Accelerator Physics Homework #5

- 1. We have a synchrotron that accelerates protons from a kinetic energy of 10 to 100 GeV in 1 second, with the energy changing linearly with time. The circumference of the ring is 3km. The transition γ_{t} is 25.
 - a. (5 points) Calculate the revolution periods at
 - i. Injection (minimum) energy.
 - ii. Just below transition (say, $\gamma = 24$).
 - iii. Extraction (maximum) energy.
 - b. (5 points) The RF system has a harmonic number of 588; that is, one revolution period corresponds to 588 RF cycles. Calculate the RF frequency in MHz at each of these three energies (this difference may seem small, but changing the resonant frequency of a cavity is always hard).
 - c. (10 points) Calculate the slip factor (including sign) at each of the three energies.
 - d. (10 points) If I have an RF voltage of 1 MV, what synchronous phase ϕ_s do I need at these three energies (hint: what is the change in energy per turn)?
 - e. (10 points) Calculate the longitudinal beta eta_L at each of the three energies.
 - f. (10 points) Calculate the maximum bucket height ΔE_b at injection (hint: Longitudinal Motion lecture, p. 12)
 - g. (5 points) Assuming the injected bunch is matched to the bucket with $\sigma_E = \frac{1}{4}E_b$, calculate σ_t and the (Gaussian) longitudinal emittance $\epsilon_L = \sigma_E \sigma_t$ at injection.
 - h. (points) Assuming that longitudinal emittance is conserved, calculate σ_E and σ_t at each of the other two energies (hint: this is really easy based on the previous two answers).