

Statistics for Linguists with R – a SIGIL course

Unit 8: Non-Randomness of Corpus Data & Generalised Linear Models

Marco Baroni¹ & Stefan Evert²

<http://purl.org/stefan.evert/SIGIL>

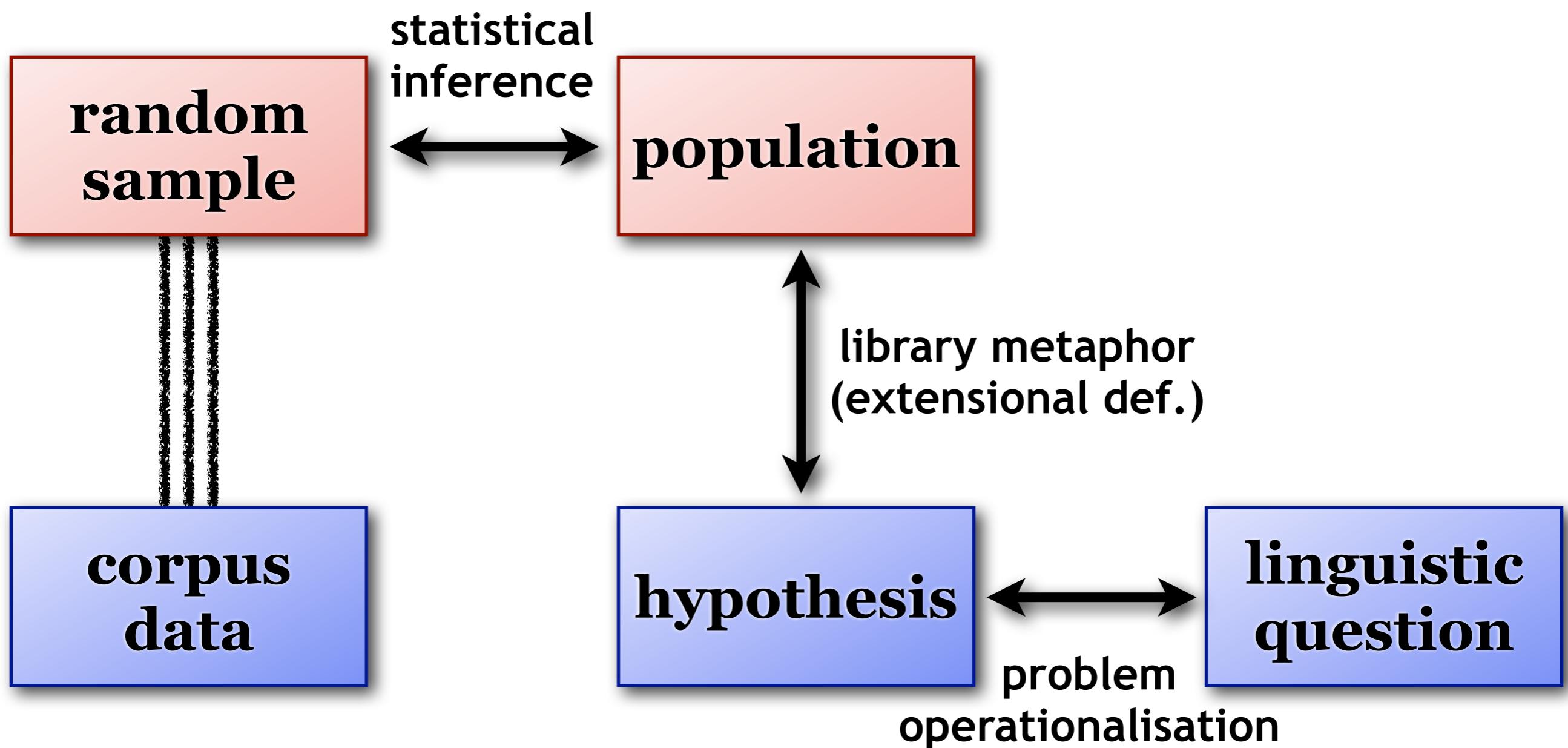
¹Center for Mind/Brain Sciences, University of Trento

²Corpus Linguistics Group, FAU Erlangen-Nürnberg

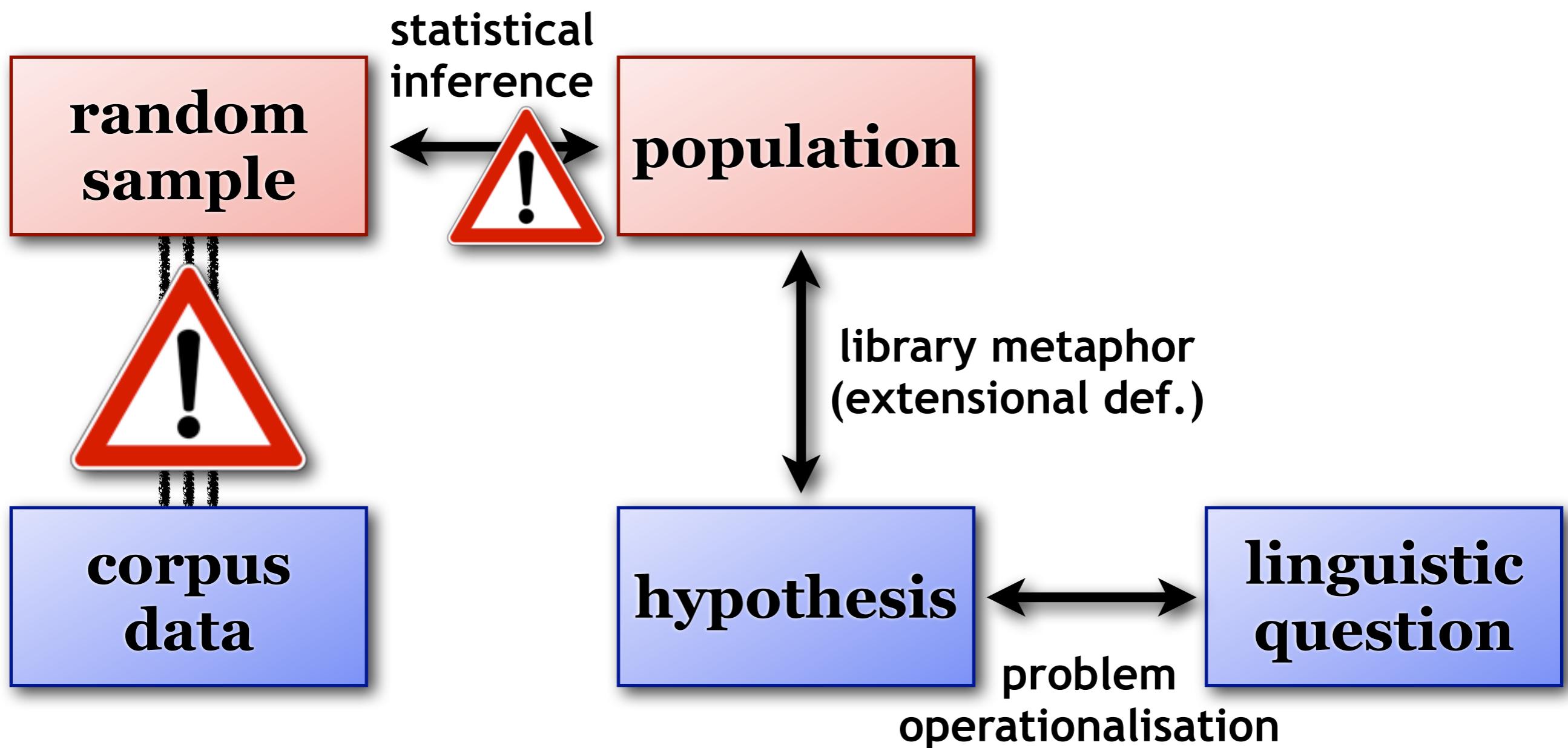


Introduction & Reminder

Problems with statistical inference



Problems with statistical inference



Mathematical problems: Significance

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 - G^2 overestimates significance for small samples (well-known in statistics, e.g. Agresti 2002)
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 - e.g. manual samples of 100–500 items (as in our examples)
 - often ignored because of its success in computational linguistics
 - Fisher is conservative & computationally expensive
 - also numerical problems, e.g. in R version 1.x



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 - not clear which measure of effect size is appropriate
 - e.g. **difference** of proportions, **relative risk** (ratio of proportions), **odds ratio**, logarithmic odds ratio, normalised X^2 , ...

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- ◆ Effect size for frequency comparison
 - not clear which measure of effect size is appropriate
 - e.g. **difference** of proportions, **relative risk** (ratio of proportions), **odds ratio**, logarithmic odds ratio, normalised X^2 , ...
- ◆ Confidence interval estimation
 - accurate & efficient estimation of confidence intervals for effect size is often very difficult
 - exact confidence intervals only available for odds ratio

Mathematical problems: Multiple hypothesis tests

- ◆ Each individual hypothesis test controls risk of type I error ... but if you carry out thousands of tests, some of them *have* to be false rejections
 - recommended reading: *Why most published research findings are false* (Ioannidis 2005)
 - a monkeys-with-typewriters scenario

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*if applied to a single candidate selected *a priori**
 - but usually candidates selected *a posteriori* from data
→ many “unreported” tests for candidates with $f = 0$!
 - large number of such word pairs according to **Zipf's law** results in substantial number of type I errors
 - can be quantified with LNRE models (Evert 2004),
cf. Unit 5 on word frequency distributions with *zipfR*



Why a corpus isn't a random sample

Corpora

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- ◆ Theoretical sampling procedure is impractical
 - it would be very tedious if you had to take a random sample from a library, especially a hypothetical one, every time you want to test some hypothesis
- ◆ Use pre-compiled sample: a **corpus**

Corpora

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 - it would be very tedious if you had to take a random sample from a library, especially a hypothetical one, every time you want to test some hypothesis
- ◆ Use pre-compiled sample: a **corpus**
 - but this is not a random sample of tokens!
 - would be prohibitively expensive to collect 10 million VPs for a BNC-sized sample at random
 - other studies will need tokens of different granularity (words, word pairs, sentences, even full texts)

The Brown corpus

- ◆ First large-scale electronic corpus
 - compiled in 1964 at Brown University (RI)
- ◆ 500 samples of approx. 2,000 words each
 - sampled from edited AmE published in 1961
 - from 15 domains (imaginative & informative prose)
 - manually entered on punch cards

The British National Corpus

- ◆ 100 M words of modern British English
 - compiled mainly for lexicographic purposes:
Brown-type corpora (such as LOB) are too small
 - both written (90%) and spoken (10%) English
 - XML edition (version 3) published in 2007
- ◆ 4048 samples from 25 to 428,300 words
 - 13 documents < 100 words, 51 > 100,000 words
 - some documents are collections (e.g. e-mail messages)
 - rich metadata available for each document

Unit of sampling

- ◆ Key problem: **unit of sampling** (text or fragment) ≠ **unit of measurement** (e.g. VP)
 - recall sampling procedure in library metaphor ...

Unit of sampling

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- ◆ Random sampling in the library metaphor
 - walk to a random shelf ...
 - ... select a random book ...
 - ... open it on a random page ...
 - ... and pick a random sentence from the page
 - ➡ repeat n times for sample size n

Unit of sampling

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 - walk to a random shelf ...
 - ... select a random book ...
 - ... open it on a random page ...
 - ... and pick a random sentence from the page
 - ➡ repeat n times for sample size n
- ◆ Corpus = random sample of books, not sentences!
 - we should only use 1 sentence from each book
 - ➡ sample size: $n=500$ (Brown) or $n=4048$ (BNC)

Pooling data

- ◆ In order to obtain larger samples, researchers usually **pool** all data from a corpus
 - i.e. they include all sentences from each book
- ◆ Do you see why this is wrong?

Pooling data

- ◆ Books aren't random samples themselves
 - each book contains relatively homogeneous material
 - but much larger differences *between* books
- ◆ Therefore, the pooled data do not form a random sample from the library
 - for each randomly selected sentence, we co-select a substantial amount of very similar material
- ◆ Consequence: sampling variation increased

Pooling data

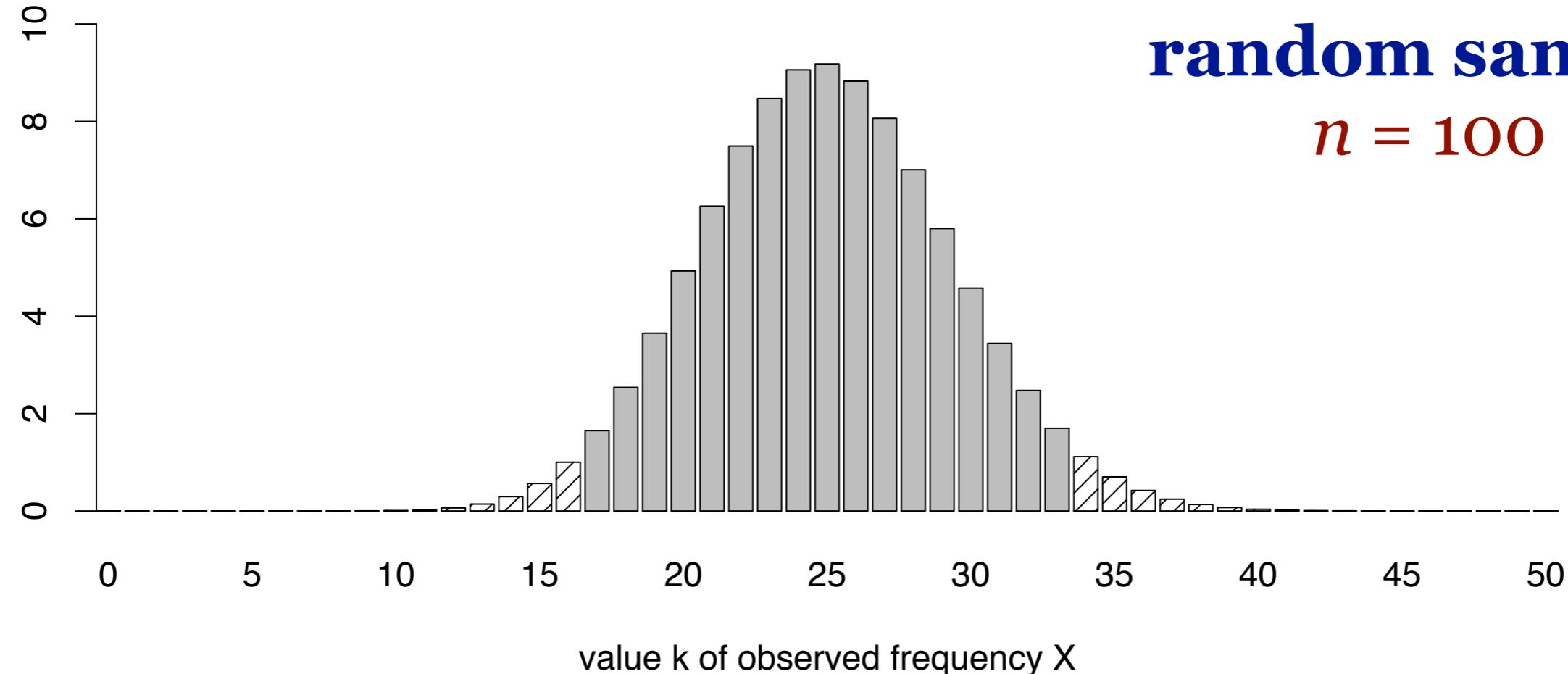
Pooling data

- ◆ Let us illustrate this with a simple example ...
 - assume library with two sections of equal size
 - e.g. spoken and written language in a corpus
 - population proportions are **10%** vs. **40%**
 - overall proportion of $\pi = 25\%$ in the library
 - this is the null hypothesis H_0 that we will be testing

