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Master Thesis

A comparison study of prediction
approaches for multiple training
data sets and test data with
block-wise missing values

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Abstract

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1 Introduction

On October 1, 1990 the international scientific research project named *Human Genome Project* was launched, with the aim to sequence the first complete human genome ever [1]. After investments of totally \$2.7 billion and 13 years of research, the sequencing was officially finished in 2003 [2]. Since then, on the one hand, there have been biomedical advances that have led to the identification of disease genes which in turn have led “to improved diagnosis and novel approaches in therapy” [3], p. 14]. On the other hand there has been an “extraordinary progress [...] in genome sequencing technologies” [[4], p. 333] leading to a sharp drop in sequencing prices. Nowadays whole genome sequencing is available and affordable for everyone - e.g. ‘Veritas Genomics’ offers whole genome sequencing for $\sim \$700$ [5].

Besides the ‘genome’ that carries the whole genetic material of an organism, there are also other types of ‘-omes’, such as ‘epigenomes’, ‘transcriptomes’, ‘proteomes’ and ‘microbiomes’. The time and costs to collect data from these different types of ‘-omes’ have been reduced drastically ever since the completion of the Human Genome Project [[6], [7], [8], [9], [10], [11]]. The methods for “fast, automated analyses of large numbers of substances including DNA, RNA, proteins, and other types of molecules” [12] are summarized under the term ‘High Throughput Technologies’. These technologies make data from molecular processes available for many patients on a large scale.

The collected data from any type of ‘-omes’ is commonly referred to as ‘omics data’. In the clinical context, it is of utmost interest to incorporate such omics data into different statistical approaches. A common example in this context is the survival time prediction for cancer patients, where in addition to regular clinical data gene expression data has been incorporated into the survival models. This additional omics data has “often been found to be useful for predicting [the] survival response” [[7], p. 1]. In “the beginning, only data from single omics was used to build such prediction models, together or without [...] clinical data” [[13], p. 1]. The usage of multiple distinct types of ‘-omes’ in a single prediction approach was the next logical step and coined the term ‘multi-omics data’. The theoretical aspects of integrating multiple omics types into a single prediction model and how to deal with the block-wise structures have been topic of several papers already - e.g. [13], [14], [15], [16], [17].

This thesis deals with a special type of missing data “that is common in practice, particular in the context of multi-omics data” [18] - the so-called ‘block-wise missingness’. Data with block-wise missingness consists of different folds and feature-blocks. While a feature-block stands for a collection of

associated covariates, a fold represents a set of observations with the same observed feature-blocks. In data sets with block-wise missingness, there is always at least one fold, with a missing feature-block, such that not all observations have the same observed feature-blocks.

Most statistical methods require fully observed data for training and predictions. In data with block-wise missingness, this requirement is not met, so that either the approaches need methodical adjustment or the data needs to be processed. This foundational problem with block-wise missingness raises the following challenges and questions: How can we fit a model on the block-wise missing data, without removing observations or whole feature-blocks? Does imputation work properly in these settings? How does a model that uses single feature-blocks only perform in comparison? How can a model predict on observations with missing feature-blocks?

In addition to the problem of block-wise missingness, there is also the challenge of “inherent high dimensionality” [[19] p. 93], when working with multi-omics data. Data from a single omics type can easily exceed thousands of covariates and the corresponding data sets usually consist of fewer observations than features [13]. Besides the predictive performance of an approach, it is furthermore important for the approach to be sparse. “Sparsity is [...] an important aspect of the model which contributes to its practical utility” [[15], p. 3], as it makes the model much more interpretable than models including several thousands of variables.

A method that handles high dimensional data, even if the number of observations is lower than the amount of features, is the random forest method [13]. The method additionally handles different input types, does not need a lot of tuning and yields comparable predictive performances [20]. The only drawback is that it is not as interpretable as “models yielding [*in*] coefficient estimates of few relevant features” [[13], p. 35], as penalised regression approaches for example. Nevertheless, variable importance measures can be extracted with the random forest method, as well as partial dependencies. Furthermore it has already been used successfully in various articles dealing with multi-omics data - e.g. [13], [14]. Moreover, there have been proposals by Hornung et al. [18] and Krautenbacher [19] that modify the random forest approach, such that it can directly handle data with block-wise missingness. The different adaptations of penalised regression, as the priority-Lasso [15] can also be modified so they can directly deal with block-wise missing data. The theoretical aspects of these approaches are not part of this thesis but of Hagenberg’s [21]. Nevertheless, the performances of the different random forest approaches and penalised regression adaptations are compared in this thesis as well.

Even though the problem of block-wise missingness is common in multi-omics data there are, to my knowledge, no comparison studies of such prediction approaches yet. Krautenbacher has already stated that “reliable analysis strategies for multi-omics data [...] [with block-wise missingness are] urgently needed” [[19] p. 94]. The thesis at hand aims to provide such a large scale comparison study of prediction approaches capable of dealing with block-wise missingness and shall help to find a reliable analysis strategy.

To investigate a reliable analysis strategy for multi-omics data with block-wise missingness this paper compares the predictive performance of two naive random forest approaches, a random forest approach on imputed data, two random forest adaptation, the mdd-sPLS method and the adaptions of penalised regression. In the second chapter, firstly the term ‘block-wise missingness’ is defined in more detail and how it can arise in multi-omics data. Then a theoretical explanation of the random forest method for classification is given. Following three data processing approaches are explained - these process the block-wise missing data such that a regular random forest can be trained with it. Moreover, two methodological adaptations of the random forest method are illustrated. These adaptations allow the random forest approach to directly deal with block-wise missing data. The first part of the third chapter covers general information on the used metrics and evaluation techniques. Following the different data sources and corresponding data sets are described and investigated. These data sets are then used to validate the performances of the various approaches. In the penultimate chapter all approaches are analysed and the predictive performance is compared, while the last chapter of this thesis discusses all findings, draws a conclusion and gives an outlook.

2 Methods

This section deals with the theory of the random forest model and the different adaptions of it to handle data with block-wise missingness.

In the beginning, block-wise missingness is defined in more detail and it is shown how it can arise in multi-omics data. Afterwards, the theory of the random forest method for classification is illustrated. Subsequent three approaches that process the data with block-wise missingness, such that a regular random forest can be fit on them, are described. The last two sections of this chapter present two different adaptations of the random forest method. These adaptions enable the random forest method to directly deal with block-wise missing data.

2.1 Block-wise missingness in multi-omics data

Collecting omics data has become significantly cheaper and faster ever since the completion of the Human Genome Project. As a result, this type of data is used more and more frequently in the biomedical research - e.g. risk prediction of childhood asthma [19]. Even though the integration of multiple types of '-omes' into a single prediction approach seems promising there are still challenges to face. One of these challenges is a special type of missingness that is common in the context of multi-omics data, the so-called block-wise missingness [18].

The term block-wise missingness needs to be defined in more detail, before clarifying how it can arise in multi-omics data. Table 1 shows a minimalist example for a data set with block-wise missingness, whereby the data consists of eight observations, 105 covariates and the binary response variable Y . While the covariates 'weight', 'height', 'income' and 'education' are pretty much self-explanatory, the features ' g_1 ', ..., ' g_{100} ' could be any type of omics data. Data with block-wise missingness always consist of different blocks and folds. On the one hand, a **block** describes a set of covariates containing all features collected based on a characteristic - basically all covariates that are related in content. The data in table 1 has three blocks in total. 'Block 1' consists of the variables 'weight' and 'height' representing the physical properties. 'Block 2' contains the variables 'income' and 'education' standing for economic properties. 'Block 3' includes the remaining variables ' g_1 ', ..., ' g_{100} ' that are measurements from a single omics type and represent genetic properties. On the other hand, a **fold** represents a set of observations with the same observed feature-blocks - basically all observations with the same observed features. The data set in table 1 consists of three folds in total.

'Fold 1' holds the observations 1, 2 and 3, as these have the same observed feature-blocks ('Block 1' & 'Block 2'). 'Fold 2' holds the observations 4 and 5, while 'Fold 3' consists of the remaining observations 6, 7 and 8. As each fold has different observed feature-blocks, each fold is unique and every observation belongs to exactly one of them. The only variable all folds must have in common is the target variable.

<i>ID</i>	<i>weight</i>	<i>height</i>	<i>income</i>	<i>education</i>	g_1	\dots	g_{100}	<i>Y</i>	
1	65.4	187	2.536	<i>Upper</i>				1	Fold1
2	83.9	192	1.342	<i>Lower</i>				0	
3	67.4	167	5.332	<i>Upper</i>				1	
4			743	<i>Lower</i>	-0.42	\dots	1.43	1	Fold2
5			2.125	<i>Lower</i>	0.52	\dots	-1.37	0	
6	105.2	175			-1.53	\dots	2.01	0	Fold3
7	71.5	173			0.93	\dots	0.53	0	
8	73.0	169			0.31	\dots	-0.07	1	

$\underbrace{\hspace{1cm}}_{Block1}$ $\underbrace{\hspace{1cm}}_{Block2}$ $\underbrace{\hspace{1cm}}_{Block3}$

Table 1: A data set with block-wise missingness - consisting of three feature-blocks, three folds and the binary target variable 'Y'.

Multi-omics data with block-wise missingness have a structure as displayed in table 1, but the single feature-blocks are usually much higher dimensional than in the given example. When working with multi-omics data this type of missingness is a common problem. There are two main reasons for this: The first one is related to the costs of collecting omics data. Even though the costs have been reduced drastically over the last 15 years, collecting omics data is still more complex and expensive than obtaining standard clinical data, as 'weight', 'height' and 'smoking status'. As a consequence, due to financial or even technical constraints, omics data can not always be collected for all participants of a study. Therefore participants from the same study can end up with different observed feature-blocks, such that the data for the whole study contains block-wise missingness.

The second reason is related to the collection of data-sets from different sources - e.g. various hospitals. Even though the different sources do research regarding the same response variable the surveyed feature-blocks can still differ. Therefore the concatenation of such data sets can result in a data set with block-wise missingness.

This scenario is illustrated in figure 1. In the top of the figure the three different data sources are displayed - 'Hospital 1', ..., 'Hospital 3'. Each

source consists of the target variable 'Y' and two feature-blocks as covariates - e.g. 'Hospital 2' consists of the target variable 'Y' and the feature-blocks 'RNA' and 'Clinical'. The feature-blocks 'RNA', 'miRNA' and 'CNV' represent high dimensional omics data, while the 'Clinical' feature-block stands for several clinical features. Even though the target variable 'Y' is the same for all data sources, the observed feature-blocks still differ. The concatenation of the data sets results in data with block-wise missingness and is displayed in the bottom of figure 1. In the concatenated data an observed block is marked with a green tick and a missing block with a red cross. The fold 'Hospital 2' only has 'RNA' and 'Clinical' as observed feature-blocks, such that the observations from this fold miss all the features from the blocks 'CNV' and 'miRNA'. The concatenated data consists of three unique folds and four different feature-blocks.

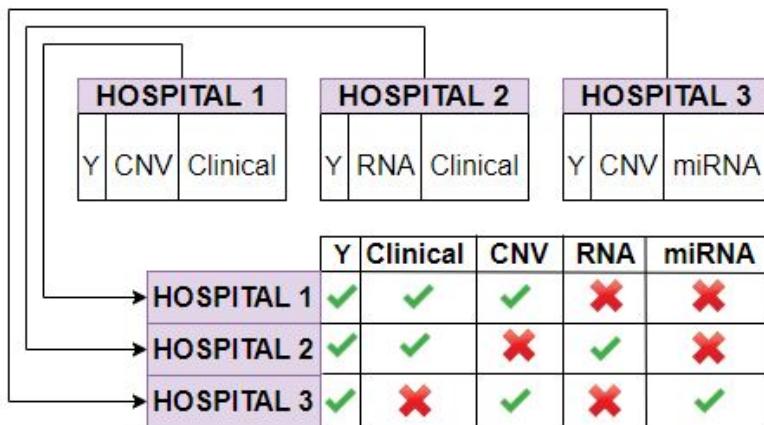


Figure 1: Block-wise missingness, when concatenating data from diverse sources.

Training a prediction model is mostly not directly possible on data with block-wise missingness. Either the methods have to be adopted or the data processed. As block-wise missingness can also affect the test data it raises the following question. How can a model predict for an observation that misses feature-blocks the model has been trained with? This challenge has to be taken into account when proposing methods capable to deal with block-wise missingness.

The remaining sections in this chapter focus on the approaches and adaptations to make model fitting on such data possible. Firstly the concept of the random forest for classification is explained and then the different approaches and adaptions to handle data with block-wise missingness.

2.2 Random Forest for classification

This chapter illustrates the random forest method that has already been applied in several articles dealing with multi-omics data [[13], [14], [15]]. It is a “powerful prediction method [...] able to capture complex dependency patterns between the outcome and the covariates” [[14] p. 2]. Furthermore it does not need a lot of tuning and naturally handles high-dimensional data with more covariates than observations [13]. The random forest method can be applied to classification-, regression- and even survival-problems. Latter was added in 2008 by Ishwaran et al. [22]. As this thesis focuses on classification tasks, only the random forest for classification is explained. Nevertheless all of the approaches and adaptions described in sections 2.3 to 2.7 can also be applied for non-categorical target variables.

The random forest is a tree-based ensemble method that was introduced by Breiman in 2001 [23]. An ensemble is a concept from machine learning that “train[s] multiple models using the same learning algorithm” [24]. Therefore an ensemble consists of η identical so-called ‘base learners’. The base learner of the random forest method is a ‘decision tree’. This is an excellent base learner for an ensemble, as a decision tree can capture complex interactions and have a relatively low bias if grown sufficiently deep. Especially as single decision trees are known to be noisy, they benefit from the ensemble [20]. Since decision trees are the basis of random forest method it is crucial to understand how these work to properly understand the random forest method.

2.2.1 Decision Tree

A decision tree is a supervised learning method that was introduced by Breiman et al. in 1984 [25]. It has a hierarchical nature, is easy to interpret and non-model based [26]. It applies recursive binary splitting to “partition the feature space into a set of rectangles” [[20] p. 305], such that the resulting rectangles are as pure as possible in terms of the target variable. A prediction is generated by assigning an observation to one of the rectangles in the partitioned feature space. The prediction then equals the distribution of the target variable within the assigned rectangle - e.g. an observation that falls into a rectangle with three negative and seven positive responses has predicted a probability of 70% for a positive response.

