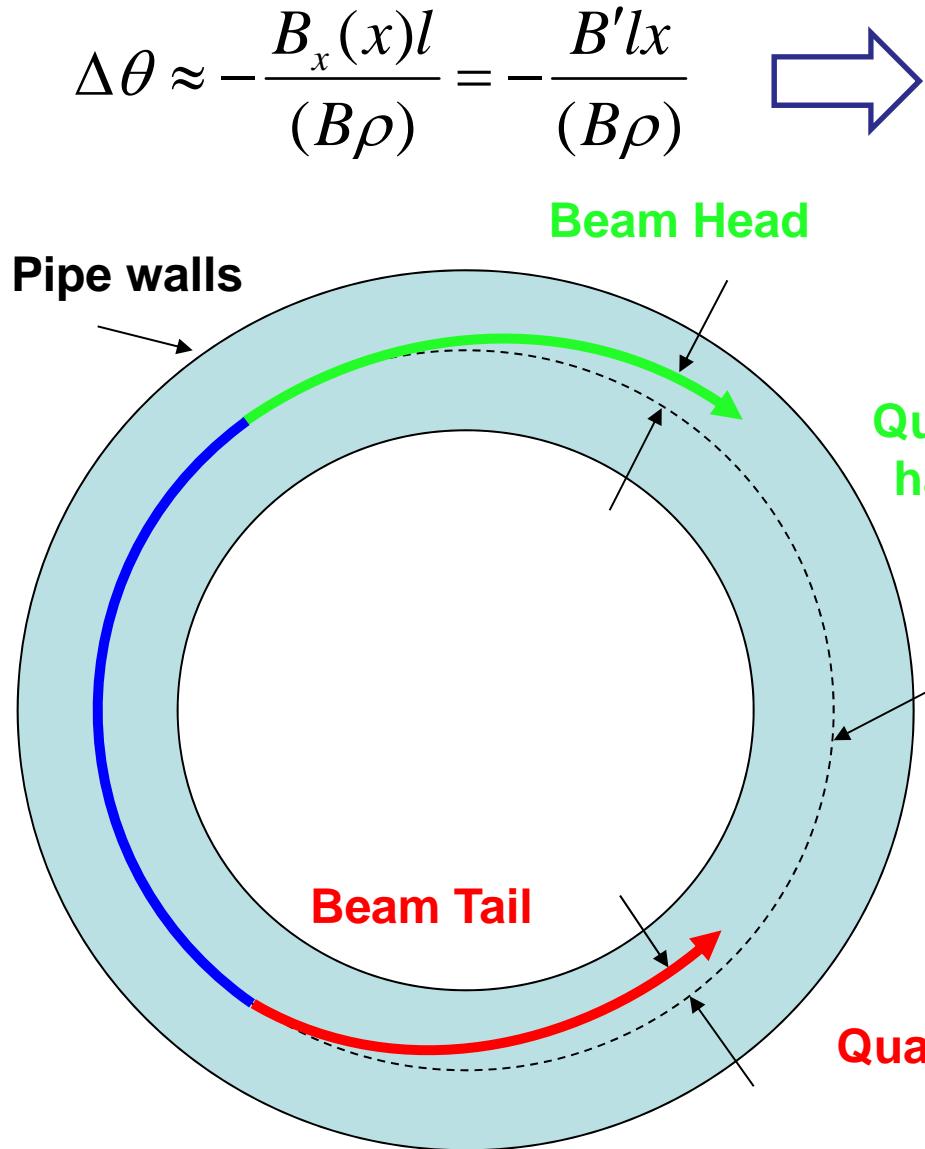


**1<sup>st</sup> Turn Intercepting Diagnostic Measured at Ring Chamber 15**

# Centroid Deflection across the Bunch Length



# Quadrupole Focusing Dependence on Momentum



On average higher momentum particles =  
Quadrupoles will effectively have a longer focal length

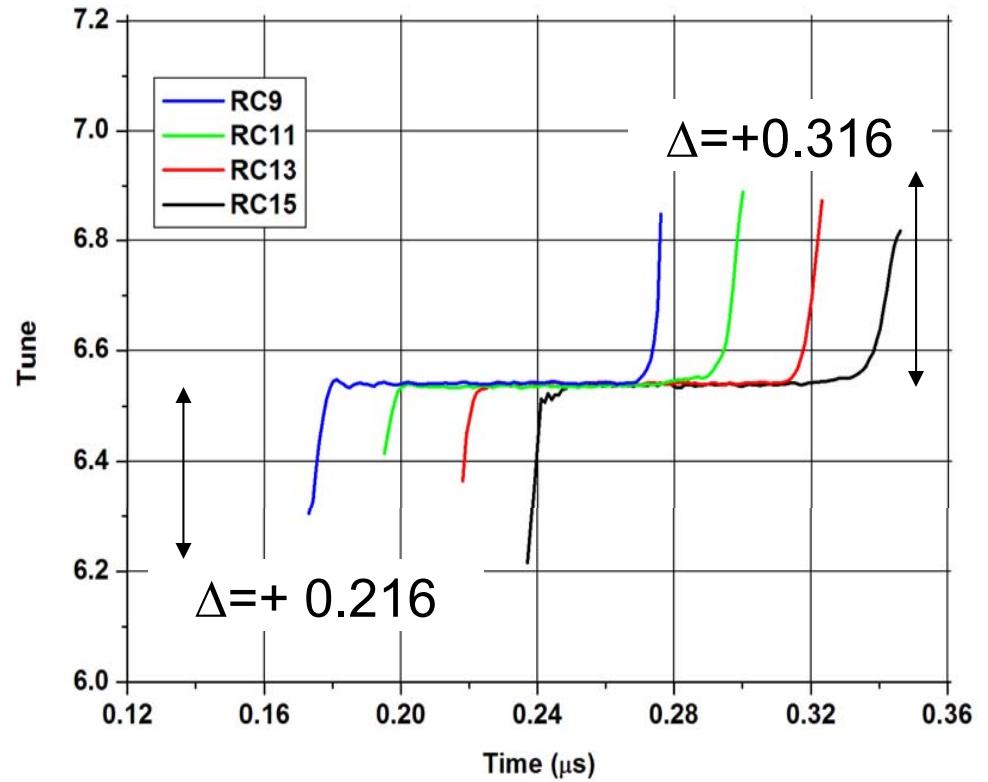
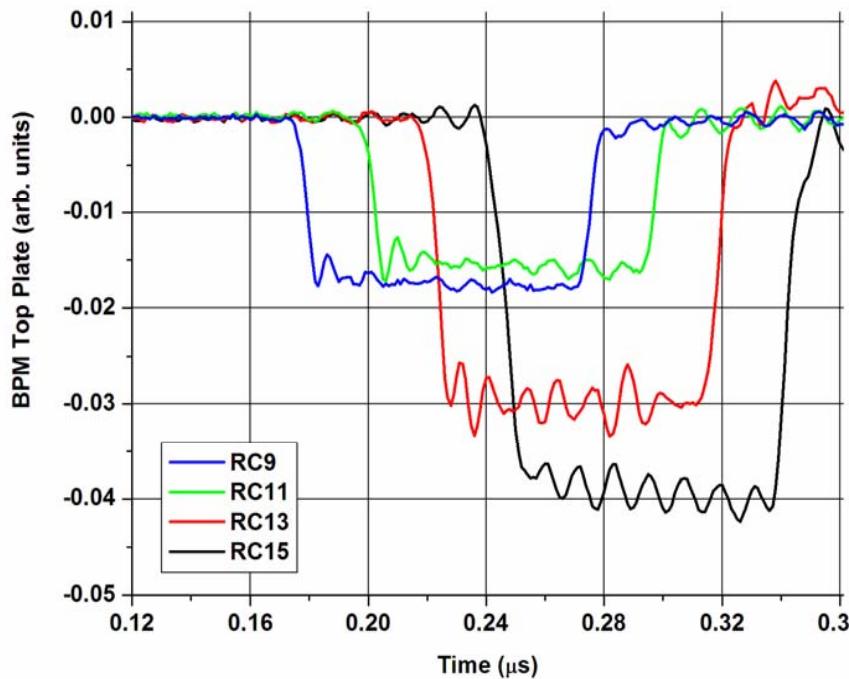
$$\sin \frac{\mu}{2} = \frac{L}{2f}$$

$$v \equiv \frac{1}{2\pi} \oint \frac{ds}{\beta(s)} = \frac{1}{2\pi} N_{cell} \mu_{cell}$$

On average lower momentum particles =  
Quadrupoles will effectively have a shorter focal length

# Fractional Tune-Shift at the Ends of the Beam

Direction beam position monitor signal

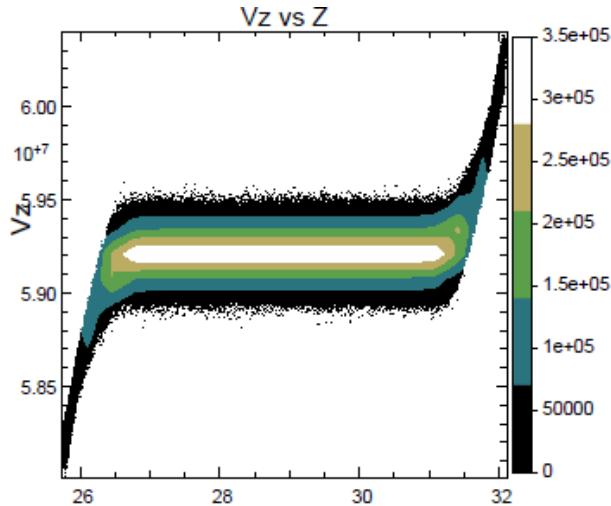


A fractional tune shift appears at the ends of the bunch, corresponding to the momentum deviations at the ends.

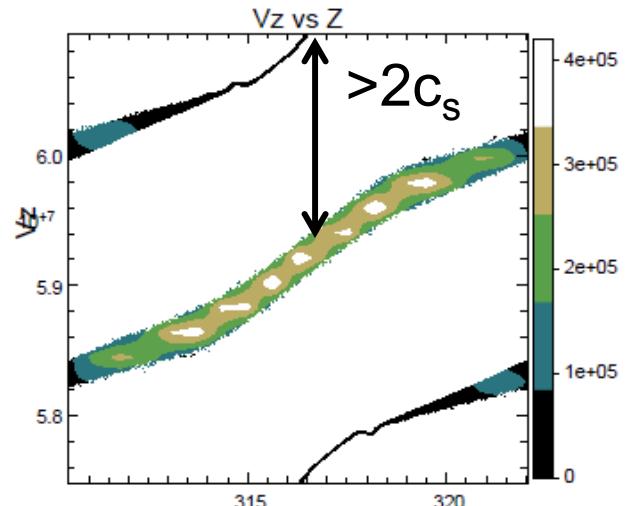
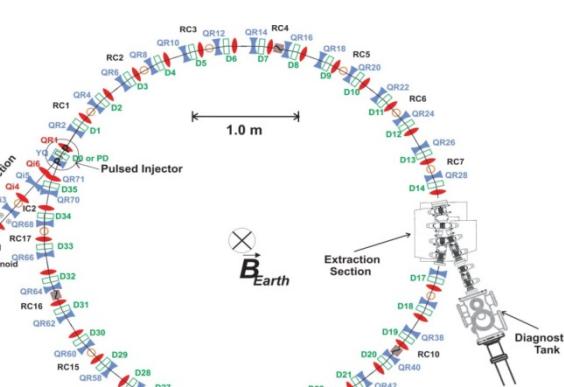