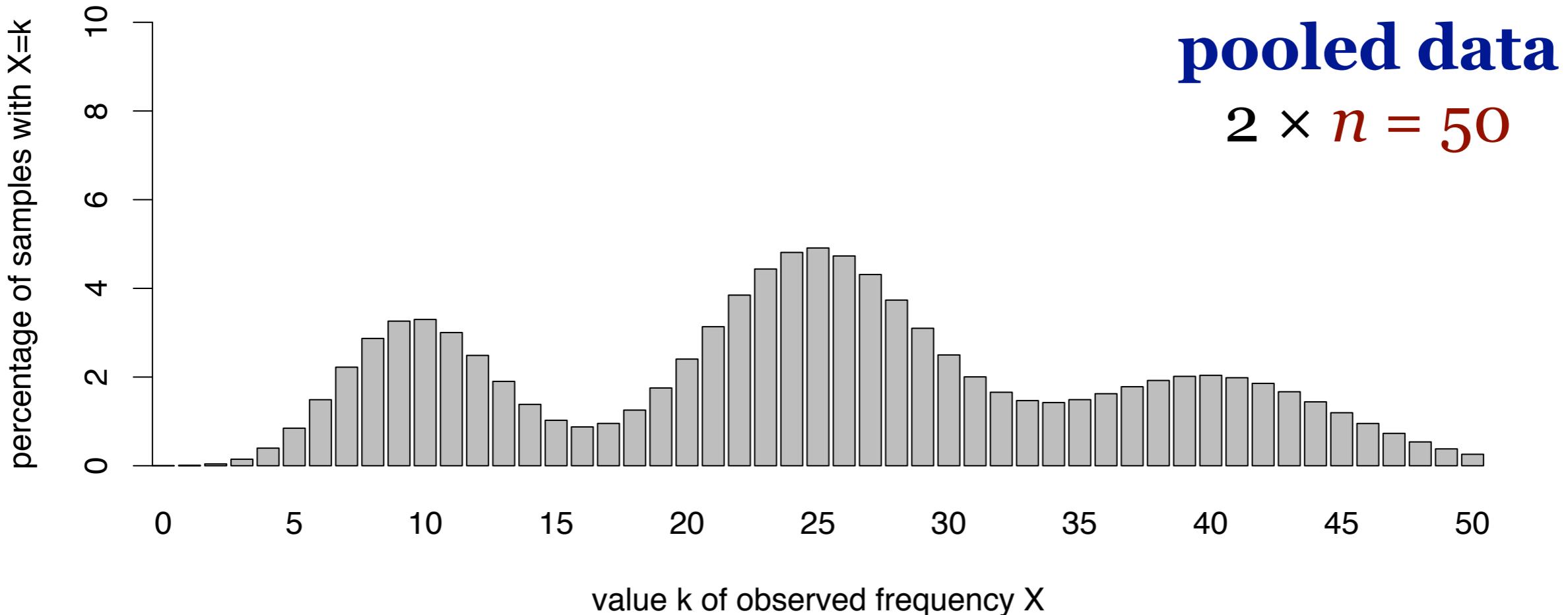
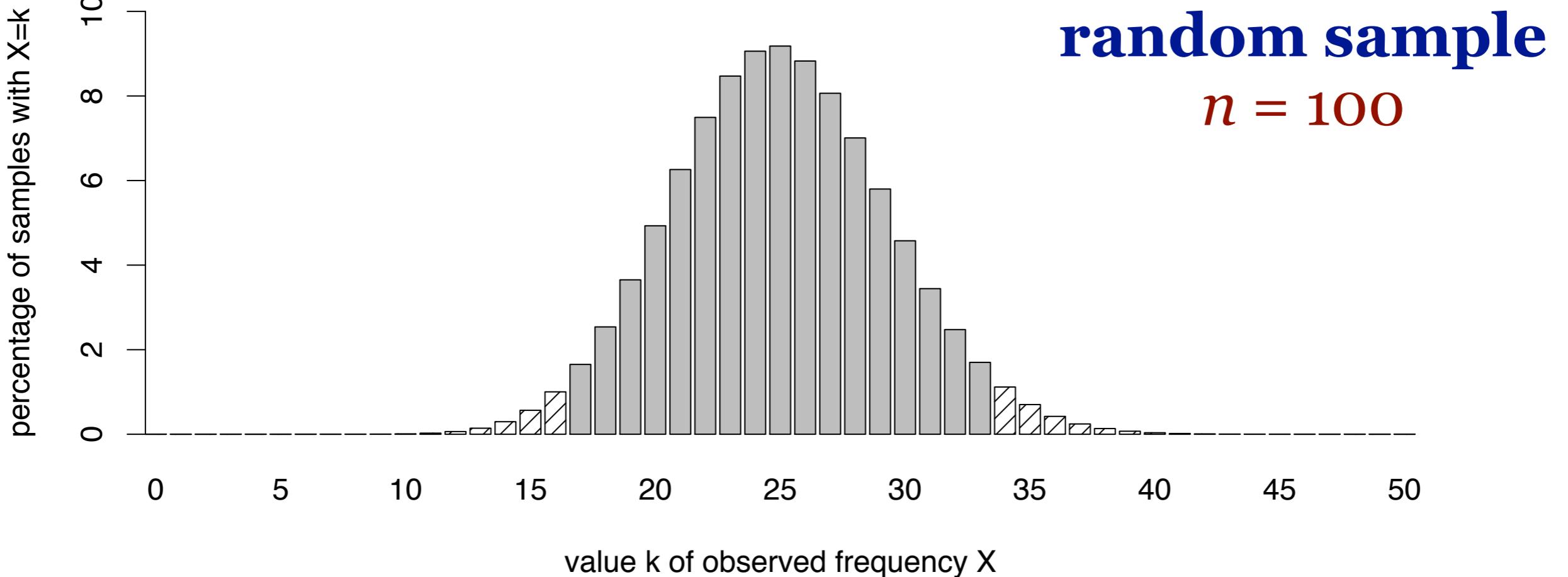
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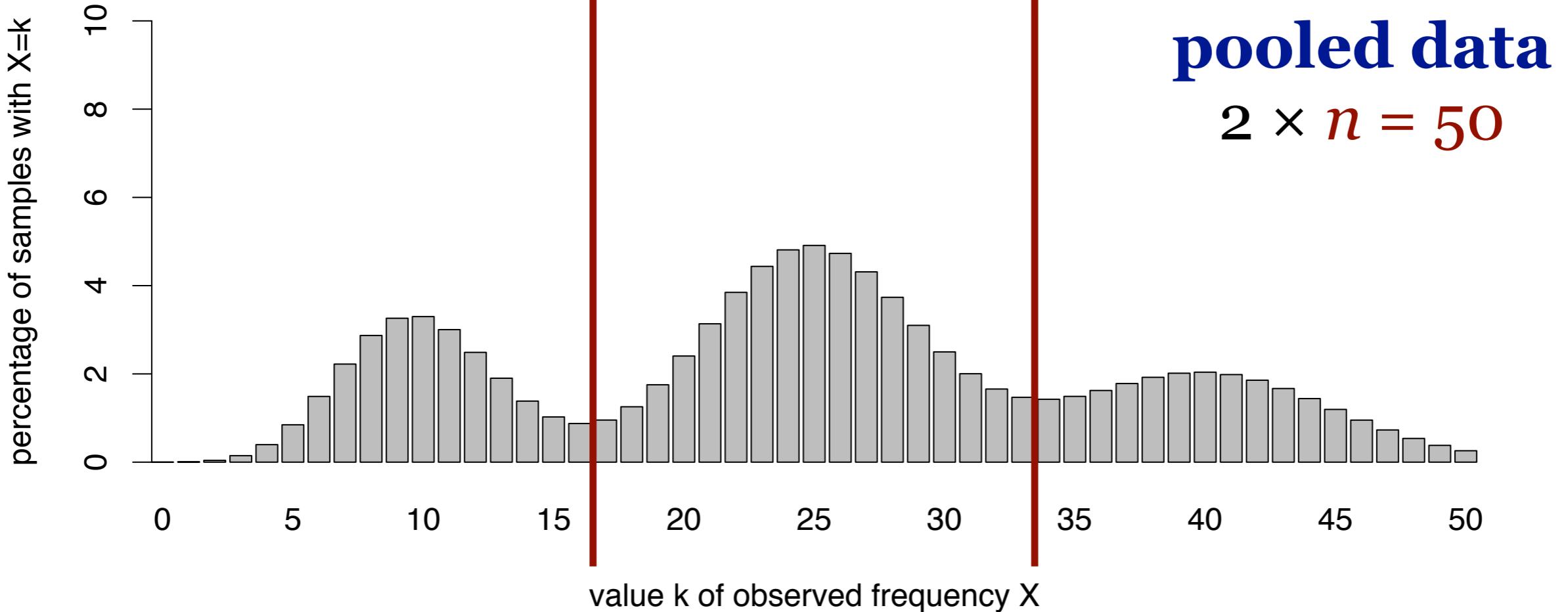
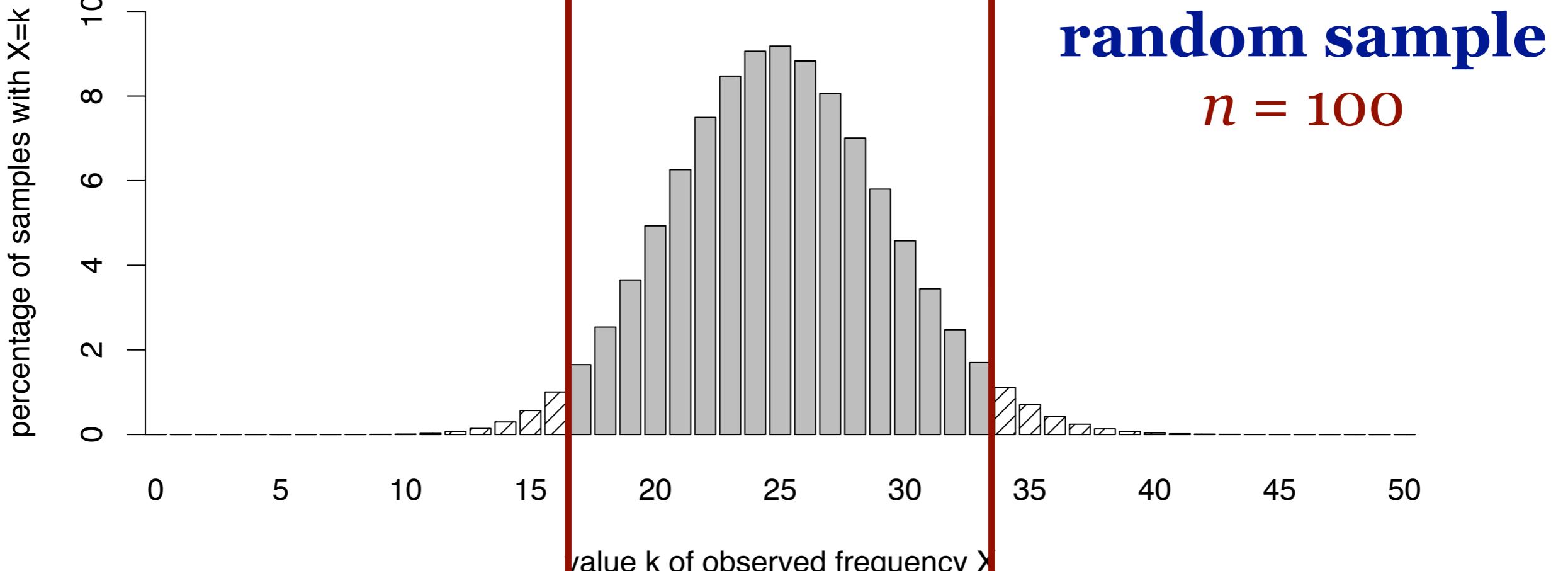
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 - this is the null hypothesis H_0 that we will be testing
- ◆ Compare sampling variation for
 - random sample of 100 tokens from the library
 - two randomly selected books of 50 tokens each
 - book is assumed to be a random sample from its section

percentage of samples with $X=k$



random sample
 $n = 100$





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 - very difficult to detect automatically
- ◆ Even worse for newspapers & Web corpora
 - see Evert (2004) for examples



Measuring non-randomness

A sample of random samples is a random sample

- ◆ Larger unit of sampling is not the original cause of non-randomness
 - if each text in a corpus is a genuinely random sample from the same population, then the pooled data also form a random sample
 - we can illustrate this with a thought experiment

The random library

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- library of **random samples**
- ◆ Pooled data from 2 (or more) boxes form a perfectly **random sample** of sentences from the original library!



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- ◆ The true cause of non-randomness
 - discrepancy between unit of sampling and unit of measurement only leads to non-randomness if the sampling units (i.e. the corpus texts) are not random samples themselves (from same population)
 - with respect to specific phenomenon of interest

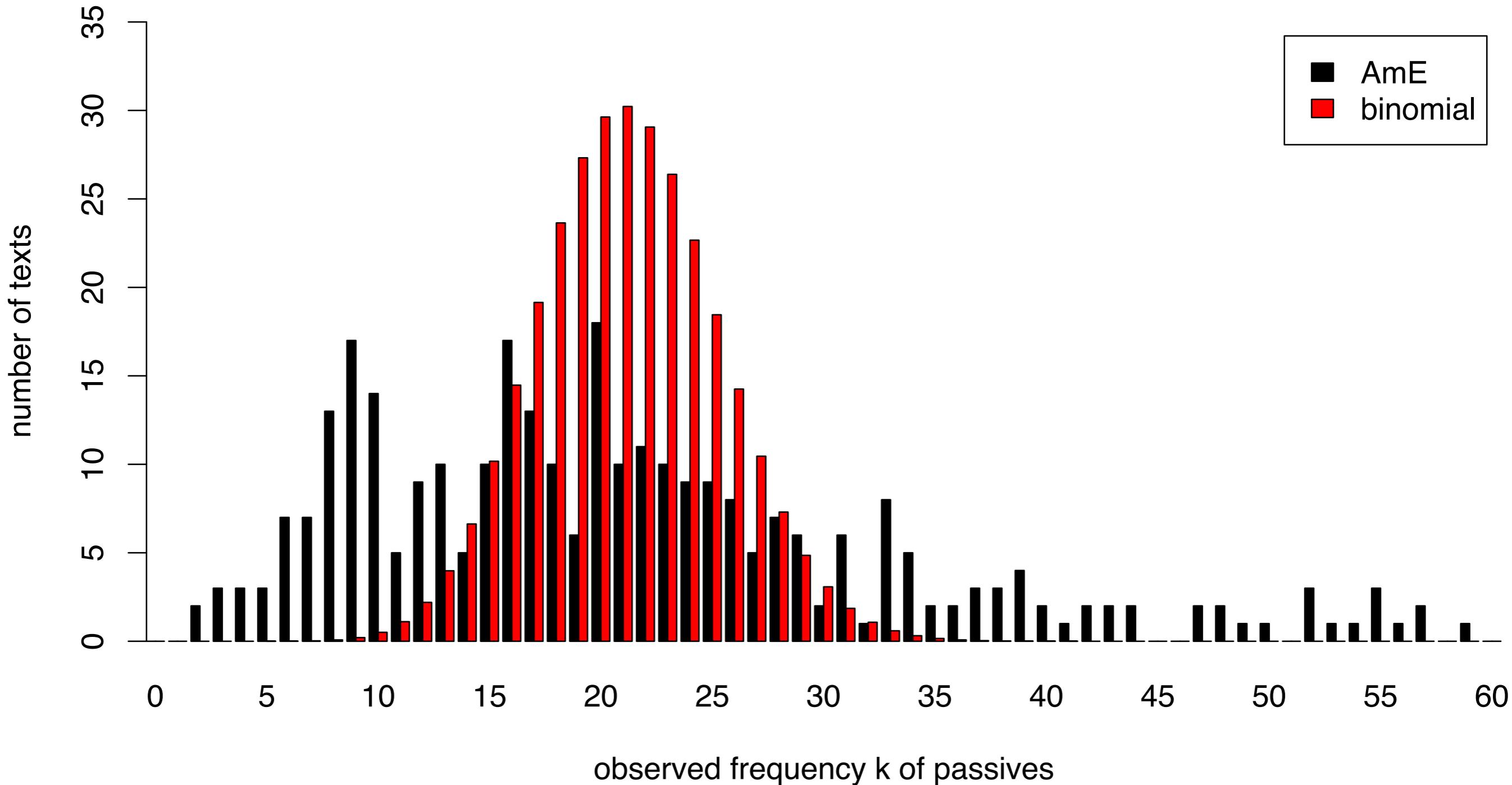
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- ◆ Now we know how to measure non-randomness
 - find out if corpus texts are random samples
 - i.e., if they follow a binomial sampling distribution
 - tabulate observed frequencies across corpus texts