To partition the feature space into the purest rectangles possible the algorithm iterates over all possible split variable/ split value combinations. For each of these possible splits, the observations from the parent node N are divided - with respect to the split variable x_j at split point t - into the

child nodes N_1 and N_2 [[27], p. 10]:

$$N_1(x_j, t) = \{(x, y) \in N : x_j \geq t\} \quad (1)$$

$$N_2(x_j, t) = \{(x, y) \in N : x_j < t\} \quad (2)$$

Hence N_1 contains all observations from the parent node N with $x_j \geq t$, while N_2 contains all observations from the parent node N with $x_j < t$. The point (x_j, t) therefore creates a binary split and partitions the data from parent node N in the two subspaces N_1 and N_2 . The split variable x_j and split point t are chosen such that the resulting child nodes N_1 and N_2 have the greatest possible purity [27]. To measure the impurity of a node N regarding a categorical response with g classes the 'Gini-Index' (3), 'Misclassification-Error' (4) or 'Shannon-Entropy' (5) can be used [[27], p. 12]:

$$I(N) = \sum_{k=1}^g \hat{\pi}_{k,N} \cdot (1 - \hat{\pi}_{k,N}) \quad (3)$$

$$I(N) = 1 - \max_k \hat{\pi}_{k,N} \quad (4)$$

$$I(N) = - \sum_{k=1}^g \hat{\pi}_{k,N} \cdot \log(\hat{\pi}_{k,N}) \quad (5)$$

- $\hat{\pi}_{k,N}$: Relative frequency of category k in node N

For all of these impurity measures applies: The lower $I(N)$ the purer the node N and a node N is completely pure, when it only contains observations of the same response class - $I(N) = 0$. The corresponding plots of these impurity functions for a binary target variable are in the attachment in figure A-1. The reduction of the impurity when splitting the parent node N into the child nodes N_1 and N_2 is calculated by [[27], p. 10]:

$$I(N) - \frac{|N_1|}{|N|} \cdot I(N_1) - \frac{|N_2|}{|N|} \cdot I(N_2) \quad (6)$$

- $|N|$: Number of observations in the parent node N
- $|N_1|$: Number of observations in child node N_1
- $|N_2|$: Number of observations in child node N_2

This equation calculates how strong the impurity from the parent node N is reduced for a given splitting point that divides the observations to the child nodes N_1 and N_2 . This impurity reduction is calculated for every possible split. The final split variable x_j and split point t are chosen, such that the impurity is maximally reduced.

For illustrative purposes, the single partition steps of a classification tree are shown in figure 2. The figure consists of three plots in total, whereby each is a scatter plot of 'weight' and 'height' for the observations from 'Fold 1' and 'Fold 3' in table 1. Observations with a positive outcome are marked in blue, while negative outcomes are marked in red.

In the very beginning, all observations are in the same feature space that has not been divided yet 'N1' - the so-called 'root node'. This is displayed in the leftmost plot of figure 2. The node contains three observations with a positive and three with a negative response - hence the class distribution in this node is 50|50. The node is not pure regarding its responses and all possible impurity measures [(3), (4), (5)] have the highest possible value. The algorithm now iterates over all features, and for each feature over all possible split points and calculates the impurity of the resulting child nodes for each of these possible splits. The split variable and corresponding split value are chosen, such that the impurity reduction according to equation (6) is maximised. In the example of figure 2 the first split variable is chosen as 'weight' with the split value 69. Therefore the data from the root node - 'N1' - is split into the two child nodes 'N2' and 'N3' - central plot in figure 2. 'N2' contains the observations with weight ≥ 69 , while 'N3' consists of the observations with a weight < 69 . The distribution of the target variable in 'N2' is 25|75 and in 'N3' 100|0. Hence both resulting child nodes are purer than their parent node 'N1'. The node 'N3' only contains observations with a positive response, therefore it is completely pure and can not be split any further - all possible impurity measures [(3), (4), (5)] have the lowest possible value. The node 'N2' on the other hand is not completely pure yet and can be split further. 'N2' is now the parent node and the algorithm tries all possible splits on this segmented feature space. The highest impurity reduction of 'N2' is achieved with the split-variable 'height' on the value 171. 'N2' is therefore further split into 'N4' - all observations from 'N2' with a height ≥ 171 - and 'N5' - all observations from 'N2' with a height < 171 . As well 'N4' as 'N5' are completely pure and the impurity of these nodes can not be reduced any further. The final partitioned feature space is displayed on the rightmost plot in figure 2. Based on this final partitioned feature space predictions can be done by assigning observations to one of the segments in the feature space. An observation with weight = 90 and height = 185 for example falls into the segment 'N4' and has a predicted class probability of 100% for response class 0 then.

Hence the decision tree algorithm splits the feature space, such that the resulting child nodes maximally gain purity regarding the target variable. This is done with an exhaustive search, trying all possible split variables and corresponding split points.

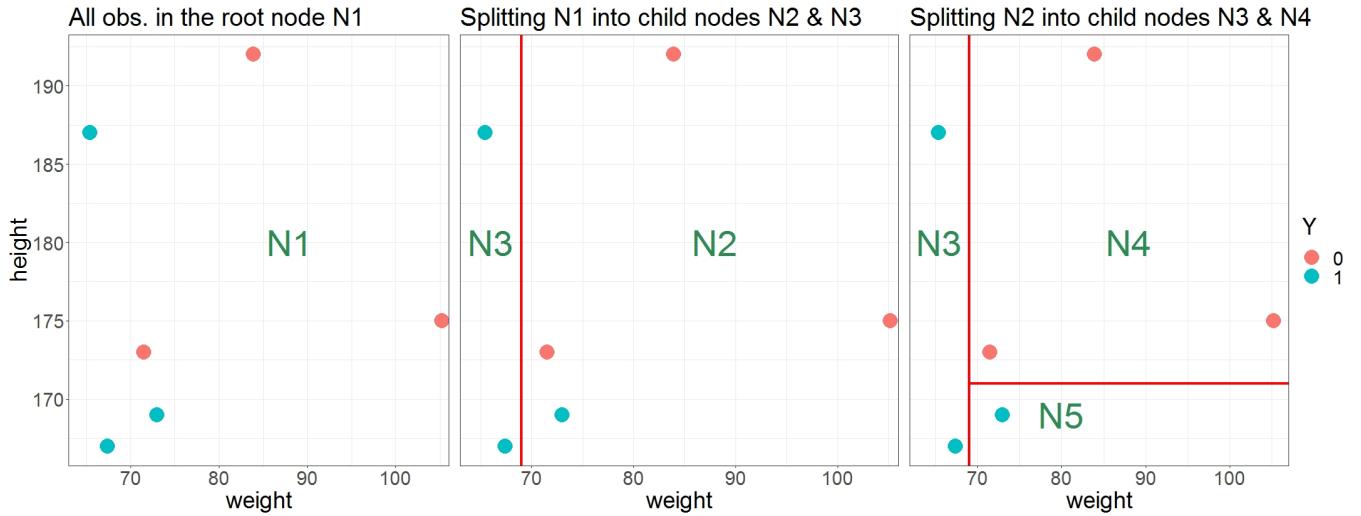


Figure 2: Recursive binary splitting of a decision tree on a two-dimensional feature space.

A very handy property of a decision tree consists of its natural graphical display, which makes it extremely easy to interpret - even for people without mathematical background. This visualisation is especially useful when the training data for the decision tree holds more than two covariates and can not be displayed as scatter plot [26].

The segmentation of the feature space from figure 2 is displayed as a graphical decision tree in figure 3. Each square in the figure represents a node of the decision tree. Each of these nodes displays the response class with the highest proportion (top), the distribution of the response classes (mid) and the fraction of observations they contain (bottom). The split variables and split values are displayed below each node - nodes without a split variable/value are so-called 'terminal nodes'. The prediction for a test observation with figure 3 is very easy and intuitive. The test observation is simply passed down the decision tree until it reaches a terminal node. This is shown for an observation with weight = 90 and height = 185. The first node splits on the variable 'weight' with the value 69. As the test observation has a weight ≥ 69 it is sent down to the left child node. The next node splits on the variable height with the value 171. As the test observation is taller than 171cm it is sent to the left child node. The observation is then in the node on the leftmost in the bottom of figure 3. This is a terminal node and can not be divided any further. The distribution of this node equals 100|0 and the prediction for the observations is, therefore, class 0 with a probability of 100%.

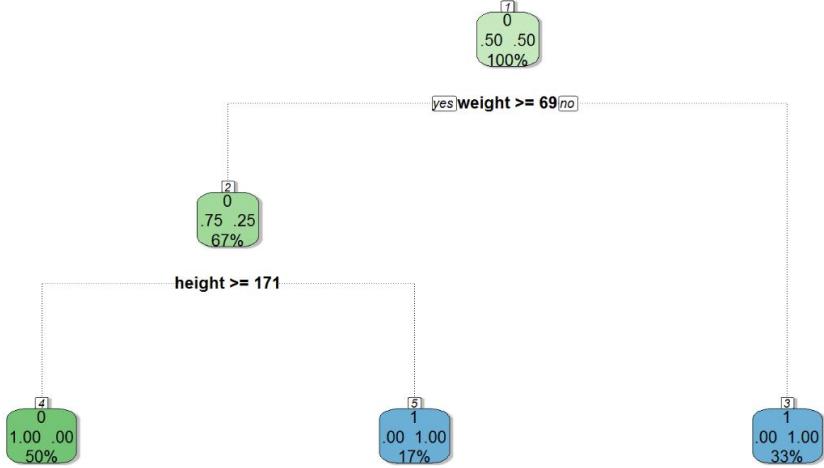


Figure 3: Corresponding decision tree for the segmented feature space on the rightmost plot in figure 2.

The complexity of a decision tree grows with the number of used splits and resulting terminal nodes [27]. The more complex a decision tree, the higher the chances of overfitting, but a tree with not enough complexity “might not capture the important structure[s]” [[26], p. 20]. So when should a tree stop with the binary partition of the feature space? There are multiple stopping criteria to control this, whereby the two most commonly used arguments are [26]:

- MinSplit:
“The minimum number of observations that must exist in a node in order for a split to be attempted” [[28], p. 22]
- Complexity:
“Split tree nodes only if the decrease in impurity due to splits exceeds some threshold” [[26], p. 20]

Both arguments have a huge impact on the complexity of a decision tree, as they control when the tree stops the partition of the feature space. The ‘MinSplit’ argument forces the tree to stop the partition, as soon as a potential parent node contains less than ‘MinSplit’ observations. The higher this argument is the earlier the tree has to stop growing and hence the less complex is the resulting tree. ‘Complexity’ on the other hand only allows splits that lead to a decrease of impurity of a given threshold when splitting the parent node N to N_1 and N_2 . The drawback of this argument is that it is rather short-sighted, as a “seemingly worthless split might lead to a very good split below” [[26], p. 20]. Hence the ‘MinSplit’ argument is preferred

over the 'Complexity' argument to control the complexity of a decision tree. The advantages of the decision tree method are numerous. It is easy to interpret, has no problems with outliers, captures interaction effects between features, handles categorical features and scales well with larger data [26]. Besides all these advantages, unfortunately, there is also a huge disadvantage. A decision tree is highly unstable meaning that "small changes in the data could lead to completely different splits, thus, to a completely different tree" [[27], p. 26]. Even the removing of a single observation/ feature from the training data can lead to a completely different decision tree.
The next chapter explains, how this alleged disadvantage of high instability of a decision tree is exploited by the random forest method to create better predictions based on multiple decision trees.

2.2.2 Random Forest Model

As already mentioned at the beginning of this chapter, the random forest model is an ensemble method that uses the decision tree as a base learner. The random forest model, therefore, consists of multiple decision trees. To meaningfully train these multiple decision trees, the random forest method uses a modified version of bagging that was originally proposed by Breiman in 1996 [29]. As bagging is an important component of the random forest method it is now explained in more detail.

To meaningfully train M base learners on a single data set, each base learner needs to be fit on a modified data set, else all resulting learners are completely identical. To generate a different data set for each of the M base learners, bagging - short for **Bootstrap Aggregation** - is applied to the original data. In the first step bootstrapping is applied. It is a "type of resampling where large numbers of [...] samples of the same size are repeatedly drawn, with replacement, from a single original sample" [30]. The bootstrapping therefore generates M different bootstrap samples of the original data and trains any base learner B on these M bootstrapped data sets. To obtain a prediction from these, each of M fitted base learners is asked for a prediction - $B_m(x)$. These M different predictions are then aggregated for a final prediction: $B(x) = \frac{1}{M} \sum_{i=1}^M B_m(x)$ [[31], p. 4]. Bagging works best for learners with a high variance - e.g. a decision tree - as it reduces the variance of the base learner and increases only the bias in return [31].

The random forest method uses a slight modification of the bagging algorithm to construct bootstrapped decorrelated decision trees [20]. To do so the random forest algorithm does not only fit each decision tree on a separate bootstrapped data set but decreases the correlation of these as well by randomly drawing 'mtry' features as possible split candidates at each split

point instead of having all ' p ' features as possible split candidates [31]. The standard value for 'mtry' with a categorical response class is $\lceil \sqrt{p} \rceil$, whereby p equals the number of covariates in the data. [32]. Hence at each node of a decision tree, only a subset of the available features are drawn as possible split variables. Therefore every single decision tree has a different set of possible split variables for each of their nodes. This modification of the original bagging algorithm ensures that the trees are grown more diversely and the resulting trees are less correlated as with the regular bagging algorithm. The modified bagging algorithm to fit a random forest is the following [[20], p. 588]:

Algorithm 1: Growing a random forest model

Input : $D \leftarrow$ data of n observations & p features
 $M \leftarrow$ number of trees in the forest
 $n_{min} \leftarrow$ 'MinSplit' argument of a decision tree
 $mtry \leftarrow$ number of variables to draw at each split

for $m \leftarrow 1$ **to** M **do**

- 1. Draw a bootstrap sample Z^* of size ' n ' from ' D ';
- 2. Grow a decision tree of the random forest, by recursively repeating the following steps for each terminal node of the tree, until the minimum node size n_{min} is reached;
 - 2.1 Randomly draw 'mtry' of the ' p ' available variables;
 - 2.2 Pick the best splitting point among the 'mtry' variables;
 - 2.3 Split the node into two daughter nodes;

The procedure to receive a prediction from a random forest model is the same as in the original bagging algorithm. The input x is passed to each of the decision trees in the random forest and each of these trees creates a prediction based on the input x - details in section 2.2.1. The final prediction in case of a categorical response can either be the average of all M predicted class probabilities or the label that was predicted by the majority of the trees.

2.2.3 OOB error

A very handy property of the random forest method is the so-called out-of-bag error (OOB error). The random forest model consists of multiple decision trees, whereby the data for each of these trees is obtained by drawing observations with replacement from the original data. For each tree, the average probability for an observation not to be drawn is ~ 0.37 [[31], p. 12]:

$$P(\text{Obs. not drawn}) = \left(1 - \frac{1}{e}\right)^n \xrightarrow{n \rightarrow \infty} \frac{1}{e} \approx 0.37 \quad (7)$$

- n : Amount of observations in the data

The remaining $\sim 37\%$ of available observations are not used to grow the decision tree and can hence be used to estimate its predictive performance - the so-called OOB error. Before explaining the OOB error, let's have a look at figure 4. The figure displays the M different decision trees of a random forest model that was originally supplied with data of n observations and p features. Under each tree the data used for growing is displayed - a pink background indicates that the observation was 'in-bag' and hence used in the training of the decision tree, while a grey background indicates that the observation is out-of-bag and was not used in the training of the decision tree. It should be noticed that the observations are drawn with replacement so that an observation can enter the in-bag samples more than once.