# Allowing the Beam to Coast Indefinitely

# Inter-Stream Spacing Shrinks as the Bunch wraps

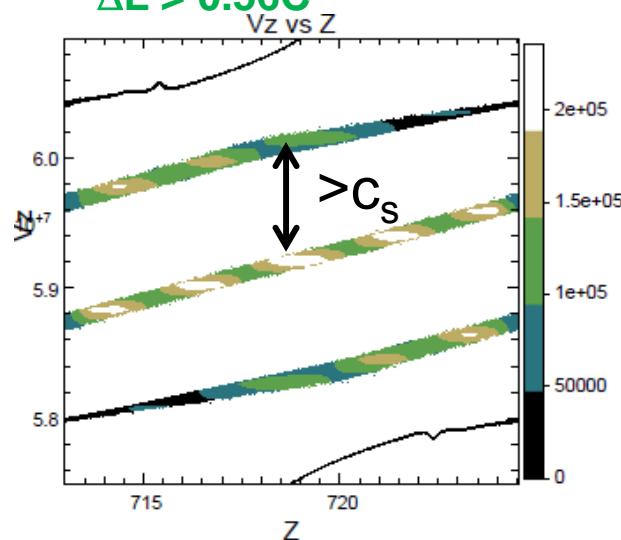


Simulated Phase Space

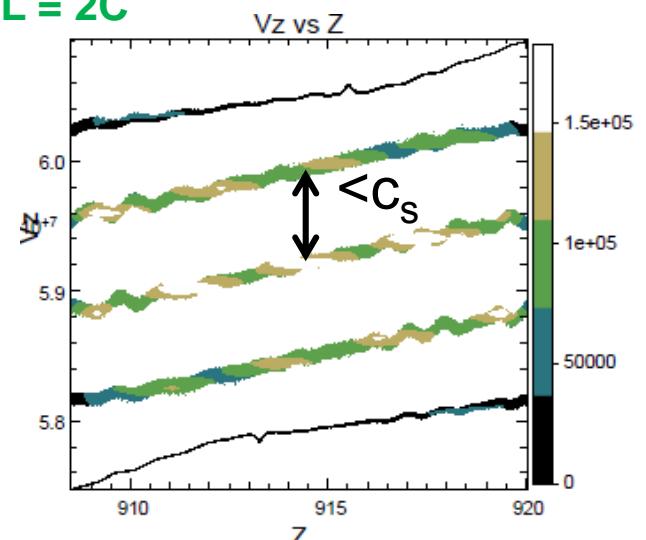


$\Delta L$  = Bunch length

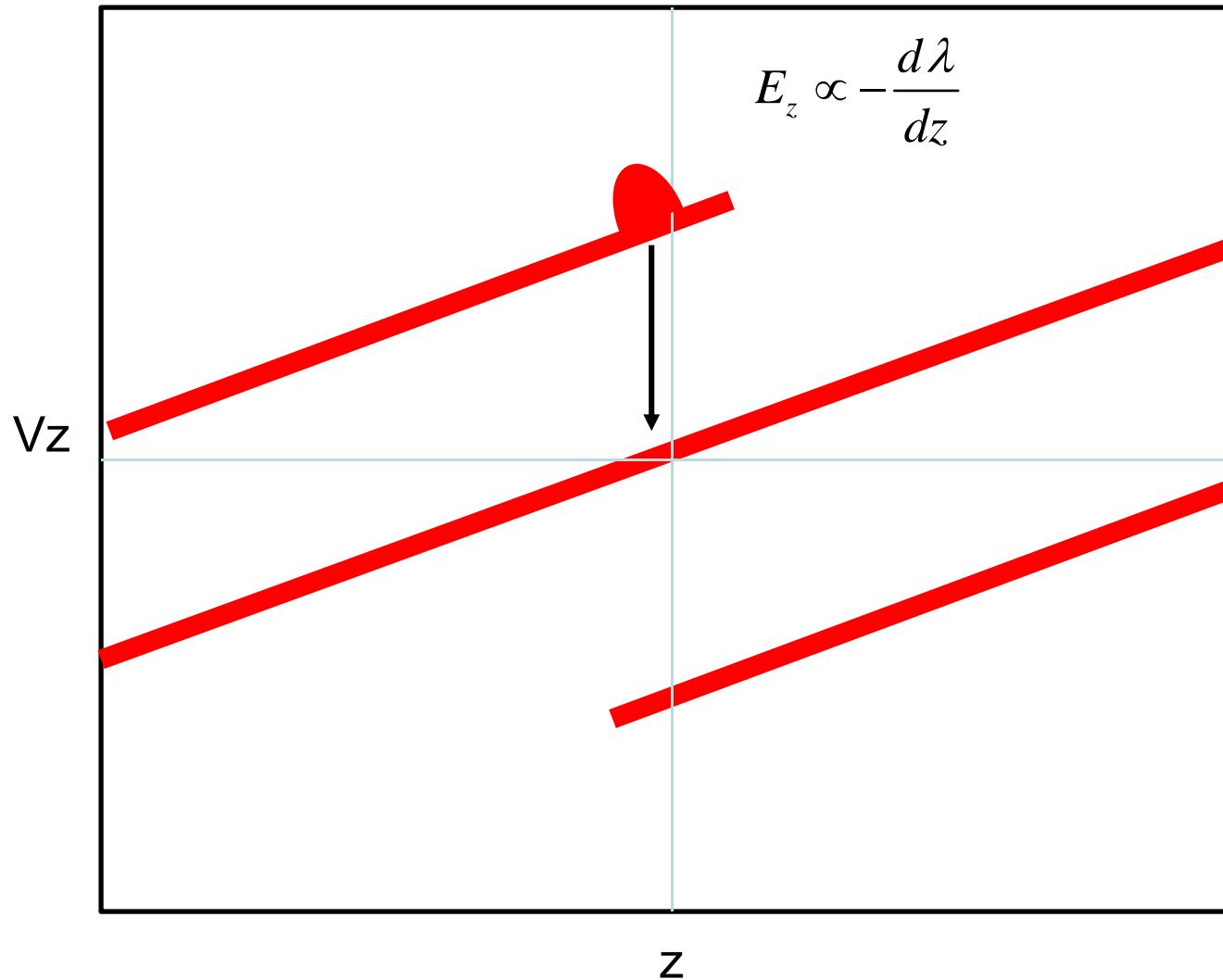
C = Ring circumference



Injected length  
 $\Delta L = 0.5C$



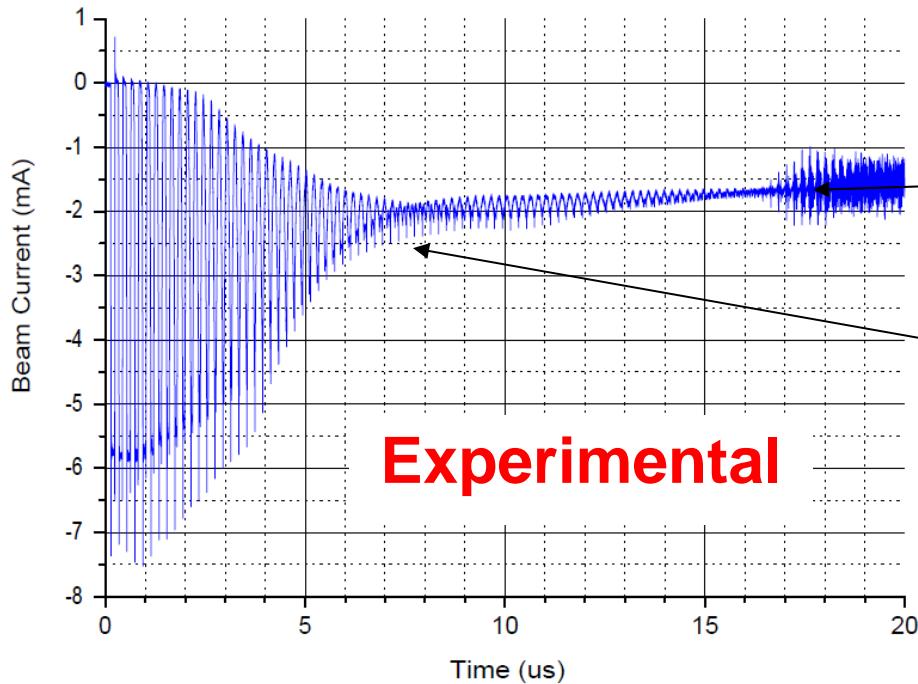
# Wrapped Streams Couple to Subsequent Streams



Density perturbations create axial electric fields that perturb other streams close in proximity. This creates other density modulations that further seed others. This self-amplification creates high-frequency modulations in the beam.

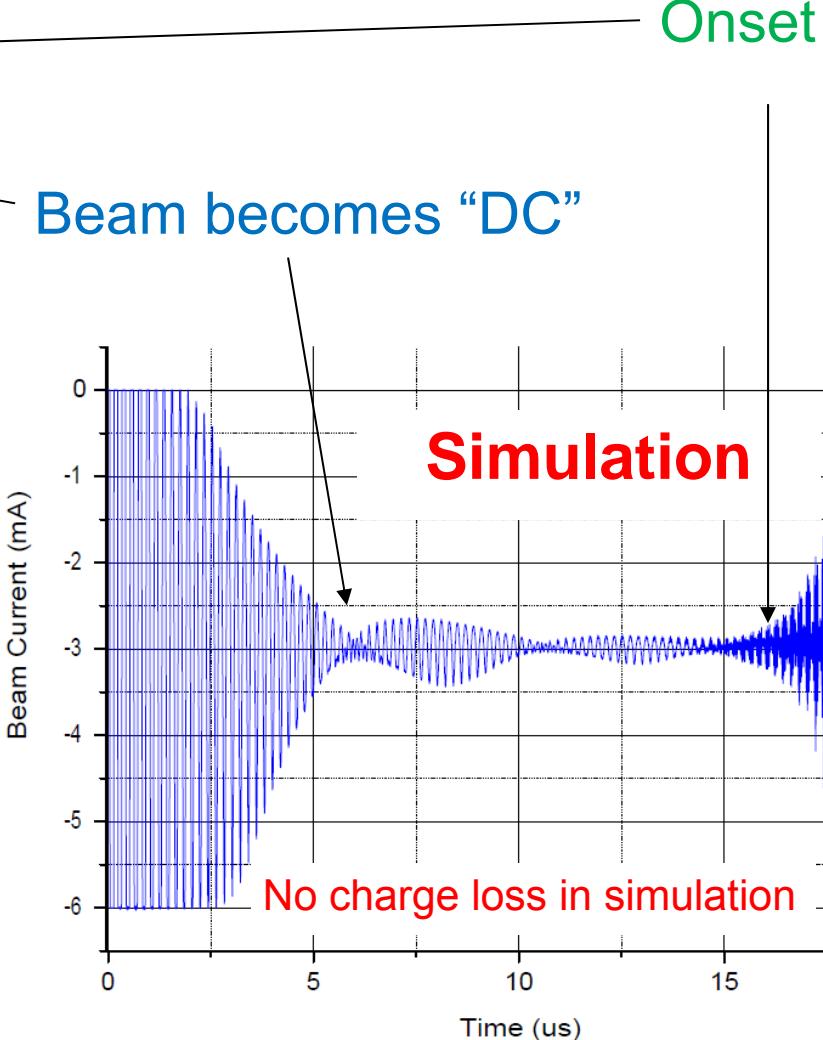
# Signature of the Onset in the Current Profiles

Current Profiles from a Wall Current Monitor



6 mA beam  
 $\eta = 0.50$

Beam becomes “DC”



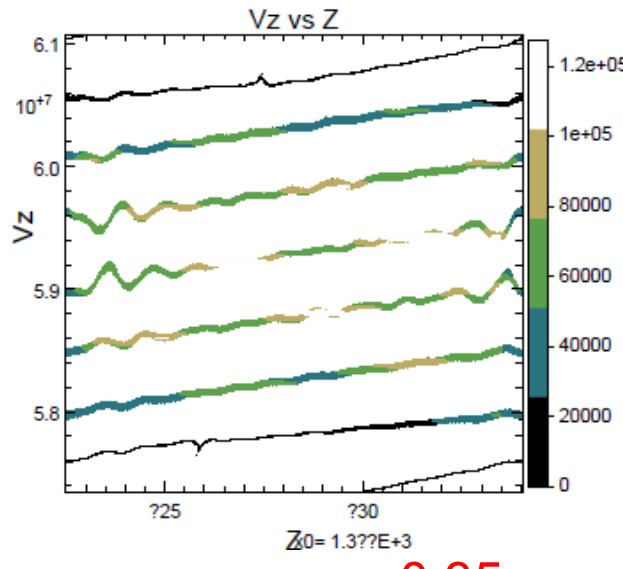
No charge loss in simulation

# Fill Factor Dependence on the Number of Filamentations

The growth rate of the modulations in phase space is also dependent on the fill factor

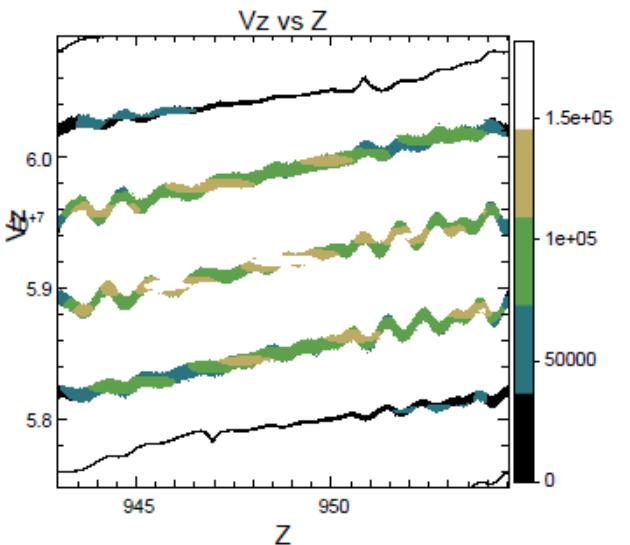
## Phase Space (6 mA beam)

70 ns long bunch



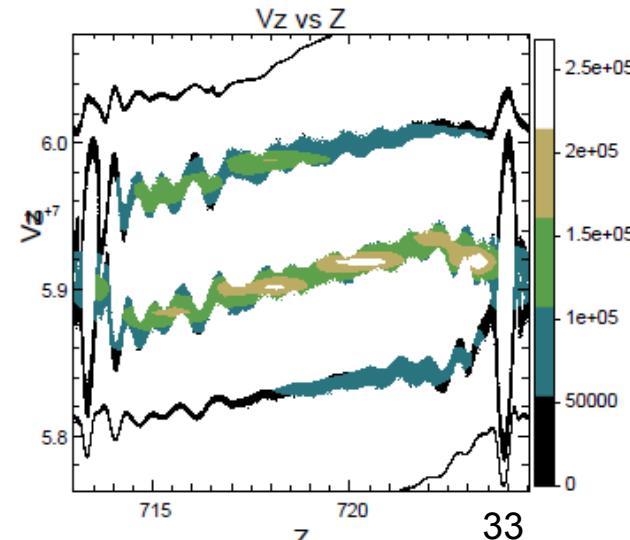
$\Delta L > 7C$   $\eta = 0.35$

100 ns long bunch



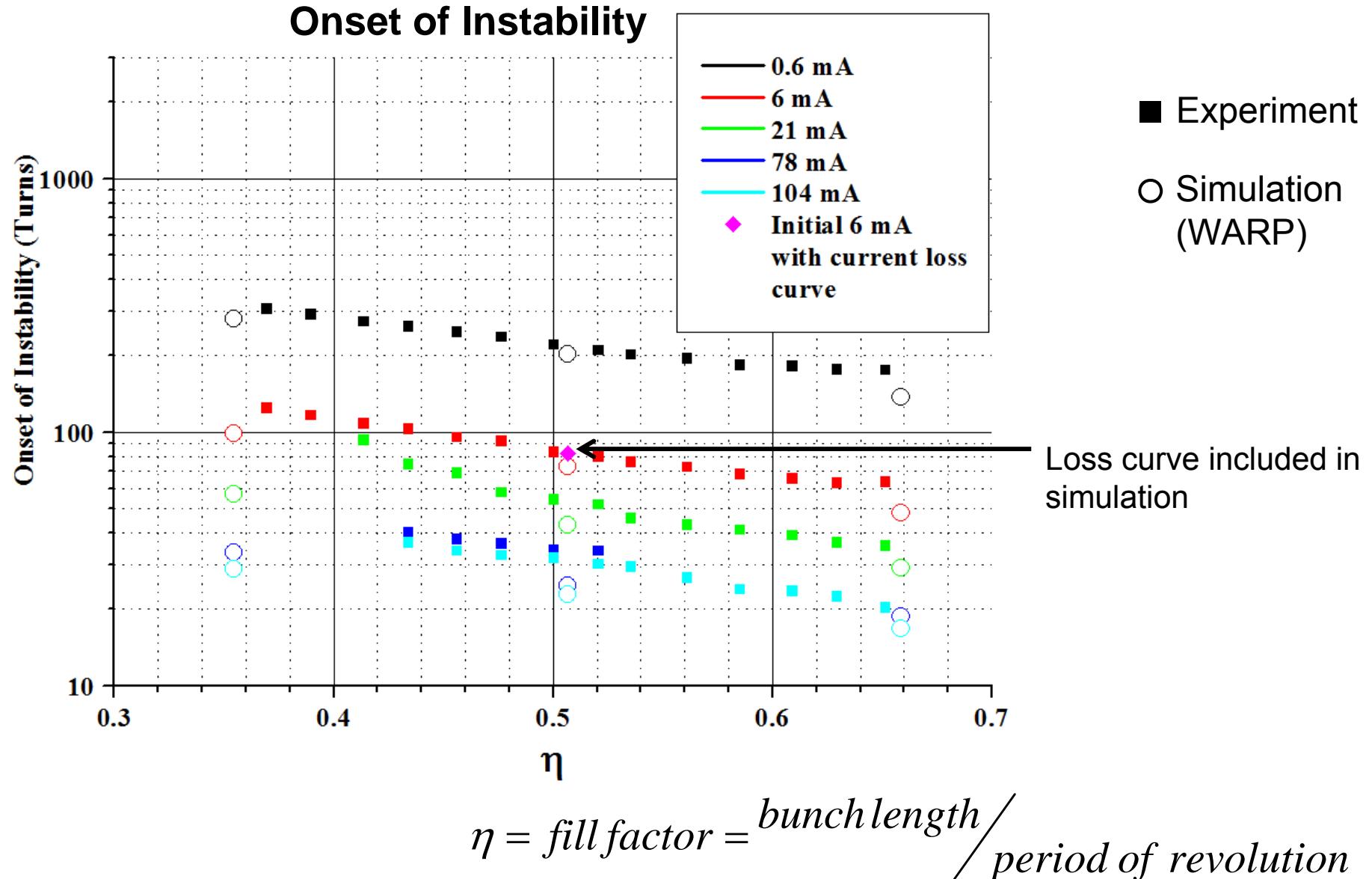
$\Delta L > 5C$   $\eta = 0.50$

130 ns long bunch



$\Delta L > 3.5C$   $\eta = 0.66$

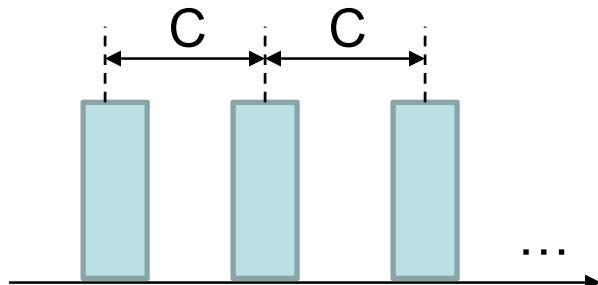
# Fill Factor and Current Dependence on the Onset



