Population Models
Python for Ecologists

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Ecological Society of America Workshop

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August 3rd, 2012

Population models in Übertool

1. Exponential
2. Logistic
3. Gompertz
4. Fox Surplus yield
5. Maximum Sustainable Yield
6. Yule-Furry
7. Feller-Arley
8. Leslie

Exponential Model

- Mathematical equation

$$N_t = N_0 e^{rt}$$

  - N_0 is the initial number of individuals
  - N_t is population size at t
  - r is intrinsic growth rate
  - t is duration
- We have three inputs and one output

Code in Python (exp)

- Define a function

```
1 def exponentialgrow(N_o , r,  T):
2     index_set = np.arange(T+1)      #How to do this in np.linspace?
                                      #index_set = np.linspace(0,T,T+1)
3     x = np.zeros(len(index_set))    #create an array to hold the results
4     x[0] = N_o                      #initial condition
5     for t in index_set[1:]:         #t starts at 0, ends at T
6         x[t] = N_o*np.exp(r*t)
7     return x
```

- Call the defined function

```
>>>N_t=exponentialgrow(10, 0.4, 10)
>>>[  10.          14.91824698   22.25540928   33.20116923   49.53032424
      73.89056099  110.23176381  164.44646771  245.32530197  365.98234444
      545.98150033]
```

It is your turn now!

- Please code the logistic population model

$$N_t = N_{t-1} + r_0 N_{t-1}(1 - \frac{N_{t-1}}{K})$$

  - N_t is population size at t
  - N_{t-1} is population size at t-1
  - K is population capacity
  - r_0 is max growth rate
  - t is simulation duration
- We have four inputs and one output

Code in Python (logistic)

- Define a function

```
1. def logisticgrow(N_o, T, r, K):
2.     index_set = np.arange(T+1)
3.     x = np.zeros(len(index_set))
4. x[0] = N_o
5.     for t in index_set[1:]:
6.         x[t] = x[t-1] + (r)*x[t-1]*(1 - x[t-1]/float(K))
7. return x
```

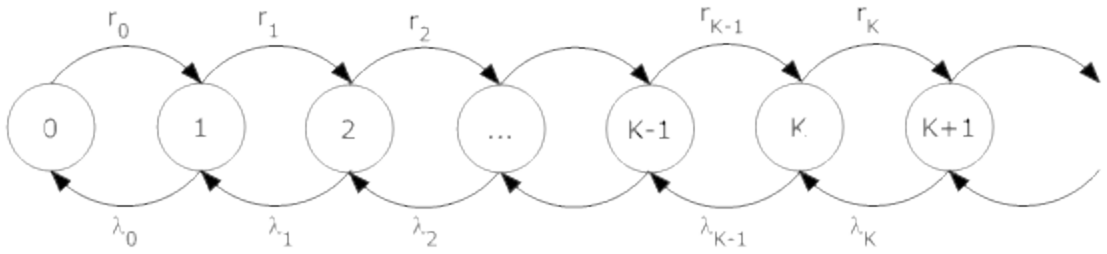
Why use float(K)?
Try 10/100
And 10/float(100)

- Call the defined function

```
>>>N_t=logisticgrow(10, 10, 0.4, 100)
>>>[ 10.         13.6        18.30016    24.28064058  31.63469878
  40.28556162  49.90808037  59.90804657  69.51536903  77.99197051
  84.85776886]
```

Feller-Arley (birth-death) Markov Process

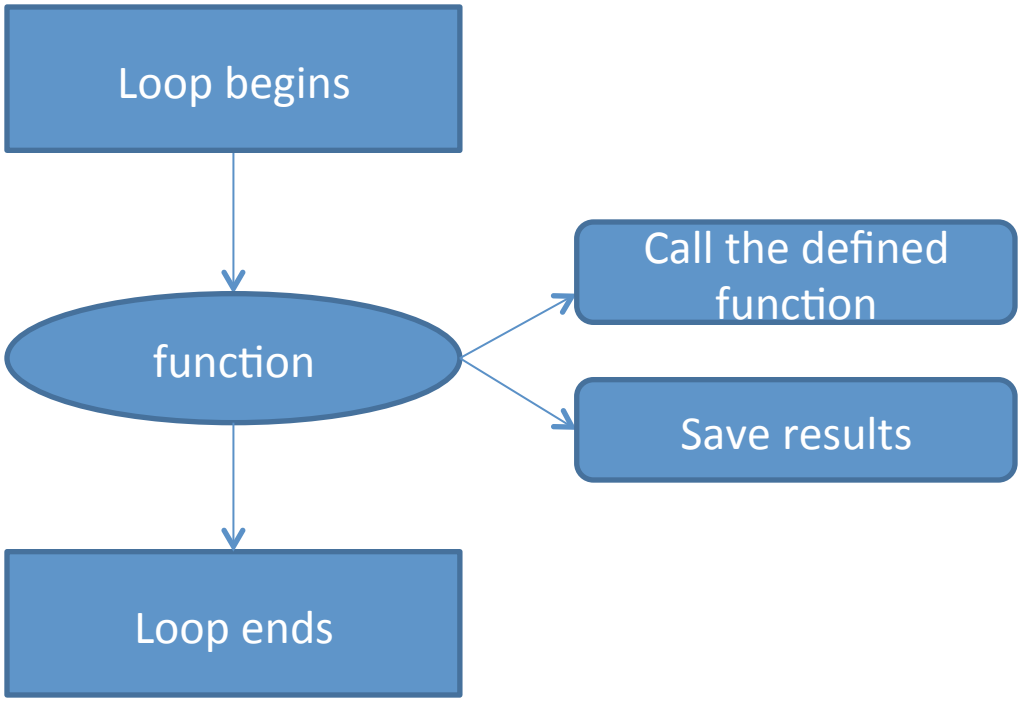
- No internal population structure and each individual can give birth and death with constant rates