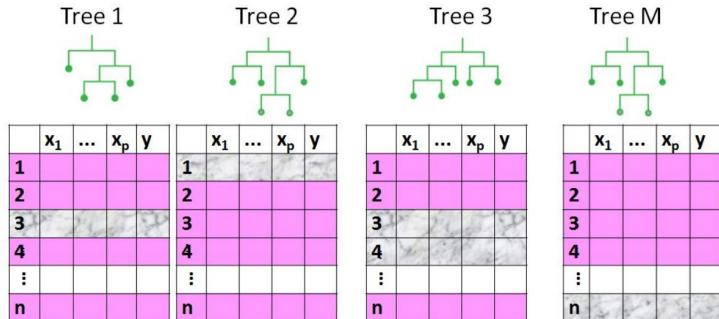


Figure 4: The data used to grow the M different decision trees of a random forest. Below each decision tree the in-bag observations are labelled in pink, while out-of-bag observations are labelled in grey [[31], p. 13].

To receive the OOB error of a random forest model, each of the M decision trees is asked for a prediction for the current observation i , but only if the observation i is an out-of-bag observation for the tree. This results in $\psi_i \leq M$ predictions for the observation i , whereby the final out-of-bag estimation for observation i equals the average of the ψ_i predictions. After receiving this out-of-bag prediction for all n observations, the final OOB error can be calculated. To compare the predicted classes and the true response class of the n observations any metric can be used - e.g. Accuracy, F-1

score. The OOB error “is almost identical to that obtained by N-fold cross validation” [[20], p. 593]. Therefore, unlike most other prediction models, the random forest can be fit and evaluated in one single step - an extremely handy property.

2.2.4 Variable importance

In most applications, not all feature variables are equally important and mostly only a few have a relevant influence. Therefore the property of variable importance in the random forest method has high practical usage. Even though the single decision trees of a random forest model are highly interpretable, the random forest model itself “lose[s] this important feature, and must, therefore, be interpreted in a different way” [[20], p. 367].

One possibility to measure the variable importance in a random forest model is based on the permutations of the out-of-bag observations. All out-of-bag observations of a decision tree T_m are passed to their tree for a prediction and the accuracy of the decision tree is recorded - acc_m , without permutation. To obtain the importance of a variable x_l , all out-of-bag observations of the decision tree T_m are permuted in the variable x_l , such that all out-of-bag observations receive a different value for the variable x_l . The permuted out-of-bag observations are then passed to the decision tree T_m and the accuracy of the decision tree is recorded again - acc_m , with permutation in x_l . The difference between the regular OOB accuracy - acc_m , without permutation - and the OOB accuracy with permuted variable x_l - acc_m , with permutation in x_l - is used as measure for the importance of the l -th variable in the decision tree T_m . The average importance of the l -th variable overall M decision trees equals the variable importance for x_l for the whole random forest model [31].

This technique to access the importance for the different variables is displayed in figure 5 for the variable x_1 . For the decision trees 1 and M the data used to train these is displayed below. A grey background marks the out-of-bag observations. Based on these observations the out-of-bag accuracy can be calculated for each of the M trees. For each tree this results in acc_m , without permutation. Then the values of the variable x_1 are permuted for the out-of-bag observations for each decision tree. Following the out-of-bag accuracy is calculated with the permuted variable x_1 resulting in acc_m , with permutation in x_1 . The difference $diff_m$ between acc_m , with permutation in x_1 and acc_m , without permutation represents the importance of variable x_1 in the decision tree T_m . The final importance of variable x_1 then equals the average over all these differences [[31], p. 16]: $\frac{1}{M} \sum_{i=1}^M diff_i$

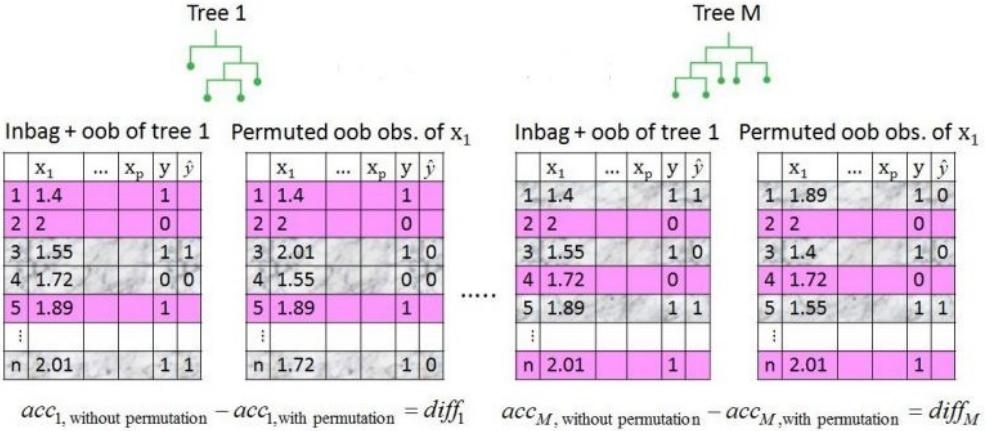


Figure 5: Calculation of the variable importance of x_1 for a random forest model consisting of M decision trees [[31], p. 16].

2.3 Complete-Case Approach

In this section, the first baseline approach to handle data with block-wise missingness is explained - the so-called 'Complete-Case' approach. This approach does not modify the random forest model itself, but processes the training data, such that it does not contain any missing values afterwards. This has the advantage that every prediction model - e.g. a random forest model - can be regularly trained on the processed data and the disadvantage of not using all available folds and feature-blocks. Therefore it is a rather simple approach and shall serve as a first baseline. The results from this first baseline approach are a hurdle to overcome for the more sophisticated approaches from the sections 2.5 - 2.7.

Let's have a look at the approach itself. As block-wise missingness can affect the test data as well as the training data the test observations may be missing feature-blocks - even if these are available in the training data. The 'Complete-Case' approach removes all folds from the training data that miss at least one of the available feature-blocks from the test data. The feature-blocks of the training data that are not available in test data are removed as well. After the processing, the training data only consists of the feature-blocks that are available in the test data with observations that were completely observed in these blocks. Based on this processed training data a random forest can be trained regularly. The prediction on the test observations with such a fitted model can then be done completely regular, as the model does not use any split variables that are not available for the test observations, as well as the test observations do not contain any features

the model has not been trained with. To make the processing of the training data easier to understand two examples are shown in figure 6. In these examples, the concatenated data with block-wise missingness from figure 1 is used as an exemplary training data:

1. Example: This example is displayed in figure 6. The test-set is shown in the top of the figure and only has two observed feature-blocks - 'Clinical' and CNV'. The train-set is displayed below and consists of four feature-blocks and three unique folds. The 'Complete-Case' approach processes the training data, such that it removes all observations that miss at least one of the available feature-blocks of the test-set. Therefore only observations from the fold 'Hospital 1' can be used, as the observations from the other folds either miss the feature-block 'Clinical' or 'CNV'. The fold and feature-blocks that can be used for the model fitting are marked with a green box. On this processed data a regular random forest model can be trained and used to create predictions for the test observations then. The processed training data contains two feature-blocks and two folds less than the original training data, as these were removed by the processing of the 'Complete-Case' approach.

	Y	Clinical	CNV		
<u>Test Set</u>	?	✓	✓		
	Y	Clinical	CNV	RNA	miRNA
<u>Processed Data</u>	HOSPITAL 1	✓	✓	✓	✗
	HOSPITAL 2	✓	✓	✗	✓
	HOSPITAL 3	✓	✗	✓	✗

Figure 6: The 'Complete Case' processing of the training data according to the available feature-blocks in the test-set.

2. Example: This example is displayed in figure 7. The available train-set is displayed at the bottom of the figure and consists of four feature-blocks, while the test-set is only observed in the feature-block 'CNV'. The 'Complete-Case' approach removes all folds from the train-set that do not have an observed 'CNV' feature-block. Therefore only the observations from the folds 'Hospital 1' and 'Hospital 3' can be used as training data. For these folds, only the feature-block 'CNV' can be used for training and the other feature-blocks need to be discarded, as they are missing in the test-set. The folds and feature-block that can be used for the model fitting are marked with a green box. On this data, a regular random forest model can be trained and used to create predictions for the test observations then. Much of the original training data is discarded by the 'Complete-Case' approach.

<u>Test Set</u>		Y	CNV		
		?	✓		
<u>Processed Data</u>	HOSPITAL 1	✓	✓	✓	✗
	HOSPITAL 2	✓	✓	✗	✓
	HOSPITAL 3	✓	✗	✓	✓

Figure 7: The 'Complete Case' processing of the training data according to the available feature-blocks in the test-set.

Besides the generous discarding of training data, the method has another disadvantage. As the 'Complete-Case' approach removes all observations from the train-set that miss at least one of the available feature-blocks of the test-set, there may be no training observations left after the processing of the training-set. In situations like this the 'Complete-Case' approach can not provide predictions for the test-set.

In summary, the 'Complete Case' approach removes all observations that miss at least one of the observed feature-blocks in the test-set. Also, all feature-blocks from the training data that are not available in the test-set are removed. This data processing approach can discard a big part of the original training data and hence it does not handle the data very efficiently.

2.4 Single-Block Approach

The second baseline approach to handle data with block-wise missingness is the 'Single-Block' approach. As well as the 'Complete-Case' approach, it does not modify the random forest model itself but processes the training data, such that it does not contain any missing data afterwards. As well as the 'Complete-Case' approach, the 'Single-Block' approach discards much of the available training data. As this approach is rather naive it is the second baseline approach and shall serve as another lower limit for the performances of the more sophisticated approaches from the coming sections 2.5 - 2.7.

As the name of the approach already suggests, it only uses a single feature-block to train a random forest model and predicts on the test-set then. To create predictions on the test-set the model must be trained with a feature-block that is also available in the test-set. Else the fitted model can not predict on the test-set, as it uses split variables that are not available in the test-set. Hence the single feature-blocks from the training data that can be

used to train a model depend on the observed feature-blocks in the test-set. The concept of this approach is now explained with the example in figure 8. The training data in this example has already been introduced in section 2.1 and has been used as an example in the previous section as well:

Example: The test-set for this example is displayed in top of figure 8 and contains two different feature-blocks - 'Clinical' and 'CNV'. The training data consists of four different feature-blocks and three different folds in total. The 'Single-Block' approach processes the training data in multiple ways to get rid of the block-wise missingness in the train-set. For each available feature-block in the test-set, it is checked, whether the train-set involves the feature-block as well. For each feature-block that the test and train-set have in common, a separate random forest model is fitted and used to predict the outcome of the test observations. In the current example, it is firstly checked, whether the training data involves a 'Clinical' or a 'CNV' feature-block. In this example, the training data involves both feature-blocks of the test-set. For each of the feature-blocks, the test and train-set have in common a separate processed data set is created.

		Y	Clinical	CNV	
<u>Test Set</u>		?	✓	✓	
<u>Processed Data 1</u>	HOSPITAL 1	✓	✓	✓	✗
	HOSPITAL 2	✓	✓	✗	✓
	HOSPITAL 3	✓	✗	✓	✗

		Y	Clinical	CNV	RNA	miRNA
<u>Test Set</u>		?	✓	✓		
<u>Processed Data 2</u>	HOSPITAL 1	✓	✓	✓	✗	✗
	HOSPITAL 2	✓	✓	✗	✓	✗
	HOSPITAL 3	✓	✗	✓	✗	✓

Figure 8: 'Single-Block' processing of the training data so a random forest model can be regularly trained with each of these processed data sets.

Processed Data 1: As the test- and train-set have the feature-block 'Clinical' in common, the first processed training data only consists of the response Y and the feature-block 'Clinical' for the observations that have been observed in this block. This subset of the data is displayed in the middle of figure 8 and marked with a green box. Based on this subset, a random forest model can be fit regularly and used to create predictions for the test-set - for the predictions, only the features from the 'Clinical' feature-block are used.

Processed Data 2: As the test- and train-set also have the feature-block 'CNV' in common, another processed train-set is created. The processed training data then only consists of the response Y and the feature-block 'CNV' for the observations that were observed in the 'CNV' block. This subset of the data is displayed in the bottom of figure 8 and marked with a green box. Based on this data, a random forest model can be regularly fit and used to create predictions for the test-set. For the predictions on the test-set, only the features from the 'CNV' feature-block are used.

Predictions: As the processing of the training data with the 'Single-Block' approach results in two processed train-sets, this approach consists of two different fitted models then. One random forest model that was fitted on the 'Clinical' feature-block and one that was fitted on the 'CNV' feature-block. Both of the fitted models can create predictions for the test-set based on the features they have been trained with. The 'Single-Block' approach can therefore result in multiple predictions for the observations in the test-set.

In summary, the 'Single-Block' approach creates an own processed train-set for each of the feature-blocks the test and train-set have in common. Each of the resulting processed train-sets consist of only one single feature-block and do not contain any missing data, as the observations with missing values are removed. On each of these processed train-sets a random forest model can be trained and used for predictions on the test-set. As the 'Complete-Case' approach, the 'Single-Block' does not handle the data very efficiently.

2.5 Imputation Approach

This section introduces an approach that deals with block-wise missingness by imputing the missing values - the so-called 'Imputation' approach. Other than the 'Complete-Case' and 'Single-Block' approach, the 'Imputation' approach does not discard any of the available training data and hence uses the data more efficiently. After the missing values in the training data have been imputed, any prediction model can be fit on this data in a regular way and provide predictions for a test observation based on a single feature-block or based on multiple different feature-blocks.

"Many established [prediction] methods [...] require fully observed datasets without any missing values" [33], p. 112] - in data with block-wise missingness this requirement is clearly not fulfilled. The idea to deal with this missingness by imputing the missing values seems natural. The data sets do not contain any missing values after the imputation, such that a prediction method can be fitted regularly then. There are two big drawbacks when imputing missing values in multi-omics data. First, multi-omics data with block-

wise missingness can consist of “many missing values making imputation techniques unreliable” [18]. Second, if the data is a concatenation of data sets from different sources, the imputation is “performed across different, potentially heterogeneous data sets” [18] - another reason for the unreliability of the imputation. Despite these disadvantages, the ‘Imputation’ approach is still worth being compared to the other approaches in this study.

Firstly a suitable imputation approach has to be found. This is not trivial, as multi-omics data usually do not only have fewer observations than features but also a mixture of continuous and categorical variables as features [33]. Furthermore “such datasets often contain complex interactions and non-linear relation structures which are notoriously hard to capture” [[33], p. 112]. The ‘k nearest neighbours’ imputation method [34] requires at least one complete case observation, an assumption that is not always true for multi-omics data with block-wise missingness. The ‘Amelia’ imputation [35] “assumes the data is distributed multivariate normal” [[36], p. 7]. Most variables in multi-omics data do not fulfil this assumption and need a transformation to fulfil it - a not very handy property with such high-dimensional data [36]. There are more imputation methods, but most of these “are restricted to one type of variable” [[33], p. 112] or “make assumptions about the distribution of the data” [[33], p. 112]. An imputation method that can handle any type of input data and makes as few as possible assumptions about the data is based on the random forest method - the so-called ‘MissForest’ [33]. This imputation approach needs “no tuning parameter, and hence it is easy to use and needs no prior knowledge about the data” [[33], p. 113]. Additionally it was shown that the ‘MissForest’ approach is competitive to the ‘k nearest neighbours’ and ‘MICE’ imputation [33]. Furthermore the ‘MissForest’ imputation method can handle “mixed-type data and is known to perform very well under barren conditions like high dimensions, complex interactions and non-linear data structures” [[33], p. 113]. Because of all these mentioned advantages, the ‘MissForest’ method is used as the imputation method in this thesis. The imputation approach is explained in more detail in the following paragraph.