-B.L. Beaudoin, I. Haber, R.A. Kishek, and T. Koeth, ["Experimental Observations of a Multi-stream Instability in a Long Intense Beam," Proceedings of the 2013 International Particle Accelerator Conference, Shanghai, China, May 2013, 2044 \(2013\).](#)

# Extending to Multiple Short Bunch Trains

Multi-Bunch Train

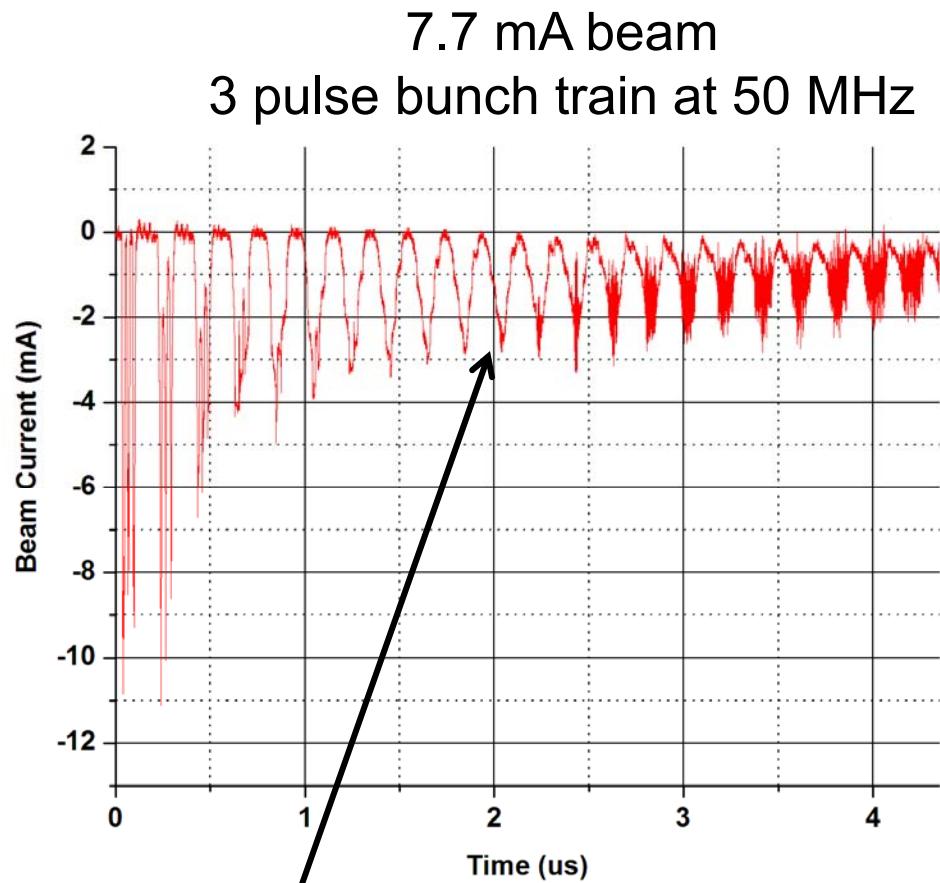


For multiple bunch trains, C is the pulse to pulse spacing

$$C = (20ns)v_o = 1.167m$$

$$\eta = \frac{12.57ns}{197.39ns} = 0.0636$$

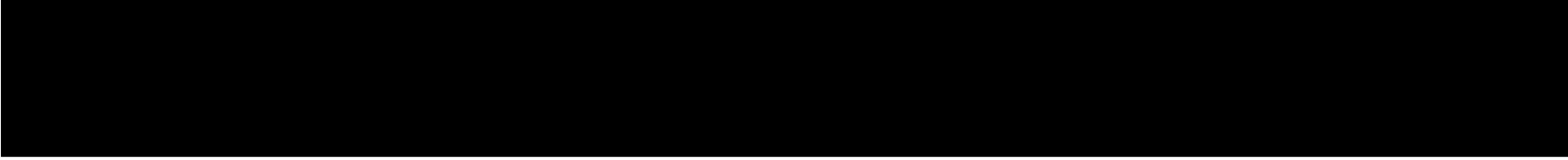
Experimental Observation



Onset of instability

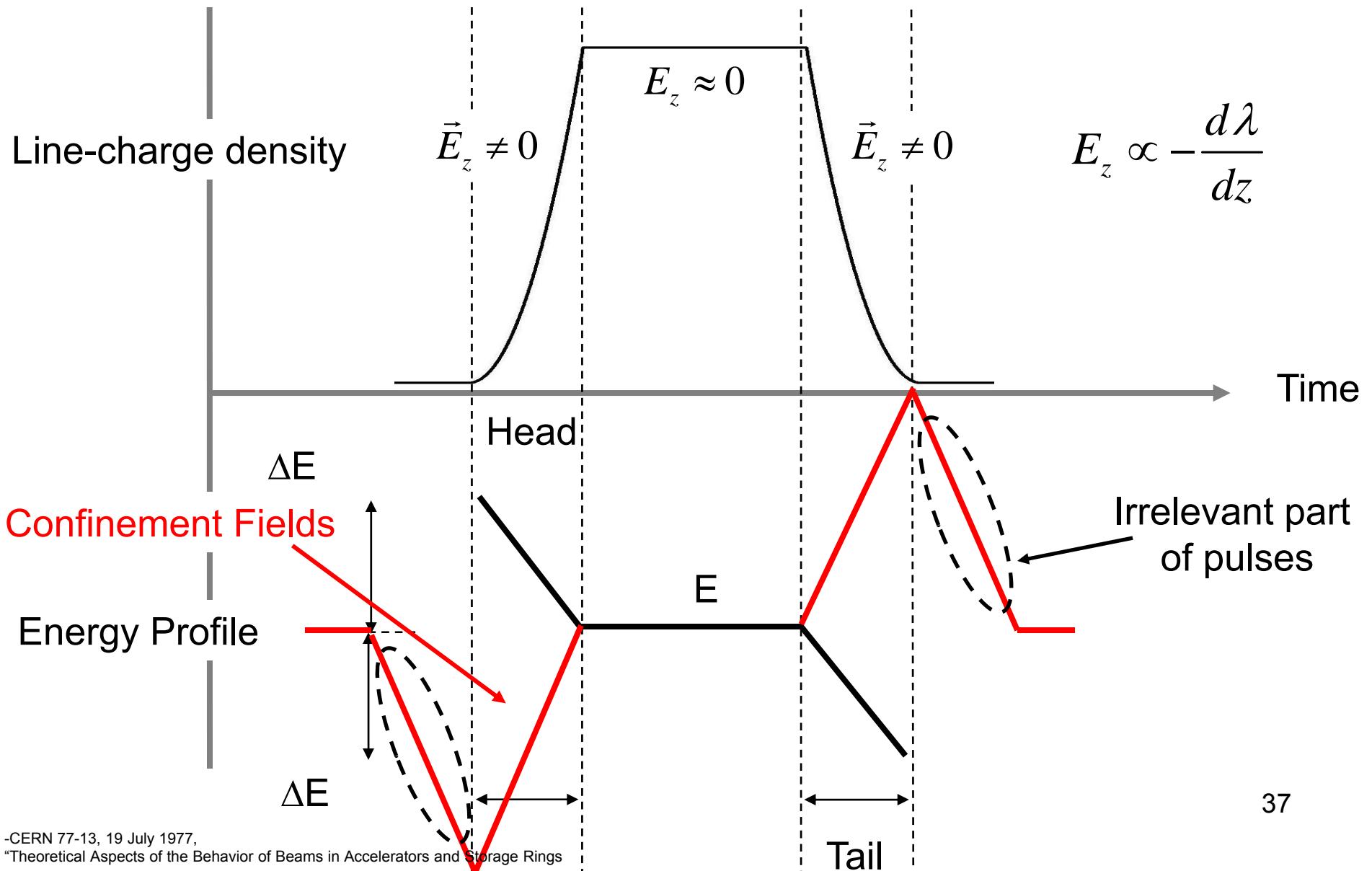
$$s_{\text{onset}} = 132.7 \text{ m}$$

$$\text{turns}_{\text{onset}} = 11.5$$



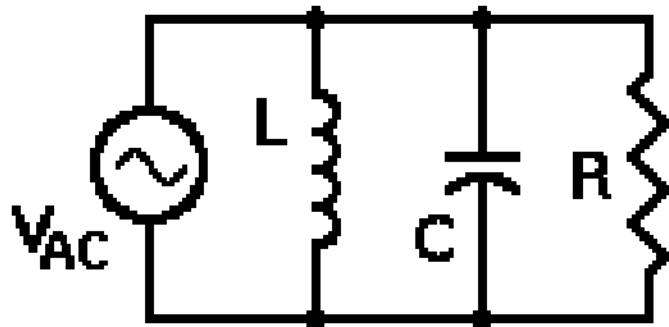
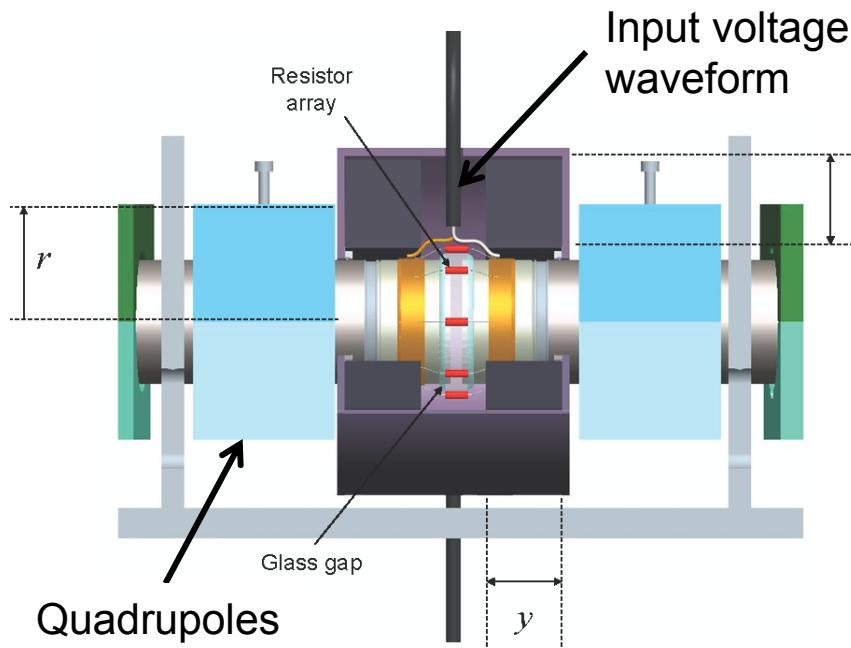
# Longitudinal Dynamics with Barrier Buckets

