

Electron Injectors & Free-Electron Lasers

Bryant Garcia

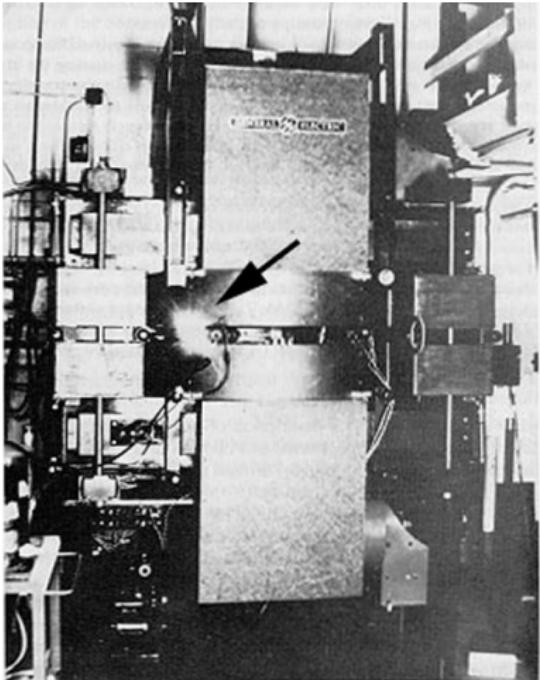
Friday, June 17 2016. USPAS Fort Collins, Colorado

- $m_e = 0.511\text{MeV}/c^2$; $m_p = 938\text{MeV}/c^2$; $m_p/m_e \approx 1835$!
- The beginning of the beamline: $E_{gun} \sim 1\text{MeV}$
 - Electrons are almost immediately relativistic
- This affects synchrotron radiation:

$$P_s \sim 1/m^4$$

- Electrons are often considered in *linear* machines because of this
- Differences in Radiation protection, beam dumps, etc. – won't cover

- Synchrotron Radiation discovered in 1947 at the 70 MeV GE synchrotron
- Originally a loss mechanism for electron synchrotrons ("On the maximal energy attainable in betatron", (1944))
- Spells the doom for (circular) electron machines as energy frontier devices but ...

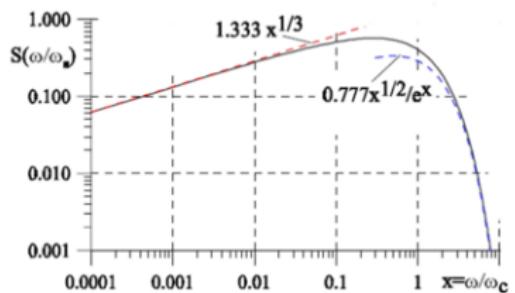
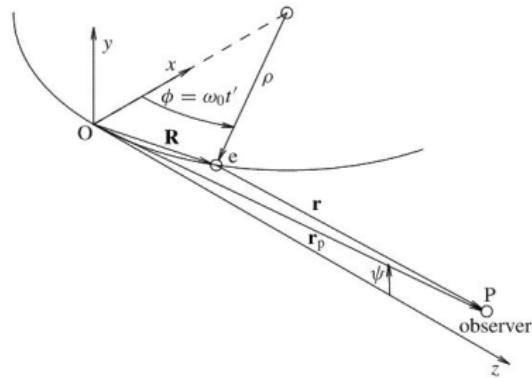


- A tough (but straightforward) EM calculation gives,

$$\frac{dW}{d\omega} = \frac{\sqrt{3}e^2}{4\pi\epsilon_0 c} \gamma \frac{\omega}{\omega_c} \int_{\omega/\omega_c}^{\infty} K_{5/3}(x) dx$$

$$\omega_c \equiv \frac{3c}{2\rho} \gamma^3, \lambda_c = \frac{4\pi}{3} \frac{\rho}{\gamma^3}$$

- Wavelength spectrum peaked near λ_c
- $\gamma \sim 500$, $\rho \sim 10\text{m}$, $\lambda_c \sim 10\text{ nm!}$ (but broad!)
- Enables the tunable production of high energy, BRIGHT photon pulses



- FEL physics
 - Insertion devices
 - High Gain FEL
 - SASE vs Seeded
- The Magnetic Chicane
 - Bunch compression
- Electron Injector / Gun
 - Photocathode guns
 - Focusing Solenoids
 - Compression stages
 - Emittance oscillation

- 1st generation: Parasitic synchrotron radiation from high energy physics machines
- 2nd generation: Dedicated synchrotron machines for production of light
- 3rd generation: Evolved facilities with insertion devices, many beamlines
- 4th generation: Free-electron Lasers and Electron-recirculating linacs

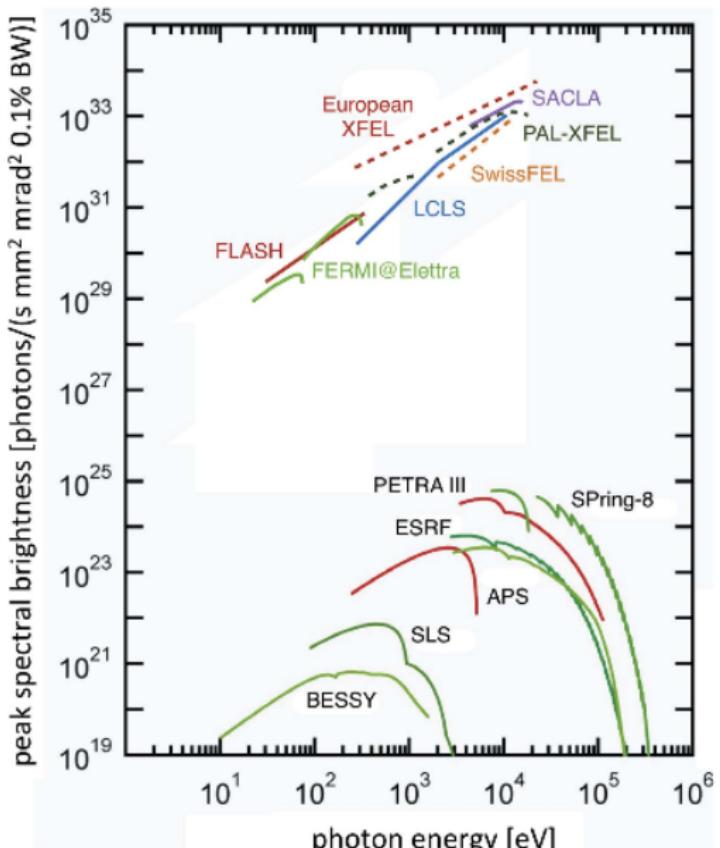


SSRL (SPEAR 2)