MissForest: The ‘MissForest’ imputation method was proposed by Stekhoven and Bühlmann in 2012 [33] and builds upon the random forest method. For the imputation of missing values, a random forest is trained on the observed parts of the data and then used to predict the missing values in the data. For the explanation, assume D to be a $n \times p$ dimensional data set with missing values in the diverse variables. For the imputation of a variable X_j with missing values at the entries $i_{mis}^{(j)} \subseteq \{1, \dots, n\}$ the data set D is separated into four parts [33]:

- 1** y_{obs}^j : Observed values of variable X_j
- 2** y_{mis}^j : Missing values of variable X_j
- 3** x_{obs}^j : Variables other than X_j with observations $i_{obs}^{(j)} = \{1, \dots, n\} \setminus i_{mis}^{(j)}$
typically not fully observed as the index $i_{obs}^{(j)}$ corresponds to the observed values in X_j
- 4** x_{mis}^j : Variables other than X_j with observations in $i_{mis}^{(j)}$
typically not completely missing as the index $i_{obs}^{(j)}$ corresponds to the observed values in X_j

The imputation procedure is explained and shown in algorithm 2 - algorithm and explanation are based on [33]:

In the beginning, all missing values in the data set D are imputed with an initial guess - e.g. mean imputation. In the next step, the variables with missing values are ordered accordingly to the number of missing values - starting with the variable with the fewest missing values. For each of these variables a random forest model is fitted with the response y_{obs}^j and x_{obs}^j as predictor variables. With this fitted random forest model, the missing values y_{mis}^j are imputed by the predictions of the random forest model based on x_{mis}^j . This procedure is repeated for a fixed amount of iterations or until the stopping criterion γ is met.

Algorithm 2: Imputation procedure of the 'MissForest'

Input : $D \leftarrow$ data of n observations & p features
 $\gamma \leftarrow$ stopping criterion

1. Make initial guess for missing values - e.g. mean imputation;
2. $k \leftarrow$ vector of sorted indices of the variables in D w.r.t.
increasing amount of missing values;
- while** not γ **do**
 1. $D_{old}^{IMP} \leftarrow$ store previously imputed data;
 - for** $j \in k$ **do**
 1. Fit a random forest: $y_{obs}^s \sim x_{obs}^s$;
 2. Predict: y_{mis}^s using x_{obs}^s ;
 3. $D_{new}^{IMP} \leftarrow$ update imputed matrix, using predictions y_{mis}^s ;
 2. Update γ ;
3. Return the imputed data set D^{IMP} ;

The stopping criterion γ measures the difference between the newly imputed data matrix D_{new}^{IMP} and the previous imputed data D_{old}^{IMP} . For continuous variables N the difference is calculated via [[33], p. 113]:

$$\Delta_{\mathbf{N}} = \frac{\sum_{j \in \mathbf{N}} (D_{new}^{IMP} - D_{old}^{IMP})^2}{\sum_{j \in \mathbf{N}} (D_{new}^{IMP})^2} \quad (8)$$

And for categorical variables \mathbf{F} it is calculated via [[33], p. 113]:

$$\Delta_{\mathbf{F}} = \frac{\sum_{j \in \mathbf{F}} \sum_{i=1}^n \mathbb{1}_{D_{new}^{IMP} \neq D_{old}^{IMP}}}{\#NA} \quad (9)$$

- #NA: Number of missing values in the categorical variables

The stopping criterion γ is fulfilled as soon as “the difference between the newly imputed data [...] and the previous one increases for the first time with respect to both variables” [[33], p. 113]. An alternative to the stopping criterion γ is a fixed amount of iterations for the imputation.

Predictions: Now that has been clarified how the ‘MissForest’ imputation works, the procedure of the ‘Imputation’ approach can be explained in more detail based on the example in figure 9. The training data has already been introduced in the section 2.1 and was used as example in the previous sections as well.

In the top of the figure the train-set with block-wise missingness is displayed. The very first step of the ‘Imputation’ approach is to impute the missing values in the train-set with the ‘MissForest’ method. After the imputation has taken place, the train-set does not contain any more missing values - displayed right below the original training data. As this data has no missing values at all, a random forest model can be fit completely regularly. But as the test-set might miss feature-blocks, the random forest model is only trained with the feature-blocks that the train- and test-set have in common. Else it might be possible that the fitted random forest model can not create predictions for the test-set, as it uses split variables that are not available for the test-set. Therefore all feature-blocks that are not available for the test-set have to be removed. Hence the imputed train-set that can actually be used to train a random forest model only consists of the feature-blocks that are also in the test-set then. Based on this usable train-set a random forest model can be fit in a regular way and can provide predictions for the test-set then.

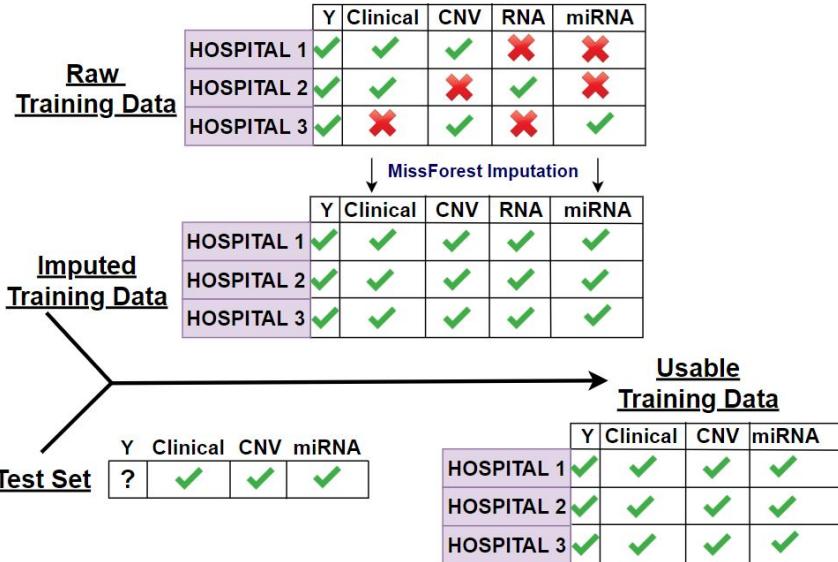


Figure 9: 'Imputation' approach to deal with block-wise missingness

Summary: With the 'Imputation' approach, the missing values in the train-set with block-wise missingness are imputed by the 'MissForest' method. After this imputation step, the train-set does not consist of missing values anymore. Based on the feature-blocks the train- and test-set have in common a regular random forest model can be trained. This fitted random forest model can then provide predictions for the test-set.

2.6 Block-wise Approach

This section introduces the 'block-wise' approach that was originally proposed by Krautenbacher in 2018 [19]. Other than the approaches from the previous sections 2.3 - 2.5 this approach does not modify the training data, but the random forest model itself. The 'block-wise' approach can directly handle block-wise missingness in the training data and does not need to process the data at all. Therefore it uses the available training data efficiently and does not discard any observations or feature-blocks. Furthermore, a 'block-wise' fitted random forest is flexibly applicable and can provide predictions for a test observation with a single feature-block, but also for a test observation with multiple feature-blocks.

As the name of the approach already suggests, the random forest model is fitted in a 'block-wise' manner to the training data. In the beginning, all available feature-blocks of the training data are extracted. On each of these

feature-blocks, a random forest model is separately fitted. This enables “all observations per [feature-block] [...] to be utilised for learning” [[19], p. 102] and no observation or feature-block has to be left out. With the ‘block-wise’ approach as many separate random forest models are fitted as the training data has feature-blocks. To create a prediction for a test observation then, each block-wise fitted random forest model is asked for a prediction. The models that were fitted on a feature-block that is not available for the test observation can not create a prediction, as these use split variables that are not available for the test observation. The remaining random forest models can create a prediction for the test observation by using the features from the test observation the models have originally been trained with. The predictions from the separate block-wise fitted models can then be aggregated to obtain a final prediction. The separate model fitting is explained in more detail with the example in figure 10. The training data in this example has already been introduced in section 2.1 and has been used as an example in the previous sections as well:

Model Fitting: The training data is displayed in the top of figure 10 and consists of four feature-blocks and three folds. To fit a separate random forest model on each feature-block, the training data needs to be split, such that each feature-block can be used to train a random forest model. This is done by merging each feature-block and the response Y to a separate train-set. In figure 10 these separate train-sets are displayed as data frames with a green background below the original training data. From each of these separate train-sets, all folds that contain missing values in the corresponding feature-block are removed - e.g. in the separate ‘Clinical’ train-set all observations from ‘Hospital 3’ had to be removed, as this hospital did not collect any clinical data. The folds that had to be removed from these separate train-sets are marked with a red horizontal line, while the usable folds are marked with a green tick. Based on each of these four different train-sets a random forest model can be trained. This results in four distinct random forest models in total - $RF_{Clinical}$, RF_{CNV} , RF_{RNA} and RF_{miRNA} . Each of these models has been trained with a single feature-block only - e.g. RF_{RNA} was only trained with the feature-block ‘RNA’.

The ‘block-wise’ approach trains the separate random forest models on the distinct feature-blocks in the training data and has as many separate random forest models as the training data consists of distinct feature-blocks. But how can these models be used to create a final prediction? As already mentioned, the block-wise predictions from the different random forest models need to be aggregated for a final prediction. This is explained in the following paragraph based on the example in figure 11.

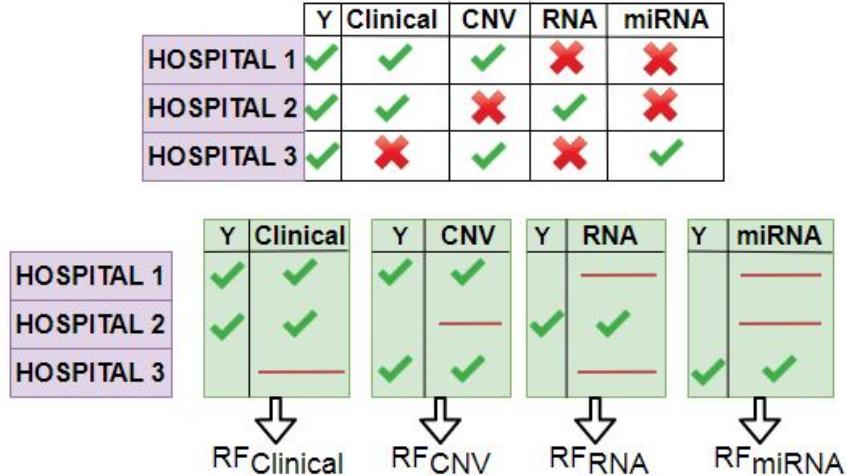


Figure 10: Training of random forest models with the 'block-wise' approach.

Predictions: Assume that the four block-wise fitted random forest models from figure 10 can be used for the example in figure 11. The test-set is displayed at the top of figure 11. For the observations in this test-set, the outcome 'Y' needs to be predicted. Other than the training data from figure 10, the test-set only contains three feature-blocks and misses the 'CNV' feature-block from the training data. To create predictions for the observations in the test-set, each of the four block-wise fitted random forest models is asked to create predictions for the test observations. As the test-set contains the feature-blocks 'Clinical', 'RNA' and 'miRNA' the corresponding random forest models $RF_{Clinical}$, RF_{RNA} and RF_{miRNA} can be used to predict on the test-set. The random forest model RF_{CNV} can not create predictions on this test-set, as the feature-block, 'CNV' is not available. Each of the three block-wise fitted models $RF_{Clinical}$, RF_{RNA} and RF_{miRNA} create a prediction for each observation in the test-set, by only using the variables from the feature-block the models have originally been trained with. Therefore each model creates a prediction for each observation in the test-set, such that there are three predicted outcomes for each observation - $\text{Preds}_{Clinical}$, Preds_{RNA} and Preds_{miRNA} . These predictions represent the probabilities for each of the possible response classes. The final prediction for the target variable 'Y' equals a weighted average of these predictions.

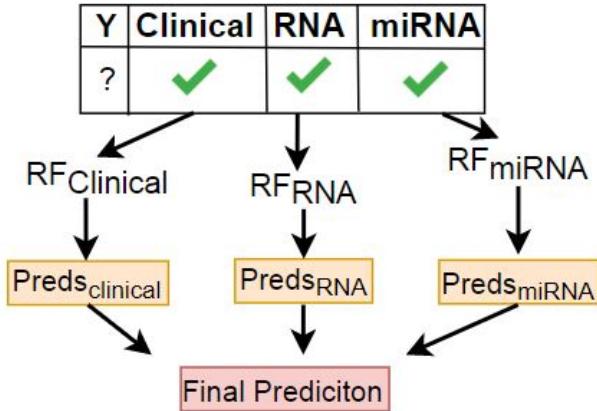


Figure 11: Prediction on test data with the 'block-wise' approach. The fitting of the random forest models was described with figure 10.

To create a meaningful weighted average of the different block-wise predictions, different techniques can be applied. The simplest method is giving each block-wise fitted model the same weight and return the plain average over all block-wise predictions. But as the block-wise fitted models have been trained on different feature-blocks this might not always be optimal, as the models might differ strongly in their prediction quality. To make this clear let us assume that the feature-block 'miRNA' is not related at all to the outcome 'Y', while the feature-block 'Clinical' is strongly related to it. In this case, it can be assumed that the predictions based on the 'miRNA' feature-block are worse than the predictions based on the 'Clinical' feature-block. Therefore it would be meaningful to put a higher weight on the predictions from the $RF_{Clinical}$ model than on the predictions from the RF_{miRNA} model. Usually, the true strength of the relation between a feature-block and the target variable is unknown. Therefore the predictive quality of the different feature-blocks needs to be estimated. This can be done with the out-of-bag error of the block-wise fitted models. For each block-wise fitted random forest model the predicted classes for all out-of-bag observations are generated - see chapter 2.2.3 for details. Based on the predicted outcomes and the true response values any metric can be calculated to judge the predictive performance of a block-wise fitted random forest model then. In this thesis either the accuracy or F-1 score is used as metric to judge the predictive quality - details on the metrics in chapter 3.1.1. The better the out-of-bag accuracy/F-1 score of a block-wise fitted model, the higher the estimated predictive quality of the model. The higher the predictive quality of a model, the higher its weight and therefore the higher its contribution to the final prediction. The reason to use the F-1 score beside the accuracy is that the F-1 score is

sensitive to class imbalances in the target variable, while the accuracy only represents the fraction of correctly classified observations.