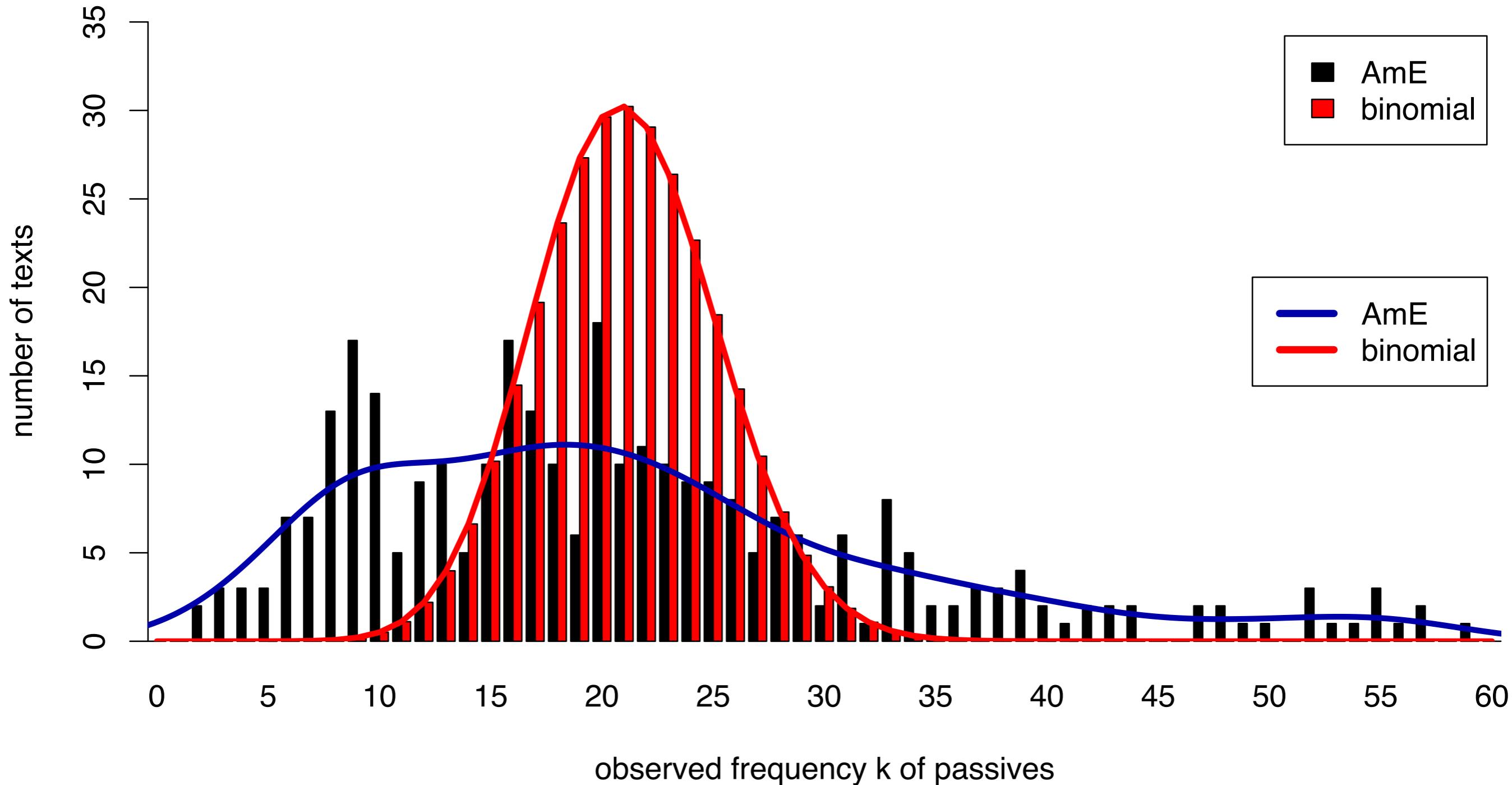
Measuring non-randomness

- ◆ Tabulate number of texts with k passives
 - illustrated for subsets of Brown/LOB (310 texts each)
 - meaningful because all texts have the same length
- ◆ Compare with binomial distribution
 - for population proportion H_0 : $\pi = 21.1\%$ (Brown) and $\pi = 22.2\%$ (LOB); approx. $n = 100$ sentences per text
 - estimated from full corpus → best possible fit
- ◆ Non-randomness → larger sampling variation

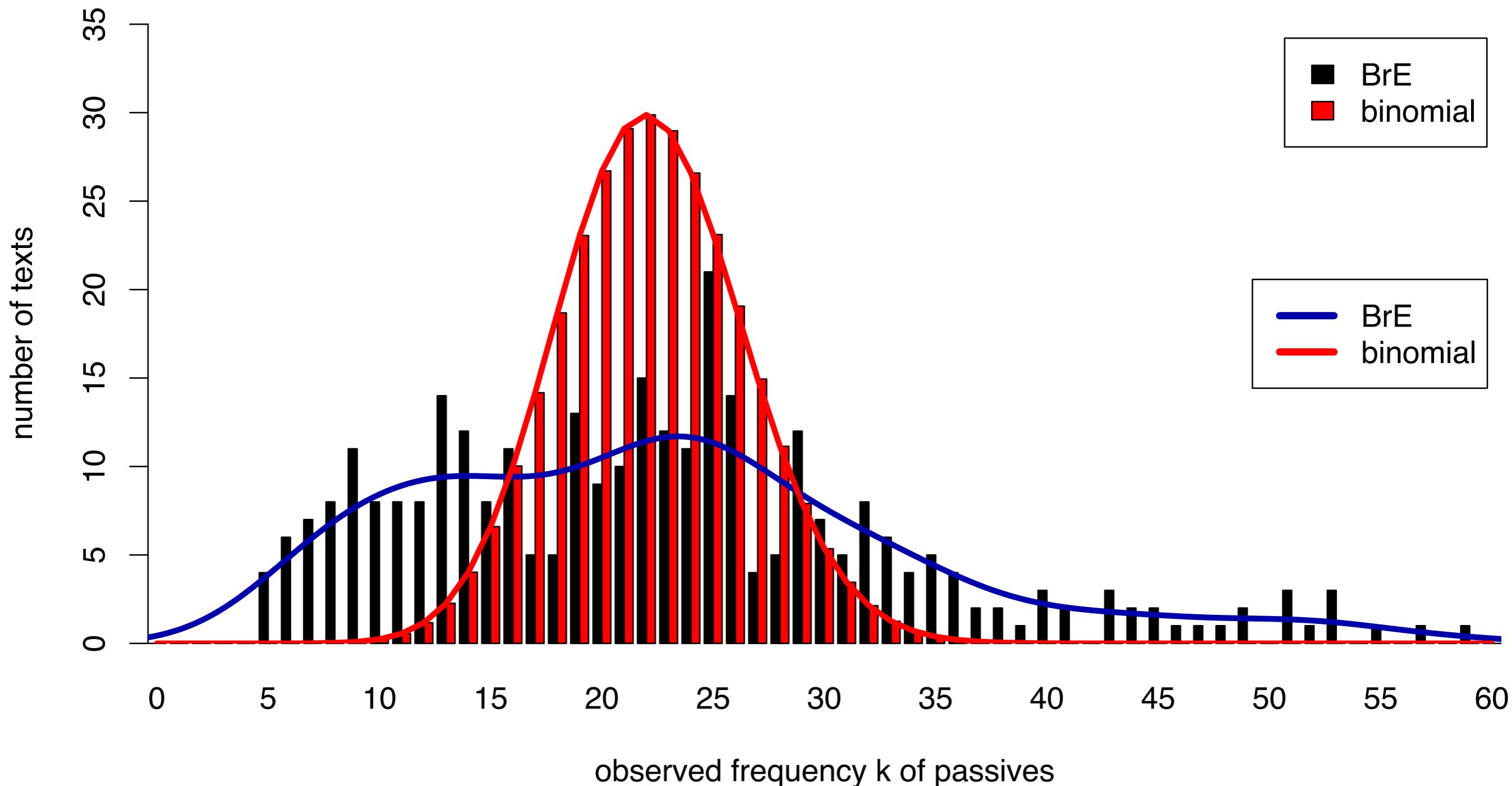
Passives in the Brown corpus

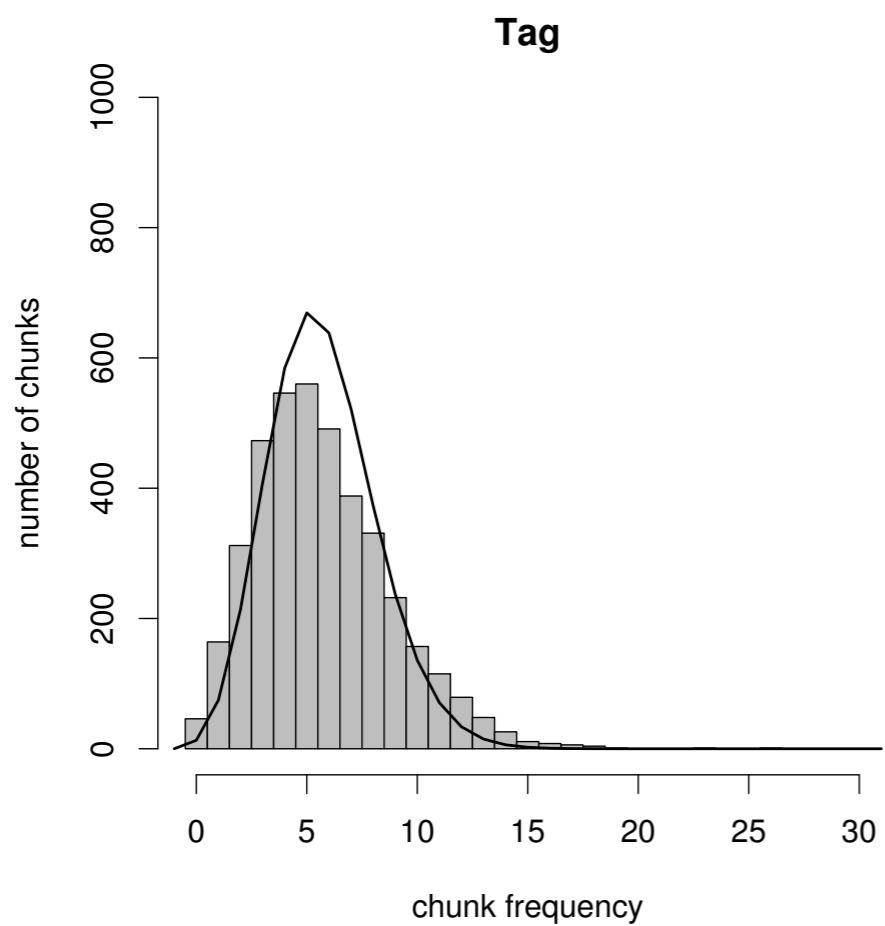


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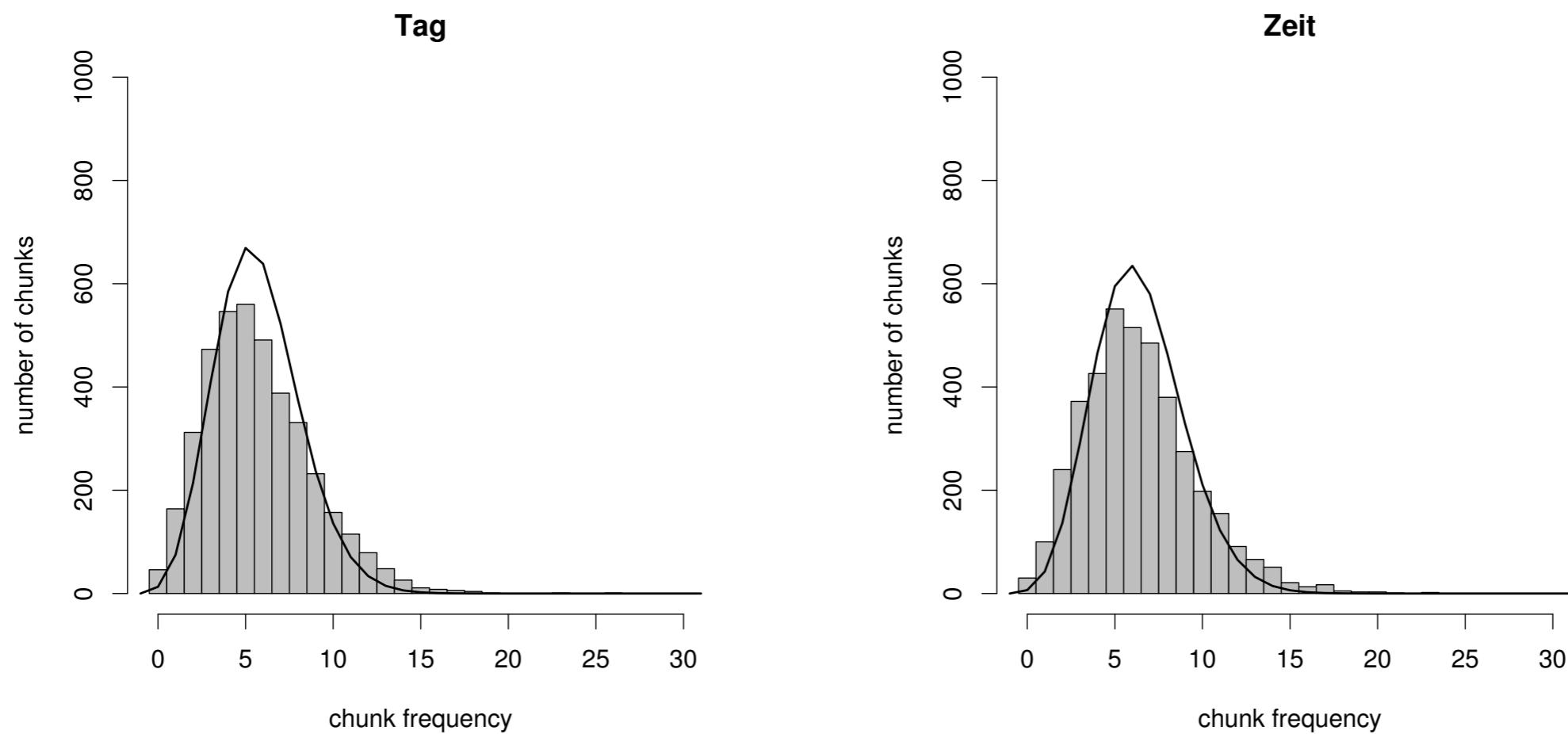