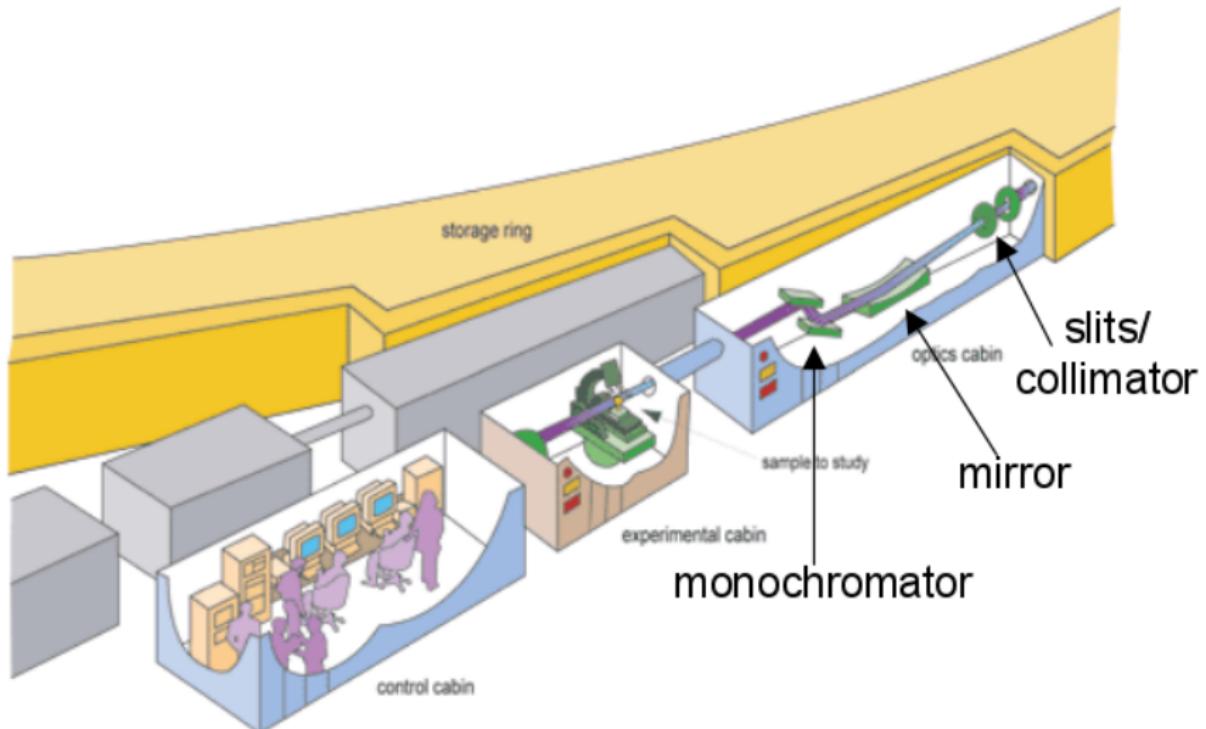


APS

The Spectral Brightness Race



The typical beamlines



The magnetic undulator

Series of alternating magnetic poles

with periodicity λ_u , $K \equiv \frac{eB_0}{k_u mc}$

$$x(z) = \frac{K}{\gamma k_u} \cos k_u z$$

Lorentz transform to the beam rest frame: $k'_u = \gamma k_u$ or $\lambda'_u = \lambda_u / \gamma$

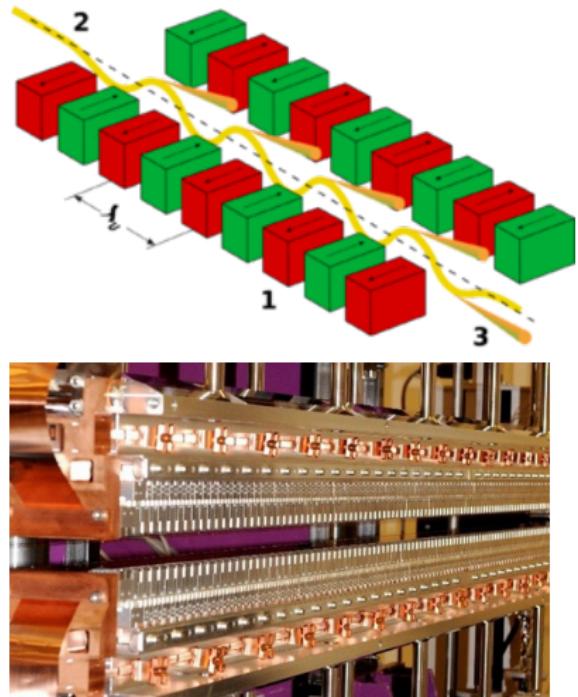
This is larmor radiation, and has

wavelength λ'_u

In the lab frame, this radiation is *blueshifted* again by a factor of 2γ , so we expect lab radiation

$$\lambda_r \sim \frac{\lambda_u}{2\gamma^2} \text{ Estimate}$$

$$\lambda_r = \frac{\lambda_u}{2\gamma^2} (1 + K^2/2 + \gamma^2 \theta^2) \text{ Reality}$$



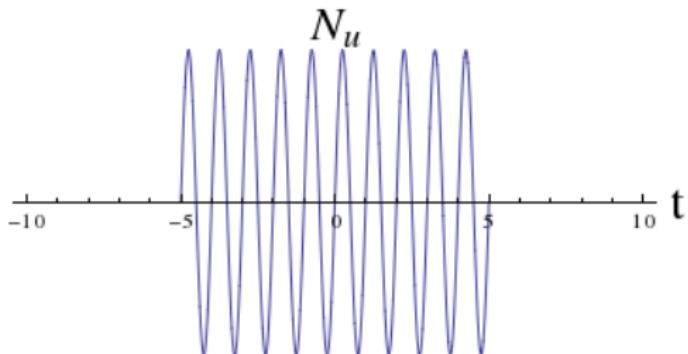
Undulator Radiation

The undulator radiation is then simply described as

$$E(t) = \begin{cases} E_0 e^{-i\omega_r t}, & -N_u \lambda_u / 2c < t < N_u \lambda_u / 2c \\ 0, & \text{otherwise} \end{cases}$$

Frequency response is found via fourier transform ($T \equiv N_u \lambda_u / 2c$)

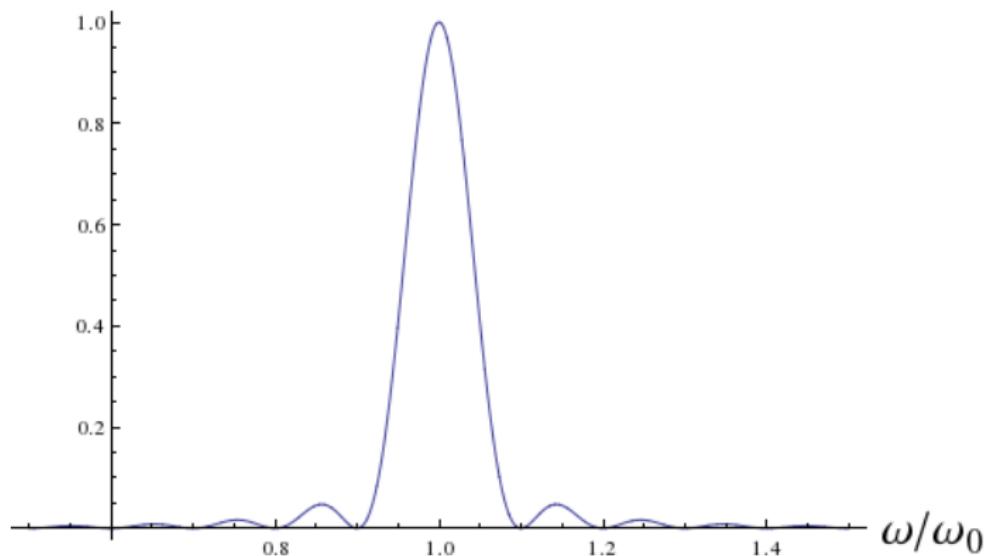
$$F(\omega) = \int_{-\infty}^{\infty} E(t) e^{i\omega t} dt = \int_{-T}^{T} E_0 e^{i(\omega - \omega_r)t} dt$$



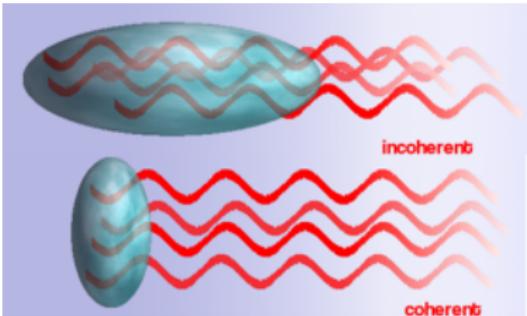
$$F(\omega) = 2TE_0 \operatorname{sinc}(T(\omega - \omega_0))$$

This spectrum has a FWHM $\Delta\omega = \omega_0/N_u$

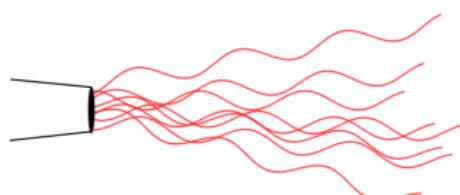
A



- Normally, electron radiation is *incoherent*, that is, the phase of each electron's emission is random.
- Incoherent power $P \approx N_e$.
- If the electron bunch has a size $< \lambda_r$, the phases are all roughly equal \Rightarrow Coherent emission
- $P \sim N_e^2$ for Coherent emission ($\sim 10^9!$)



