

# CS 736 : Assignment - Brain MRI Segmentation: FCM, Artifact Modeling, HMRF-GMM-EM

Instructor : Suyash P. Awate

Maximum Marks: 50

Due Date : 2 Apr 2018, Sunday, 11:55 pm

Items with **0 marks** are a necessary part of the assignment, without which the assignment won't be graded.

## 1. (25 marks) Segmenting a Brain Magnetic Resonance (MR) Image.

Download the bias-corrupted and noise-corrupted magnitude-MR image of a human brain from: `assignmentSegmentBrain.mat.zip`

The mat file also contains a binary (mask) image that separates the set of pixels within the brain from those outside the brain.

Implement the algorithm (covered in class lectures) for segmenting the brain in 3 segments, namely, (i) white matter, (ii) gray matter, and (iii) cerebrospinal fluid, using a **modified fuzzy-c-means (FCM) to estimate, and account for, the bias/inhomogeneity field in the brain MR image**.

Assume the number of classes  $K = 3$ .

Run the segmentation algorithm only on the image data inside the brain.

Manually tune values for (i) parameter  $q$  that controls the fuzziness of the segmentation and (ii) neighborhood mask (size and values) that gives the weights  $w_{ij}$  (you may choose the weights based on a Gaussian with mean as the center pixel of the mask; you should rescale the weight, if needed, so that they sum to 1). You must choose  $q$  to be greater than 1.5.

You must choose the **initial estimate for the bias field** to be a **constant** image.

After finding the optimal estimates of the (i) class means  $c_k$  for each class  $k$ , (ii) memberships  $u_{nk}$  at each pixel  $n$  inside the brain, and (iii) bias-field values  $b_n$ , construct the following images:

- Construct a **bias-removed-image**  $A$  as follows: at each pixel  $n$ , the intensity  $A_n$  in the bias-removed image equals the weighted sum:  $A_n := \sum_k u_{nk} c_k$ .
- Construct a **residual-image**  $R$  as follows: at each pixel  $n$ , the intensity  $R_n$  in the residual image equals the difference:  $R_n := Y_n - A_n b_n$ , where  $Y$  is the corrupted data image.

Implement the following functionality as part of the segmentation algorithm:

- (3 marks) Code to find the optimal value of the class means, within every iteration.
- (3 marks) Code to find the optimal value of the memberships, within every iteration.

(c) (3 marks) Code to find the optimal value of the bias field, within every iteration.

Report the following:

- (a) (0 marks) The chosen value for  $q$ .
- (b) (0 marks) The neighborhood mask  $w_{ij}$  seen as an image.
- (c) (0 marks) The initial estimate for the membership values shown as 3 images, i.e., one image that shows the membership values of all pixels to a particular class. Describe your motivation and algorithm for choosing this initialization.
- (d) (0 marks) The initial estimates of the class means. Describe your motivation and algorithm for choosing this initialization.
- (e) (6 marks) The value of the objective function at each iteration in the modified-FCM algorithm.
- (f) (10 marks) Show the following 5 images in the report (i) Corrupted image provided, (ii) Optimal class-membership image estimates, (iii) Optimal bias-field image estimate (iv) Bias-removed image, (v) Residual image.
- (g) (0 marks) The optimal estimates for the class means.

2. (25 marks) Segmenting a Brain Magnetic Resonance (MR) Image.

Download the corrupted magnitude-MR image of a human brain from: `assignmentSegmentBrainGmmEmMrf.mat.zip`

The mat file also contains a binary (mask) image that separates the set of pixels within the brain from those outside the brain.

Implement the algorithm (covered in class lectures) for segmenting the brain in 3 segments, namely, (i) white matter, (ii) gray matter, and (iii) cerebrospinal fluid, using an **expectation-maximization (EM) optimization algorithm** that relies on a **Gaussian mixture model (GMM) for intensities** and a **Markov random field (MRF) model on the labels**.

Assume the number of classes  $K = 3$ .

Run the segmentation algorithm only on the image data inside the brain.

Manually tune the  $\beta$  parameter value underlying the potential function in the MRF model on the label image, to control the smoothness on the labeling (and memberships).

Implement the following functionality as part of the segmentation algorithm:

- (a) (2 marks) Code to find the optimal value of the memberships, within every iteration.
- (b) (2 marks) Code to find the optimal value of the class means, within every iteration.
- (c) (2 marks) Code to find the optimal value of the class standard deviations, within every iteration.
- (d) (6 marks) Code to find the optimal labeling, within every iteration, based on a **modified iterated-conditional-mode (ICM)** optimization that updates all labels at once ensuring that the posterior probability (computed upto the normalization constant  $Z$ ; recall that, within any iteration,  $Z$  will be a function of  $\beta$  as well as the Gaussians' parameters) increases.

Report the following:

- (a) (0 marks) The chosen value for  $\beta$  that, in your judgement, gives a smooth and realistic segmentation.
- (b) (0 marks) The initial estimate for the label image  $x$ . Describe your motivation and algorithm for choosing this initialization.
- (c) (0 marks) The initial estimates of the Gaussian parameters  $\theta$ , i.e., the class means and standard deviations. Describe your motivation and algorithm for choosing this initialization.
- (d) (3 marks) Within every iteration, for the modified ICM segmentation, the values of the log posterior probability for the labels, i.e.,  $P(x|y, \theta, \beta)$ , before and after the ICM update.
- (e) (10 marks) Show the following 5 images in the report (i) Corrupted image provided, (ii) Optimal class-membership image estimates for chosen  $\beta$ , (iii) Optimal label image estimate for chosen  $\beta$ , (iv) Optimal class-membership image estimates  $\beta = 0$ , i.e., NO MRF prior on labels, (v) Optimal label image estimate for  $\beta = 0$ , i.e., NO MRF prior on labels.
- (f) (0 marks) The optimal estimates for the class means for the chosen  $\beta$ .