Passives in the LOB corpus

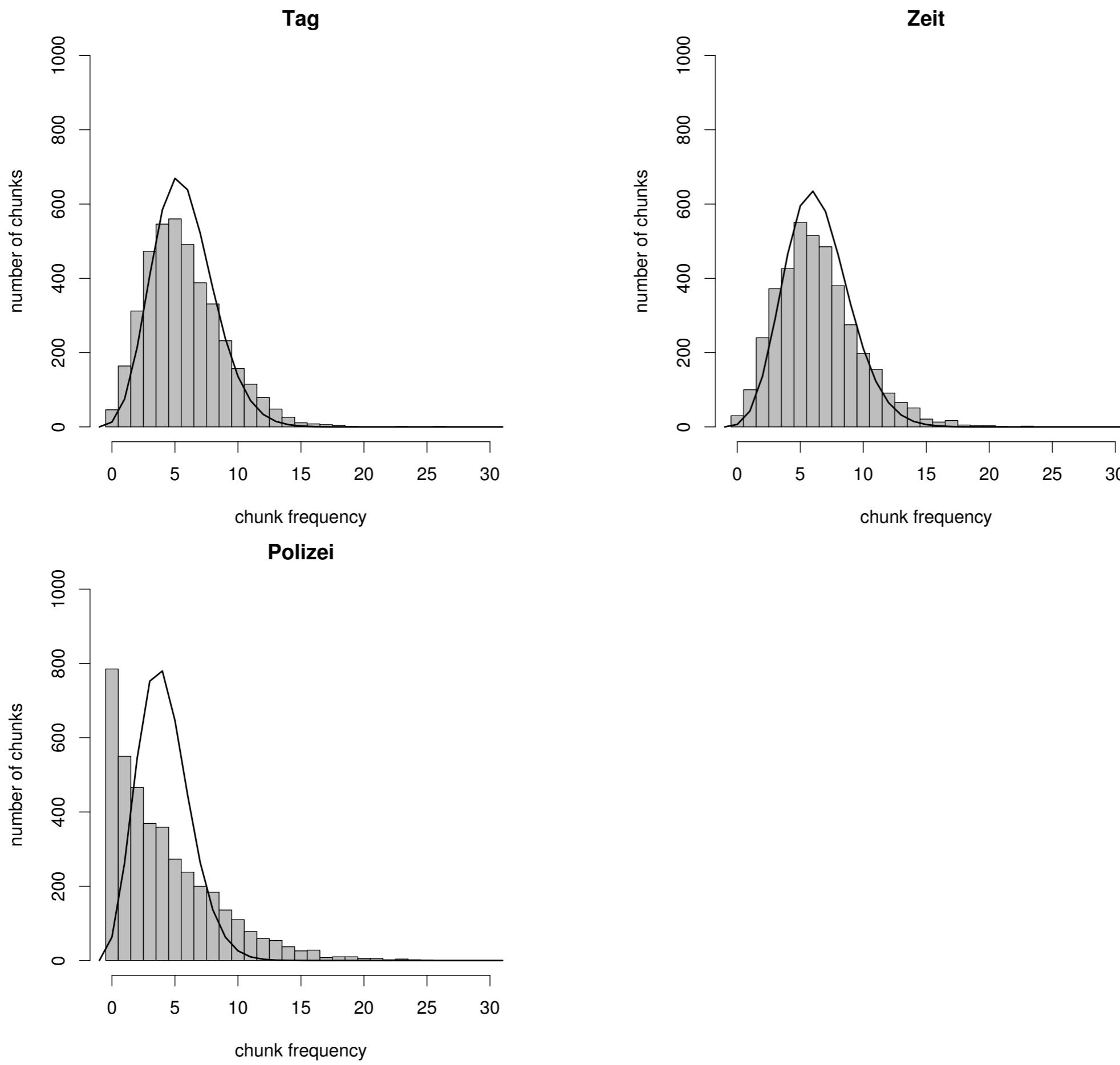




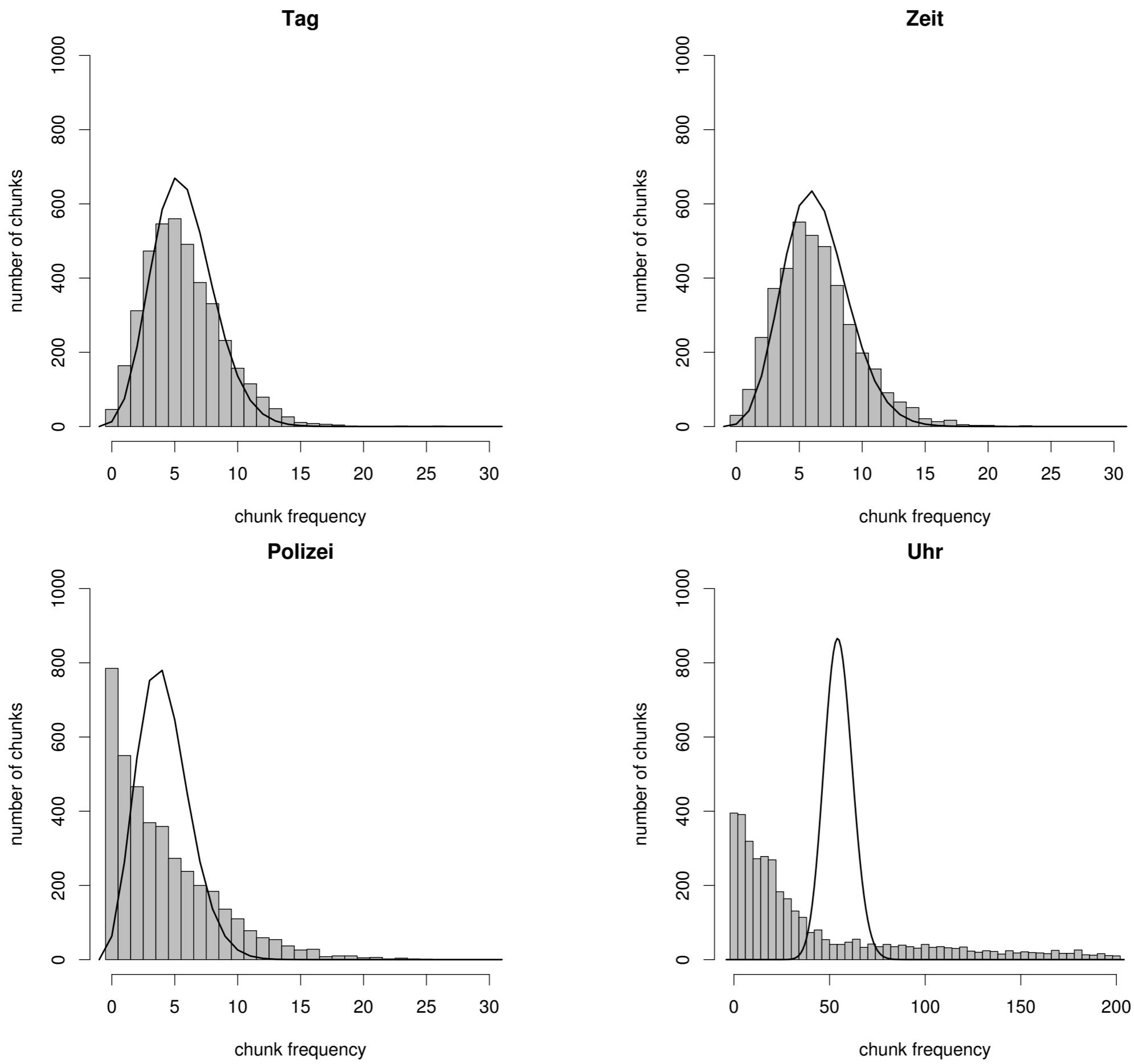
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- ◆ Accept that corpus is a **sample of texts**
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 - results in much smaller sample size ...
(BNC: 4,048 texts rather than 6,023,627 sentences)
 - ... but more informative measurements (relative frequencies on interval rather than nominal scale)

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 - ... but more informative measurements (relative frequencies on interval rather than nominal scale)
- ◆ Use statistical techniques that account for the **overdispersion** of relative frequencies
 - Gaussian distribution allows us to estimate **spread** (variance) independently from **location**
 - Standard technique: **Student's t-test**

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 - based on data from subsets of Brown and LOB
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- ◆ Chi-squared test (→ pooled data, binomial)
vs. **t-test** (→ sample of texts, Gaussian)

Let's do that in R ...

```
# passive counts for each text in Brown and LOB corpus  
> library(SIGIL)  
> Passives <- BrownLOBPassives  
  
# display 10 random rows to get an idea of the table layout  
> Passives[sample(nrow(Passives), 10), ]  
  
# annotate relative frequency of passives in each file (%)  
> Passives <- transform(Passives,  
    relfreq = 100 * passive / n_s)  
  
# split into separate data frames for Brown and LOB texts  
> Brown <- subset(Passives, lang == "AmE")  
> LOB <- subset(Passives, lang == "BrE")
```

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- ◆ R code: pooled counts + proportions test

```
> passives.B <- sum(Brown$passive)
> n_s.B <- sum(Brown$n_s)
> passives.L <- sum(L0B$passive)
> n_s.L <- sum(L0B$n_s)

> prop.test(c(passives.L, passives.B) ,
  c(n_s.L, n_s.B))
```

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◆ R code: `t.test()` function (from Unit #3)

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> t.test(LOB$relfreq, Brown$relfreq)  
  
# alternative syntax: “formula” interface  
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# visualize the distributions being compared  
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Why does this
put AmE first?

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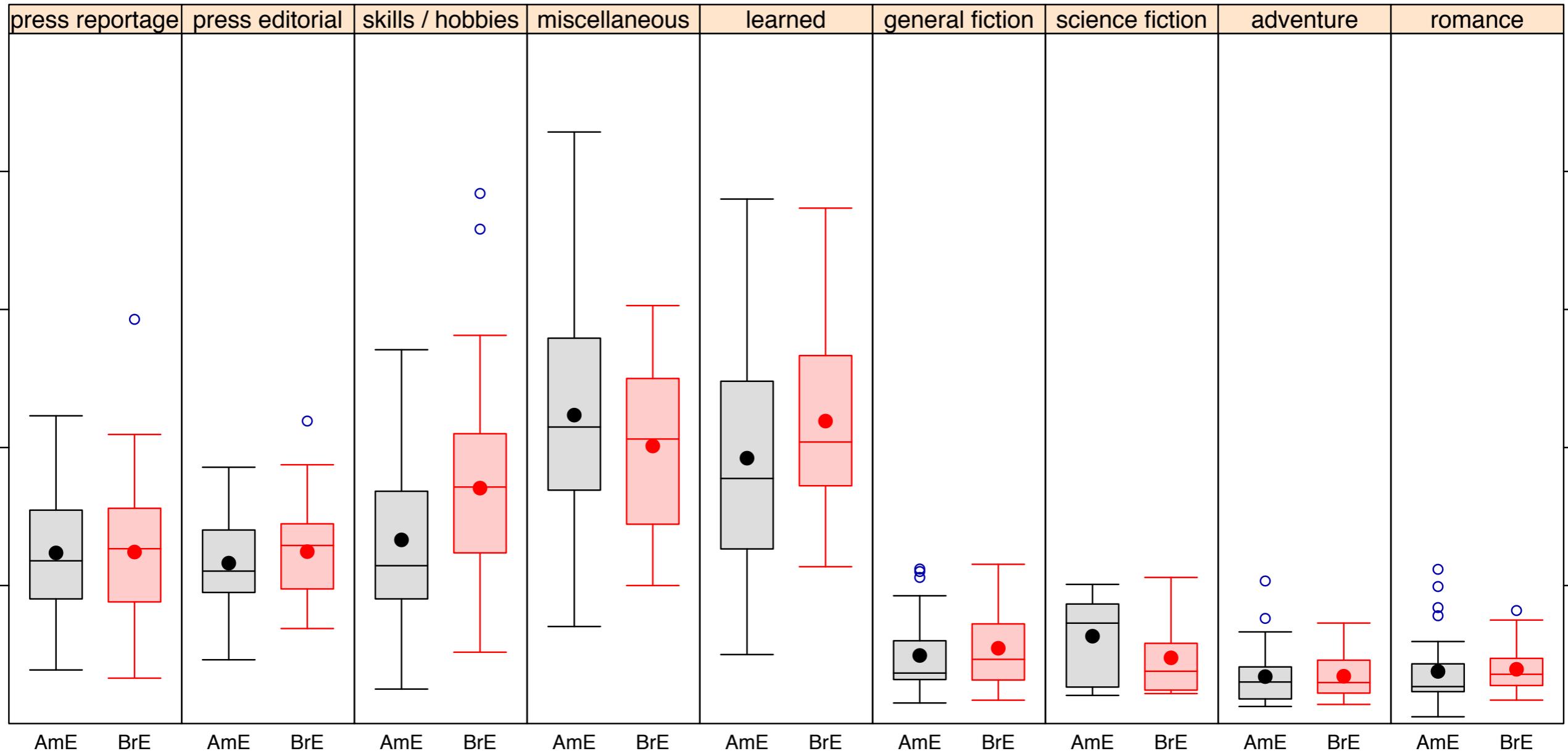
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 - 90% written / 10% spoken: $\pi = 16.6\%$

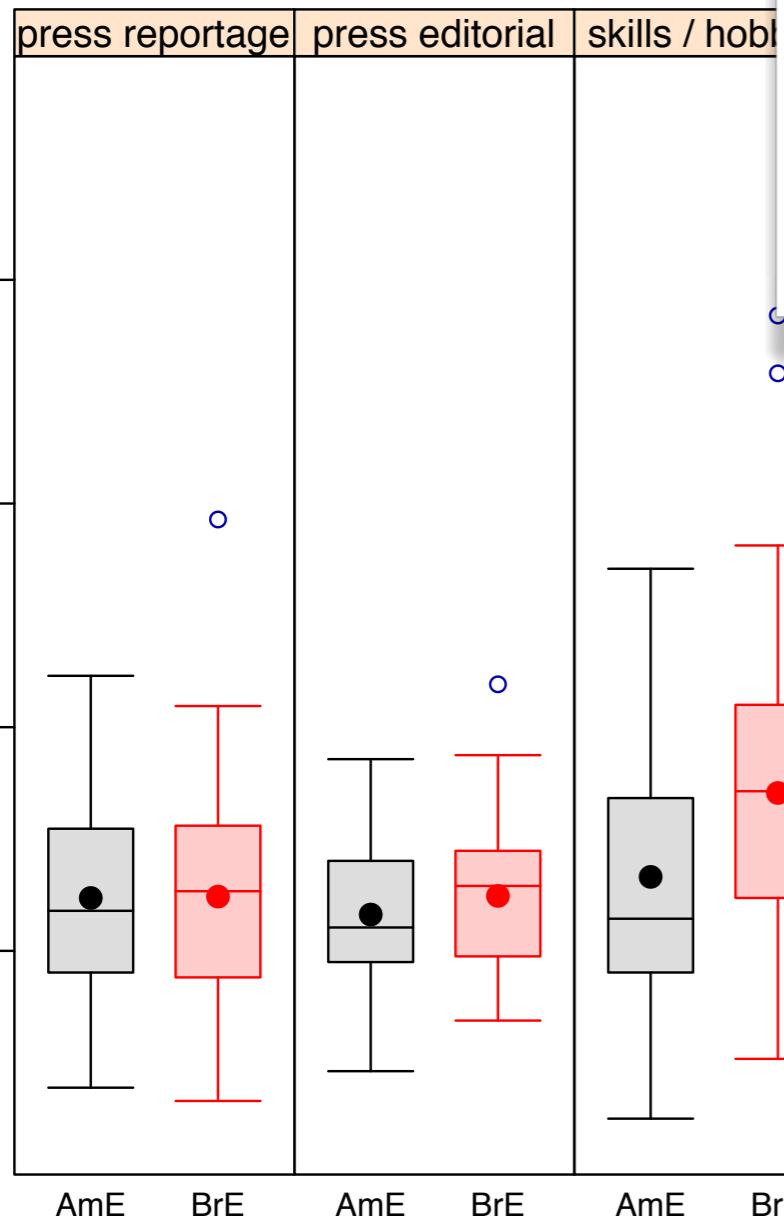
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 - 20% written / 80% spoken: $\pi = 6.8\%$

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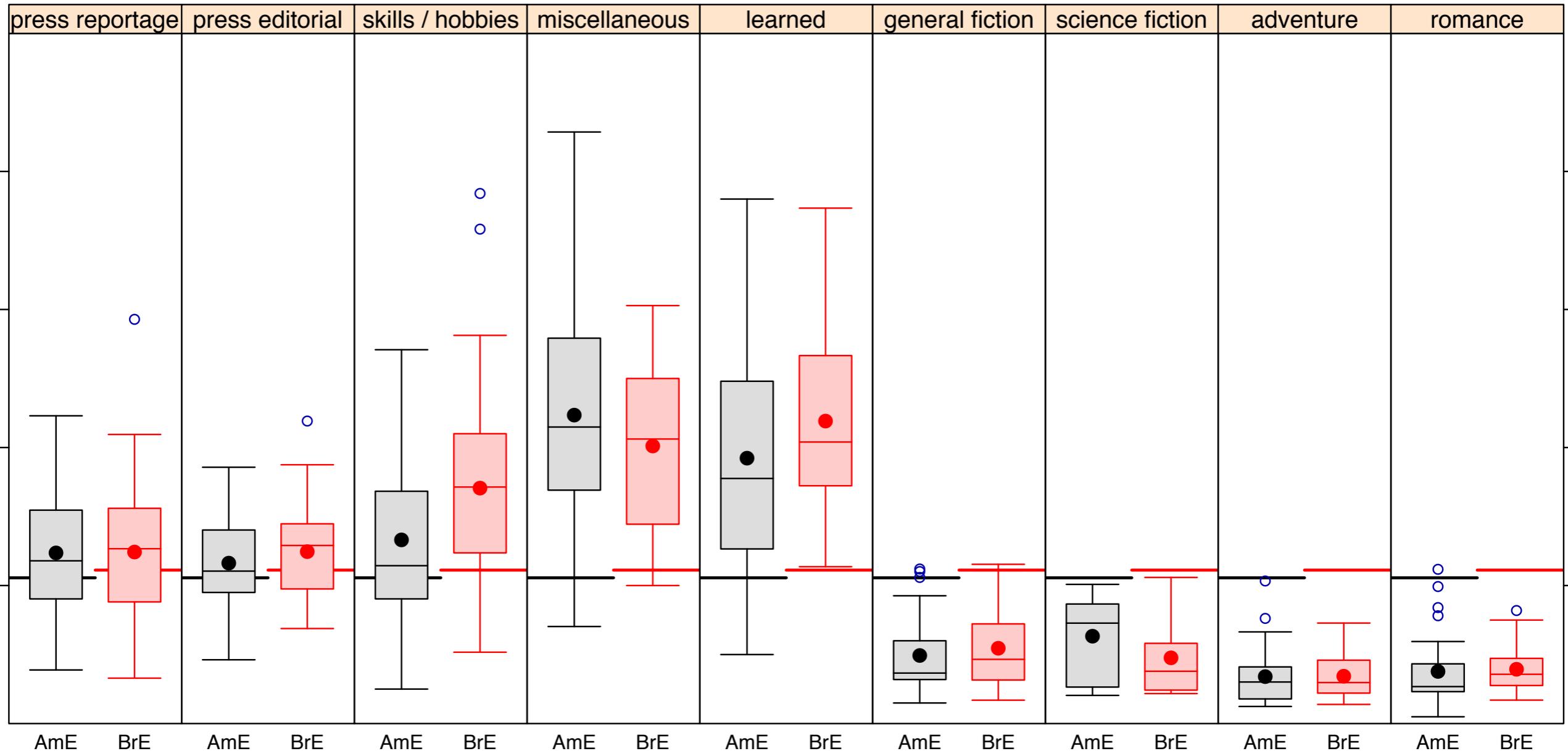