Coherent Laser Light

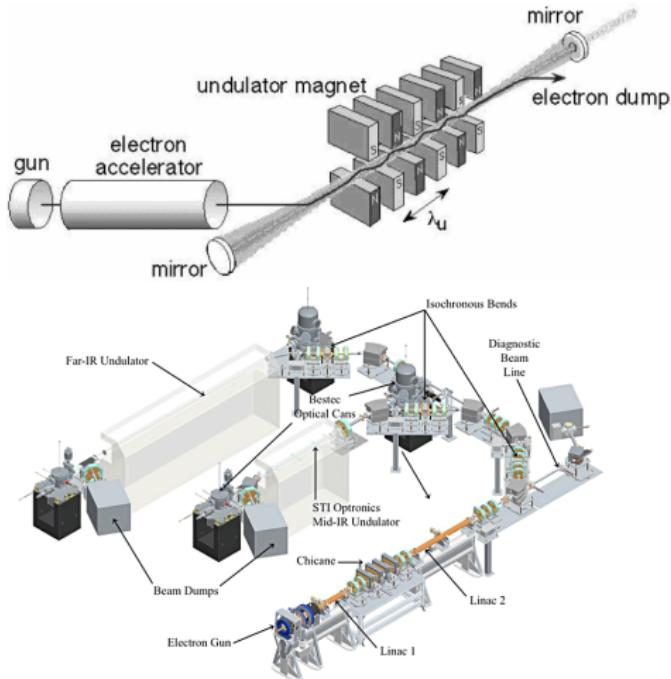


Incoherent LED Light

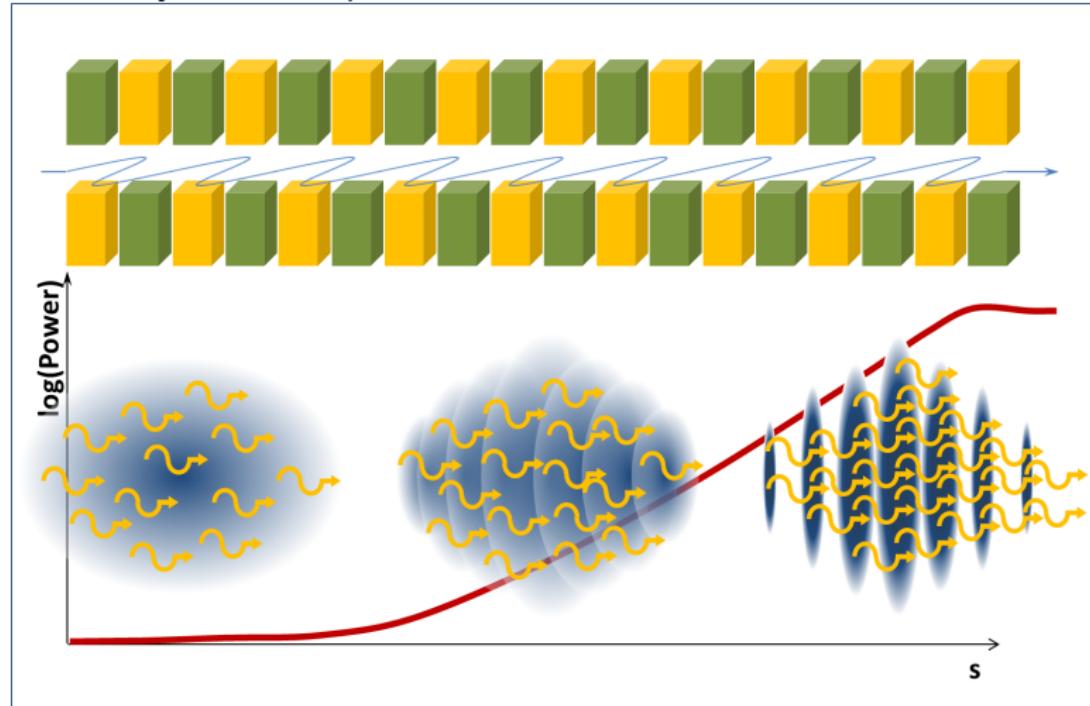
Free-Electron Lasers - Oscillators



- We can achieve coherence through *low-gain* operation and a cavity, as in a traditional laser
- Can use low energy e beams to make Visible-Microwave radiation
- Requires *reflective optics* at the wavelengths of interest \Rightarrow no X-rays

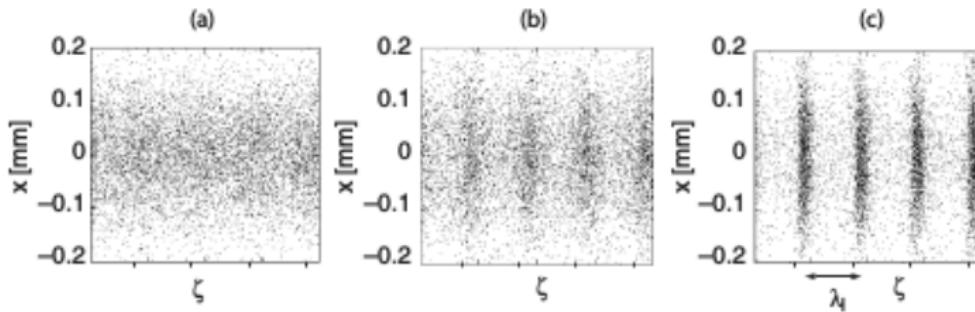


Another option is to have a very LONG undulator, and allow an instability to develop:



<http://lcls.slac.stanford.edu/AnimationViewLCLS.aspx>

- The radiated light becomes intense enough to back-react on the electron bunch
- The effect is to *bunch* the electrons up at the radiation wavelength



- The bunching \Rightarrow more coherent emission \Rightarrow stronger EM field \Rightarrow more bunching

[Video]

- The physics of the FEL process is all (basically) controlled by a single parameter ρ :

$$\rho = \frac{1}{2\gamma} \left(\frac{\hat{K} \lambda_u}{2\pi\sigma_b} \right)^{2/3} \left(\frac{I}{I_A} \right)^{1/3}$$

$$P_{\text{sat}} = \rho \left(\frac{IE_b}{e} \right) = \rho P_{\text{beam}}$$

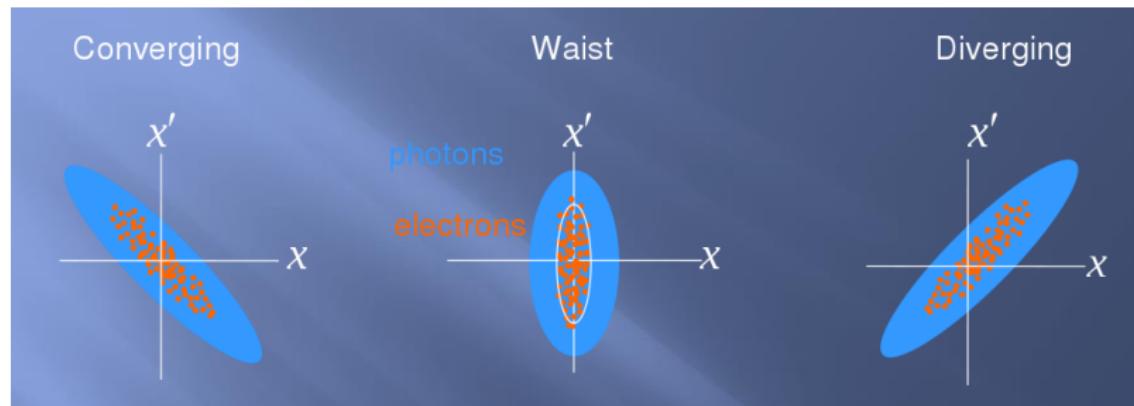
$$L_g = \frac{\lambda_u}{4\pi\sqrt{3}\rho}$$

- For reference, modern X-ray FELs have $\rho \sim 5 \times 10^{-4}$, $\lambda_u \sim \text{cm}$. So $L_g \sim \text{few meters}$.
- Turns out you need $\sim 20L_g$ to saturate \Rightarrow very long undulators

To maintain *spatial* coherence, the phase space volume of the electrons should be less than the phase space volume of the photons:

$$\epsilon_{\text{electrons}} < \epsilon_{\text{photon}}$$

$$\epsilon_{\text{electrons}} < \frac{\lambda_r}{4\pi}$$



$\lambda_r \approx 1\text{nm} \Rightarrow \epsilon < 0.1\text{nm}!$ This is very small!