# Longitudinal Physics

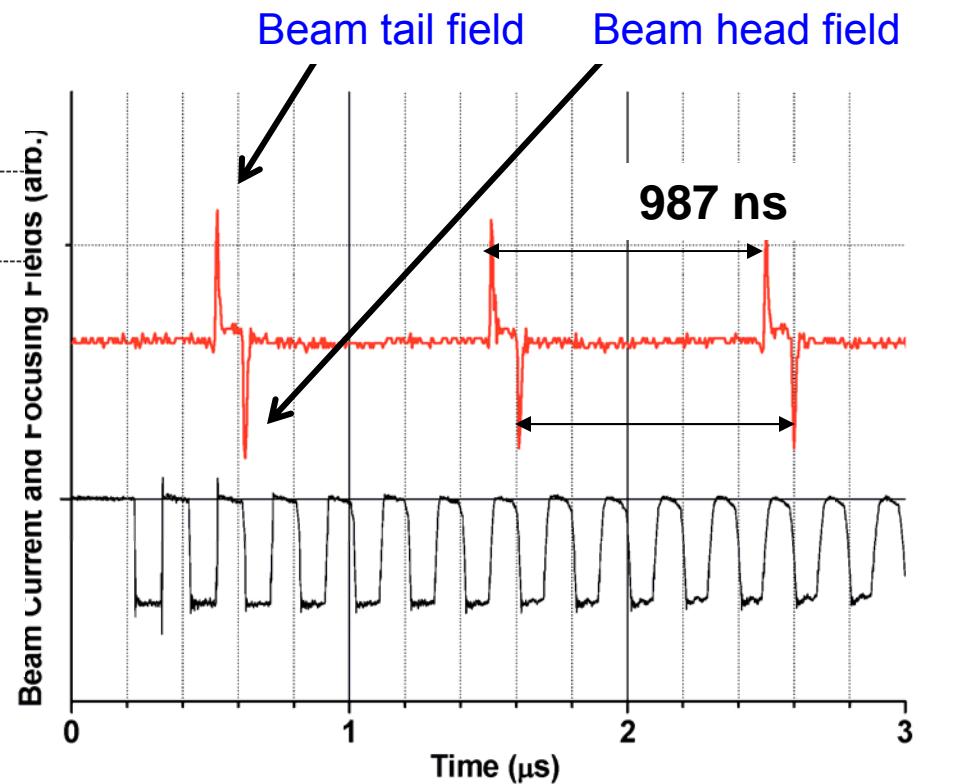


# Barrier Buckets to Confine Beam-Ends

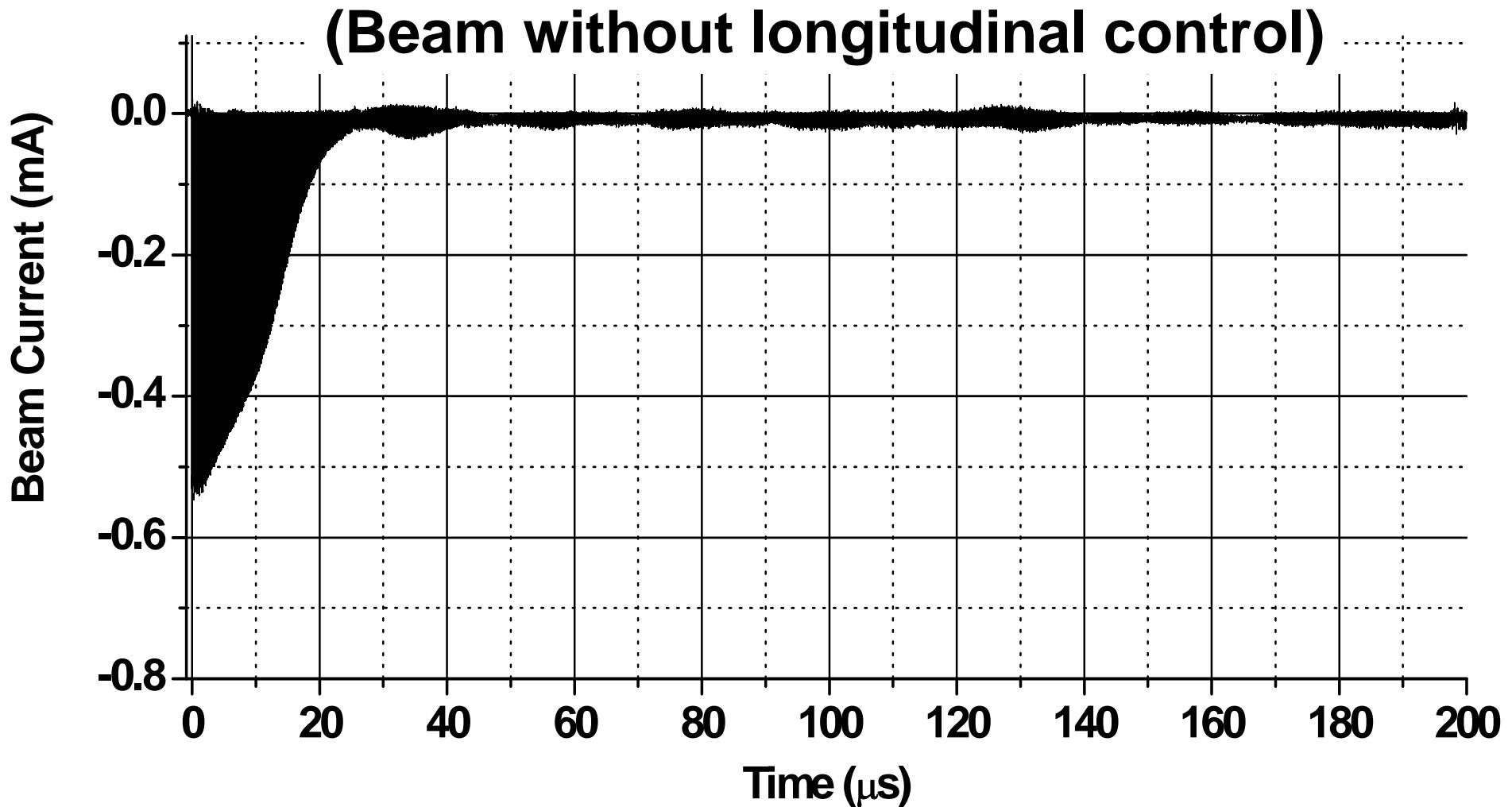
Induction Cell in between Quadrupoles



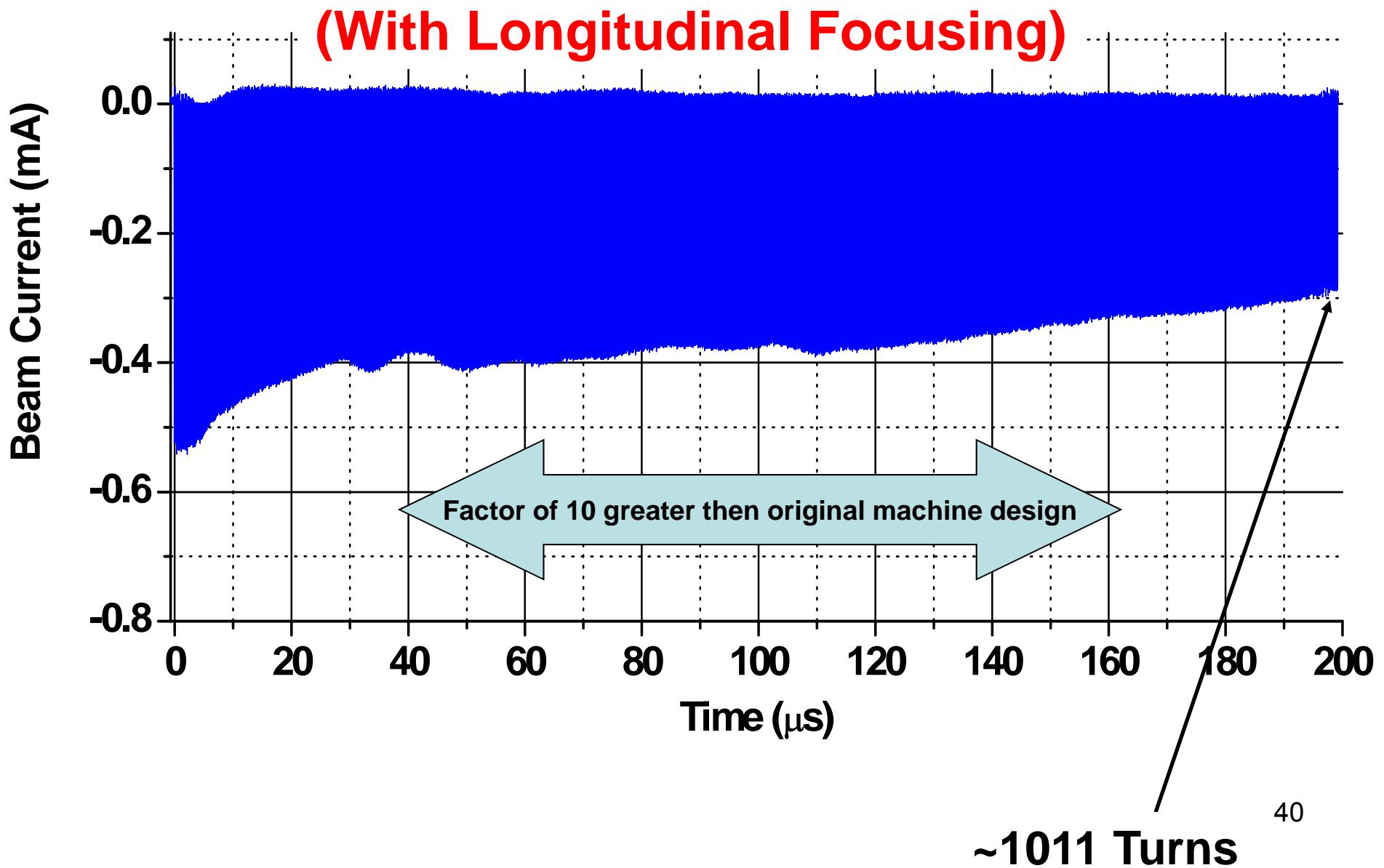
Barrier fields synchronized to revolution frequency



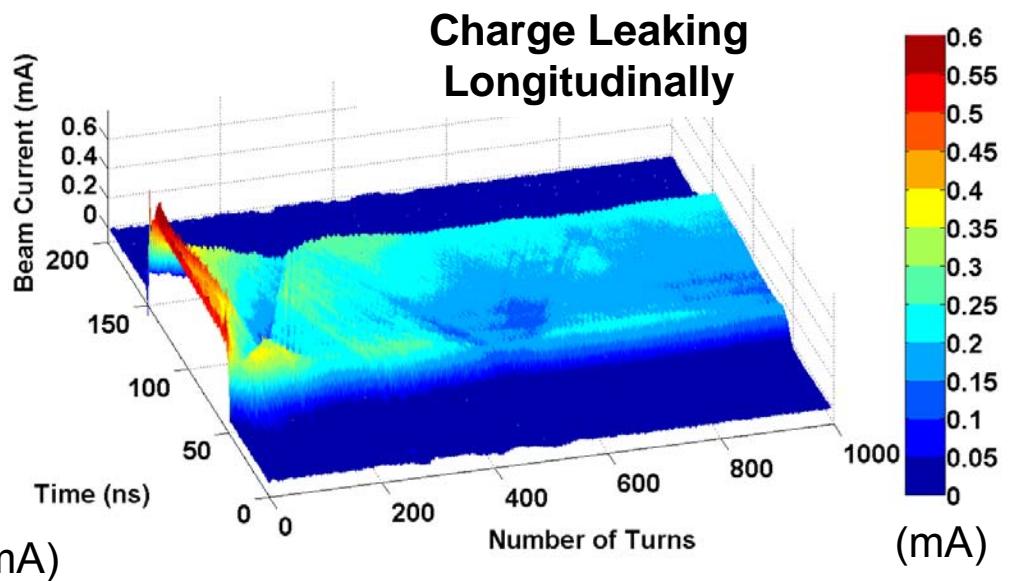
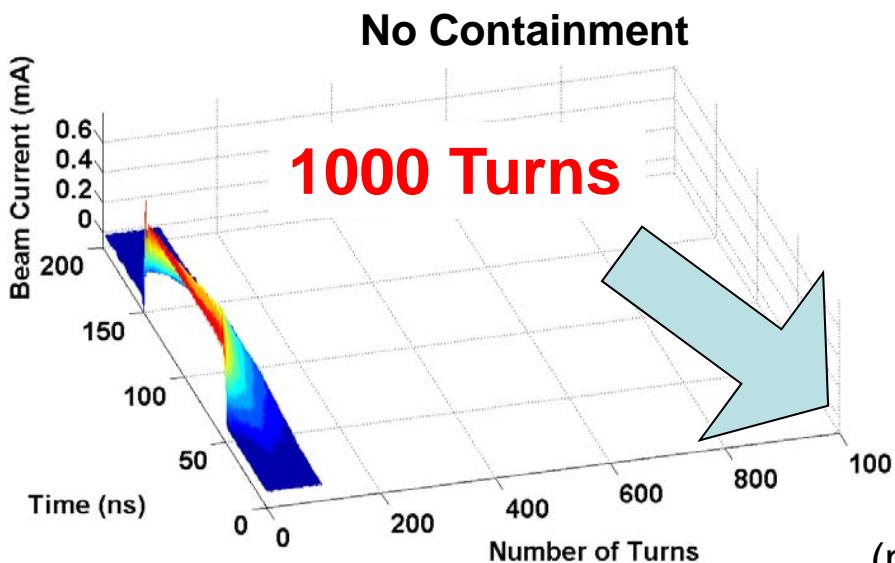
# Bunch Shape Diminishes as a Result of Longitudinal Space-Charge Forces



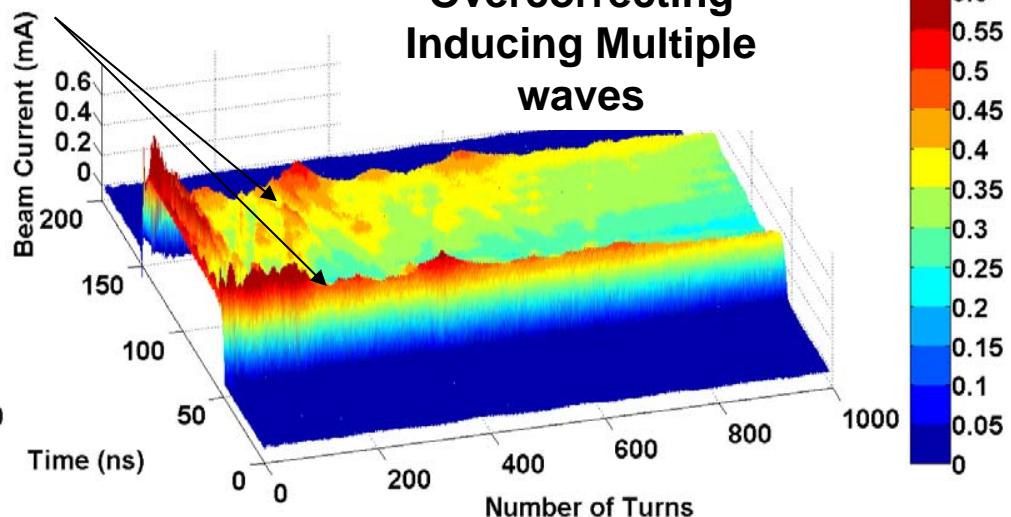
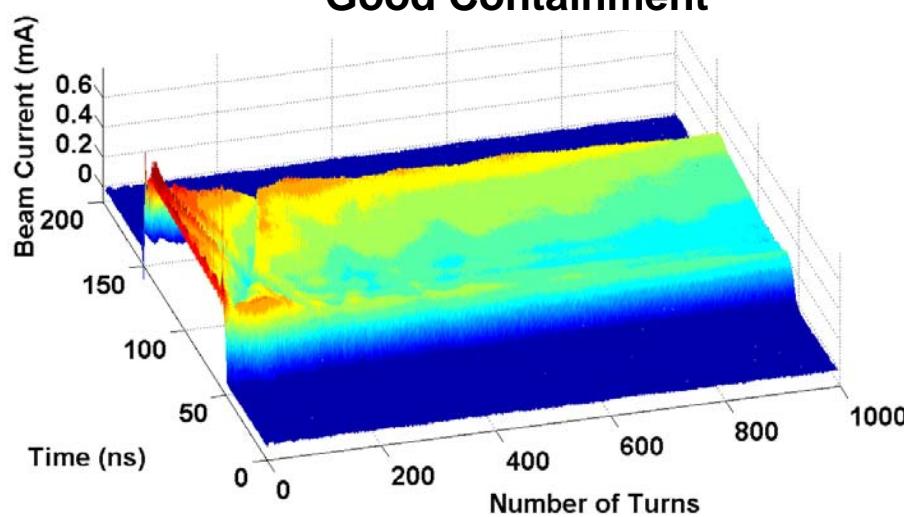
# Bunch Lifetime is Extended with Longitudinal Control