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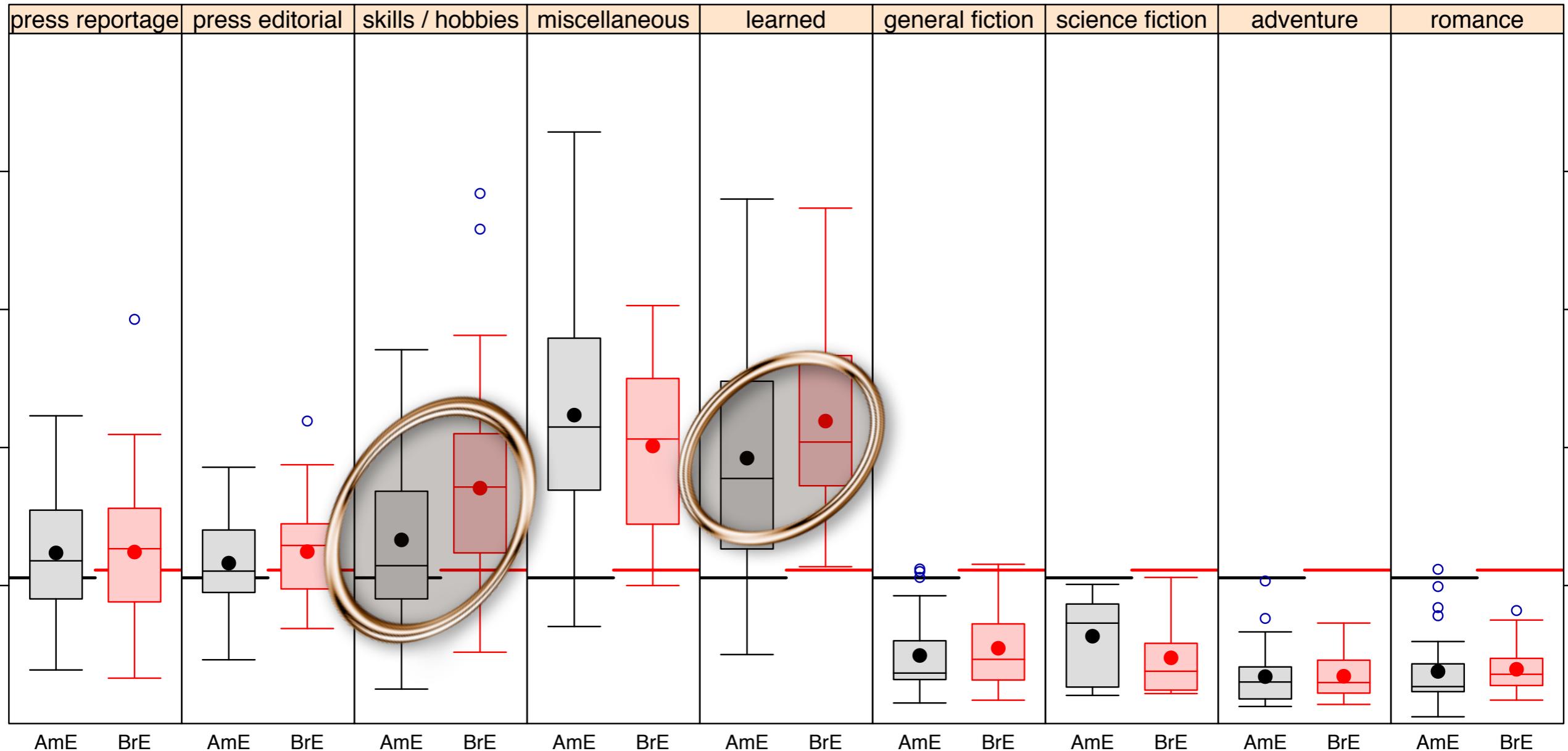


```
> library(lattice)  
> bwplot(relfreq ~ lang | genre,  
        data=Passives)  
# bw = "box and whiskers"
```

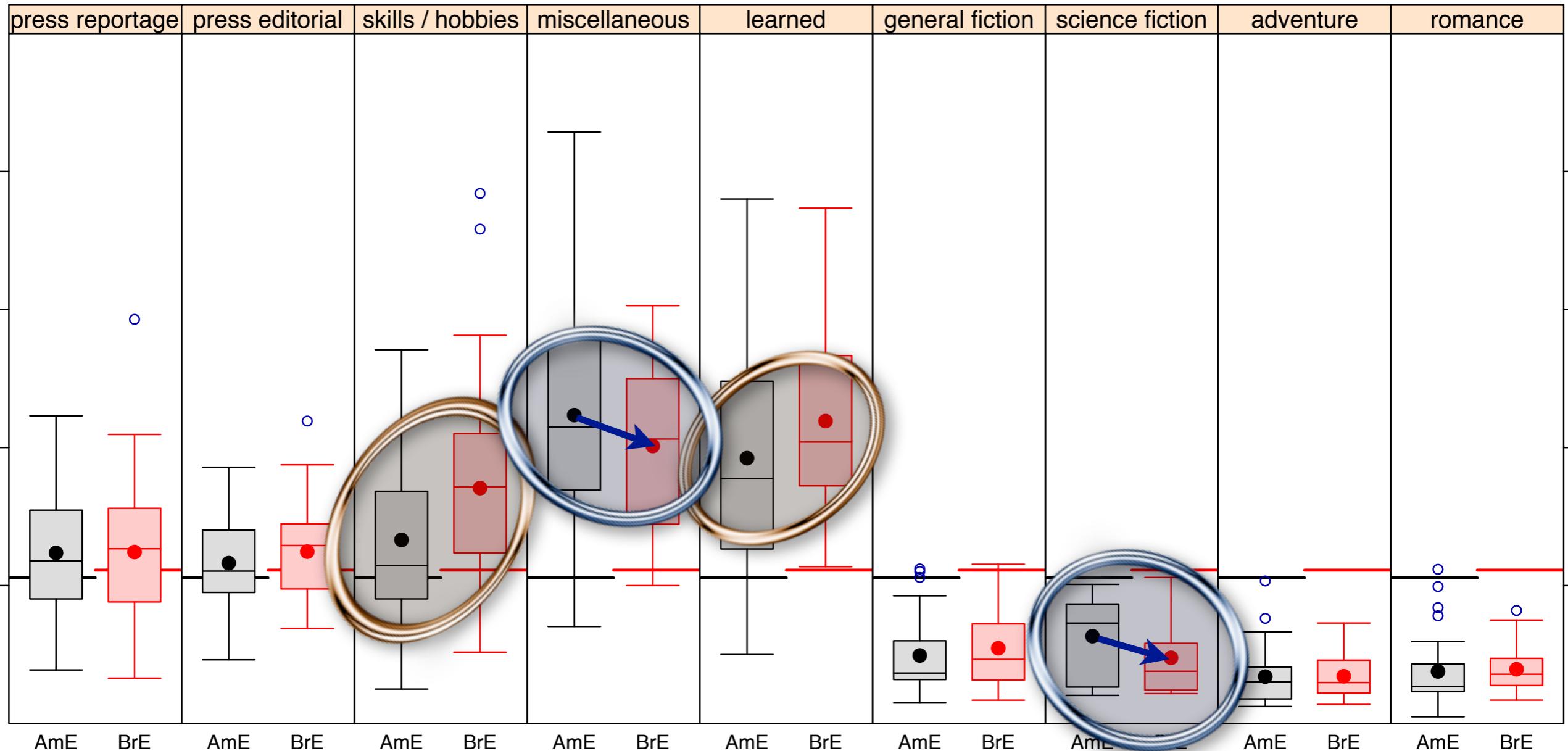
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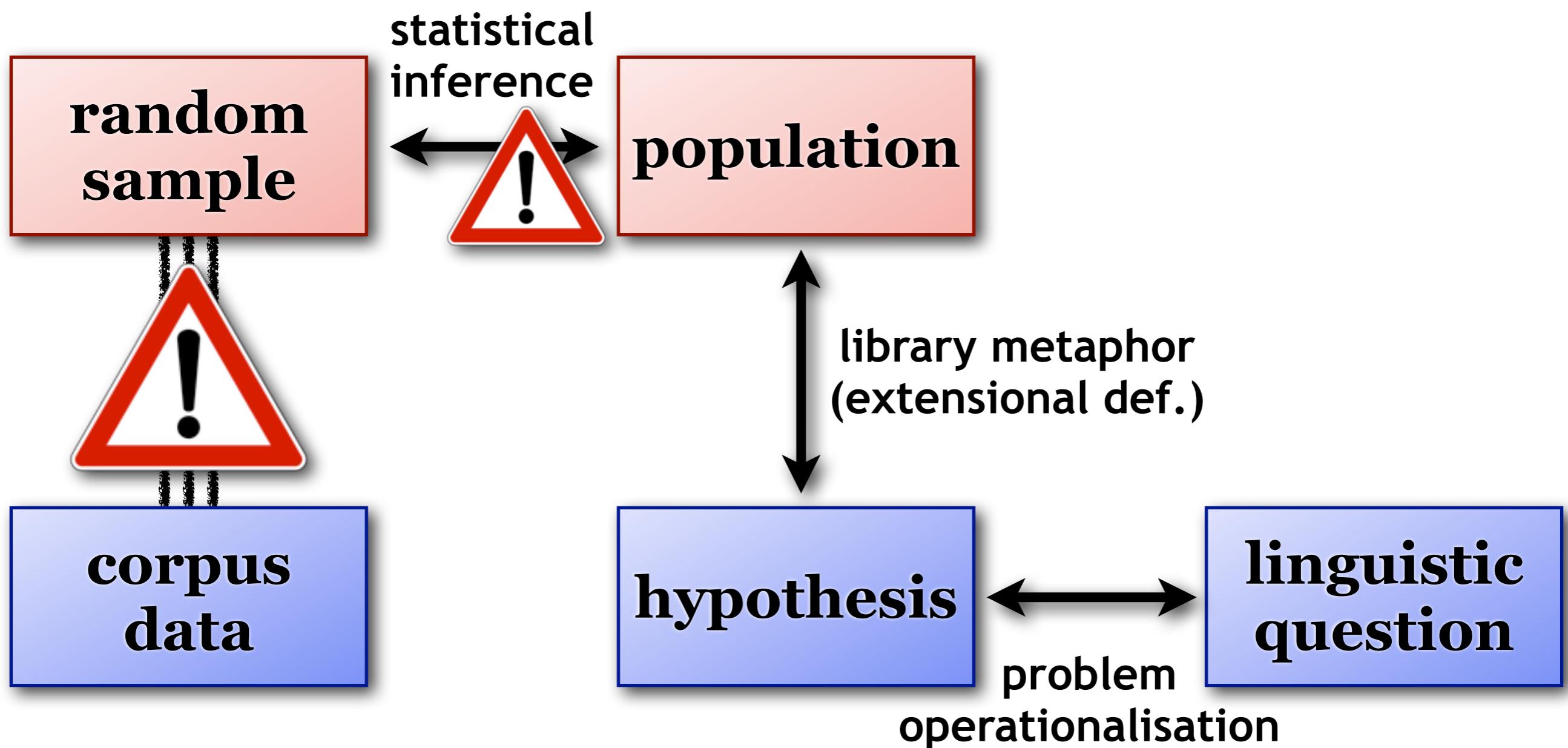
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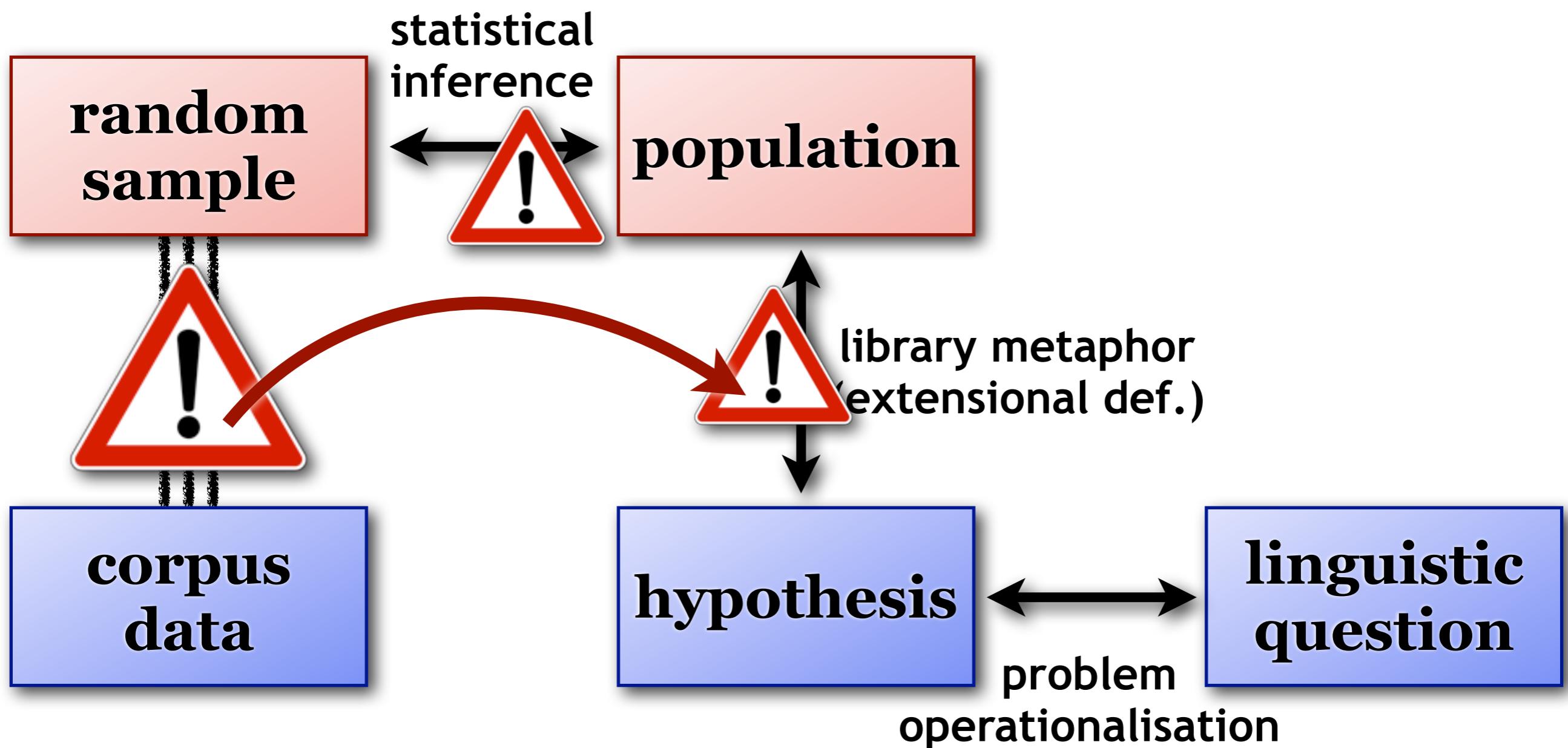
Average relative frequency?