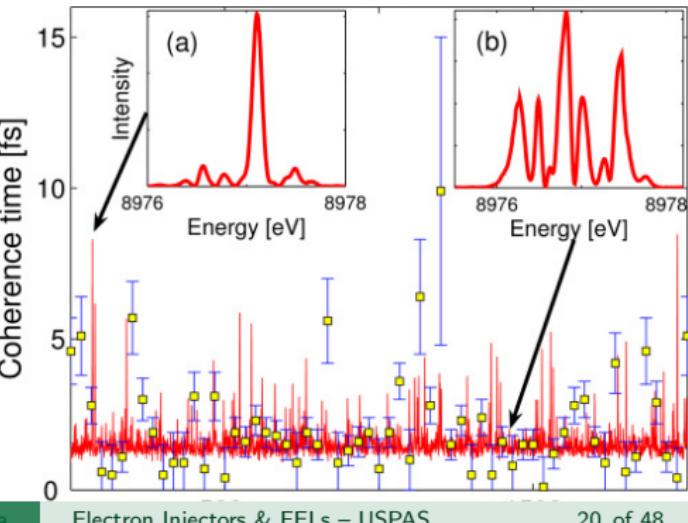
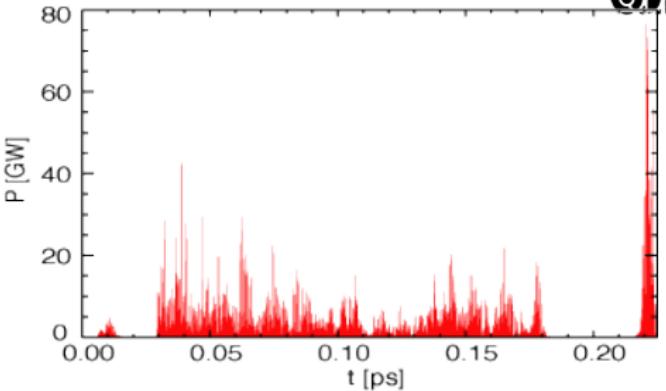
Storage rings have a natural emittance $\sim\text{nm}$ at best, so cannot be used for X-ray FELs \Rightarrow linac sources

- Require very low emittance (for transverse matching)
- Require high energy electrons (for low λ_r)
- Require high peak current I/I_A (for high ρ)



SASE Operation Mode

- Random electron beam seeds the instability with *noise*
- Locations/size of lasing regions are stochastic
- Many spectral spikes, non-utilization of full electron beam
- *Spatially but not temporally* coherent radiation

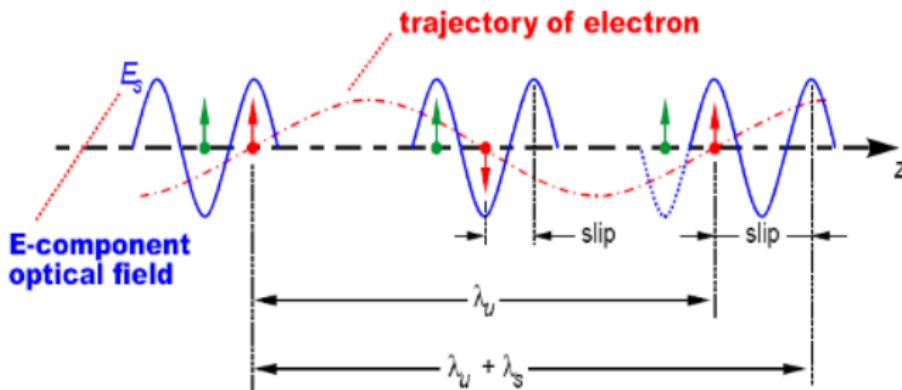


Coherence Length

The reason for the many spikes is that information is generally not propagated through the whole electron beam

$$\lambda_r = \frac{\lambda_u}{2\gamma^2} (1 + K^2/2)$$

This is also a *resonance* condition:

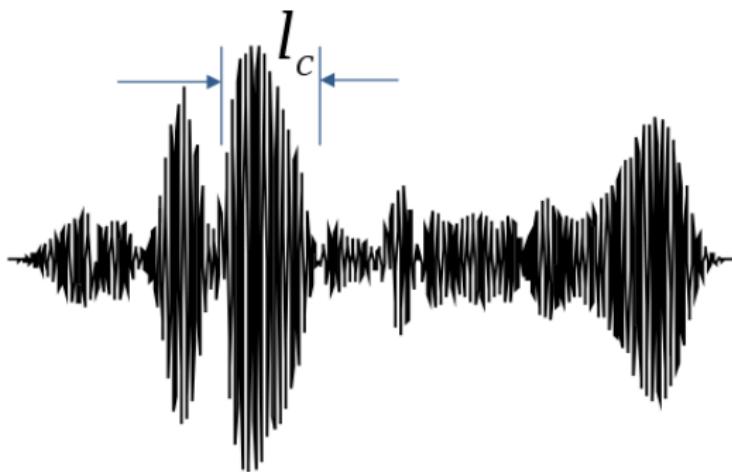


$$\frac{\lambda_u + \lambda_s}{c} = \frac{\lambda_u}{v_z} \iff \lambda_s = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} \right)$$

The light slips forward by one radiation wavelength per undulator period

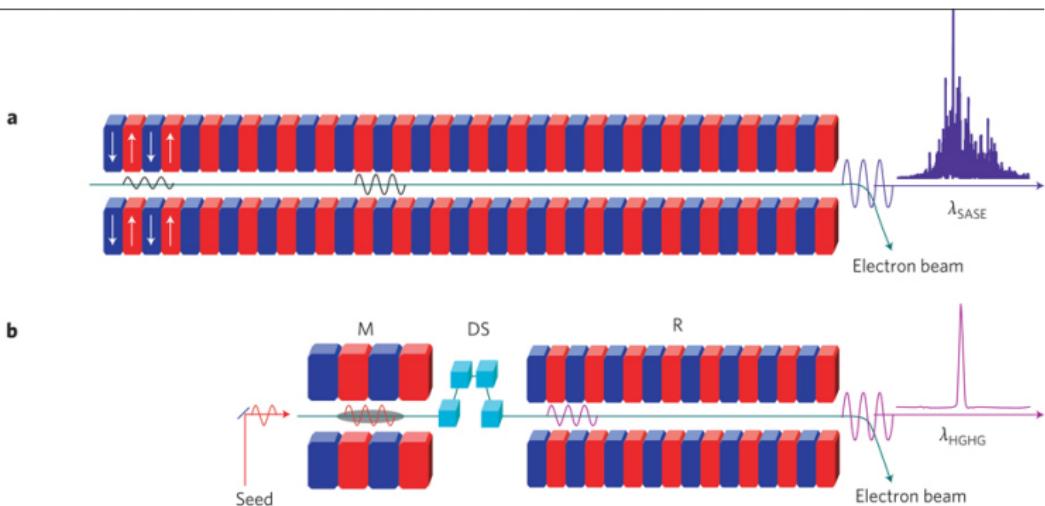
Coherence Length: Slippage in one gain length