Let us have a look at a minimalist example to make the idea of the weighted average clearer. Assume the block-wise fitted random forest models from figure 11 have the following out-of-bag accuracy and predicted probabilities for the observation i :

$$\begin{array}{ll} OOB_{Acc}(RF_{Clinical}) = 0.67 & \text{Preds}_{Clinical}(\text{Obs}_i) = 0.19 \\ OOB_{Acc}(RF_{RNA}) = 0.86 & \text{Preds}_{RNA}(\text{Obs}_i) = 0.33 \\ OOB_{Acc}(RF_{miRNA}) = 0.21 & \text{Preds}_{miRNA}(\text{Obs}_i) = 0.99 \end{array}$$

The predictions of the models represent the probability for a positive response, such that all probabilities < 0.5 result in a predicted negative class, while probabilities ≥ 0.5 result in a positive predicted response class. The true response class for the observation i is negative, as well as the predictions of $RF_{Clinical}$ and RF_{RNA} . Only the RF_{miRNA} model predicts the response for observation i wrongly as positive. When calculating the plain average of all these predicted probabilities it results in 0.503. Therefore the final predicted probability is ≥ 0.5 and the predicted class is the positive class - which is wrong for observation i . If we use the out-of-bag accuracy of the models as weights for a weighted average the the final predicted probability is $0.355 < 0.5$ and therefore the predicted class is the negative class - which is correct for observation i . So instead of giving all block-wise predictions the same weight, the predictive power of the single feature-blocks can be estimated with any out-of-bag metric and used to weight the block-wise predictions. The better the out-of-bag metric, the higher the weight for the predictions from the given feature-block.

In summary: With the 'block-wise' approach a separate random forest model is fitted on each feature-block of the training data. For a prediction on a test observation, all block-wise fitted models are asked for a prediction. Only those models that have been trained with a feature-block that is available for the test observation can create a prediction. These predictions can then be averaged in a weighted/ unweighted way to create a final prediction for the test observation.

2.7 Fold-wise Approach

This section introduces the 'fold-wise' approach that was originally proposed by Hornung et al. [18]. This approach was originally not proposed to deal with block-wise missingness in multi-omics data, but to deal with multiple train-

sets with the same target variable and different partly overlapping feature-blocks. Nevertheless, this approach can also deal with block-wise missingness in multi-omics data. Other than the approaches from the sections 2.3 - 2.5 this approach does not modify the training data, but the random forest model itself. The 'fold-wise' approach can directly handle block-wise missingness in the training data and does not need to process the data at all. Therefore it does not discard any of the available observations or feature-blocks and uses the available training data efficiently. Furthermore a 'fold-wise' fitted random forest is flexibly applicable and can "provide predictions for test data that do not feature all covariates available from training" [18].

As the name of the approach already suggests, the random forest model is fitted in a 'fold-wise' manner to the training data. In the beginning, all available folds of the training data are extracted. On each of these folds, a random forest model is then separately fitted. This results in as many fold-wise fitted random forest models as the training data has folds. As the different folds of the training data usually consist of multiple feature-blocks, each fold-wise fitted random forest model generally incorporates the covariates from multiple different feature-blocks. To receive a prediction on a test data only "the subsets of covariates included in the test data that are also included in at least one of the" [18] train-sets is used. The prediction of a single fold-wise fitted random forest model is then obtained as follows:

- (1) Remove all trees from the fold-wise fitted random forest that use a split variable as the first split that is not available for the test observation. These trees can not even split the test data once, as the first split variable is not available for the test observation. Therefore these decision trees are of no value for the given test observation.
- (2) For each remaining decision tree "follow each branch of the tree and cut the branch as soon as a covariate is used for splitting that is not available" [18] for the test data. This process of cutting branches is called 'pruning'. A node that had to be pruned is a new terminal node of the decision tree then. After these two steps have been applied to the fold-wise fitted model the predictions can be obtained as for a standard random forest model. The predictions from the separate fold-wise fitted models can then be aggregated to obtain a final prediction. The fold-wise model fitting is explained in more detail with the example in figure 12. The training data in this example has already been introduced in section 2.1 and has been used as an example in the previous sections as well:

Model Fitting: The training data is displayed at the top of figure 12 and consists of four feature-blocks and three folds. To fit a separate random forest model on each fold, the training data needs to be split, such that each fold can be used to train a random forest model. This is done by merging the

feature-blocks of a fold and the corresponding response Y to a separate train-set. The feature-blocks that were not observed for a certain fold are removed from the fold-wise training data - e.g. the feature-blocks 'RNA' and 'MIRNA' were not observed for the fold 'Hospital 1' and had to be removed from the training data of the fold. In figure 12 these separate train-sets are displayed as data frames with a green background below the original training data. Based on each of these three different train-sets a random forest model can be trained. This results in three random forest models in total - $RF_{Hospital1}$, $RF_{Hospital2}$ and $RF_{Hospital3}$. Each of these models has only been trained with the observed feature-blocks of the different folds - e.g. $RF_{Hospital1}$ was trained with the feature-blocks 'Clinical' and 'CNV'.

	Y	Clinical	CNV	RNA	miRNA
HOSPITAL 1	✓	✓	✓	✗	✗
HOSPITAL 2	✓	✓	✗	✓	✗
HOSPITAL 3	✓	✗	✓	✗	✓

	Y	Clinical	CNV	
HOSPITAL 1	✓	✓	✓	→ $RF_{Hospital1}$

	Y	Clinical	RNA	
HOSPITAL 2	✓	✓	✓	→ $RF_{Hospital2}$

	Y	CNV	miRNA	
HOSPITAL 3	✓	✓	✓	→ $RF_{Hospital3}$

Figure 12: Training of random forest models with the 'fold-wise' approach.

The 'fold-wise' approach trains the separate random forest models on the distinct folds of the training data and consists of as many separate random forest models as the training data consists of unique folds. But how can these models be used to create a prediction? As already mentioned, the fold-wise predictions from the different random forest models need to be aggregated for a final prediction. To receive a prediction from a fold-wise fitted random forest model the single decision trees of such a model might be pruned. Before explaining the aggregation of the fold-wise predictions it is important to understand the pruning process. It is explained in the following paragraph with the help of figure 13:

Pruning: Pruning describes a process applied to a decision tree to avoid overfitting. But it can also be applied to a decision tree if it contains split variables that are not available for a test observation for which a prediction is asked for. The latter idea is used in this 'fold-wise' approach and explained in more detail with the help of figure 13. On the left of the figure, the original decision tree from figure 3 can be seen. It was grown based on the two feature variables 'weight' and 'height'. To obtain a prediction the observation is simply passed down the tree until it reaches a terminal node. The predicted probabilities equal the distribution of the target variable in the terminal node. But how can this decision tree be used to predict an observation with an unknown 'height'? To receive such a prediction the original decision tree has to be pruned. For this, all nodes that split with the variable 'height' needs to be cut off. This is displayed on the right side of figure 13. The scissors indicate the pruning at the node that uses 'height' as a split variable - this node is a terminal node then. The pruned tree has one terminal node less than the original decision tree and can create predictions for observations without a 'height' variable, as the pruned decision tree does not use this variable as split variable anymore.

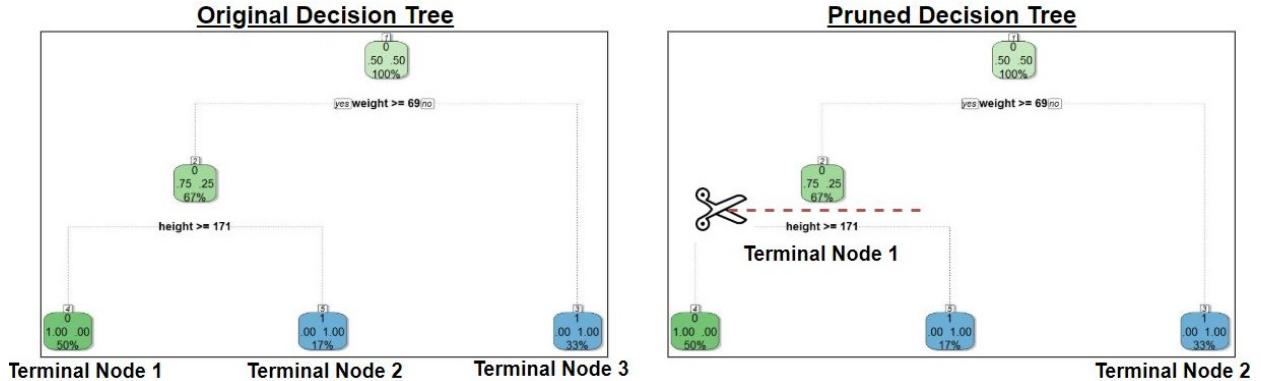


Figure 13: The pruning of a single decision tree. The decision tree was originally introduced in figure 3

The process of receiving a final prediction for an observation based on the predicted classes from multiple fold-wise fitted random forest models is explained in the next paragraph based on the example in figure 14.

Predictions: Assume that the three fold-wise fitted random forest models from figure 12 can be used for the example in figure 14. The test-set is displayed at the leftmost of figure 14, whereby the outcome 'Y' needs to be predicted. Other than the training data from figure 12, the test-set only contains three feature-blocks and misses the 'CNV' block. To

create predictions for the observations in the test-set the three fold-wise fitted random forest models from figure 12 can be used. Each of these models is asked for a prediction. As $RF_{Hospital2}$ was only trained on feature-blocks that are also available in the test-set - 'Clinical' and 'RNA' - no tree needs to be pruned, as all of the used split variables in this random forest model are available for the test-set. The prediction on the test-set with $RF_{Hospital2}$ is therefore completely regular. The fold-wise fitted random forest models $RF_{Hospital1}$ and $RF_{Hospital3}$ were both trained under the inclusion of the feature-block 'CNV'. This feature-block is not available for the test observations from figure 14. Therefore the single decision trees in $RF_{Hospital1}$ and $RF_{Hospital3}$ need to be pruned, as these trees could contain nodes with split variables that are not available for the test observations. Firstly all decision trees of these models that use a 'CNV' covariate as the first split variable have to be removed, as these trees can not even partition the test data once. Secondly, all remaining trees are pruned as explained in the paragraph before. After applying these two steps to the models $RF_{Hospital1}$ and $RF_{Hospital3}$, the predictions for the test observations can be obtained "as in the case of a standard" [14] random forest model. In the end, each fold-wise fitted model creates a prediction for each observation in the test-set, such that there are three predicted outcomes for each observation - $Preds_{Hospital1}$, $Preds_{Hospital2}$ and $Preds_{Hospital3}$. These predictions represent the probabilities for each of the possible response classes. The final predictions for the target variable 'Y' equal a weighted average of these predictions then.

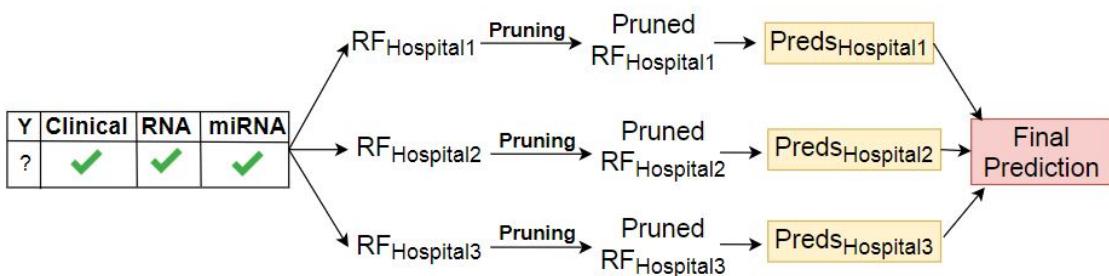


Figure 14: The prediction on test data with the 'fold-wise' approach. The training of the models was described with figure 12.

To create a meaningful weighted average of the different fold-wise predictions, different techniques can be applied. The simplest method is giving each fold-wise fitted model the same weight and return the plain average over all the fold-wise predictions. This might not always be optimal, as the fold-wise fitted random forest models were trained with different combina-

tions of feature-blocks and might differ in their predictive quality. As for the 'block-wise' approach from section 2.6 the predictive quality of the different prediction models can be estimated with an out-of-bag metric - e.g. accuracy or F-1 score. The out-of-bag metrics of the fold-wise fitted random forest models can then be used to weight the predictions of the different models. The higher the out-of-bag metric for a model, the higher the contribution of the model to the final prediction. There is only one difference in the out-of-bag calculation between the block- and fold-wise approach. As the fold-wise fitted random forest models might be pruned - depending on the test data. The out-of-bag predictions are generated with the pruned trees of the random forest then. This is meaningful, as pruning might reduce the predictive power of a model and we want to obtain a realistic estimation of the predictive power of a random forest model.

In summary: The fold-wise approach fits a separate random forest model on each fold of the training data. Depending on the available feature-blocks in the test-set, the fold-wise fitted random forest models might be pruned. After the pruning process, each fold-wise fitted model can generate predictions for the test-set. These predictions can then be averaged in a weighted/unweighted way to create final predictions for the test-set.

3 Benchmark Experiments

This section deals with the benchmark experiment for the comparison of the predictive performance of different approaches on data with block-wise missingness. It is not expected that such comparison experiments “result [in] an absolute truth applicable to all situations” [[37], p. 14f], but with enough different data sets and sufficient objective evaluation criteria general trends can be determined [37].

In the beginning, the different metrics used in this thesis are introduced and defined. Afterwards, it is explained how the predictive performance of an approach can be estimated. Subsequently, the different data sources and corresponding data sets are investigated, as well as the diverse structures of block-wise missingness. Furthermore, the evaluation technique for each data source is explained separately after the data sources have been introduced and investigated.

3.1 Assessing the Performance

This part of the thesis supplies the essential information needed to estimate the predictive performance of a classification model. In the first chapter, different metrics are introduced and defined. These are used to rate and compare the predictive performance of the different approaches. Subsequently ‘k-fold cross validation’ is introduced and explained. This technique is used to estimate the predictive performance of a model when there is no separate test-set to do so.

3.1.1 Metrics

This subsection introduces the diverse metrics used in this thesis to rate the predictive performances of the different approaches. Metrics are needed “in order to evaluate the performance of a statistical learning method on a given data set [...] [and] measure how well its predictions actually match the observed data” [[38], p. 29]. As this thesis aims to compare classification approaches, only performance metrics suitable for classification problems are introduced. The thesis only uses data sets with a binary response variable to compare the different approaches. Therefore the metrics are only explained for a binary response, but most of the metrics can also be applied to multi-class problems. The selection of metrics is very important, as it influences how the performance of the approaches are measured and compared.

Confusion Matrix

The confusion matrix itself is not a performance measure, but the basis for most classification metrics [39]. It is used in classification problems and the matrix always consists of as many rows and columns, as the response variable has unique classes.