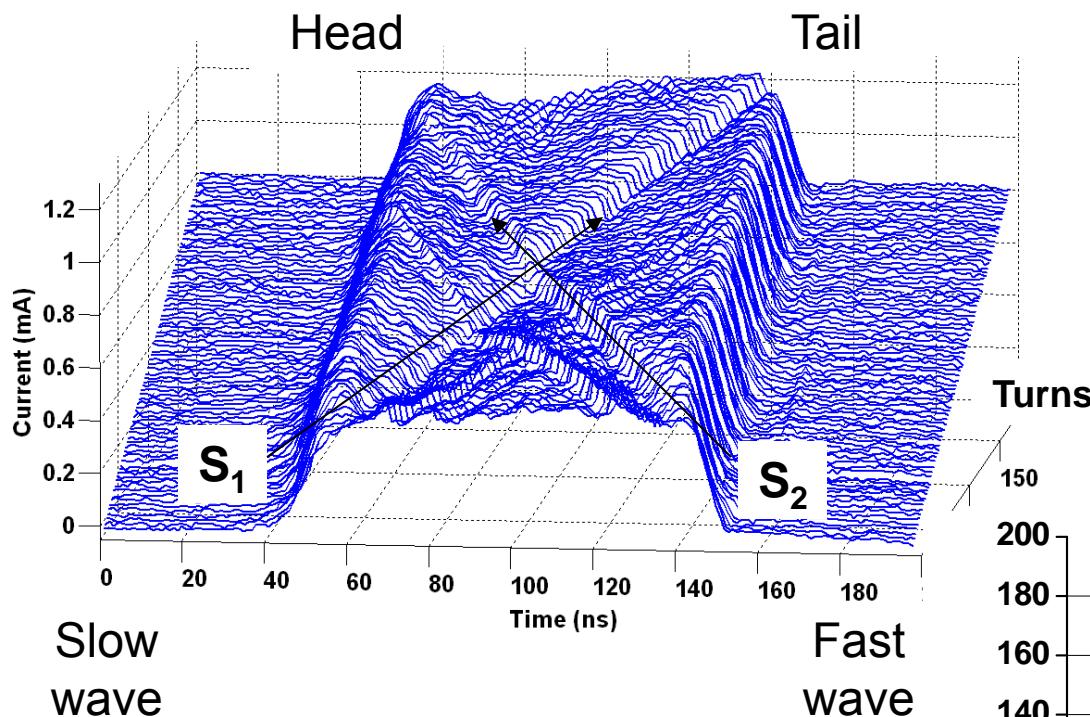
# Experimental Results of Longitudinal Bunch Shape



**Space-Charge Waves**



# Waves Propagate/Reflect Along a Confined Bunch



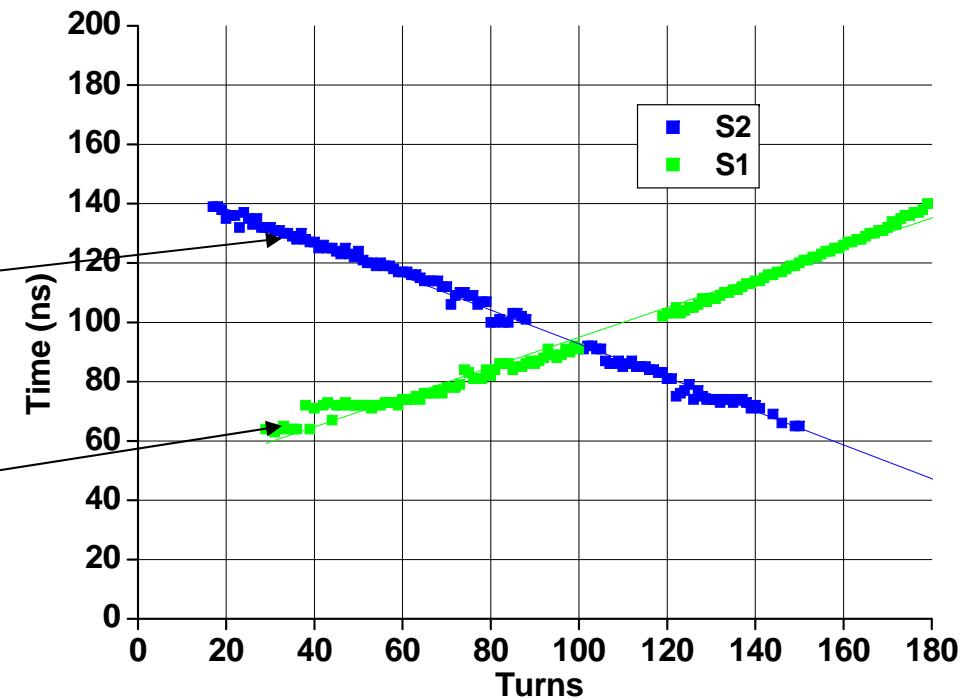
$$0.569 \text{ ns} / \text{turn} = 1.68(1 \times 10^5) \text{ m} / \text{s}$$

$$0.503 \text{ ns} / \text{turn} = 1.49(1 \times 10^5) \text{ m} / \text{s}$$

**Wave velocity**

$$c_s = \sqrt{\frac{qg\lambda}{4\pi\epsilon_0\gamma_o^5 m}}$$

$$c_s = \text{slope} \times \frac{V_o^2}{11.52}$$



# Analogy to Transmission Lines

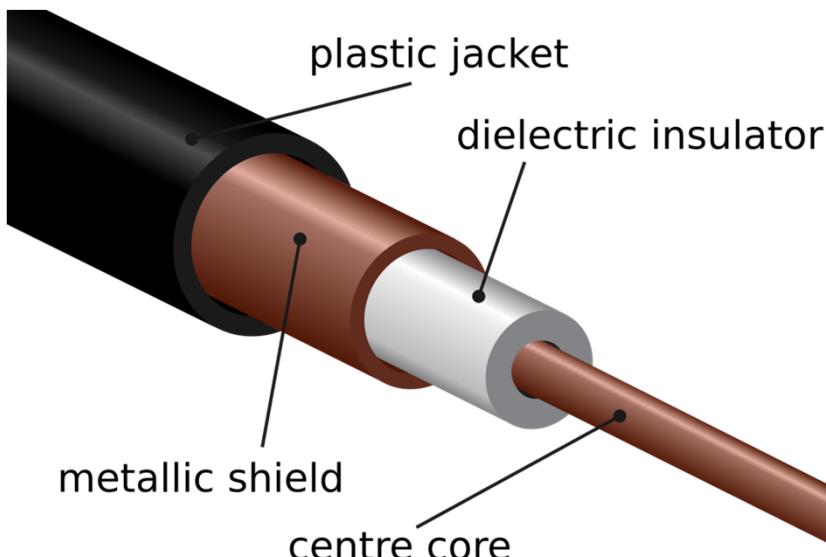
Reflection Coefficient

$$\Gamma = \frac{Z_L - Z_o}{Z_L + Z_o}$$

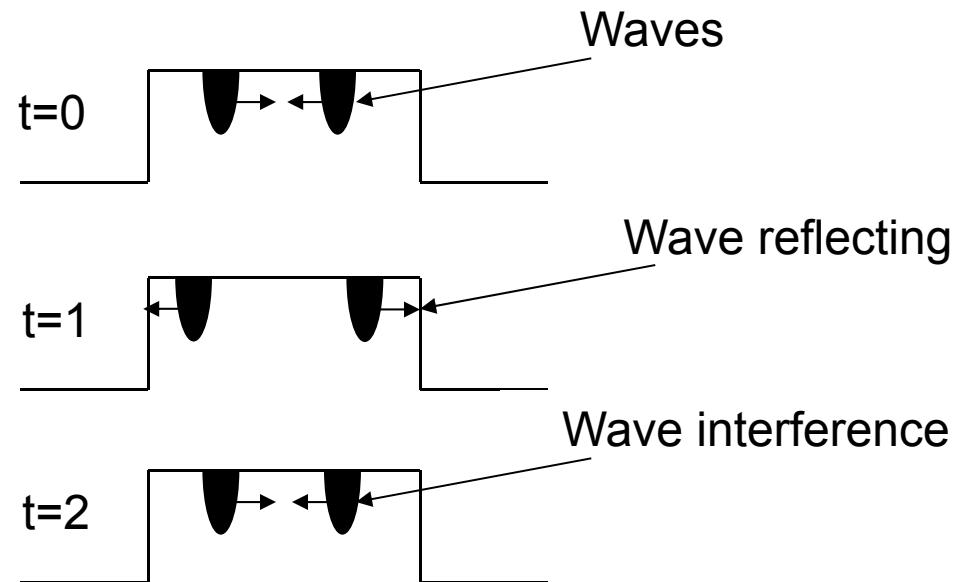
$\Gamma = 1, Z_L \gg Z_o, \text{open circuit}$

$\Gamma = -1, Z_L \ll Z_o, \text{short circuit}$

$$\Gamma = 1$$



Waves moving along a confined bunch corresponds to a wave reflecting on a transmission line



# UMER Realignment



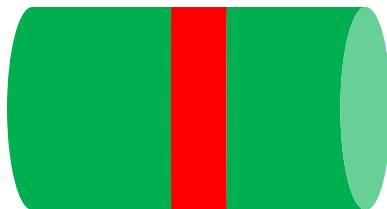
<https://youtu.be/EZcCYs80T8k>



# Additional Slides

# Space-Charge Waves on Long Beams

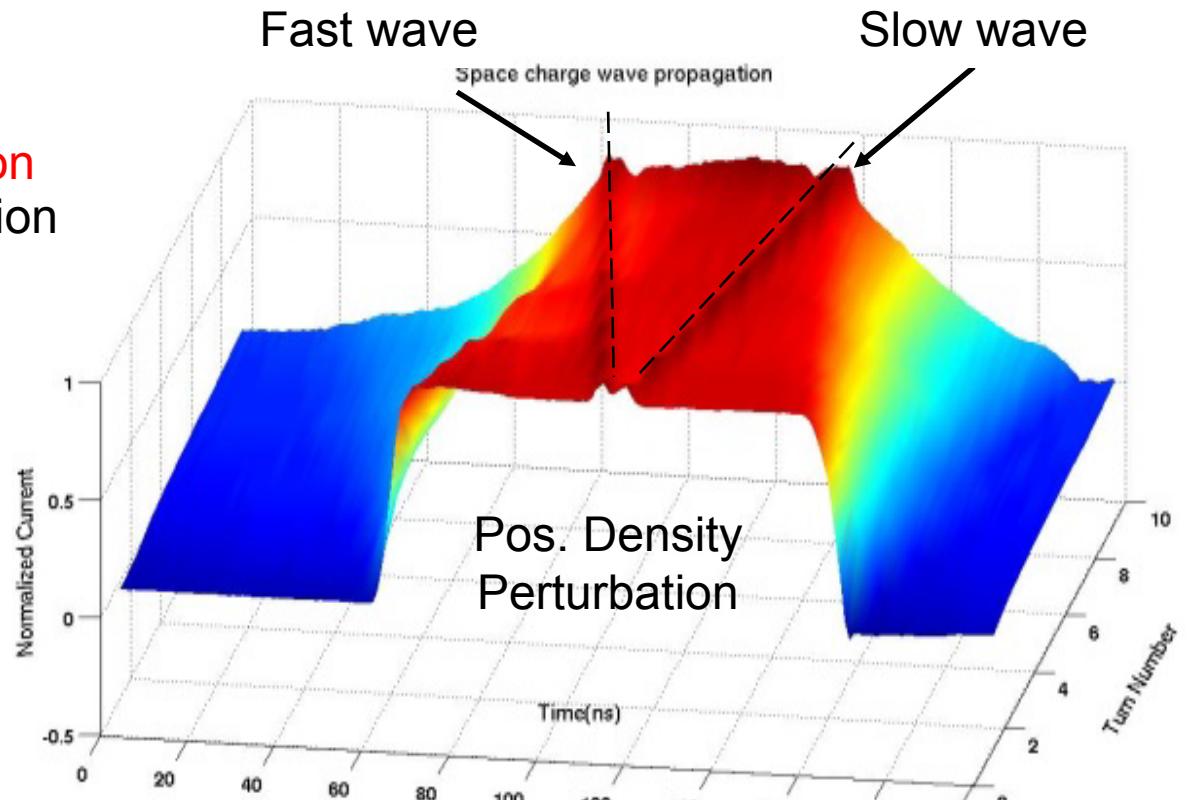
Perturbations to the beam density and/or energy initiates a fast and slow space-charge wave



**Density and/or energy perturbation**  
Wave Amplitude for a perturbation

	+F	-F
+S	<i>Pos. Density Perturbation</i>	Neg. Energy Perturbation
-S	Pos. Energy Perturbation	Neg. Density Perturbation

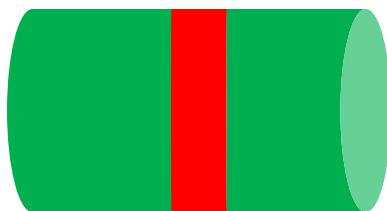
$$(\omega - v_o k)^2 = c_{so}^2 k^2 \quad c_{so}^2 = \frac{qg}{4\pi\epsilon_0\gamma_0^5} \lambda_0$$



**Experimental**

# Space-Charge Waves on Long Beams

Perturbations to the beam density and/or energy initiates a fast and slow space-charge wave

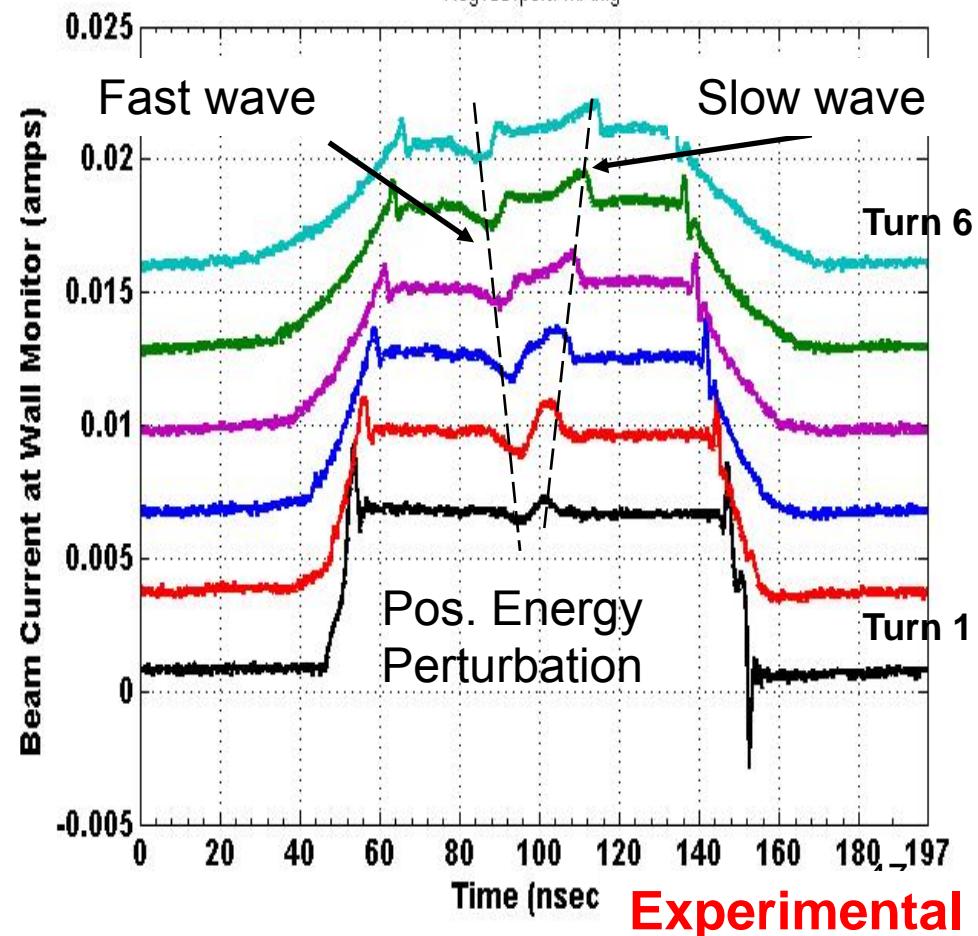


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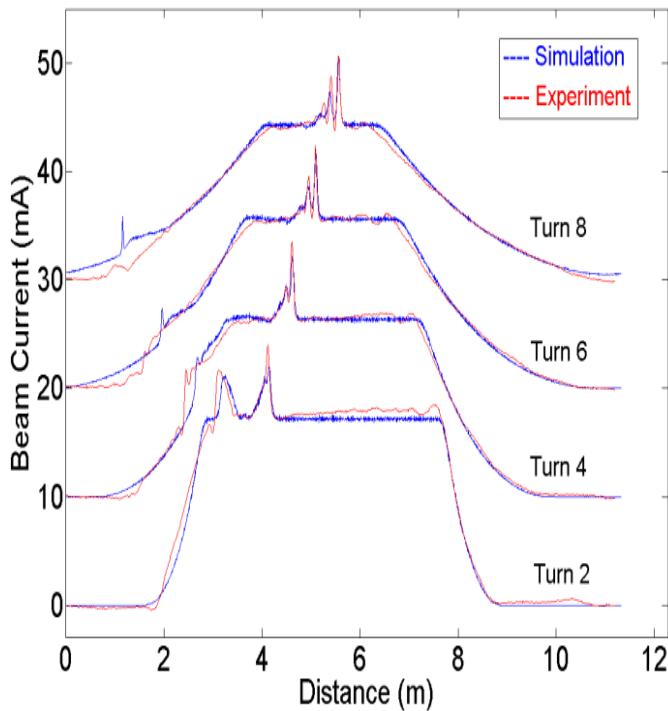
Neg100vpert7mA.fig