$$L_c \approx \lambda_r / \pi \rho \ll l_{\text{beam}}$$



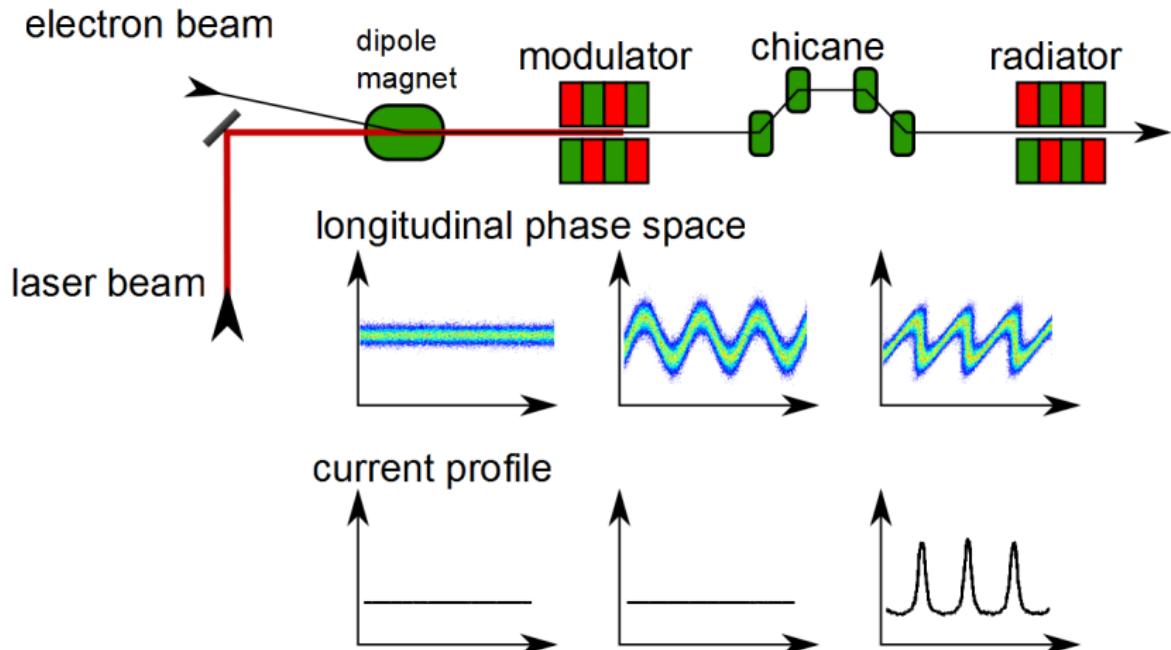
So the individual SASE spikes never have time to fully communicate

If we could introduce a coherent seed to the process, all areas of the beam would (ideally) radiate identically – Pure spectrum



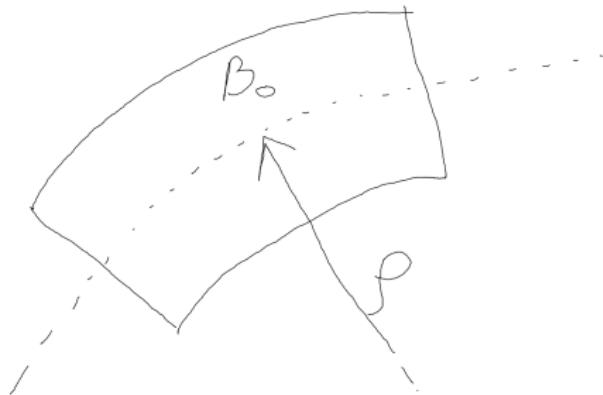
But how can we do this without the required lasers?

Use a conventional laser to create high harmonic density bunching
(to seed the coherent emission)



- We've focused on transverse dynamics so far, but the need for peak current (and seeding) forces us to look in the longitudinal plane
- To compress, we need to be able to move particles longitudinally (R_5 ; transport components)

Consider a simple dipole magnet, bending in a radius ρ through an angle θ for the reference particle with momentum p .



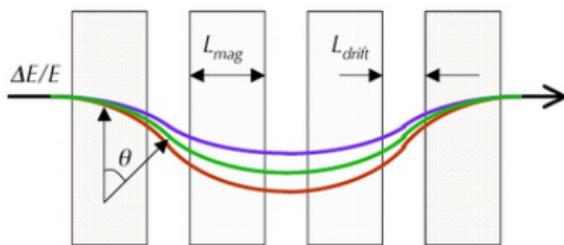
The result is that

$$ds/(\delta p/p) = \rho_0 (\theta - \sin \theta) - \frac{\rho_0 \theta}{\gamma^2}$$

- More energetic electrons travel a longer distance
- For relativistic particles $\gamma \gg 1$, they arrive *later* than their low energy counterpart \Rightarrow prism!

Magnetic dipoles are longitudinally (as well as transversely) dispersing optics

Put 4 dipoles, to have the trajectory return to the straight path to form a chicane:



Higher energy particles travel a shorter distance \Rightarrow dispersing in longitudinal space:

$$ds/(\delta p/p) = 2\theta^2(L_{\text{drift}} + \frac{2}{3}L_{\text{mag}})$$

Note: Can use 2 dipoles if you desire a beamline shift (but horizontally dispersing)

JLab Magnetic Chicane



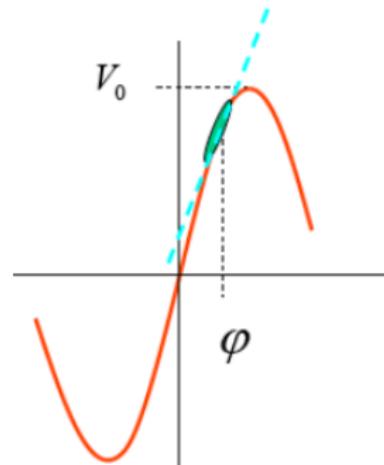
- Enter accelerating cavity off-crest to provide an energy-time(distance) correlation

$$V(z) = V_0 \sin(k_0 z)$$

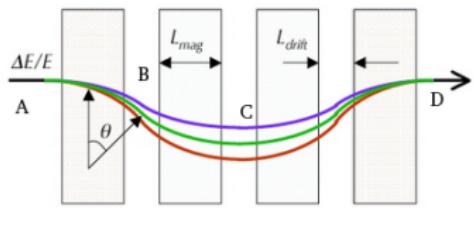
Where $k_0 = 2\pi/\lambda_{RF}$ is the RF wavevector, so (assuming the bunch is ultra-relativistic and does not slip with respect to the RF wave)

$$E(z) = E_0 + eV_0 \sin(k_0 z + \varphi)$$

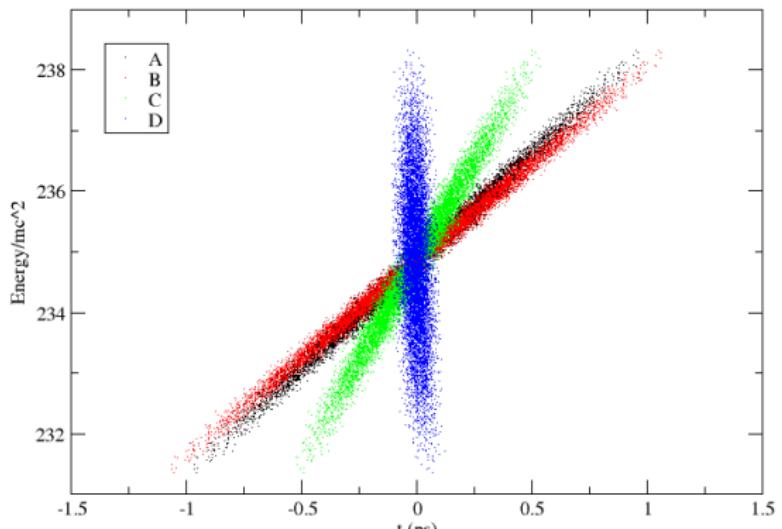
$$\frac{dE}{dz} = eV_0 k_0 \cos(k_0 z + \varphi) \approx eV_0 k_0 \cos(\varphi)$$