An example of a confusion matrix for a binary target can be seen in table 2 - it displays a matrix with the dimensions 2×2 . The rows of the table represent the predicted class - $\hat{Y} \in [0; 1]$ -, while the columns represent the actual class - $Y \in [0; 1]$ [40]. Each cell of the matrix displays the amount of observations that were classified correctly | wrongly:

- **TP:** True Positives - amount of observations where the true outcome and the predicted outcome is both positive ($Y = 1 \& \hat{Y} = 1$)
- **FN:** False Negatives - amount of observations where the true outcome is positive ($Y = 1$), but the predicted outcome is negative ($\hat{Y} = 0$)
- **FP:** False Positives - amount of observations where the true outcome is negative ($Y = 0$), but the predicted outcome is positive ($\hat{Y} = 1$)
- **TN:** True Negatives - amount of observations where the true outcome and the predicted outcome is both negative ($Y = 0 \& \hat{Y} = 0$)

	$Y = 1$	$Y = 0$	
$\hat{Y} = 1$	TP	FP	Predicted Classes
$\hat{Y} = 0$	FN	TN	
True Classes			

Table 2: Confusion matrix for a binary response.

Therefore **TP** and **TN** show the amount of observations that were labelled correctly, while **FN** and **FP** represent the wrongly labelled observations. Hence the confusion matrix shows the amount of correctly and wrongly labelled observations and can be used for the calculation of sophisticated classification metrics.

The confusion matrix from table 2 is used as a running example for the introduction of the different metrics in the next paragraphs.

Error-rate & Accuracy

“The most common approach for quantifying the accuracy [...] [of a prediction model is the] error-rate” [[38], p. 37]. It represents the proportion of mistakes a prediction model did when predicting the classes for the given set of observations - it can be calculated with help of the confusion matrix: **Error-rate** = $\frac{FP+FN}{TP+TN+FN+FP}$ [[40], p. 4]. The accuracy on the other hand represents the exact opposite, as it represents the fraction of correctly classified observations. It can also be calculated directly from the confusion-matrix: **Accuracy** = $\frac{TP+TN}{TP+TN+FN+FP}$ [[40], p. 4].

The error-rate and accuracy are rather simple metrics and intuitively understandable. The accuracy is $\in [0, 1]$ and is better the higher its value, while the error-rate is $\in [0, 1]$ and is worse the higher its value.

Both metrics are good measures when the classes of the response variable are nearly balanced, but should not be used if the classes of the target variable are highly imbalanced [39]. Thinking of a data set where only 1% of the observations is labelled as ‘positive’ and the remaining 99% as ‘negative’. If a model is naive and always predicts a negative outcome, it still has an accuracy of 99% even though the model is terrible at predicting the actual outcome. To overcome this drawback of the error-rate and accuracy, other metrics are introduced in the following.

Precision

The precision metric represents the fraction of observations with an predicted positive response - $\hat{Y} = 1$ - that also have an actual positive response - $Y = 1$. On basis of the confusion matrix it can be calculated via: **Precision** = $\frac{TP}{TP+FP}$ [[40], p. 4].

As the precision metric only respects the observations with a predicted positive class, it is less sensitive to class imbalances than the accuracy and error-rate. The precision metric is $\in [0, 1]$ and the lower its value the worse the predictive performance. Another common term for this metric is ‘positive predictive value’.

Recall

The recall metric represents the fraction of observations with an actual positive response - $Y = 1$ - that were correctly classified as positive - $\hat{Y} = 1$. It can be calculated on basis of the confusion matrix via: **Recall** = $\frac{TP}{TP+FN}$ [[41], p. 2].

As it measures how accurate the predictions for observations with an actual positive outcome are, the recall metric ignores the observations with an actual

negative outcome. Therefore this metric is less sensitive to class imbalances than the accuracy and error-rate metric. The recall metric is $\in [0, 1]$ and the higher its value the better the predictive performance. Another common term for this metric is 'sensitivity'.

F-1 Score

The F-1 score is a very common metric that represents the two metrics precision and recall at once. It is the harmonic mean of both metrics and based on the precision and recall it can be calculated via [[40], p. 4]:

$$\text{F-1 Score} = 2 * \frac{\text{Precision} * \text{Recall}}{\text{Precision} + \text{Recall}} \quad (10)$$

The F-1 score is $\in [0, 1]$ and the better the predictive performance of a model the higher the F-1 score.

Balanced Accuracy

The balanced accuracy is a metric that “avoids inflated performance estimates on imbalanced data sets” [42]. Basically it calculates the accuracy for each possible response class separately and returns the average of these class-wise accuracies. This average of the class-wise accuracies can be determined with the confusion matrix [43]:

$$\text{Balanced Accuracy} = \frac{\frac{\text{TP}}{\text{TP} + \text{FN}} + \frac{\text{TN}}{\text{TN} + \text{FP}}}{2} \quad (11)$$

As the regular accuracy, it is $\in [0, 1]$ and the better the higher its value.

Matthews correlation coefficient

The Matthews correlation coefficient (MCC) is a metric that is insensitive to class imbalances. It is a “widely used performance measure in biomedical research” [[41], p. 1] and can be seen as a “discretization of the Pearson correlation for binary variables” [[41], p. 1]. It can directly be calculated with the confusion matrix via [[44], p. 415]:

$$\text{MMC} = \frac{\text{TP} * \text{TN} - \text{FP} * \text{FN}}{\sqrt{(\text{TP} + \text{FP}) * (\text{TP} + \text{FN}) * (\text{TN} + \text{FP}) * (\text{TN} + \text{FN})}} \quad (12)$$

The MMC is in “essence a correlation coefficient” [42] with values $\in [-1, 1]$. 1 is the best possible value and represents perfect predictions, 0 indicates that the predictions are random on average and a value of -1 indicates the worst possible predictive performance [42].

3.1.2 k-fold Cross Validation

'K-fold cross validation' is a technique to estimate the predictive performance of a model, when there is no separate test-set. Before explaining the technique in more detail, it is important to understand the difference between the calculation of a metric on the test- and train-set.

Regardless of the metric, there is a big difference whether the metric is calculated on the train- or the test-set. The train-set consists of the data used to train a prediction model, while the data of the test-set "was not used in training the model" [[38], p. 176]. The results of calculating a metric on the train-set are often quite different from the metric obtained when calculating it on the test-set - "in particular the former can dramatically underestimate the latter" [[38], p. 176]. The calculation of a metric on the train-set is therefore over-optimistic, as "the same data is being used to fit the method and assess its [predictive performance]" [[20], p. 228]. Hence the calculation of a metric should always be done with data that has not been used to train the model. In case of having no designated test-set, there are diverse techniques to estimate the predictive performance by using only the available training data.

A very simple approach to obtain a metric on a test-set is the so-called 'hold-out' method. With this technique a data set D is split to a train-set D_{train} and a test-set D_{test} . A model can then be trained on D_{train} and evaluated on D_{test} to see how well that model performs on unseen data. Such a single train-test split can be problematic and lead to distorted estimates, as the metric highly depends on how the data is split into train- and test-set. Different train-test splits of the data can, therefore, lead to completely distinct results. In general, the smaller the test-set D_{test} "the higher the variance of our estimated metric" [[45], p. 18]. And the smaller the train-set D_{train} , the bigger the introduced pessimistic bias, as the model is trained on fewer data and will, therefore, learn less and perform worse [45].

To avoid this bias-variance trade-off with the 'hold-out' method, there are techniques that use the data more efficiently through resampling. Resampling, in general, describes the process of repeatedly splitting the training data D into train- and tests-sets, whereby the resulting metrics can be calculated for each of these splits and aggregated then [45]. This leads to a more stable performance estimation. A well-known method to do so is the so-called 'k-fold cross validation'.

'K-fold cross validation' divides the available training data into k groups of approximately equal size. By using only $k-1$ of these folds for the training of the model, the trained model can then be evaluated on the remaining fold - the so-called held-out fold. Based "on the observations in the held-out fold"

[[38], p. 181] any metric can then be calculated. This process is repeated until each fold has been the held-out fold once. This results in k estimates of a metric, whereby the final k -fold cross validation estimation for this metric equals the average of the k values [38]: $CV(k) = \frac{1}{k} \sum_{i=1}^k \text{Metric}_i$

The process of the 'k-fold cross validation' method is illustrated in figure 15. In the top of the figure, the whole data is displayed. In the first step of the cross validation, the data is shuffled and partitioned into five equally sized folds. In the first of the five iterations, the first fold is used as a held-out fold, while the folds 2, 3, 4 and 5 are used to train the model. The fitted model is then evaluated with the observations from the first fold, which results in Metric_1 . The same process is repeated for the remaining iterations 2-5. In each of these iterations, a different fold is used as held-out fold. Therefore each of these iterations results in an estimated metric based on a different held-out fold - $\text{Metric}_1, \dots, \text{Metric}_5$. The final estimation of the metric equals the average of the metric overall five iterations: $\frac{1}{5} \sum_{i=1}^5 \text{Metric}_i$

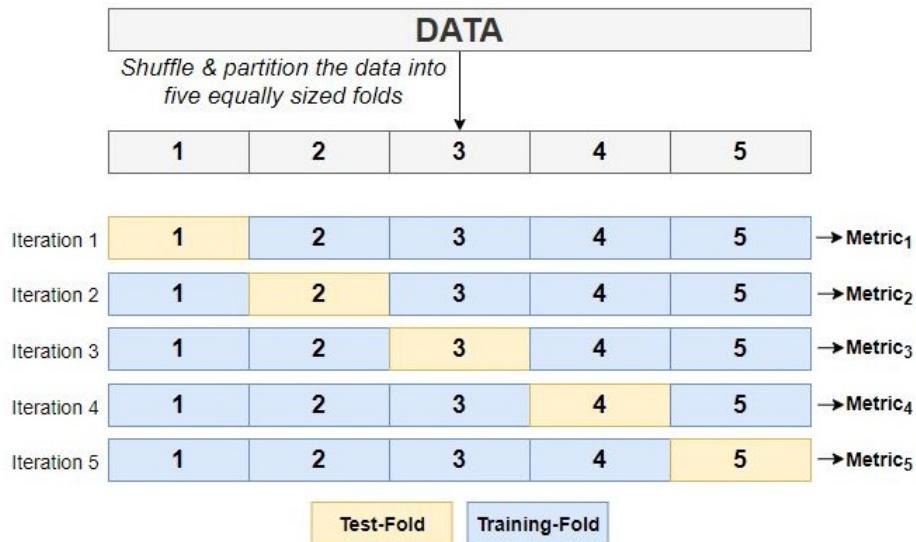


Figure 15: Example for 5-fold cross validation.

In summary: 'K-fold cross validation' is a technique to estimate the predictive performance of an approach on unseen data. It can be applied if there is only a train-set, but no separate test-set.

3.2 Data

In this subsection, the data sets from the diverse sources are investigated. In total there are two diverse sources of data for the comparison of the different approaches. The comparison of approaches with an insufficient number of data sets leads to underpowered results, as the performance of the approaches across the different data sets can be highly variable [37]. Therefore enough data sets from different sources are needed for a meaningful comparison of the approaches. In the coming sections, the different sources and corresponding data sets are introduced in more detail, as well as their different structures of block-wise missingness. After the introduction of each source, the technique for the evaluation is explained.

3.2.1 TCGA Data

The first source for multi-omics data is 'The Cancer Genome Atlas' (TCGA) that provides "real multi-omics data sets [...], where each of these data sets contains the measurements of patients with a certain cancer type" [[14], p. 14]. The data was not directly accessed via TCGA, but provided by R. Hornung who has used the data in one of his articles already [14]. In total 21 different data sets were provided, whereby these data sets have already been processed. The processing included the imputation of "missing values in the clinical block" [[14], p. 14] and the transformation of categorical feature variables into binary numerical features. For the imputation of the clinical covariates the 'k nearest neighbours imputation' and 'univariate logistic regression' have been used - further details can be found in the article itself [14]. Hence the 21 provided data sets do not miss any values and only consist of numerical covariates.

The 21 data sets have a survival outcome, but as this thesis aims to compare classification approaches this outcome is not used as the target variable. Instead, the covariate 'gender' from the 'Clinical' feature-block is used as a binary categorical response variable. This is not an unusual procedure and has been applied in other studies already - e.g. [46]. Even though the 'gender' variable "is not a clinically meaningful outcome in biomedical applications, it features major advantages for a purely methodological investigation" [[46], p. 5]. Seven of the 21 available data sets do not contain a 'gender' covariate and had to be removed, such that a total of 14 usable data sets remained. Each of the 14 remaining data sets is fully observed and consists of the same five feature-blocks. Even though the number of available covariates for each feature-block differs between the 14 data sets, they are still in a similar field. The average amount of covariates over the 14 data sets for each feature-

block is displayed in table 3. While the 'Clinical' feature-block represents clinical information like 'weight', 'height' and 'smoking status' the remaining four feature-blocks are different types of omics data and represent biological properties. The 'Clinical' feature-block has the lowest number of covariates on average, while the 'CNV' block has by far the most.

Feature-Block	Average amount of covariates
Clinical	3.5
miRNA	770
Mutation	16218
CNV	57964
RNA	23559

Table 3: The average amount of covariates in each feature-block over the 14 TCGA data sets.

The average amount of observations for the 14 data sets is ~ 280 and hence the amount of features is on much higher than the number of observations - a very common property of multi-omics data.

Reducing the dimensionality of the omics feature-blocks

A problem that comes with the choice of 'gender' as target variable are the "overly strong biological signal[s]" [[46], p. 5] contained in the different omics feature-blocks. It is aimed to reduce these biological signals by only using a subset of variables for each omics block and "thus make it comparable to signals observed in applications of clinical relevance" [[46], p. 5]. Another reason for using only a subset of the available covariates per feature-block is the computational expense of evaluating models on such high dimensional data. The reduction of the computational effort is especially important for the 'fold-wise' approach from section 2.7. This approach was implemented on basis of the 'simpleRF' package [47] in plain R, as no package offered a method to dynamically prune the single trees of a random forest model. Therefore this approach is computational much slower than the other approaches from sections 2.3 - 2.6, as these were implemented with the 'randomForestSRC' package [32] that directly builds upon 'Java' and 'C'.

To find a reasonable subset for each omics feature-block, the performance of a random forest model is evaluated on each of the single feature-blocks and their corresponding subsets. The predictive performance of the models on the different omics blocks is evaluated with 5-fold cross validation and rated

with the accuracy - general details on the metrics/ k-fold cross validation in the section 3.1.1/ 3.1.2. The predictive performance of a random forest model on the single omics blocks and their corresponding subsets - based on all 14 available TCGA data sets - is displayed in figure 16.

The figure consists of totally four plots, whereby each plot represents a single omics feature-block. Each of these plots contains eight boxplots representing the accuracy - y-axis - of the model for different subsets of used covariates - x-axis. The predictive performance for the feature-blocks 'CNV' and 'RNA' is, in general, the best, while the feature-blocks 'miRNA' and 'Mutation' are much worse. The feature-blocks 'miRNA' and 'Mutation' are therefore only trimmed to reduce the computational effort. As the 'miRNA' block only consists of 770 covariates on average, only 50% of the available covariates are removed. The feature-block 'Mutation' has 16218 covariates on average from which 90% are removed. While the trimming of these two feature-blocks reduces the computational effort, it does not reduce the predictive quality of these single feature-blocks too much. The number of covariates in the 'CNV' and 'RNA' feature-blocks have to be trimmed to reduce the biological signals in these blocks. 85% of the available covariates were removed from the 'RNA' block. This leads to a lower but still reasonable predictive performance with this block. The 'CNV' block leads to the best predictive performances and seems to contain a lot of strong biological signals. Therefore 95% of the available covariates from this feature-block were removed. The predictive performance with the trimmed 'CNV' block is still by far the best and not much worse than on the complete 'CNV' feature-block. The same plot but with the F-1 score as a metric is displayed in figure A-2 in the attachment - the results are about the same.