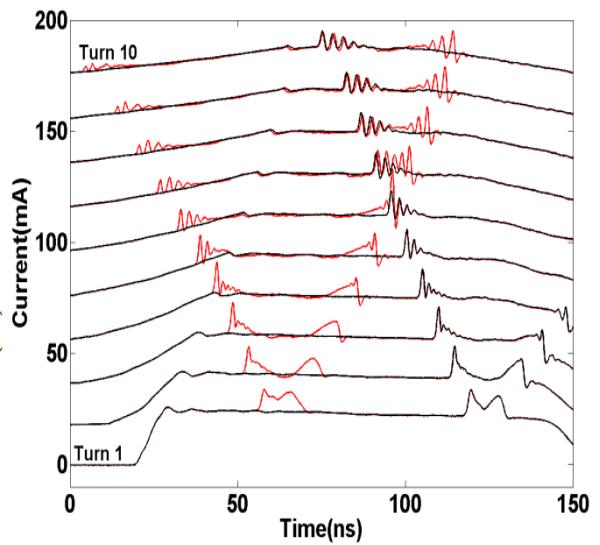
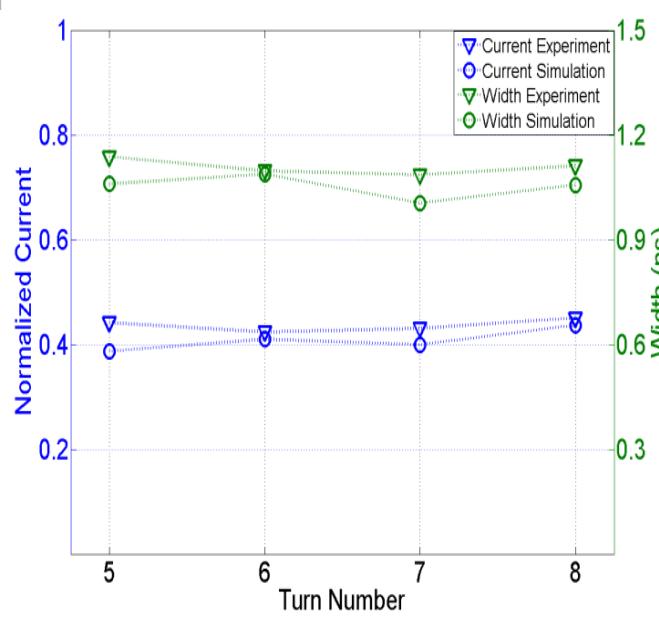
# Soliton Wave Trains on Intense Beams

- With a large and narrow perturbation on a long intense beam, the perturbation begins to steepen and spawn soliton wave trains
- The pulse width and amplitude remains unchanged over a long propagation distance

## Experimental and Simulation Comparison



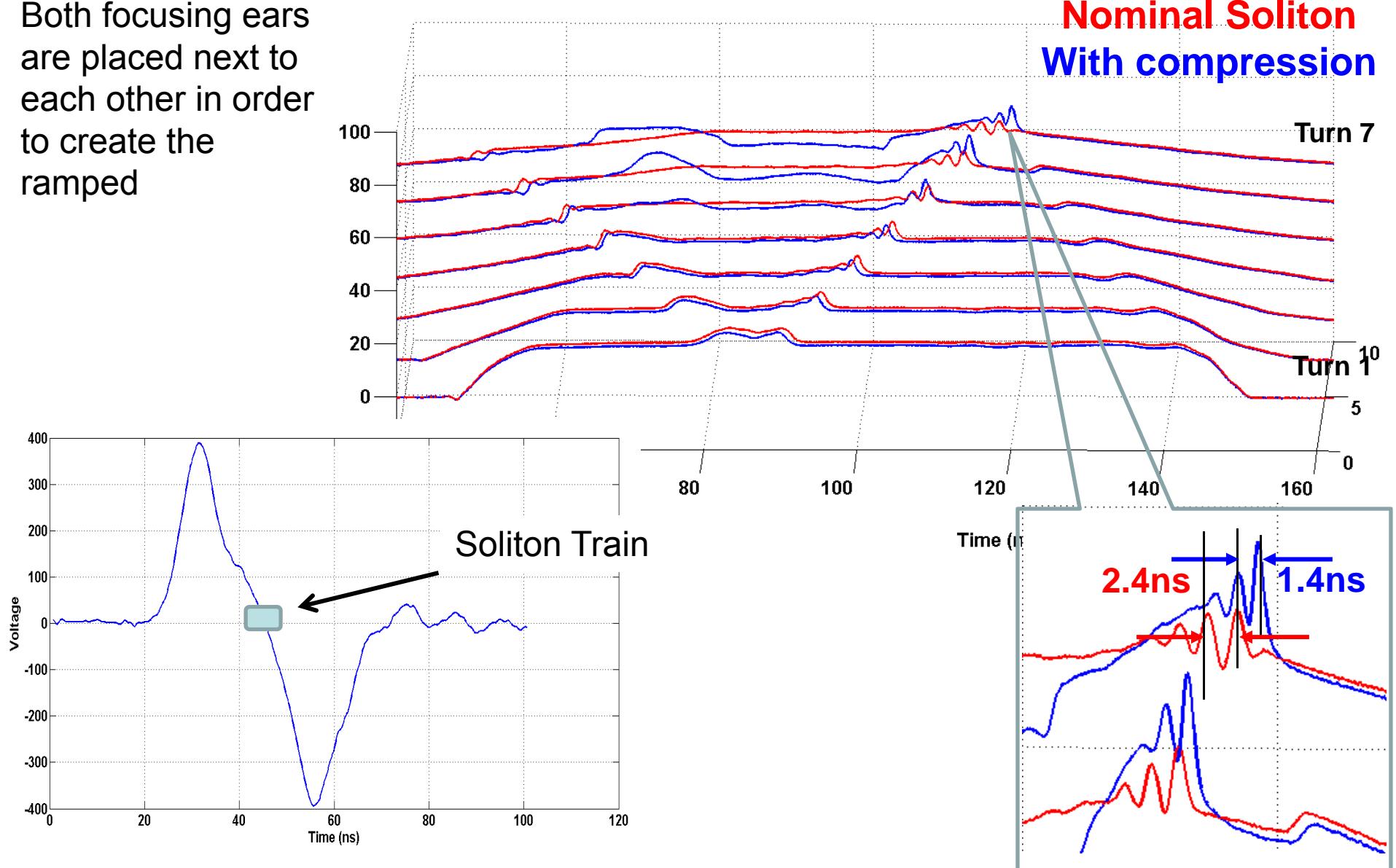
Sub pulses maintain their shape



Interaction with other solitons and emerges unchanged

# Soliton Compression

Both focusing ears  
are placed next to  
each other in order  
to create the  
ramped

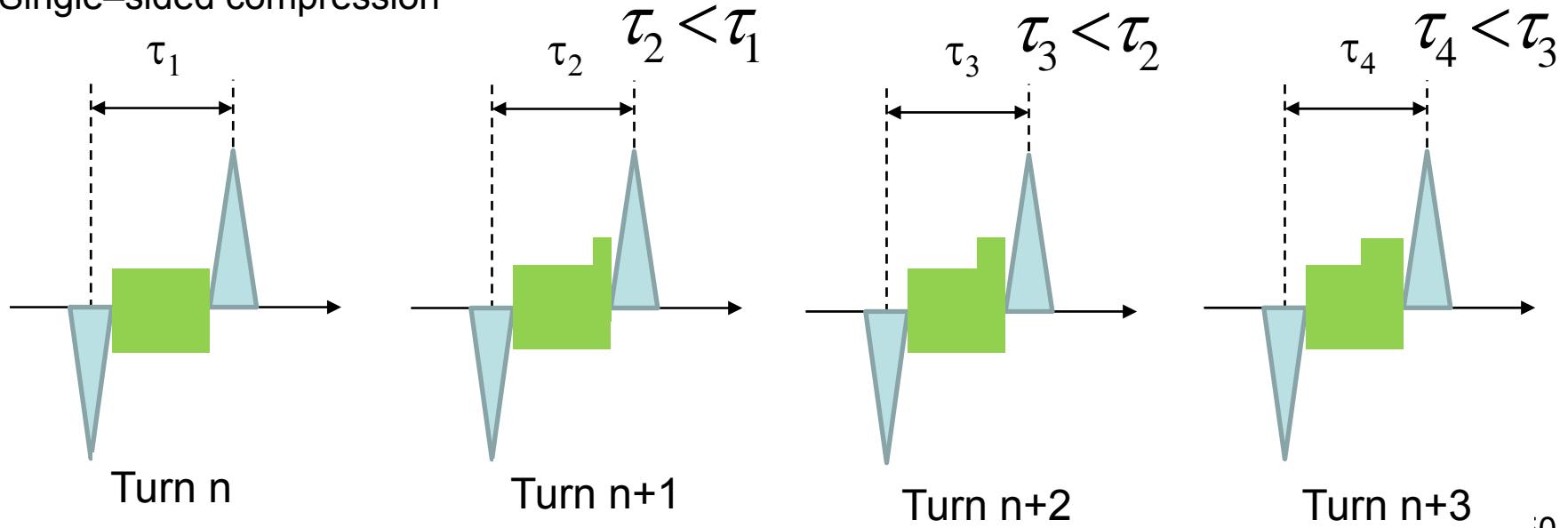


# Shock-Wave Bunch Compression

- Bunch compression in barrier system is usually slow
- The presence of longitudinal space-charge improves the efficiency of barrier compression by taking advantage of the shock-front that launches naturally if the barrier moves in a space-charge dominated beam
- The duration depends on the velocity of the shock front