- $N_t = N_{t-1} - 1 + N_{birth} - N_{death}$
- $N_{birth} \sim$ binomial (N, P_{birth})
- $N_{death} \sim$ binomial (N, P_{death})
- Let's look at the code 'population_modeling_bdp.py'

Monte Carlo Simulation

- Wrap the code by a loop
- Save results of each iteration



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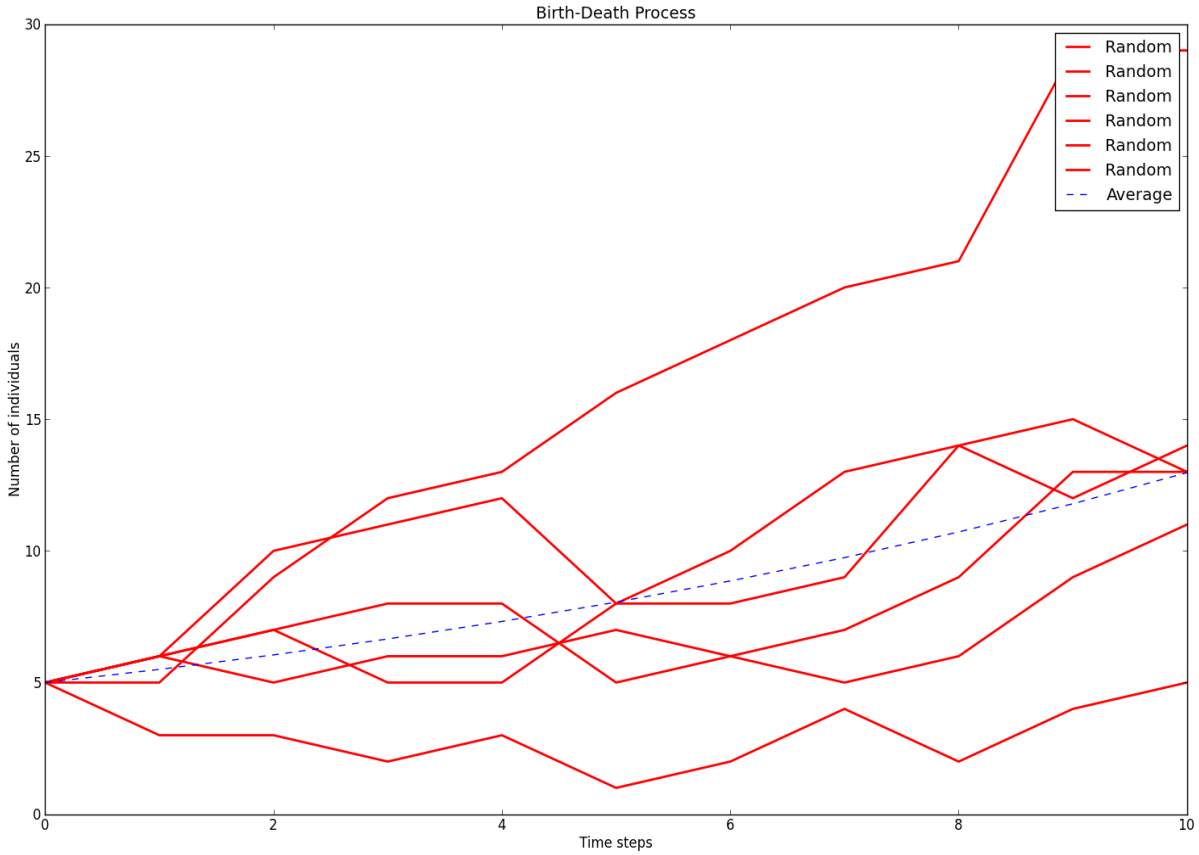
Plot Results

- matplotlib, a library to illustrate your data



Leslie Model

$$\begin{bmatrix} n_0 \\ n_1 \\ \mathrm{M} \\ n_k \end{bmatrix}_{t+1} = \begin{bmatrix} F_o & F_1 & \mathrm{L} & F_k \\ S_0 & 0 & \mathrm{L} & 0 \\ 0 & \mathrm{O} & \mathrm{L} & 0 \\ 0 & 0 & S_{k-1} & 0 \end{bmatrix} \begin{bmatrix} n_0 \\ n_1 \\ \mathrm{M} \\ n_k \end{bmatrix}_t$$

```
for i in range(0, T):
    n=np.dot(l_m, n_o)
    n_o=n
    n_f[:,i]=n.squeeze()
```

Why squeeze?
Try n.ndim and
n.squeeze().ndim

Let's look at the script 'population_modeling_lm.py'