Removing 50% of the covariates from the 'miRNA' block, 90% from the 'Mutation' block, 85% from the 'RNA' block and 95% from the 'CNV' block lead to data sets with much lower dimensions than originally. Nonetheless, the important multi-omics property of more observed covariates than observations is still valid for the trimmed data sets. The average amount of covariates over the 14 data sets for each reduced feature-block is displayed in table 4.

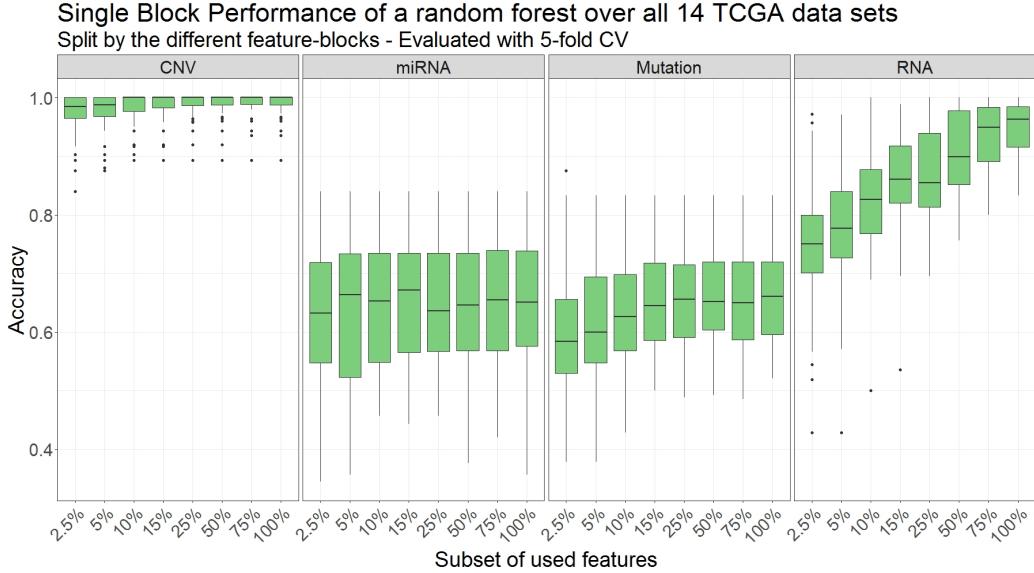


Figure 16: The accuracy of a random forest model evaluated on the single omics feature-blocks for a range of possible subsets on all 14 TCGA data-sets.

Reduced Feature-Block	Average amount of covariates
Clinical	3.5
miRNA	385
Mutation	1616
CNV	2898
RNA	3555

Table 4: The average dimensionality of the five trimmed feature-blocks for the 14 TCGA data set.

Inducing block-wise missingness

To estimate the predictive performance of the different approaches k-fold cross validation is applied. The 14 provided TCGA data sets are completely observed and do not contain any missing values. But as these data sets shall be used for the investigation of different approaches capable to deal with block-wise missingness, block-wise missingness needs to be induced into the training-sets in the cross validation - more details on this in algorithm 3. Each of the 14 TCGA data sets consists of the response variable 'Y' and the five feature-blocks 'Clinical', 'CNV', 'RNA', 'Mutation' and 'miRNA'. These 14 data sets are induced with block-wise missingness according to the

following patterns. In the tables of these patterns, a red cross indicates a missing feature-block for a fold, while a green tick indicates an observed feature-block.

Pattern 1 The first pattern of block-wise missingness is displayed in table 5. Every fold consists of the same amount of observations and to each of them, there is an observed response variable 'Y', the 'Clinical' feature-block and one additional omics feature-block. Therefore every single fold consists of two feature-blocks as observed covariates - one 'Clinical' and one omics block. The 'Clinical' block is the same for all folds, while the omics blocks differ from fold to fold.

	Y	Clinical	CNV	RNA	Mutation	miRNA
Fold 1	✓	✓	✓	✗	✗	✗
Fold 2	✓	✓	✗	✓	✗	✗
Fold 3	✓	✓	✗	✗	✓	✗
Fold 4	✓	✓	✗	✗	✗	✓

Table 5: The first block-wise missingness pattern for the TCGA data sets.

Pattern 2 The second pattern of block-wise missingness is displayed in table 6. The amount of observations in the different folds is equal for all folds, while the number of observed feature-blocks differ from fold to fold. The order of the feature-blocks was randomly changed in comparison to 'Pattern 1', whereby the last omics block 'CNV' is observed for all folds and the first omics block 'miRNA' only for the first fold. The amount of available feature-blocks decreases from 'Fold 1' to 'Fold 4'. 'Fold 1' is completely observed within all five feature-blocks and 'Fold 4' in only two feature-blocks - 'Clinical' and 'CNV'.

	Y	Clinical	miRNA	RNA	Mutation	CNV
Fold 1	✓	✓	✓	✓	✓	✓
Fold 2	✓	✓	✗	✓	✓	✓
Fold 3	✓	✓	✗	✗	✓	✓
Fold 4	✓	✓	✗	✗	✗	✓

Table 6: The second block-wise missingness pattern for the TCGA data sets.

Pattern 3 The third pattern of block-wise missingness is displayed in table 7. The amount of observations is equally split into the four folds. For each of these folds, it is randomly drawn which feature-blocks are observed. The probability for any feature-block to be observed equals $\frac{2}{3}$ and the probability of not observing a block, therefore, $\frac{1}{3}$. The 'Clinical', as well as the 'RNA' feature-block, were sampled for every fold. Therefore the four folds only differ in the feature-blocks 'CNV', 'Mutation' and 'miRNA'. The same feature-blocks were sampled for 'Fold 3' and 'Fold 4', such that these folds have the same covariates. Therefore these two folds are a single fold and the data consists of only three unique folds then.

	Y	Clinical	CNV	RNA	Mutation	miRNA	
Fold 1	✓	✓	✓	✓	✗	✓	
Fold 2	✓	✓	✓	✓	✗	✗	
Fold 3	✓	✓	✗	✓	✓	✓	
Fold 4	✓	✓	✗	✓	✓	✓	

} Fold3

Table 7: The third block-wise missingness pattern for the TCGA data sets.

Pattern 4 The fourth and last pattern of block-wise missingness is displayed in table 8. Other than in the three patterns before, the amount of observations is equally split in two instead of four folds. The next difference to the first three patterns is that the amount of feature-blocks is reduced from five to three. For this two of each of the four available omics feature-blocks were combined into a single omics feature-block - this has been done randomly. The feature-blocks 'RNA' and 'miRNA' were combined to a single feature-block, as well as the feature-blocks 'Mutation' and 'CNV'. Therefore the whole data consists of three feature-blocks - 'Clinical', 'RNA & miRNA' and 'Mutation & CNV' - and two folds.

	Y	Clinical	RNA & miRNA	Mutation & CNV
Fold 1	✓	✓	✓	✗
Fold 2	✓	✓	✗	✓

Table 8: The fourth block-wise missingness pattern for the TCGA data sets.

Evaluation Technique

The 14 data sets from the TCGA source are used to assess the predictive performance of the different random forest adaptions for data with block-wise missingness. All data sets are completely observed and to none of these exists a separate test-set. A slightly modified version of 5-fold cross validation is applied to assess the predictive performance of the different approaches on this data. The process is illustrated in algorithm 3.

In the very beginning a data-set D , an approach App and a block-wise missingness pattern $Patt$ have to be selected. The data set D is split into five equally sized folds, whereby a single fold is used as test-set and the remaining four folds as train-set. Then block-wise missingness is induced into the train-set according to the selected pattern of missingness $Patt$ and the model is fitted on this data. The predictive performance of an approach does not only depend on the train-set, but also on the available feature-blocks in the test-set. Hence the approach App is evaluated not only on a fully observed test-set, but also on the same test-set, but with different combinations of missing feature-blocks. This is relevant, as block-wise missingness can affect the train-set as well as the test-set. Therefore the predictive performance of the fitted model is evaluated on the same test-set for all possible combinations of observed feature-blocks. Firstly the approach is evaluated on the test-set with all feature-blocks available (2.3.1). Then it is further evaluated on the same test-sets with one missing feature-block (2.3.2) - e.g. missing 'CNV' feature-block. Following it is evaluated on all possible test-sets with two missing feature-blocks (2.3.3) - e.g. missing 'CNV' & 'RNA' feature-block. Subsequently it is evaluated on all possible test-sets with three missing feature-blocks (2.3.4) - e.g. missing 'CNV' & 'RNA' & 'miRNA' feature-block. And finally, it is evaluated on the test-sets with only a single observed feature-block (2.3.5) - e.g. test-set has only the 'CNV' feature-block. For each of these possible test-sets, the metrics are calculated. When the evaluation of an approach App on a data-set D with the block-wise missingness pattern $Patt$ is done, to each possible test-set there are five values of each metric. The average of these metrics for each possible test-set is then used to compare the predictive performance of the different approaches - section 4.1.

In summary: To evaluate an approach on a TCGA data-set 5-fold cross validation is applied. The training data is induced with a block-wise missingness pattern and the model is fitted on this data. The model is then not only evaluated on the fully observed test-set, but also on the same test-set for all possible combinations of block-wise missingness.

Algorithm 3: Evaluation of the approaches with the TCGA data

Input : $D \leftarrow$ TCGA data-set with n observations & p features

$App \leftarrow$ Approach

$Patt \leftarrow$ Pattern of block-wise missingness

1. Split the fully observed data-set D into five equally sized folds
 2. **for** $k \leftarrow 1$ to 5 **do**
 - 2.1 Use fold k as test-set and the remaining four folds as train-set;
 - 2.2 Induce the block-wise missingness according to $Patt$ into the train-set;
 - 2.3 Fit the App on the train-set with block-wise missingness;
 - 2.4 Evaluate the predictive performance of the approach App for different combinations of observed feature-blocks in the test-set;
 - 2.4.1 Evaluation on the fully observed test-set;
 - 2.4.2 Evaluation on test-sets with one missing feature-block;
 - 2.4.3 Evaluation on test-sets with two missing feature-blocks;
 - 2.4.4 Evaluation on test-sets with three missing feature-blocks;
 - 2.4.5 Evaluation on test-sets with a single feature-block;
-

3.2.2 Clinical asthma data

This subsection introduces the second source for multi-omics data - the so-called 'clinical asthma data'. It is a real-world data set with block-wise missingness that was provided by the group of Prof. Dr. med. Bianca Schaub at the 'paediatric clinic Dr. von Haunersches Kinderspital'. The data was collected as part of a clinical case-control study in the field of asthma research, whereby the target variable of the data is binary and defined as the presence of asthma. The data set contains 521 observations in total (age 5-16), whereby 265 observations have a negative response and the remaining 256 observations have a positive response. The data comprises five different data sources with 268 variables in total. 44 of those variables originated from a questionnaire, 16 from a clinical routine diagnostics, 19 from the information on allergen sensitization, 29 are from cytokine expression data, and 166 from gene expression data. As the feature space of the gene expression data had a block-wise missing structure itself, the gene expression data was split into two data sets - 'gene expression data I' (82 variables) and 'gene expression data II' (84 variables). The number of observations and variables in the different data sources is displayed in table 9. The amount of observations in the different data sources inversely reflects the effort of generating the data - e.g. the fewer observations the more valuable the measured features.

ID	Feature-Block	Number of observations	Number of variables
1	Questionnaire	521	44
2	Clinical routine diagnostics	385	16
3	Allergen sensitization	472	19
4	Cytokine expression data	149	29
5	Gene expression data I	66	82
6	Gene expression data II	46	84

Table 9: The number of observations and variables for the different data sets in the clinical asthma data.

The data preparation was carried out by the project partner and conducted as follows:

- (1) Feature variables (especially from the questionnaire) were selected such that they are reasonable/ useful/ interpretable as predictor variables and either continuous or binary distributed.
- (2) All data sources were cleaned by removing variables with a high proportion of missing values ($\geq 30\%$) and imputing the remaining missing values with the 'missForest' imputation approach.
- (3) The data sets from the different sources were then combined into a single data set.

The merged data set has the dimensions 521×274 and consists of six different feature-blocks in total - each data source corresponds to a feature-block. The single variable names of the different feature-blocks were censored because of data protection regulations. Every single of the 521 observations in the data misses at least one feature-block, such that there is no single observation that is completely observed in all six feature-blocks. The structure of the block-wise missingness is displayed in figure 17. In this figure, each row corresponds to an observation in the data set and each column stands for a single data source. A green line indicates that an observation was completely observed for a given feature-block, while a red line indicates that the observation was not observed at all for the corresponding feature-block. The 'Questionnaire' feature-block was observed for every patient of the data set, and there is no single patient that is observed in both 'gene expression data I' and 'gene expression data II' feature-blocks.

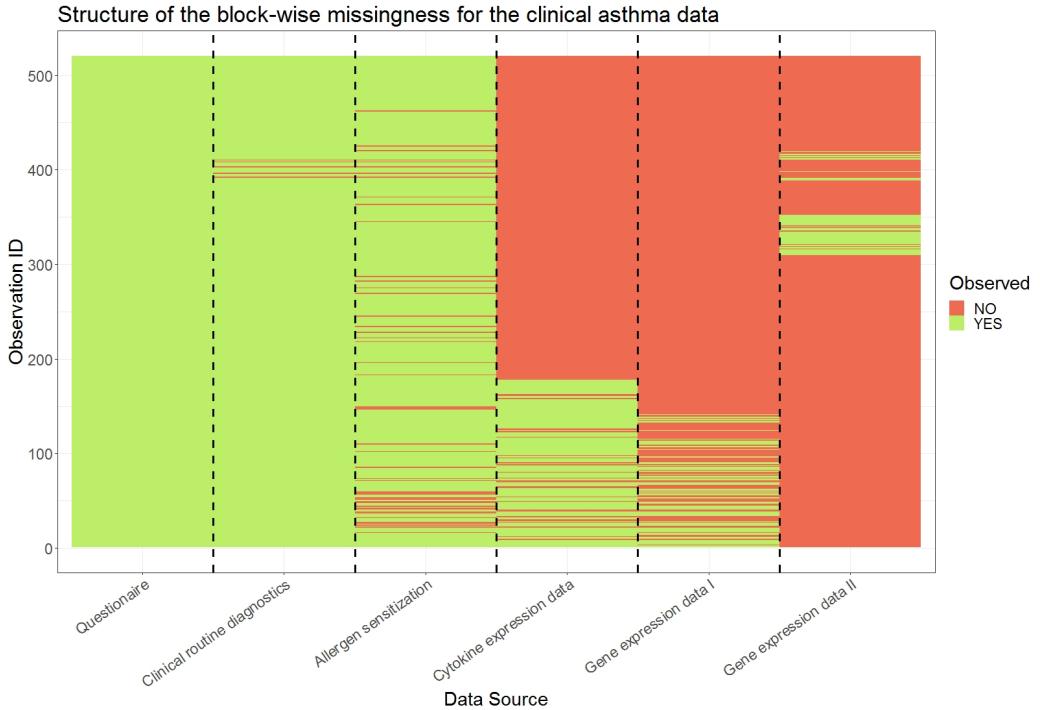


Figure 17: Structure of block-wise missingness in the clinical asthma data.