## Creating the shock-front

Single-sided compression



# Simulations of Barrier Shock-Compression

The 0.6 mA beam

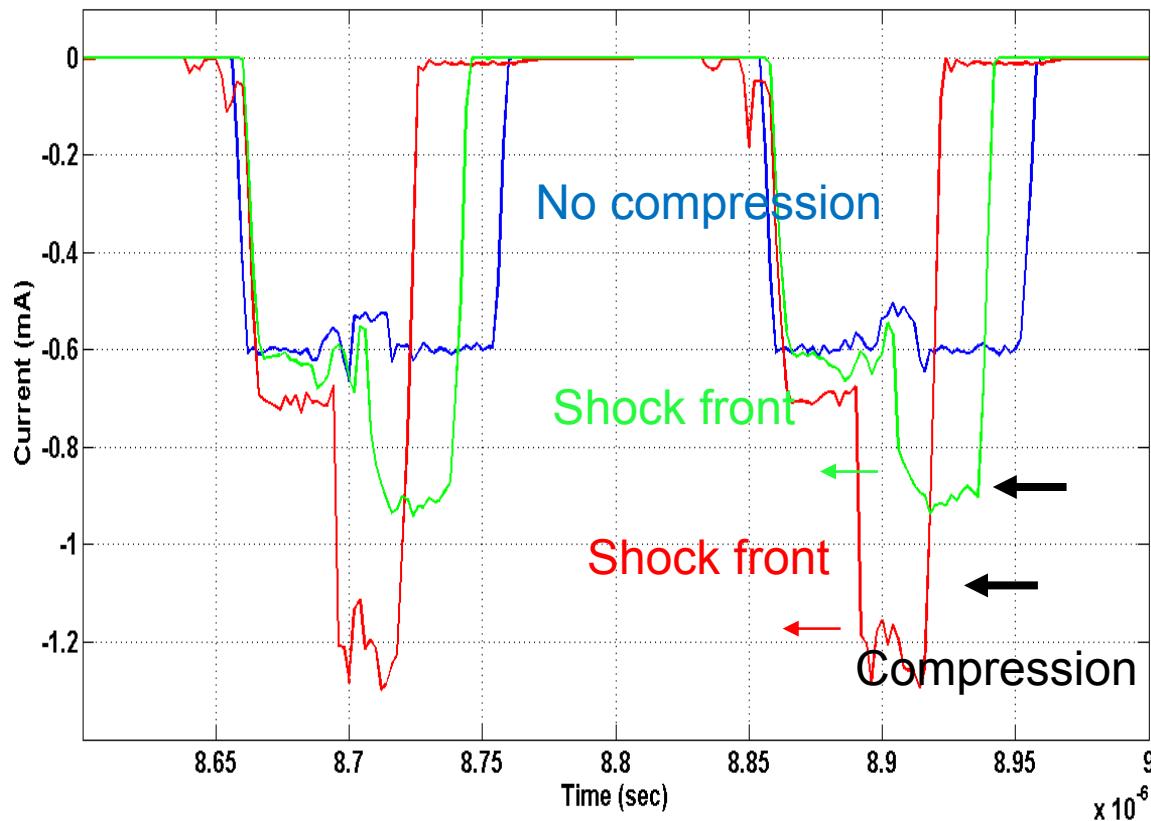
$$\frac{c_{so}}{V_o} = 0.0049$$

Initially  
 $\eta = 0.50$

**Current as a function of time**

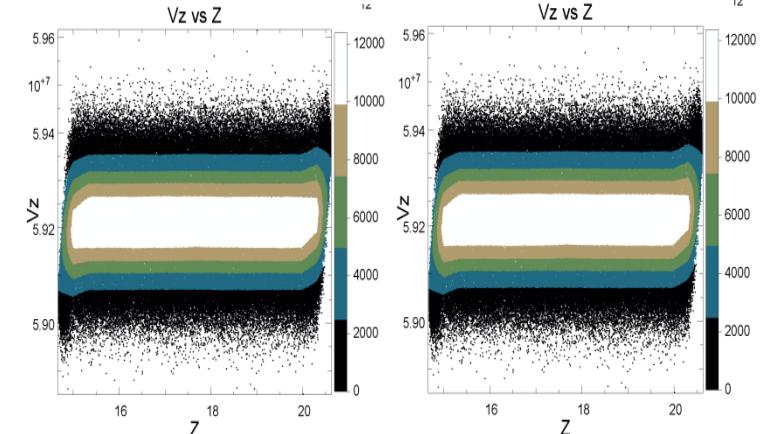
Turn 45

Turn 46

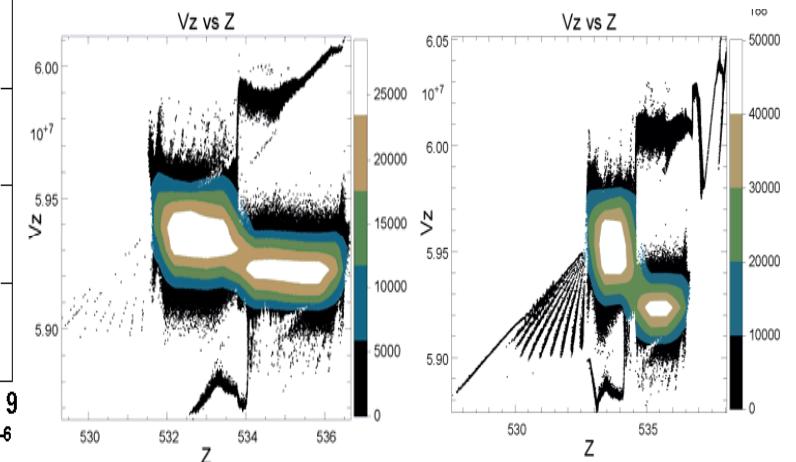


**Phase Space**

Slightly after Injection



Turn 45

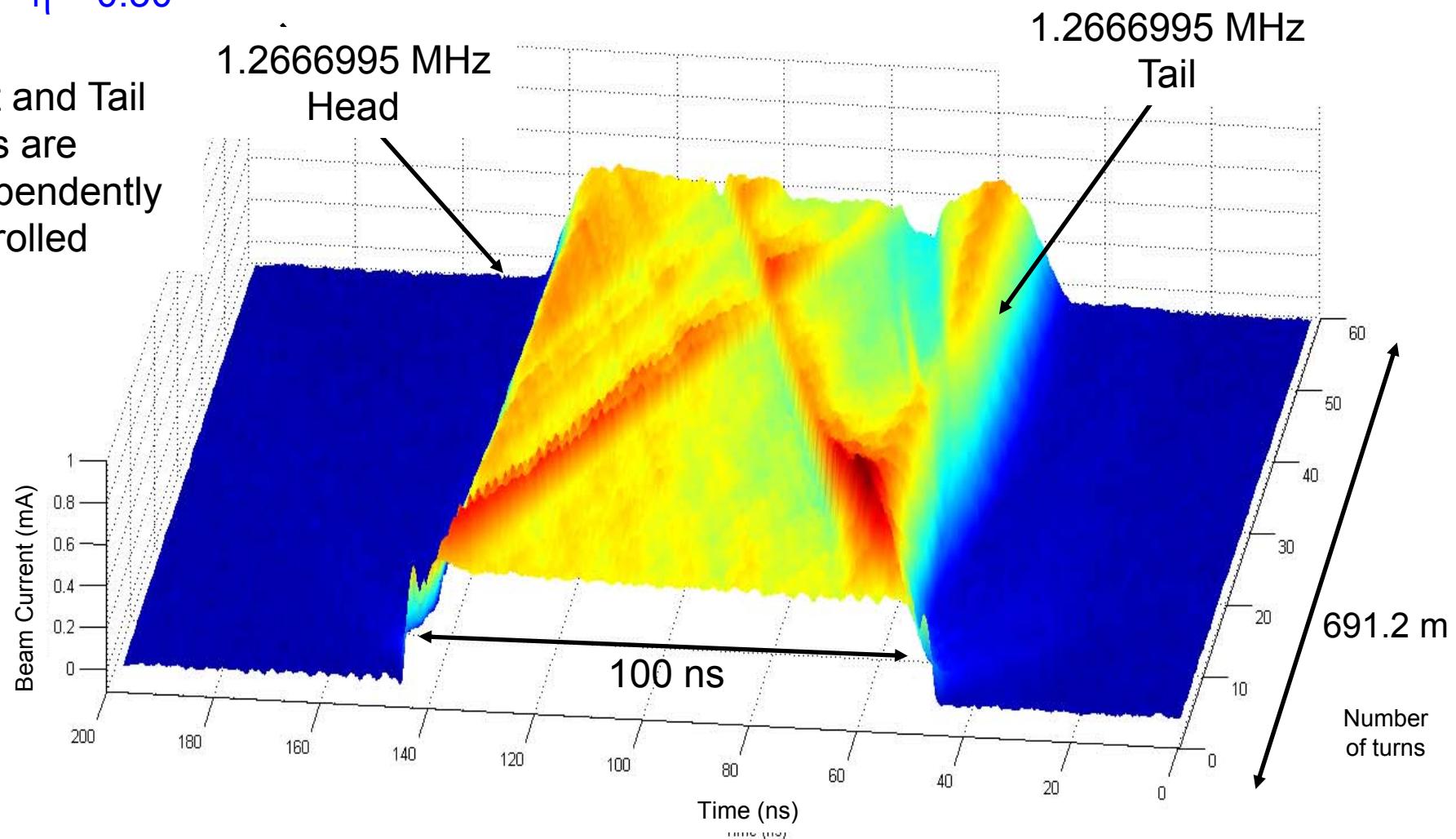


# Experimental Results of Symmetric Focusing

$$\frac{c_{so}}{v_o} = 0.0049$$
$$\eta = 0.50$$

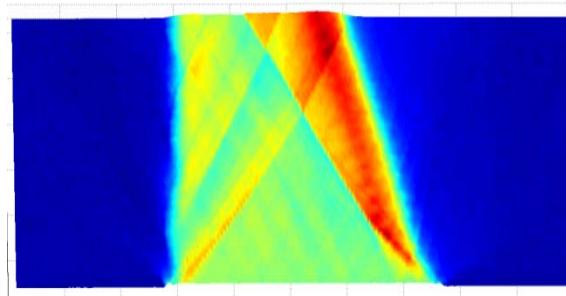
Heat and Tail fields are independently controlled

Nominally Contained No Compression

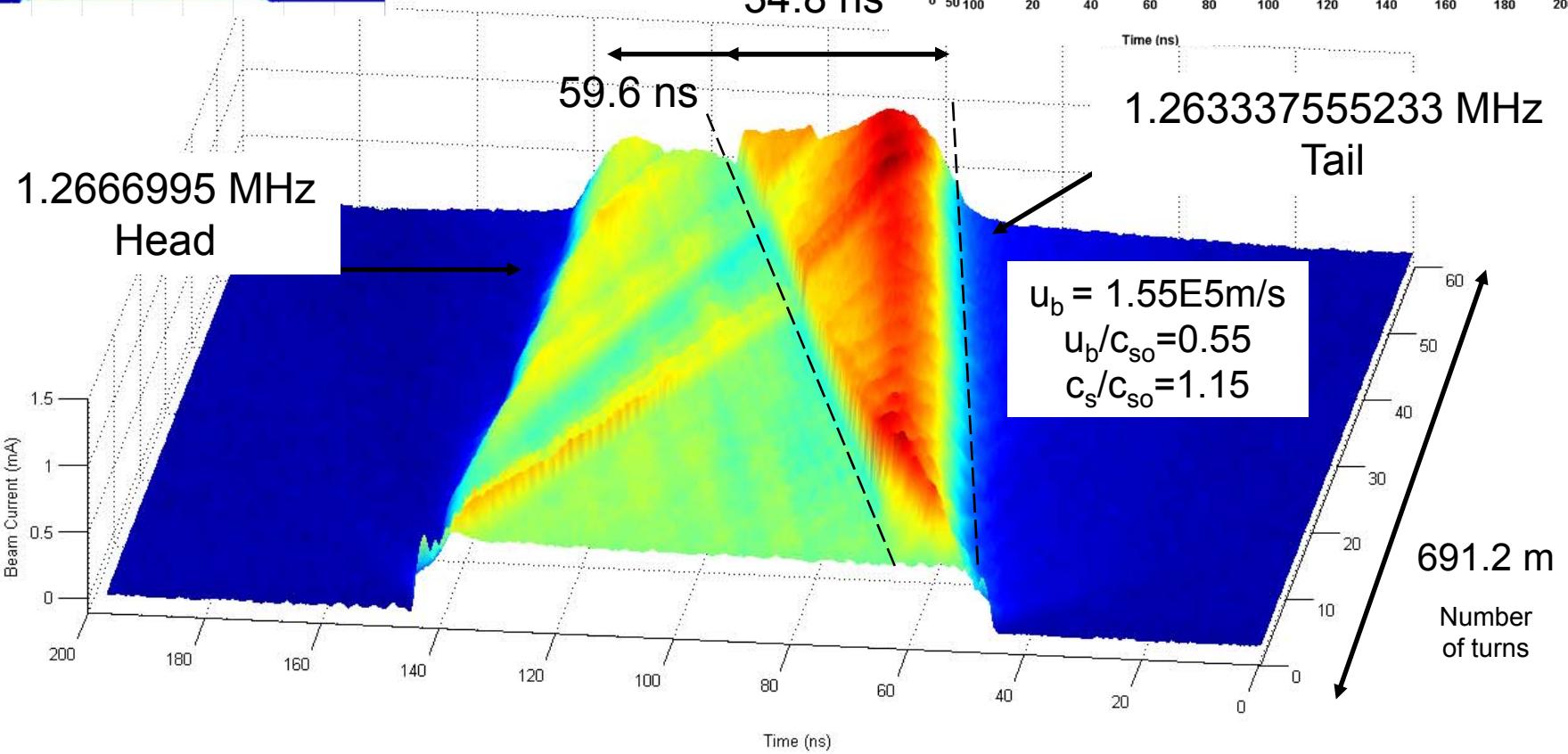


# Experimental Results of Asymmetric Focusing

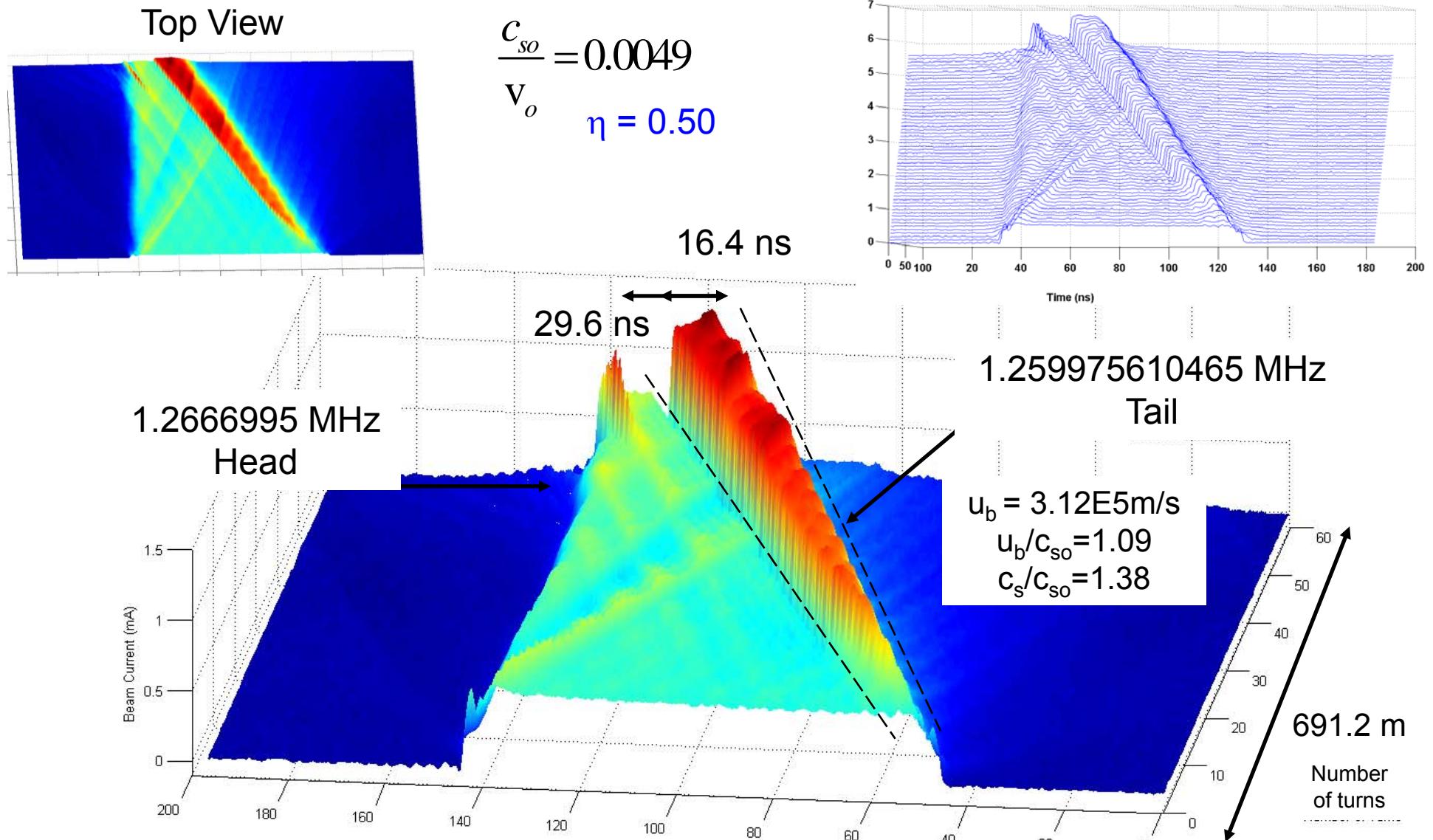
Top View



$$\frac{c_{so}}{v_o} = 0.0049$$
$$\eta = 0.50$$



# Experimental Results of Asymmetric Focusing



-B.L. Beaudoin, I. Haber, and R.A. Kishek, "Barrier Shock Compression with Longitudinal Space Charge", Proceedings of the 2015 International Particle Accelerator Conference, Richmond, VA, USA, May 2015, MOPMA044 (2015).