Problems with statistical inference



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Rethinking corpus frequencies

Studying variation in language

- ◆ It seems absurd now to measure & compare relative frequencies in “language” (= library)
 - proportion π depends more on composition of library than on properties of the language itself
- ◆ Quantitative corpus analysis has to account for the variation of relative frequencies between individual texts (cf. Gries 2006)
 - research question → one factor behind this variation

Studying variation in language

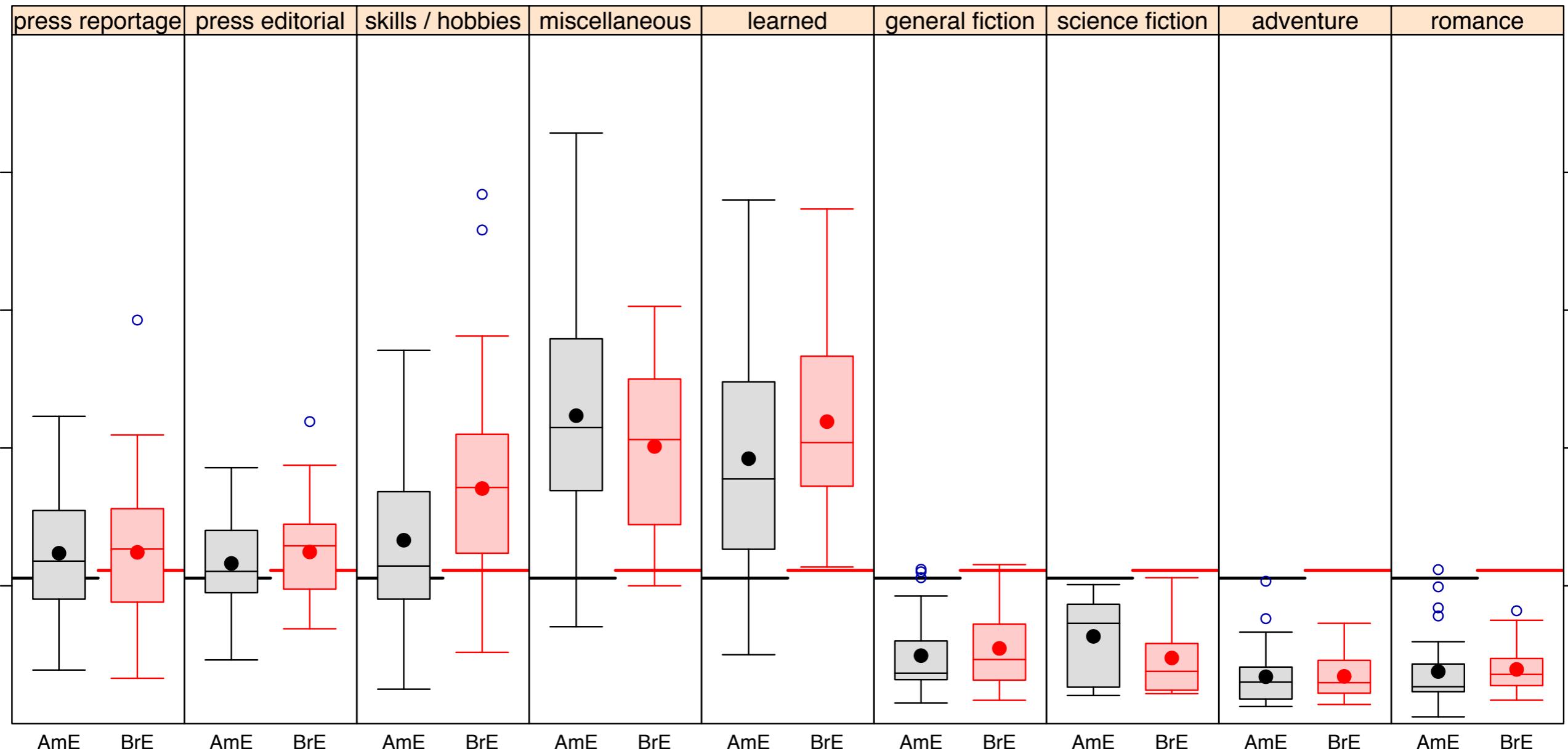
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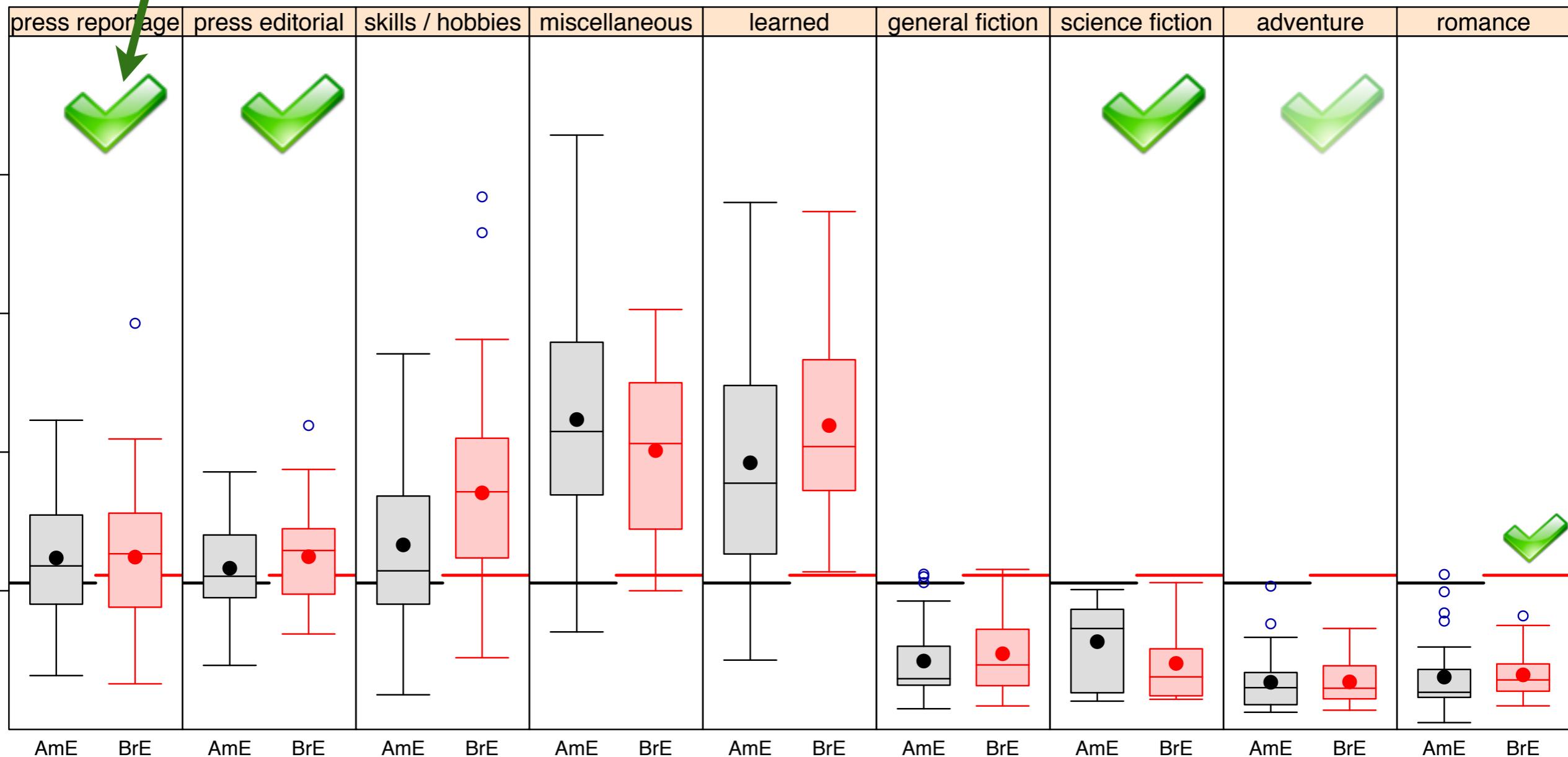
- ◆ Approach 1: restrict study to sublanguage in order to eliminate non-randomness
 - data from this sublanguage (= single section in library) can be pooled into large random sample
 - ◆ Approach 2: goal of quantitative corpus analysis is to **explain variation** between texts in terms of
 - random sampling (of tokens within text)
 - stylistic variation: genre, author, domain, register, ...
 - subject matter of text → term clustering effects
 - differences between language varieties
- research question** ←

Eliminating non-randomness



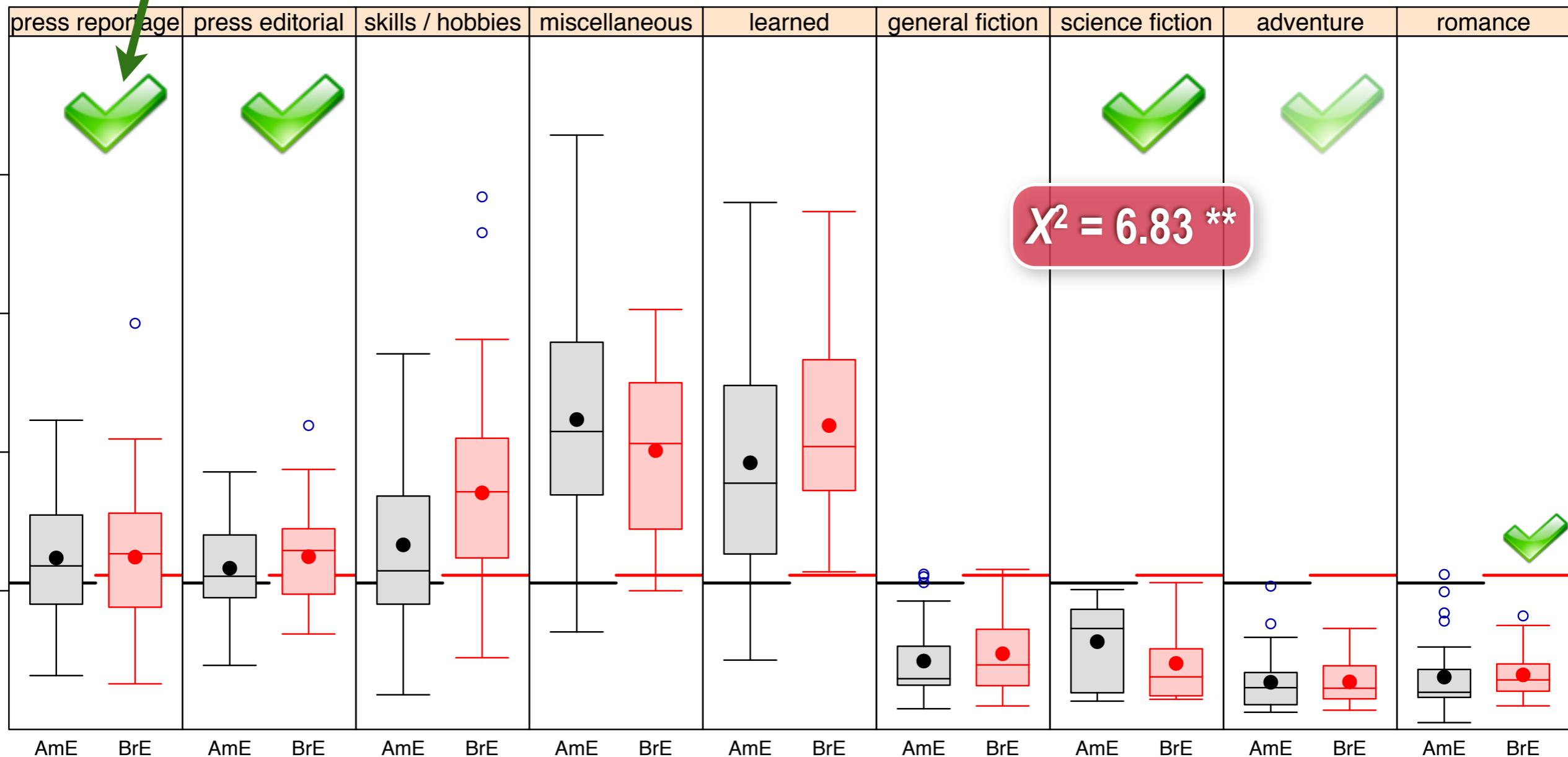
Eliminating non-randomness

binomial distribution across texts (almost)



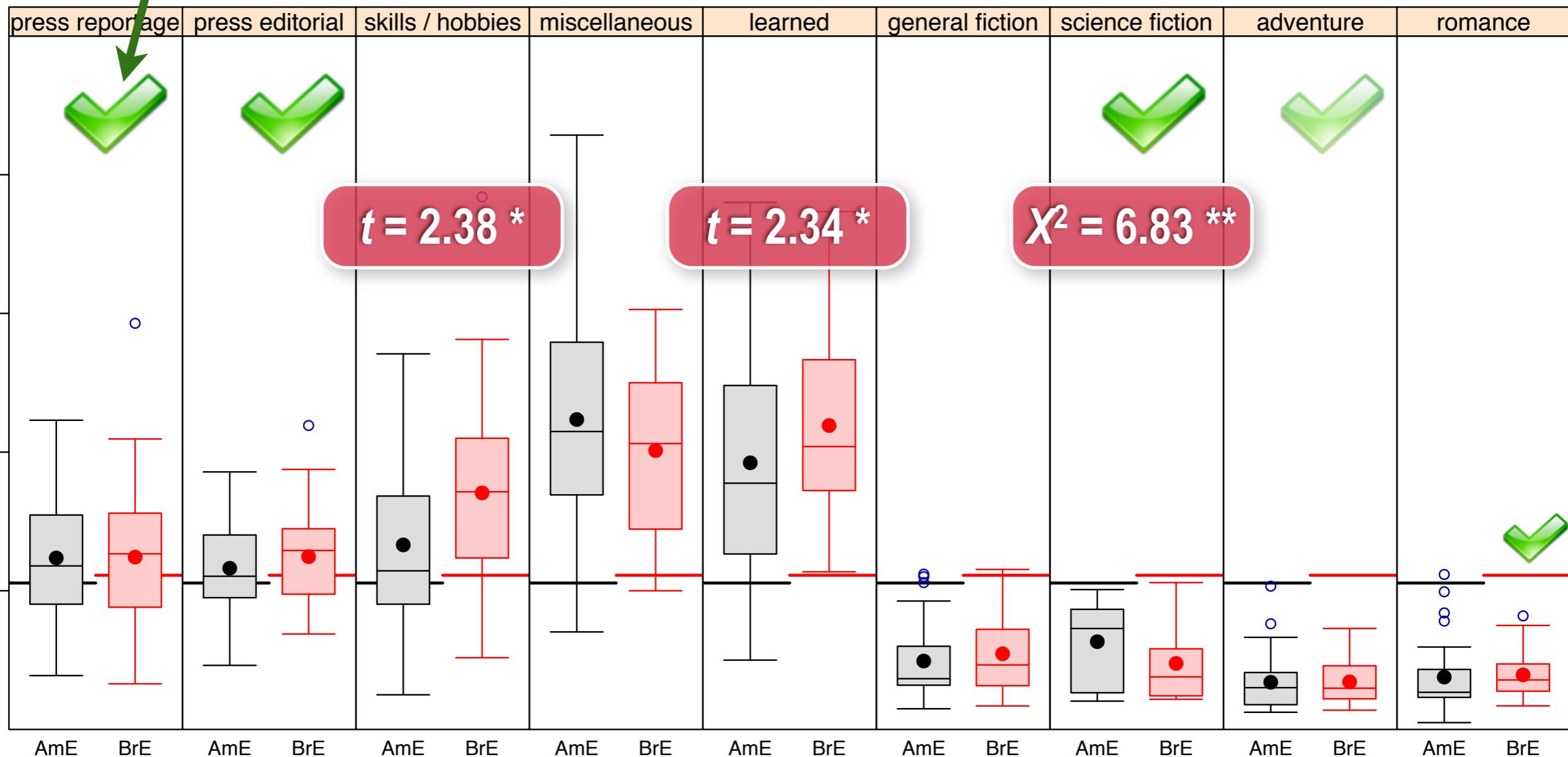
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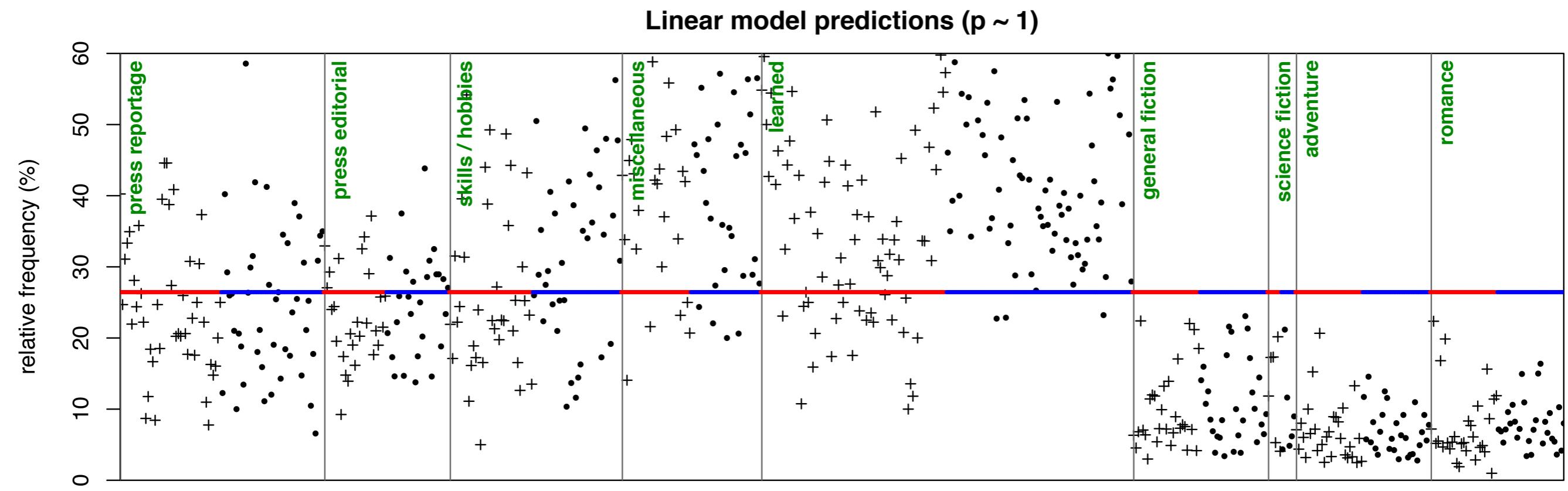
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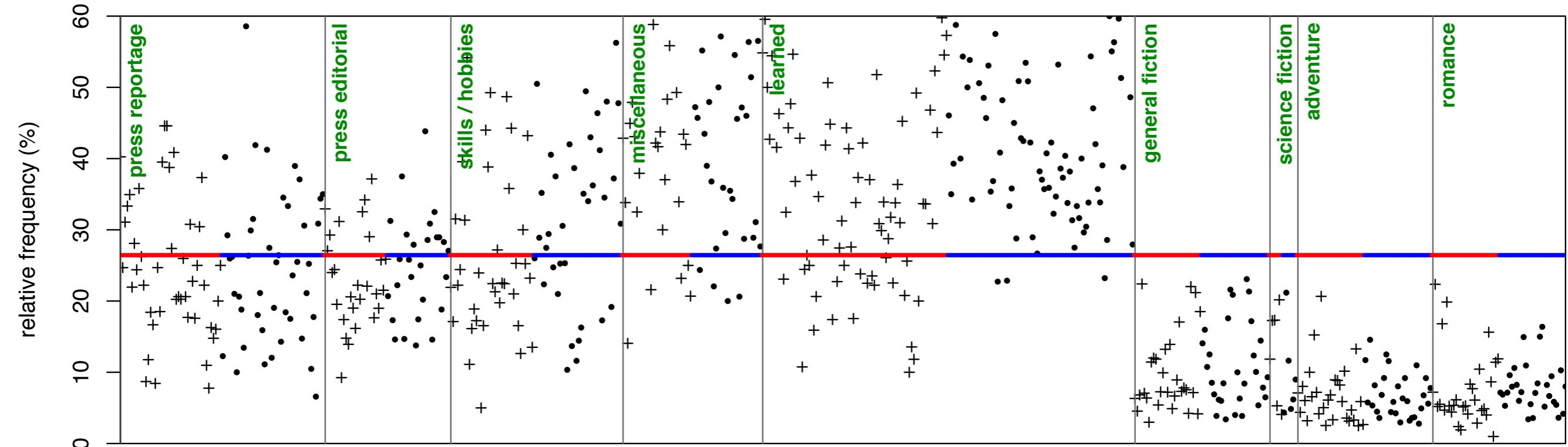
I'm just an ANOVA ...