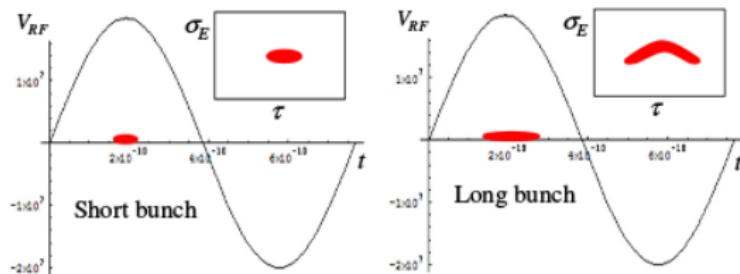
Bunch Compression



$$\sigma_{z,f} = (R_{56,O})\sigma_{\delta i}E_0/E$$



- For a bunch with comparable length to RF, the beam acquires quadratic curvature:



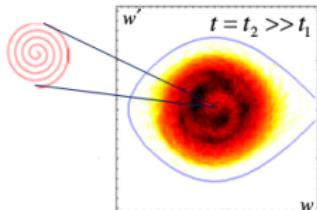
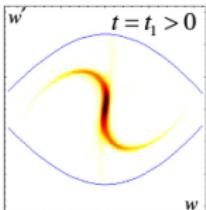
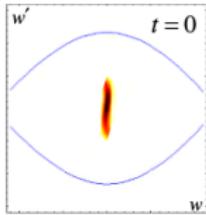
- 'Banana shape' limits compression
- Can use a harmonic cavity to correct the quadratic curvature term
- An infinite harmonic series \Rightarrow a perfectly linear beam over ALL scales

Electron Injectors

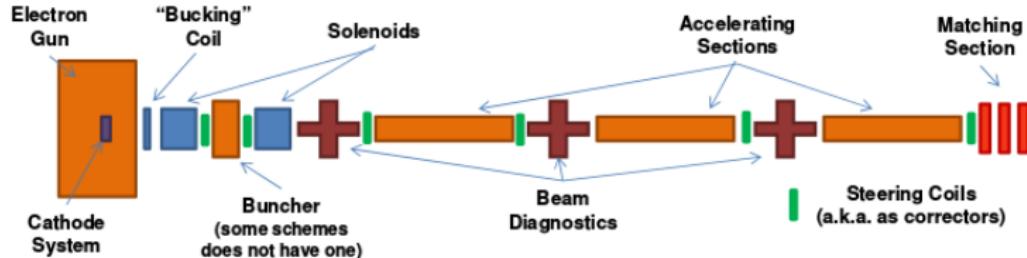
* Many slides taken/adapted from USPAS 2016 Course “Electron Injectors for 4th Generation Light Sources” F. Sannibale, D. Filipetto, C. Mitchell

- The electron injector is where the electrons are born and enter the accelerator environment
- Accelerator complex divided between 'injector' and 'accelerator'
 - Generally 'injector' ends when space charge forces are negligible
 - Space charge are beam self-forces, $\sim 1/\gamma^2$
- Space charge forces are in general *non-linear*, and can *increase* the rms emittance of the beam
- So the injector performance defines a limit for beam emittance

$$B = \frac{N}{\epsilon N_x \epsilon N_y \epsilon N_z} \quad \text{6-D Beam Brightness}$$

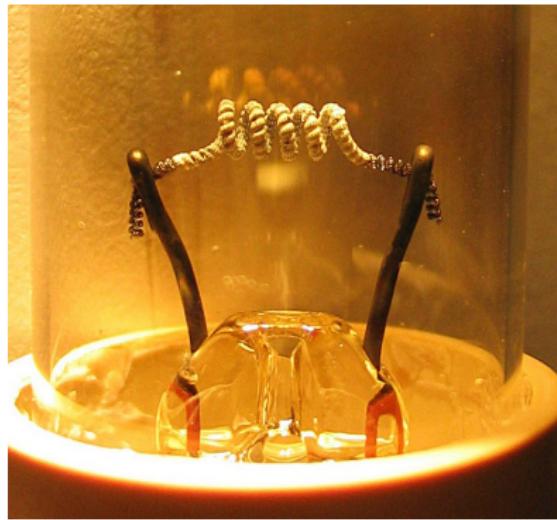


Electron Injector Subsystems



- Cathode system
- Gun
- Focusing Solenoids
- Buncher
- Accelerating systems
- Matching

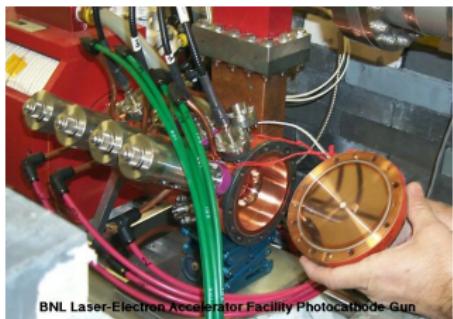
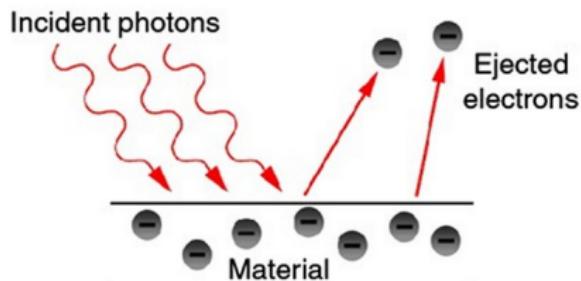
- Hot filament simply emits electrons when heated
- Energy of electrons depends on temperature
- Electron distribution depends critically on cathode geometry
- CONTINUOUS (every RF Bucket) OPERATION



- Photocathodes: Laser impinges on material, photoelectric effect liberates electrons

$$E = \hbar\omega - \phi$$

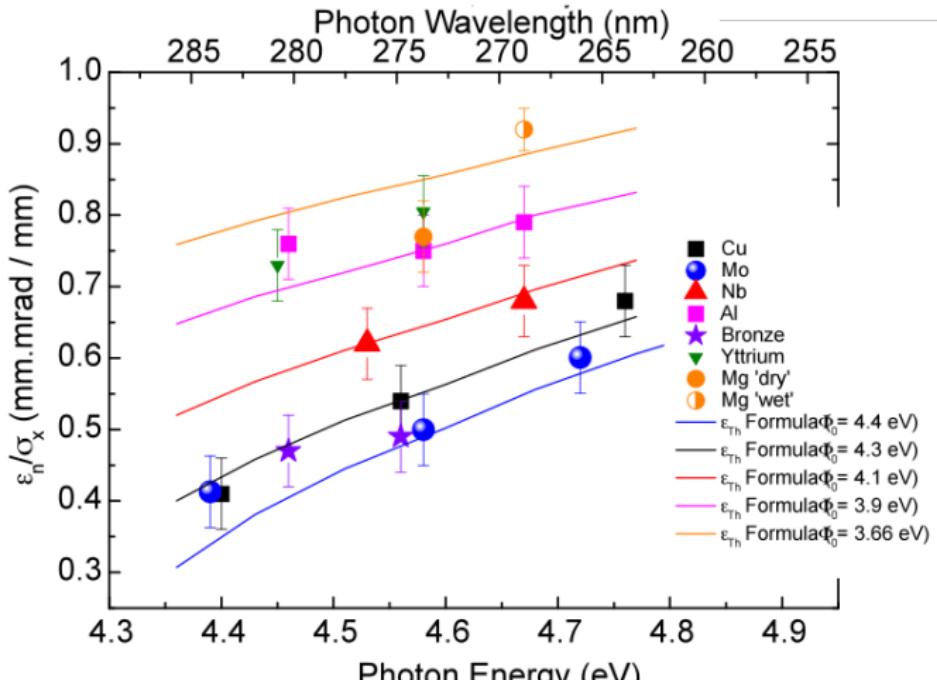
- Work function ϕ , and QE depend critically on material
- Requires laser system, usually in the UV (266nm)
- Fairly tunable via laser spot size, pulse duration. Prompt response.
- usually PULSED OPERATION