# Shock Velocity as a function of Barrier Velocity

The 0.6 mA beam

$$\frac{c_s}{c_{so}} = 2\sqrt{-Q} \cos\left(\frac{\theta}{3}\right) + \frac{2u_b}{3c_{so}}$$

$$\theta = \arccos\left(\frac{R}{\sqrt{-Q^3}}\right)$$

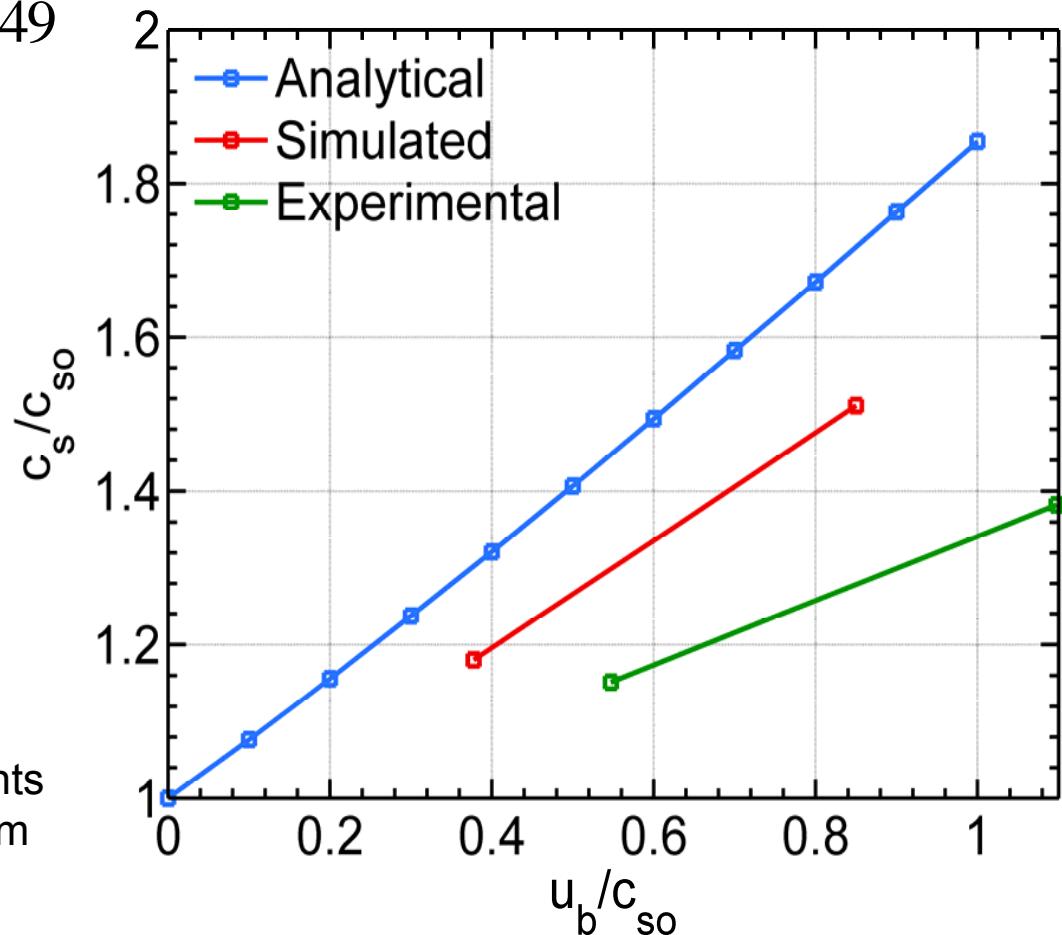
$$R = -\frac{1}{27} \left( \frac{u_b}{c_{so}} \right)^3 + \frac{u_b}{12c_{so}}$$

$$Q = -\frac{1}{9} \left( \frac{u_b}{c_{so}} \right)^2 - \frac{1}{3}$$

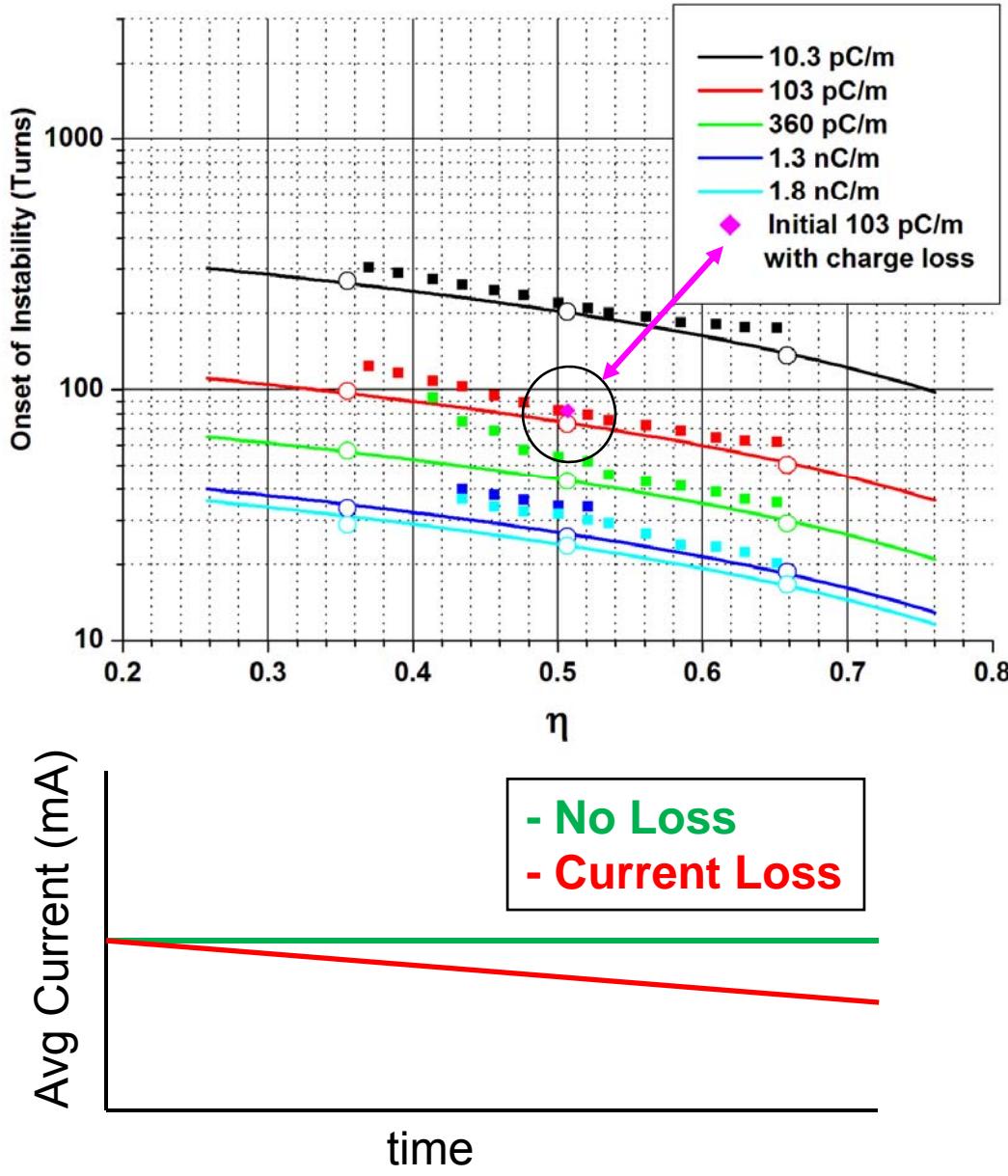
- The peak current increases with barrier velocity  $u_b$
- Expand study to other beam currents to understand dependence on beam intensity

$$\frac{c_{so}}{v_o} = 0.0049$$

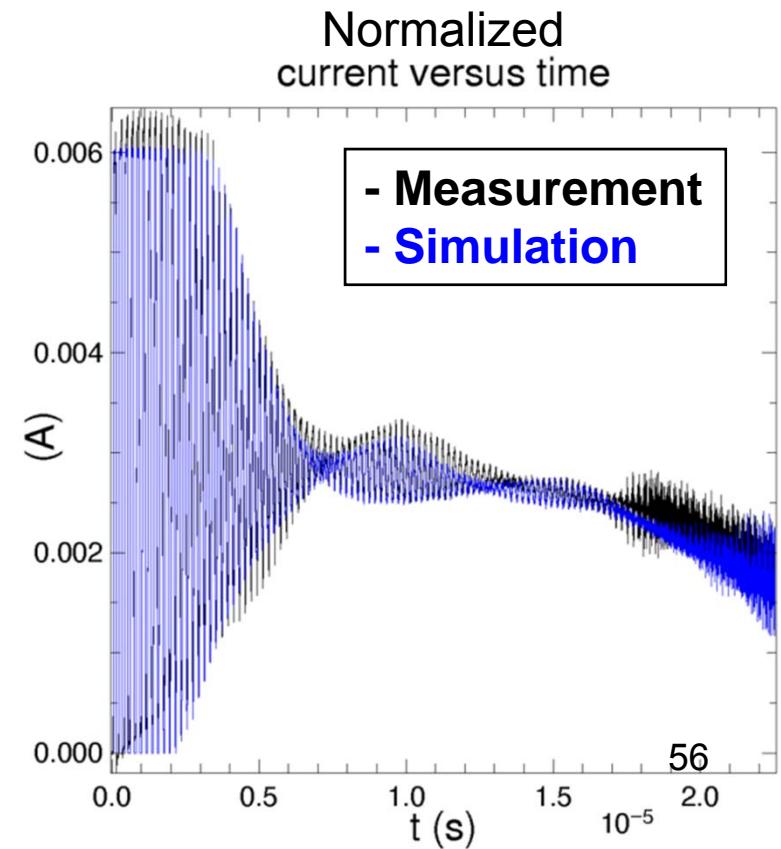
Initially  
 $\eta = 0.50$



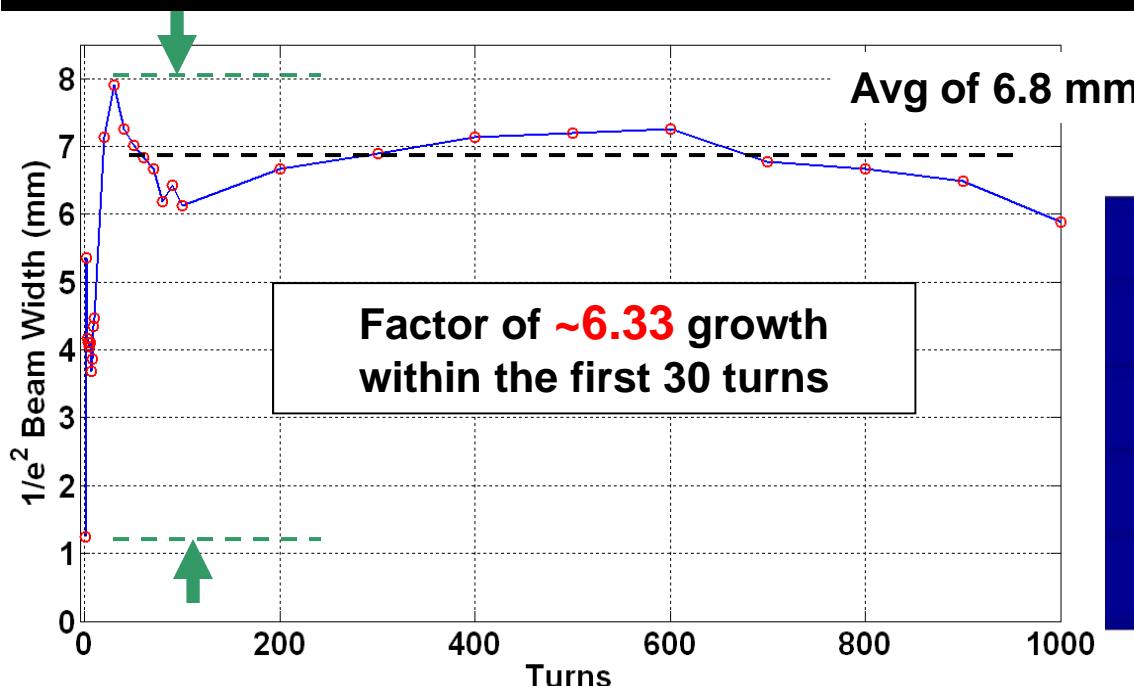
# Incorporating Transverse Current Loss into the Simulation Model



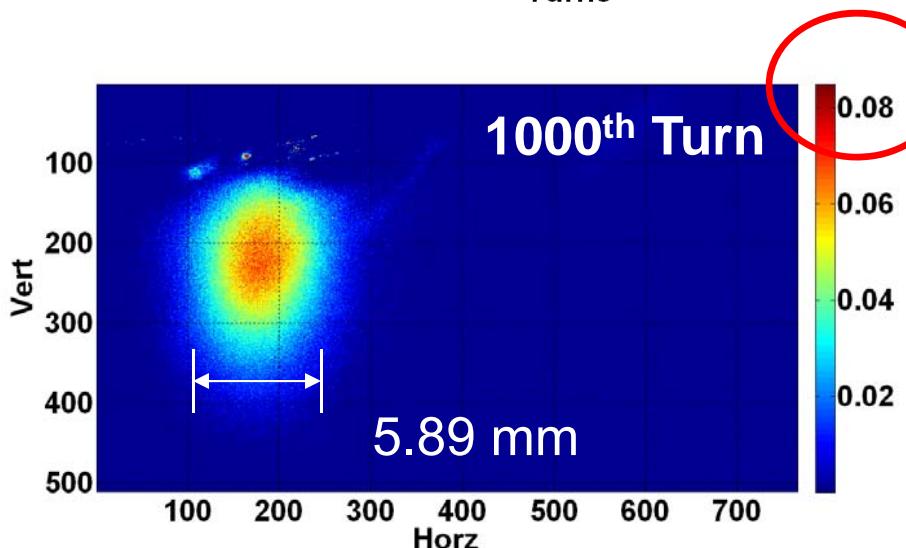
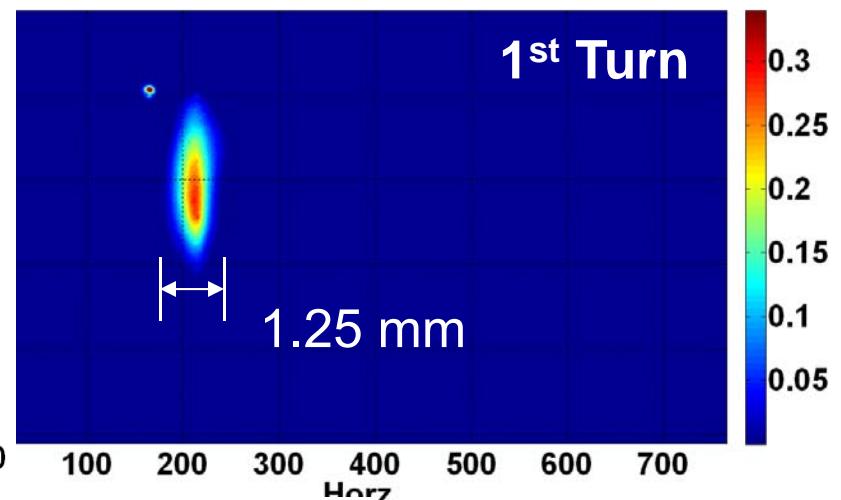
Current loss delays the longitudinal wave velocity,  $c_s$  and thus delays the onset of the instability



# Method to Confirm Beam Size per Turn



Vertical Extraction  
At RC8



Preserving 76 %  
of the intensity