Linear model for passives

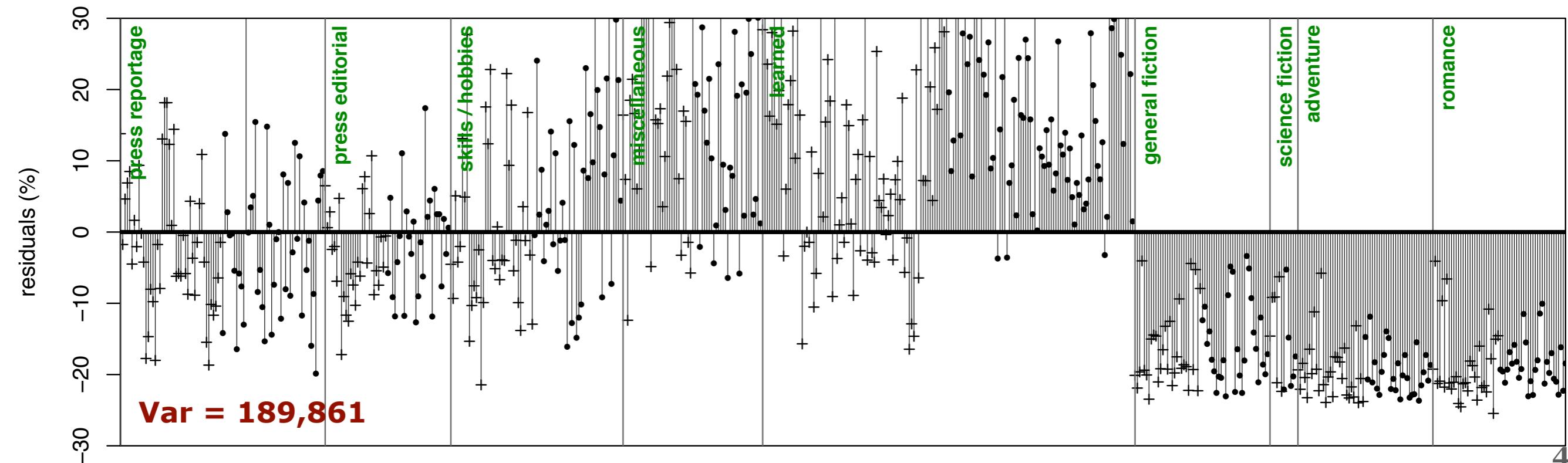


Linear model for passives

Linear model predictions ($p \sim 1$)

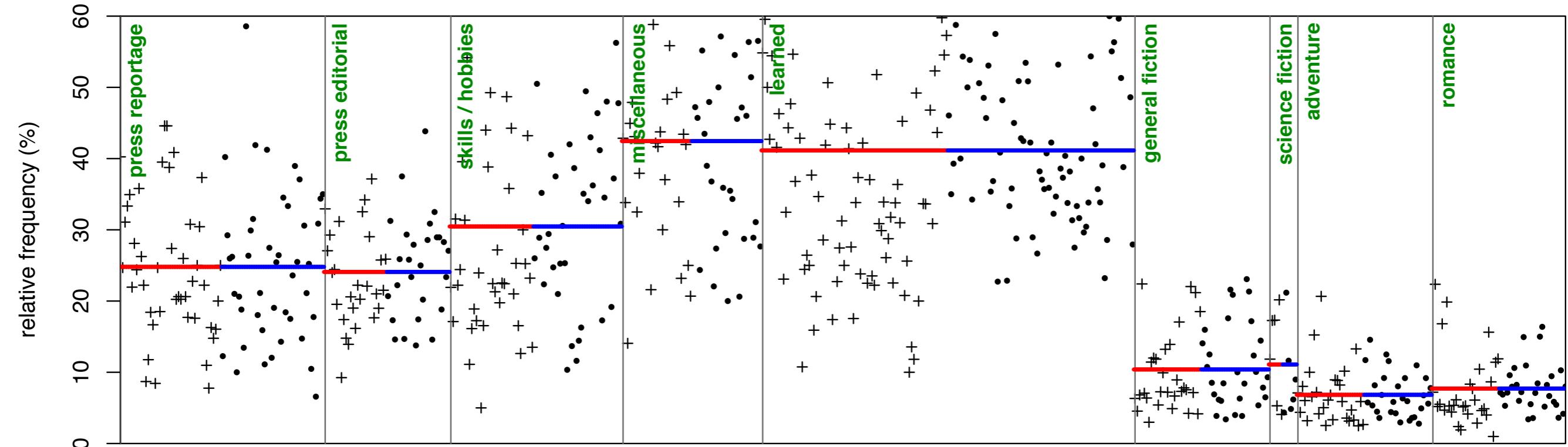


Unexplained residuals of linear model

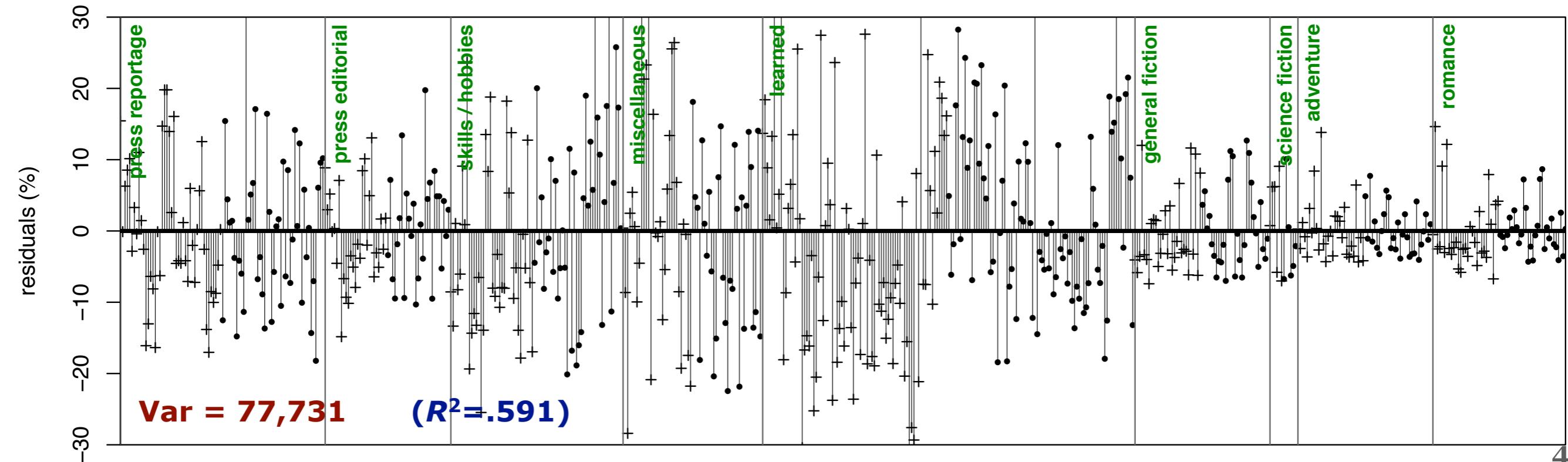


Linear model for passives

Linear model predictions ($p \sim 1 + \text{genre}$)

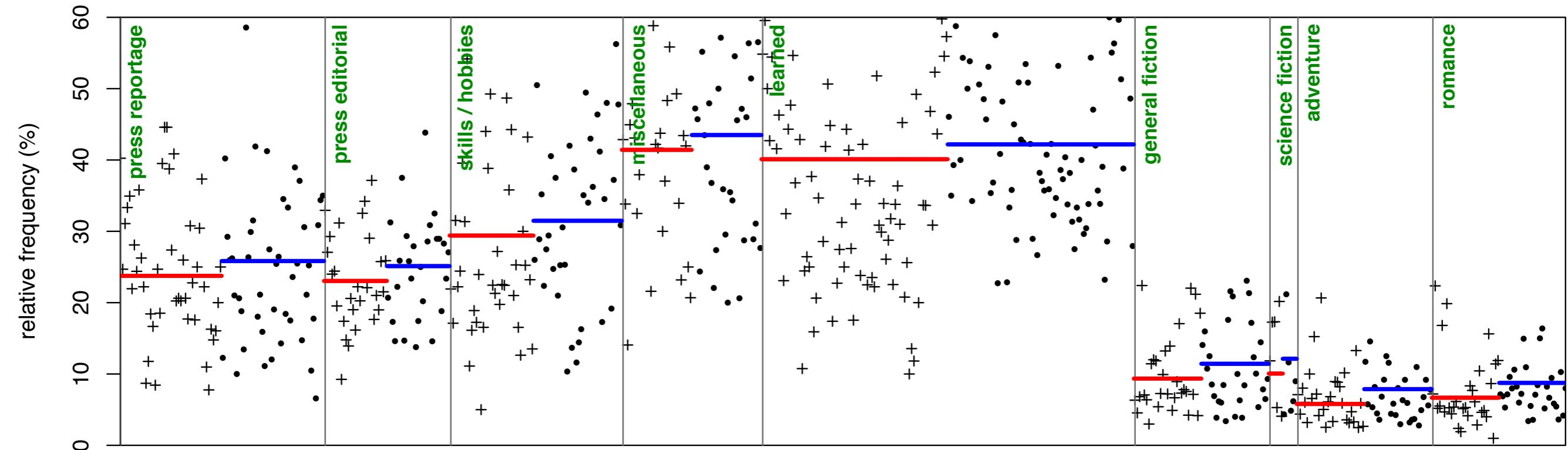


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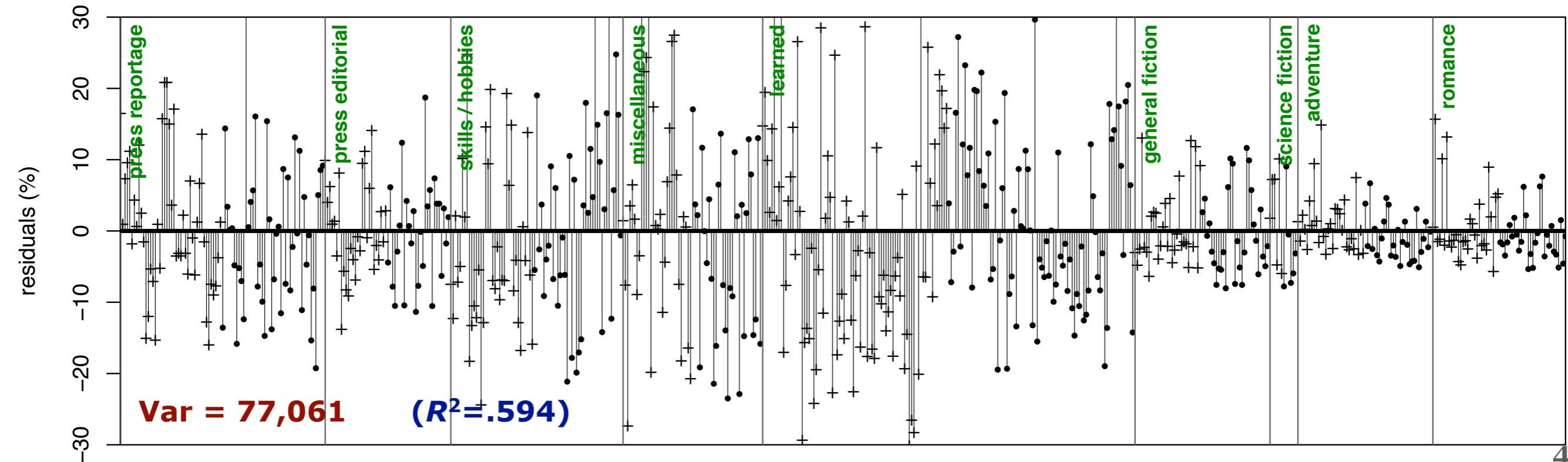


Linear model for passives

Linear model predictions ($p \sim 1 + \text{genre} + \text{Am/Br}$)



Unexplained residuals of linear model



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- ◆ Is variance explained well enough?
 - binomial sampling variation: ca. 10,200 (= 5.4%)

Linear models in R

```
# linear model “formula”: response ~ explanatory factors
> LM <- lm(relfreq ~ genre + lang, data=Passives)

# analysis of variance shows which factors are significant
> anova(LM)      # see ?anova.lm for details

# individual coefficients + standard errors
> summary(LM)    # difficult to interpret for genre (why?)
> confint(LM)     # corresponding confidence intervals
```

Linear model for passives

- ◆ F-tests show significant effects of genre ($p < 10^{-15}$) and AmE / BrE ($p = .0198$)
- ◆ 95% confidence intervals for effect sizes:
 - AmE / BrE: 0.3% ... 3.8%
 - genre = learned 13.4% ... 19.3%
 - compared to “press reportage” genre as baseline
 - genre = romance -20.8% ... -13.4%
 - genre = ...