Photocathode Emittance

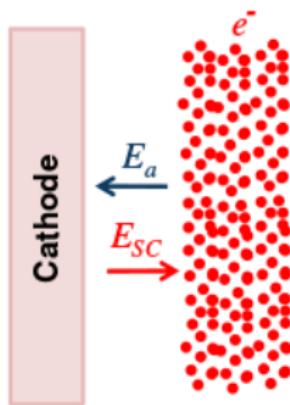
Excess energy from the photons leads to increased electron (transverse!) velocity \Rightarrow increased emittance

$$\epsilon \sim \sqrt{\hbar\omega - \phi + E_{\text{schottky}}}$$



Extractable Charge

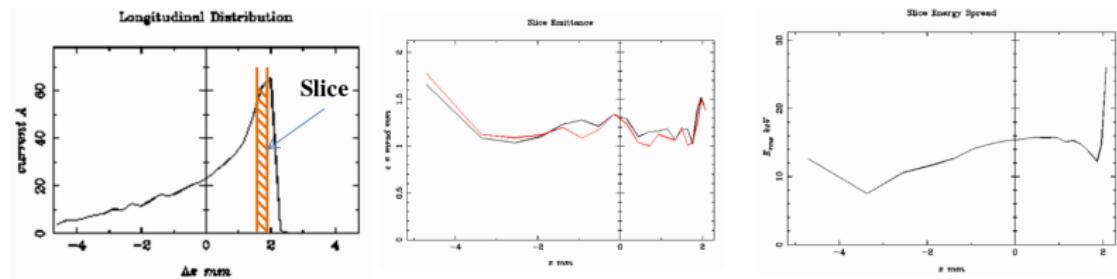
- FELs sensitive to peak current AND total beam power \Rightarrow want a lot of charge, and high peak current
- Operational optimum usually found \sim 100s of pC/bunch
- Note: Can trade lower peak power for shorter gain length (generally)
- Space charge field defines maximum charge density extractable (Higher acc. field helps!)



Digression - Slice Vs. Projected Quantities



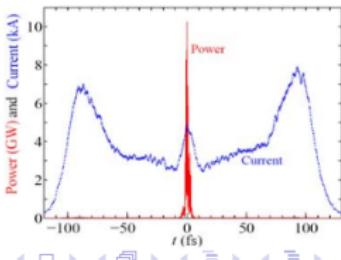
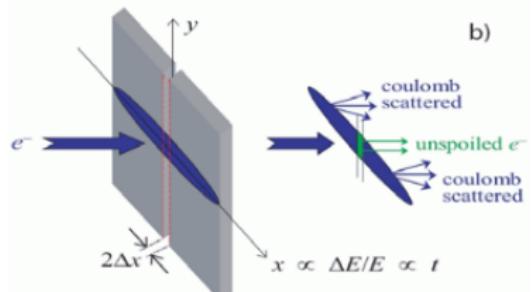
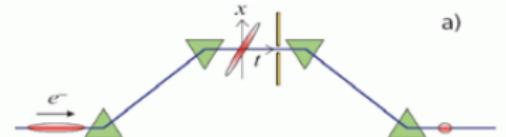
The FEL physics ρ is generally sensitive only to the parameters in a local region 'slice' of the electron beam



Length of slice is \sim slippage length over the undulator $\sim N_u \lambda_r$
So we generally only require a *portion* of the electron beam to have good parameters out of the injector

Digression - Emittance Spoiling

- Can use this slice v. projected to lase on select portions of the beam
- Dispersive chicane + slotted foil picks out a *temporal* portion of the beam to preserve emittance
- Elaborate foils can be used to fully tune multiple pulses w/ durations and separations

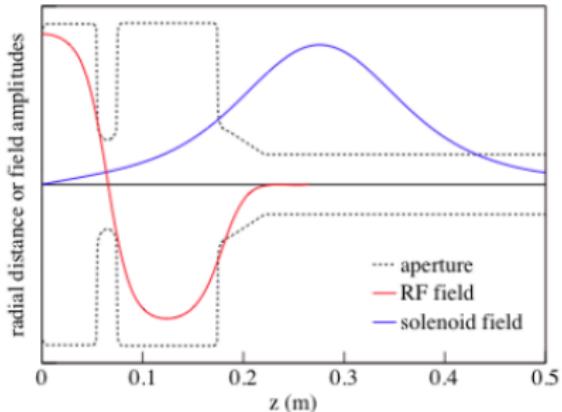


High Gradient RF Gun

- Electrons emitted, need to capture them and accelerate quickly \Rightarrow high gradient RF fields
- At this point, electrons are very non-relativistic, so they slip relative to the RF wave by a lot
- Need to adjust phase of RF for maximum acceleration gradient \Rightarrow ride the wave

$$L_{\text{acc}} = \frac{mc^2}{eE_0} < \lambda_{RF}$$

$\lambda_{RF} \sim \text{mm} \Rightarrow E_0 \sim 50\text{MV/m} !!!$



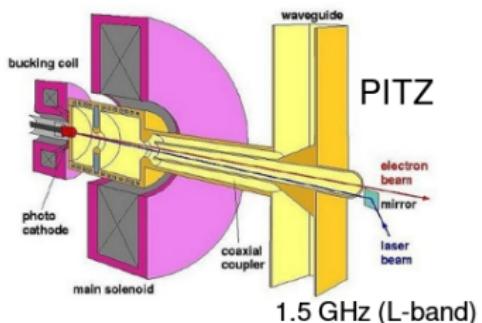
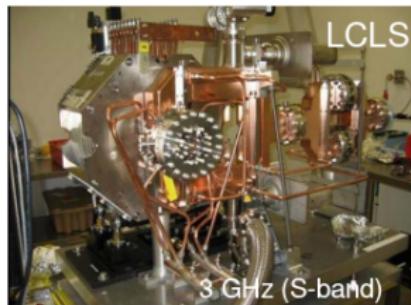
Normal Conducting High Frequency RF Guns



LCLS

Pros:

- High gradients from ~50 to ~140 MV/m
(20 – 60 MV/m at cathode during photo-emission)
- “Mature” technology.
- Full compatibility with magnetic fields.
- Compatible with most photocathodes
- Proved high-brightness performance.
(LCLS, PITZ, ...)

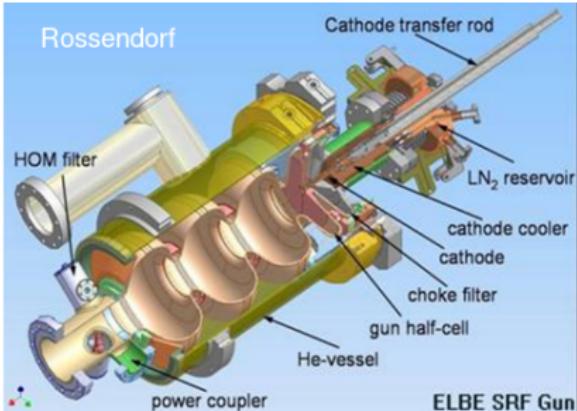


Areas for improvement:

- High power density on the RF structure ($\sim 100 \text{ W/cm}^2$) limits the achievable repetition rate at high gradient to $\sim 10 \text{ kHz}$.
- Relatively small pumping apertures can limit the vacuum performance.

Pros:

- Potential for relatively high gradients (several tens of MV/m)
- CW operation
- Excellent vacuum performance.
- Promising results by several groups (Rossendorf, Wisconsin, HZB, BNL, ...)