Linear models in R

```
# more intuitive than coefficients: model predictions for each
# genre and language variety; based on “dummy” data frame with
# all possible genre/language combinations (ordered by genre)
> Predictions <-  
  unique(Passives[, c("genre", "lang")])  
> Predictions <- Predictions[  
  order(Predictions$genre, Predictions$lang), ]  
  
# predicted average relative frequency of passives in each category  
> transform(Predictions,  
  predicted=predict(LM, newdata=Predictions))  
  
# confidence and prediction intervals (see Unit #6 for details)  
> cbind(Predictions, predict(LM,  
  newdata=Predictions, interval="confidence"))  
> cbind(Predictions, predict(LM,  
  newdata=Predictions, interval="prediction"))
```

Linear models in R

		genre	lang	fit	lwr	upr
1	press	reportage	AmE	23.76	21.25	26.27
311	press	reportage	BrE	25.83	23.32	28.34
45	press	editorial	AmE	23.05	19.92	26.17
355	press	editorial	BrE	25.12	22.00	28.25
72	skills / hobbies		AmE	29.40	26.69	32.12
382	skills / hobbies		BrE	31.48	28.78	34.18
108		miscellaneous	AmE	41.42	38.44	44.40
420		miscellaneous	BrE	43.50	40.52	46.48
138		learned	AmE	40.11	38.15	42.06
450		learned	BrE	42.18	40.23	44.14
218	general	fiction	AmE	9.35	6.33	12.38
530	general	fiction	BrE	11.43	8.41	14.46
247	science	fiction	AmE	10.06	3.63	16.48
559	science	fiction	BrE	12.13	5.71	18.56
253		adventure	AmE	5.80	2.77	8.82
565		adventure	BrE	7.87	4.85	10.90
282		romance	AmE	6.67	3.65	9.70
594		romance	BrE	8.75	5.73	11.78

Linear models in R

```
# alternative: compute partial effects with effects package
> library(effects)
> eff <- Effect(c("genre", "lang"), LM)
> print(eff) # predicted values for each category

# visualization of partial effects
> plot(eff, multiline=TRUE, rotx=30)

# some display options
> topR <- list(x=0.95, y=0.95, corner=c(1,1))
> plot(eff, multiline=TRUE, rotx=30,
       ci.style="bars", key.args=topR)

# partial main effects average over other predictors
> plot(Effect("genre", LM), rotx=30, ylim=c(0,50))
```

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```
> LM <- lm(relfreq ~ genre + lang +
            genre:lang, data=Passives)
> anova(LM)
```
- ◆ Interaction is **not significant** here ($p = .055$)
 - data give no evidence for genre-specific differences



Linear models are not appropriate!

```
> par(mfrow=c(2, 2))  
> plot(LM)  
> par(mfrow=c(1, 1))
```



Linear models are not appropriate!

Why linear models are not appropriate for frequency data

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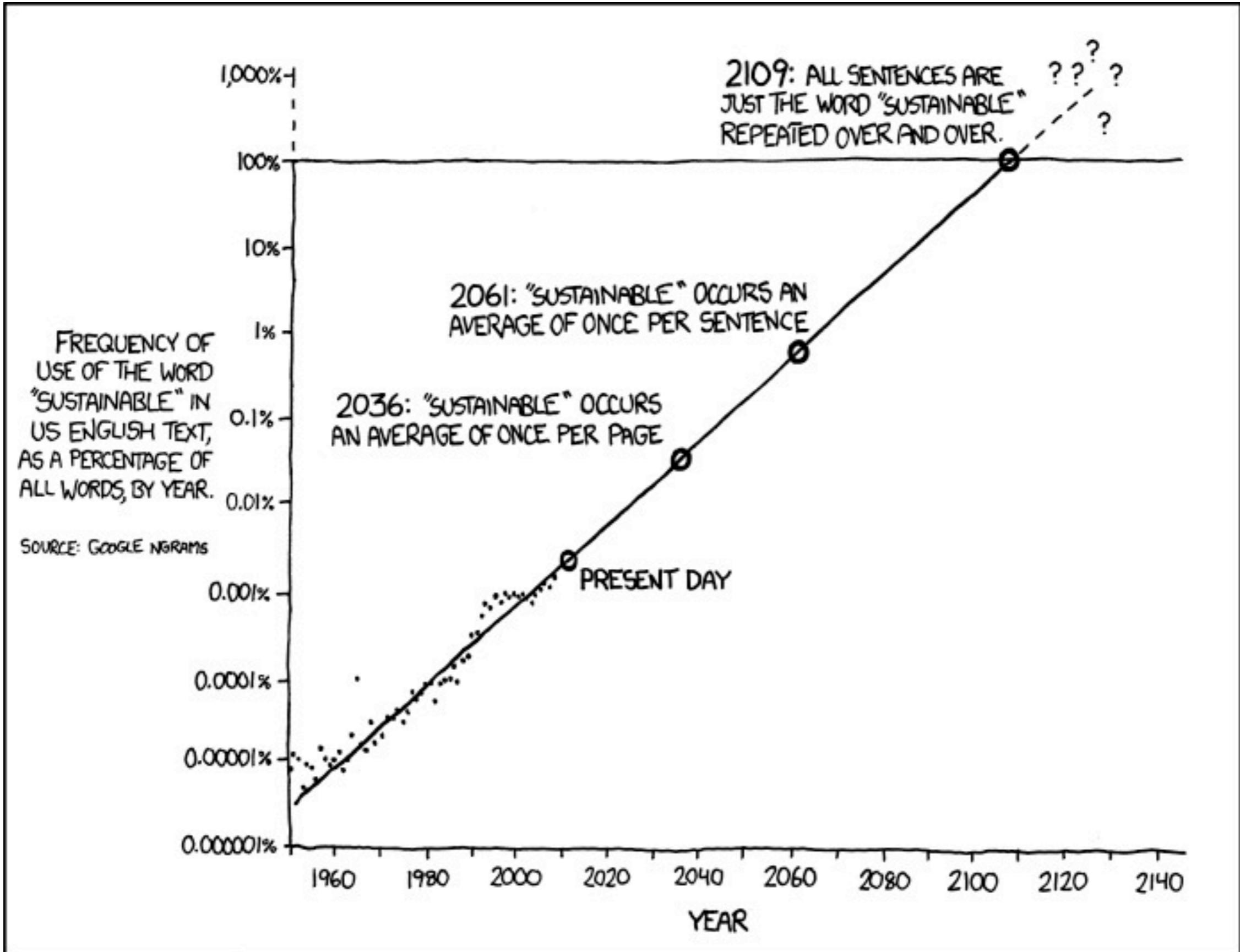
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 - different sample sizes (texts in Brown/LOB: 40 – 250 sentences; huge differences in BNC)
- ◆ Predictions not restricted to range 0% – 100%



THE WORD "SUSTAINABLE" IS UNSUSTAINABLE.

Generalised linear models

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$$f_i \sim B(n_i, \pi_i)$$

binomial sampling
("family")

$$\pi_i = \frac{1}{1 + e^{-\theta_i}}$$

"link" function

"response" → $\theta_i = \beta_0 + \beta_1(\text{genre}) + \beta_2(\text{AmE/BrE})$

linear predictor →

GLM for passives

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- ◆ Interpretation of confidence intervals difficult

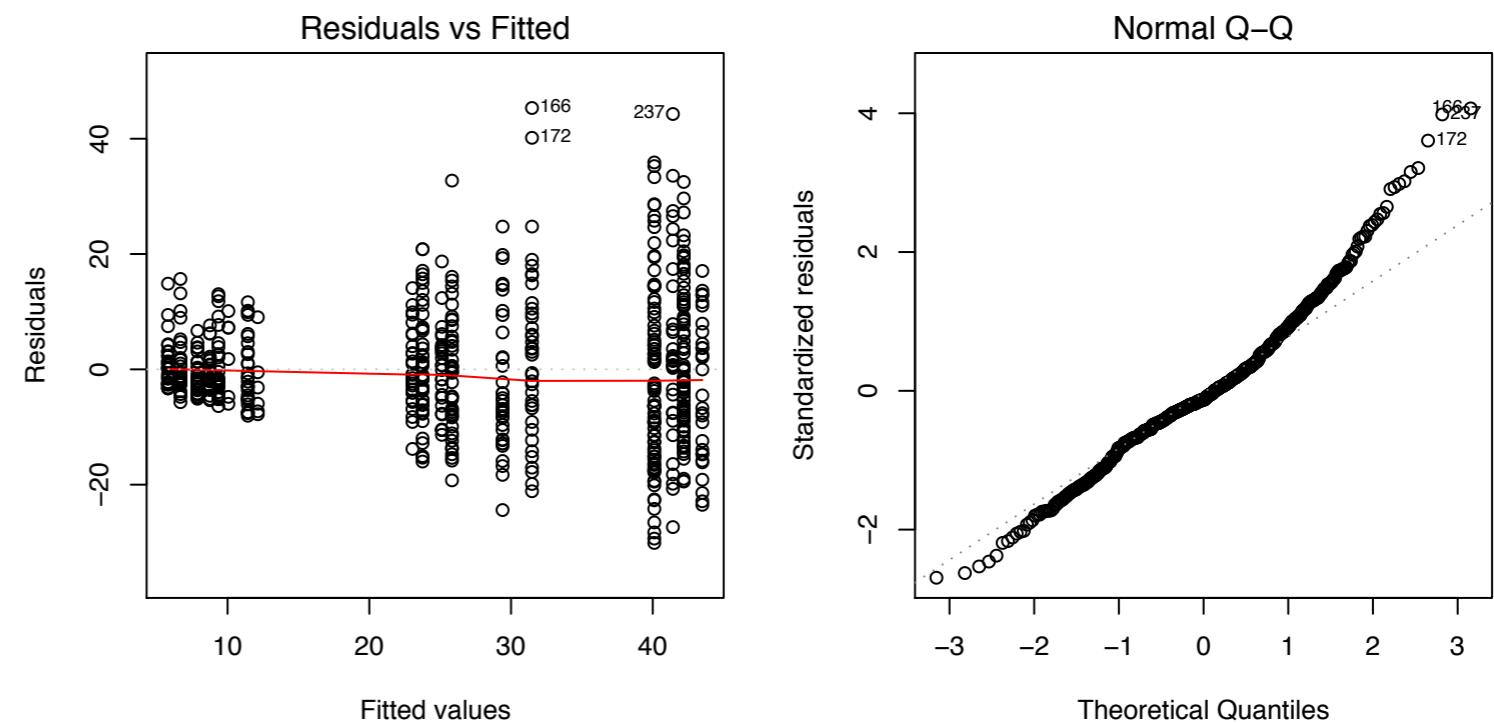
GLM in R

(note the extra options needed!)

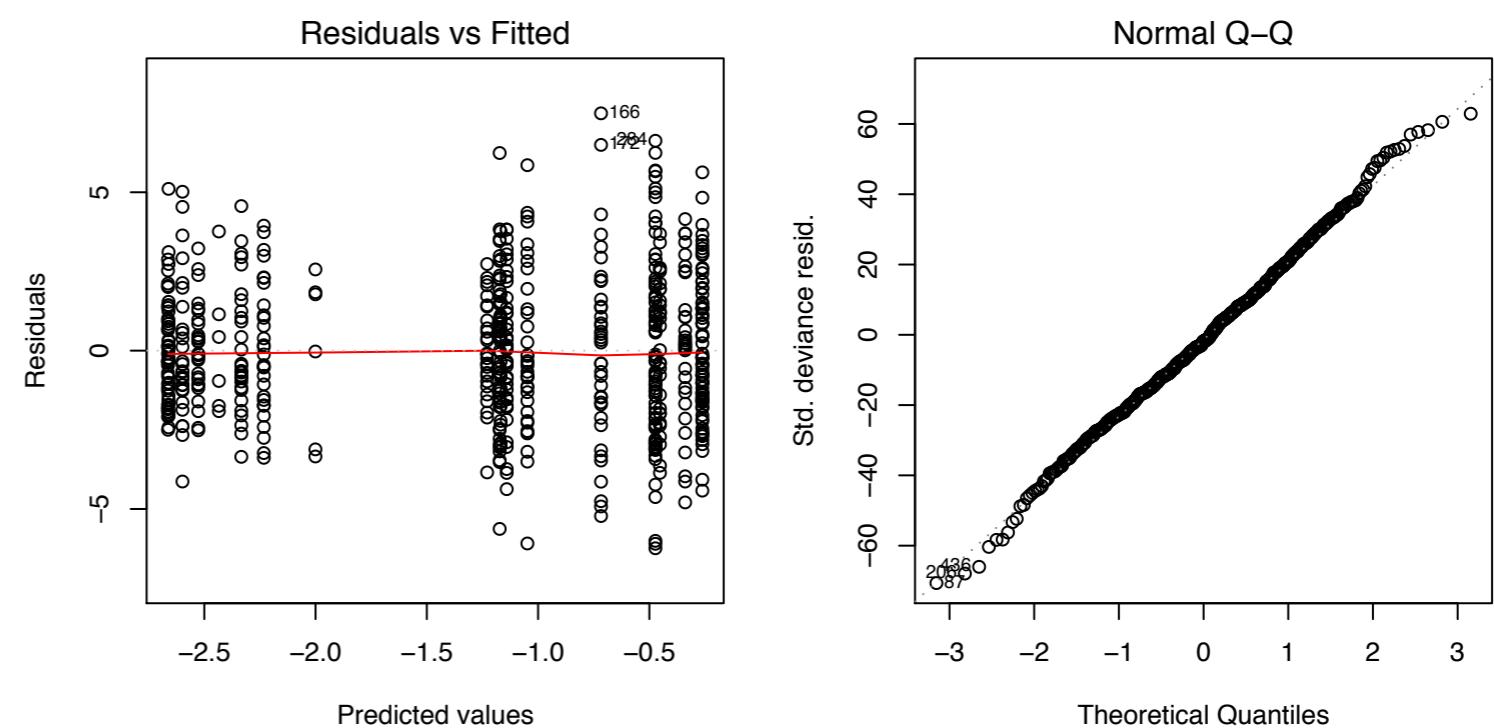
```
# for GLM with binomial family, responses are pairs of  
# passive / active counts ( $f_k, n_k-f_k$ ) = “successes” / “failures”  
> response.matrix <- cbind(Passives$passive,  
    Passives$n_s - Passives$passive)  
  
# genre * lang is shorthand for main effects + all interactions  
> GLM <- glm(response.matrix ~ genre * lang,  
    family="binomial", data=Passives)  
  
# individual coefficients + standard errors  
> anova(GLM, test="Chisq") # interaction significant now  
  
> summary(GLM) # even more difficult to interpret than for LM  
> confint(GLM)  
  
# diagnostics plot ( ; separate multiple commands in single line)  
> par(mfrow=c(2,2)); plot(GLM); par(mfrow=c(1,1))
```

Model diagnostics comparison

Linear Model



Generalised Linear Model



Still no satisfactory explanation for observed variation in frequency of passives between texts!

GLM in R

(note the extra options needed!)

```
# predictions for each genre and language variety
> transform(Predictions, predicted =
  100 * predict(GLM, type="response",
                 newdata=Predictions))

# calculate confidence intervals from standard errors
> res <- predict(GLM, type="response",
                  newdata=Predictions, se.fit=TRUE)
> transform(Predictions,
            predicted = 100*res$fit,
            lwr=100*(res$fit - 1.96*res$se.fit),
            upr=100*(res$fit + 1.96*res$se.fit))

# we can't compute prediction intervals for new texts — why?
```

Partial effects for GLM

```
# the effects package also supports GLM  
> eff <- Effect(c("genre", "lang"), GLM)  
> print(eff) # predicted values for each category  
  
# visualization of partial effects (note the interaction)  
> plot(eff, multiline=TRUE, rotx=30,  
       ci.style="bars", key.args=topR)  
  
# partial main effects average over interactions in this case  
> plot(Effect("genre", GLM), rotx=30,  
       ylim=c(-3,0)) # ylim refers to linear predictor  
> plot(Effect("lang", GLM), rotx=30,  
       ylim=c(-3,0))
```

Take-home messages

- ◆ Don't trust statistic(ian)s blindly
 - You know how complex language really is!
 - linguists and statisticians should work together
- ◆ No excuse to avoid significance testing
 - good reasons to believe that binomial sampling distribution is a lower bound on variation in language
- ◆ Needed: large corpora with rich metadata
 - study & “explain” variation with statistical models
 - full data need to be available (not Web interfaces!)

T H A N K
Y O U

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