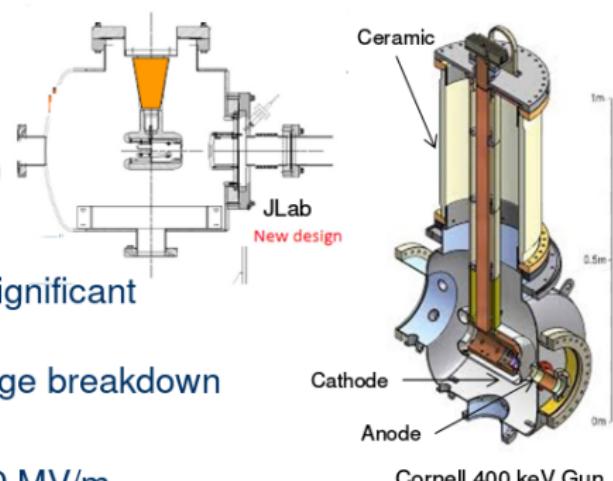


Areas for improvement:

- Move technology into a more mature phase. Significant progresses under way.
- Experimentally verify cathode/SRF compatibility issues (Promising results with Cs₂Te at Rossendorf, DC-SRF Peking approach). Develop higher QE super-conducting cathodes.
- Difficult emittance compensation (Meissner field exclusion, magnetic field induced quenching, ...).

Pros:

- DC operation
- DC guns reliably operate at 350~380 kV (JLAB, Cornell), ongoing effort to increase the final energy (Cornell, Daresbury, Jlab, JAEA, KEK,...).
- Simulations and recent results (Cornell) demonstrated the capability of sub-micron emittances at ~ 0.3 nC, with ~380 keV beam energies.
- Full compatibility with magnetic fields.
- Excellent vacuum performance
- Compatible with most photo-cathodes.
(The only one operating GaAs cathodes)



Areas for improvements:

- Higher energies require further R&D and significant technology improvement.
- In particular, improvement of the high voltage breakdown ceramic design and fabrication.
- Relative low gradients at the cathode $<\sim 10$ MV/m
- Developing and test new gun geometries (inverted geometry, SLAC, JLab)
Very interesting results from a “pulsed” DC gun at Spring-8.

The Solenoid Magnet

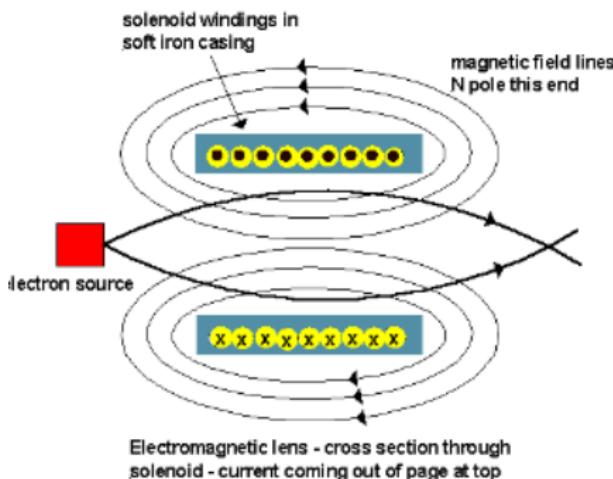
- Solenoids are capable of focusing *in both planes*

$$B_z(r, z) = B_z(z) - \frac{r^2}{4} B_z''(z)$$

$$B_r(r, z) = -\frac{r}{2} B'(z) + \frac{r^3}{16} B_z'''(z)$$

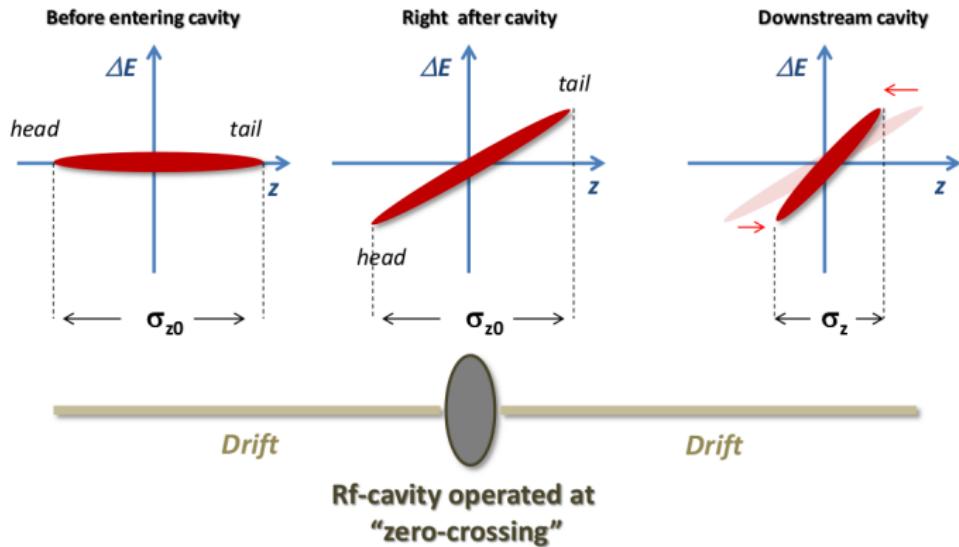
$-\frac{r}{2} B'(z)$ induces a rotative velocity, which in turn focuses the beam in $r \Rightarrow$ both x and y!

- Useful for focusing and controlling the beam *quickly* in the low energy region



Velocity Bunching

Low energy electrons streaked with a zero-phased RF cavity



Recall in a drift

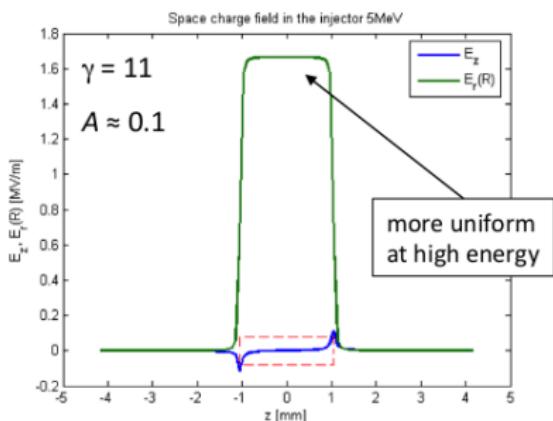
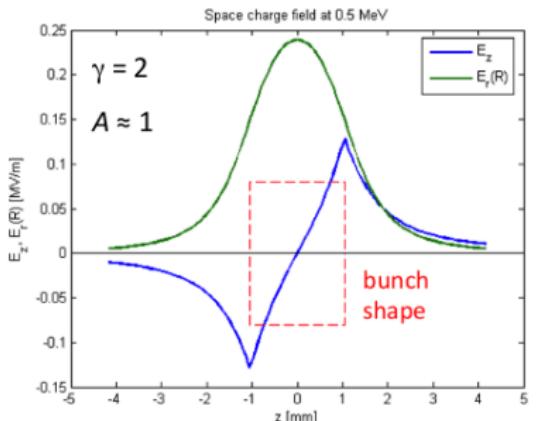
$$ds/(dp/p) = \frac{L}{\gamma^2}$$

Effective compression at low energy!

Relativistic Space Charge & Emittance Oscillation

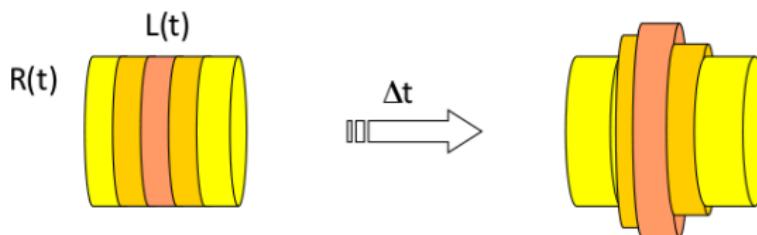


Space charge electric field components E_z and E_r for a finite, uniform cylindrical bunch:



$$A = R/(\gamma L)$$

effect of space charge fields on the bunch over a time Δt



How will this affect the emittance of the beam?

Emittance Oscillation & Compensation

- The different longitudinal positions of the beam trace out different ellipses
- The projected result *looks* like an RMS emittance increase
- Focus and align them all, THEN 'freeze in' emittance via accelerating section