Evaluation Technique

The clinical asthma data is used to assess the predictive performance of the different approaches for data with block-wise missingness. Besides the comparison of the predictive performance of the different random forest based approaches, also the performance of the mdd-sPLS method and the diverse priority-Lasso adaptions from Hagenberg [21] are compared on basis of this data. To assess the predictive performance of the different approaches on this data regular 5-fold cross validation is applied - the distribution of the target variable is approximately equal for all folds (50:50). Other than the TCGA data, the clinical asthma data already consists of block-wise missingness. As the data is randomly split into five folds, each of these folds consist of observations with diverse block-wise missing values. Hence not only the training-sets consist of different block-wise missingness structures but also the test-sets (\cong held-out folds) contain observations with different observed feature-blocks. This is completely different compared to the cross validation on the TCGA data, where the observations in the test-set always have the same observed feature-blocks. The 5-fold cross validation technique for the clinical asthma data is explained now and illustrated in algorithm 4.

In the beginning the clinical asthma data is split into five equally sized folds. In each iteration of the 5-fold cross validation one of the folds is used as test-set (held-out fold) and the remaining folds as train-set. Firstly, the different patterns of block-wise missingness are extracted from the test-set. For each pattern of block-wise missingness in the test-set, the approach App is fitted on the train-set, such that it can provide predictions for the test-observations with the current pattern of block-wise missingness. After the outcome was predicted for each observation in the test-set, the predicted classes are compared with the true classes and the resulting metric for the current cross validation fold is returned.

Algorithm 4: Evaluation of the random forest based approaches with the clinical asthma data

Input : $D \leftarrow$ clinical asthma data with block-wise missingness
 $App \leftarrow$ Approach

1. Split the clinical asthma data D into five equally sized folds
2. **for** $k \leftarrow 1$ **to** 5 **do**
 - 2.1 Use fold k as test-set and the remaining four folds as train-set;
 - 2.2 Extract the unique patterns of block-wise missingness in the test-set - $test_{patterns}$;
 - 2.3 **for** $pattern_{current} \in test_{patterns}$ **do**
 - 2.3.1 Fit App on the train-set, such that it can be used for the prediction on $pattern_{current}$;
 - 2.3.2 Generate predictions for the test-observations with block-wise missingness according to $current_{pattern}$
 - 2.4 Evaluate the predictive performance of the approach App by comparing the predicted classes with the true classes;

4 Results

This section presents the results of the different approaches for data with block-wise missing values on the diverse data sources. Firstly the results of the different random forest adaptions on the TCGA data are shown and analysed. Afterwards, the results of the different random forest adaptions, the mdd-sPLS method and the priority-Lasso adaptions from Hagenberg [21] are shown and analysed based on the clinical asthma data.

4.1 TCGA

This subsection contains all cross validation results of the different random forest adaptions for the diverse patterns of block-wise missingness in the TCGA data. Detailed information on the evaluation technique with the TCGA data can be found in the paragraph 'Evaluation Technique' of section 3.2.1. Details on the diverse patterns of block-wise missingness can be found in the paragraph 'Inducing block-wise missingness' of section 3.2.1. Firstly, the results for each approach on the diverse patterns of block-wise missingness ('Pattern 1', ..., 'Pattern 4') are shown and explained separately before the different approaches are compared then.

The figures that show the results for the different approaches always have a similar structure. The figure consists of a separate plot for each pattern of block-wise missingness in the training data. Each plot shows the results as boxplots, whereby the y-axis shows the F-1 score as metric and the x-axis the different combinations of feature-blocks in the test-set - e.g. 'miss2_BD' shows the results of an approach on a test-set with missing feature-blocks 'B' and 'D'. For each of the different combinations of feature-blocks in the test-set - so-called 'test-situations' - the results are plotted as a boxplot. The data in the different test-situations is always the same and only differs in the observed feature-blocks - e.g. in a given pattern, the test-situations 'miss1_A' (observed feature-blocks: [B, C, D & Clin]) and 'miss1_B' (observed feature-blocks: [A, C, D & Clin]) only differ in the observed feature-blocks, while everything else is completely equal (the observations and feature-blocks [C, D & Clin] are exactly equal for both test-situations).

4.1.1 Complete-Case Approach

This part of the thesis introduces the results of the complete case approach on the diverse patterns of block-wise missingness on the TCGA data - details on the approach itself can be found in section 2.3.

Figure 18 shows the average results of the 5-fold cross validation of the

complete-case approach on the 14 TCGA data sets for the first three patterns of block-wise missingness. The first thing that stands out is that there are not always results for each test-situation - e.g. with 'Pattern 1' there are no results (for the situations) where the test-set is fully observed ('full'), misses a single feature-block (e.g. 'miss1_A') or misses two feature-blocks (e.g. 'miss2_CD'). The complete-case approach only uses observations that are observed in the same feature-blocks as the test-set to train a random forest model. As the training-set with 'Pattern 1' only contains observations with an observed clinical and one additional omics feature-block, there are simply no complete case observations for these test-situations. Hence the complete case approach can not generate predictions for these test-situations. Only with 'Pattern 2' the complete case approach can create predictions in all possible test-situations. In 'Pattern 1' and 'Pattern 3' it is noticeable that the results are much better in test-situations with the feature-block 'A' - e.g. 'miss3_BCD' / 'single_A' (in both patterns 'A' stands for the CNV block). In

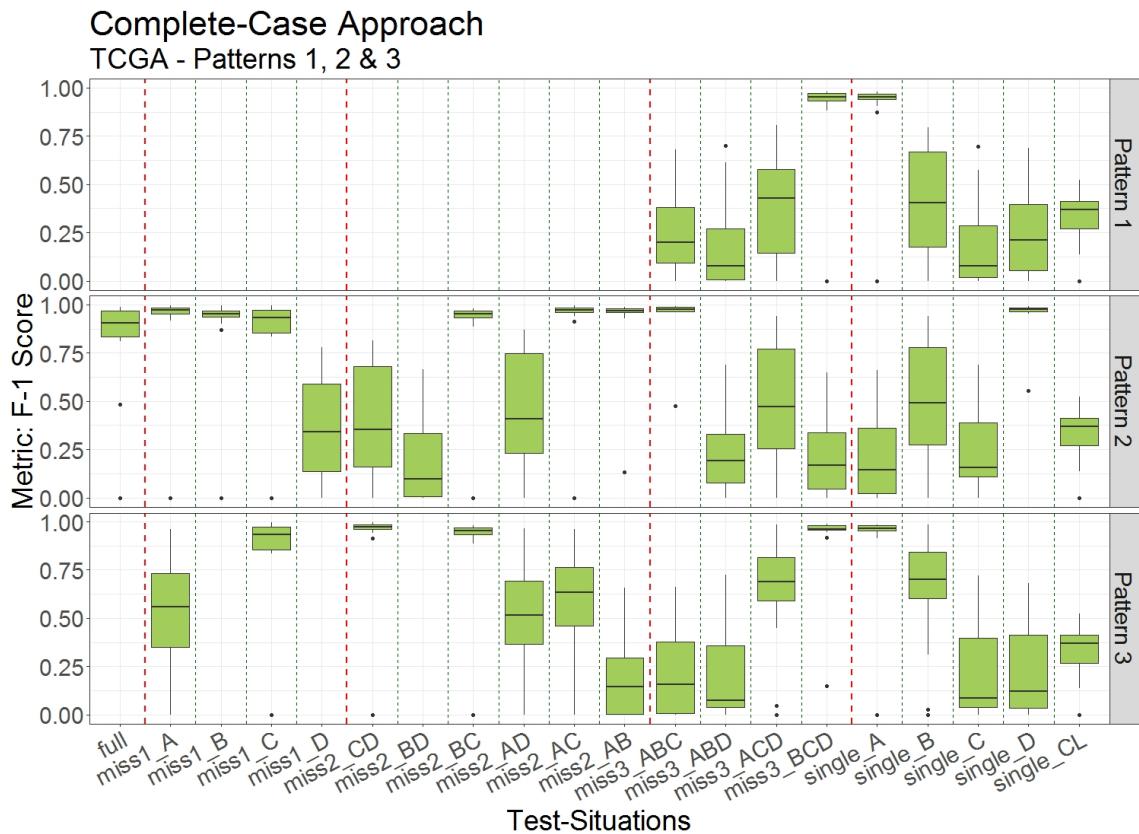


Figure 18: Results of the 'Complete-Case' approach on the TCGA data with induced block-wise missingness according to pattern 1, 2 & 3.

'Pattern 2' the results are the best in test-situations with the feature-block 'D' - e.g. 'miss1_A' / 'miss1_B' / 'miss1_C' (in this pattern 'D' stands for the CNV block).

4.1.2 Single-Block Approach

This part of the thesis introduces the results of the single-block approach on the diverse patterns of block-wise missingness on the TCGA data - details on the approach itself can be found in section 2.4.

Figure 19 shows the average results of the 5-fold cross validation of the single-block approach on the 14 TCGA data sets for the first three patterns of block-wise missingness. To each test-situation, the results are shown structured according to the feature-block that was used for the training of the single-block approach. The first thing that stands out is that the single-block approach can only create predictions in the test-situations that contain the feature-block the random forest model has originally been trained with - e.g. when training a random forest on the 'Clinical' feature-block, the resulting model can only generate predictions for observations/ test-sets that are observed in this feature-block. Moreover, the performance of the single-block approach on a given feature-block is the same for all test-situations. This makes sense, as the test-sets in the different test-situations only differ in their observed feature-blocks and as the single-block approach uses the same feature-block for the predictions, the performance is equal for the different test-situations. Regarding the predictive performance, the fehlt hier ein Komma? single-block approach it is clear to see that in 'Pattern 1' and 'Pattern 3' the performance is the best when using the feature-block 'A' (in both patterns 'A' stands for the CNV block). In 'Pattern 2' the single-block approach has its best performance with the feature-block 'D' (in this pattern 'D' stands for the CNV block).

Single-Block Approach

TCGA - Patterns 1, 2 & 3

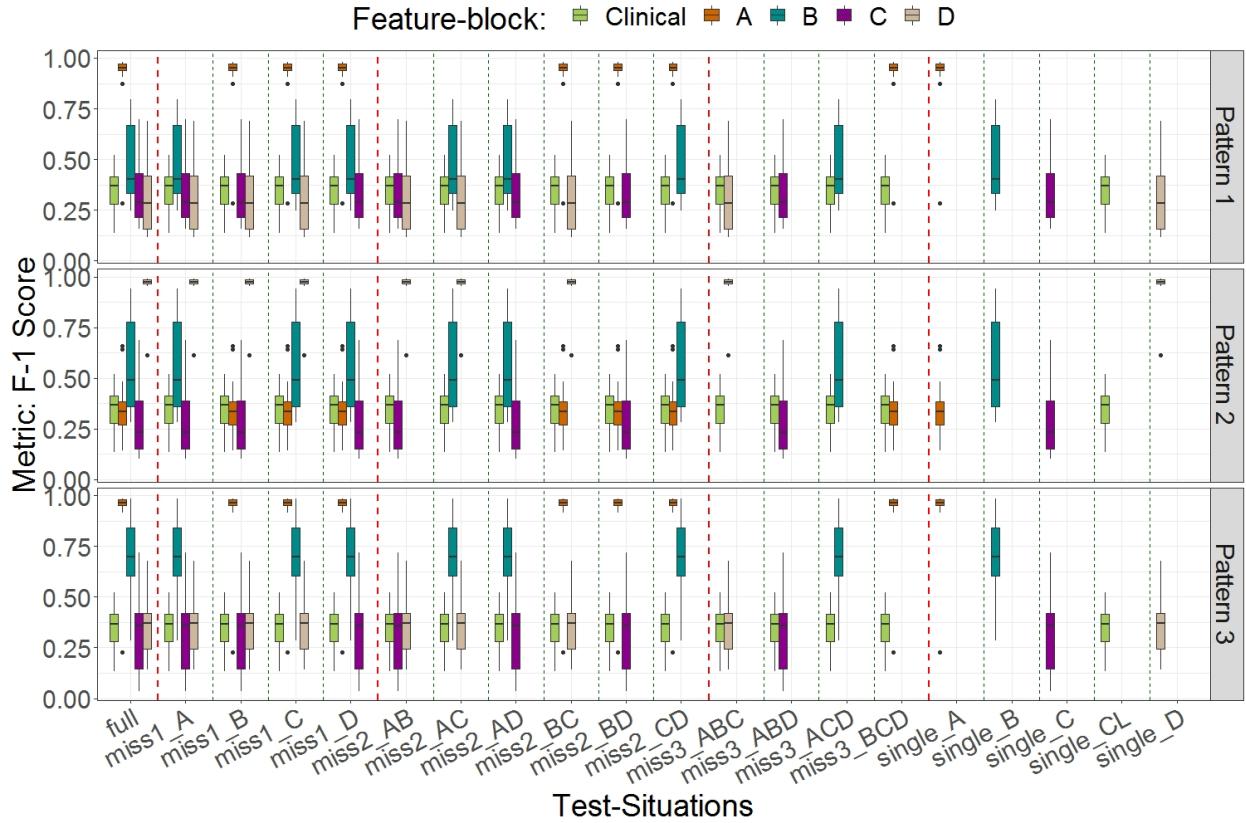


Figure 19: Results of the 'Single-Block' approach on the TCGA data with induced block-wise missingness according to pattern 1, 2 & 3.

4.1.3 Imputation Approach

This part of the thesis introduces the results of the imputation approach on the diverse patterns of block-wise missingness on the TCGA data - details on the approach itself can be found in section 2.5.

Figure 20 shows the average results of the 5-fold cross validation of the imputation approach on the 14 TCGA data sets for the first three patterns of block-wise missingness. The first thing that stands out is that the imputation approach can provide predictions for any possible test-situation. This is possible, as the imputation approach firstly imputes all missing values in the data, such that the data is completely observed then. With this completely observed data, a random forest model can be fitted and provide predictions for all possible test-situations then. Regarding the predictive performance

in 'Pattern 1' and 'Pattern 3', it is the best in the test-situations with the feature-block 'A' (in both patterns 'A' stands for the CNV block). In 'Pattern 2' the imputation approach has its best performance with the feature-block 'D' (in this pattern 'D' stands for the CNV block). Therefore, as with the previous two approaches, the performance in the diverse test-situations is always the best in test-situations with the feature-block CNV.

unnötige wiederholung

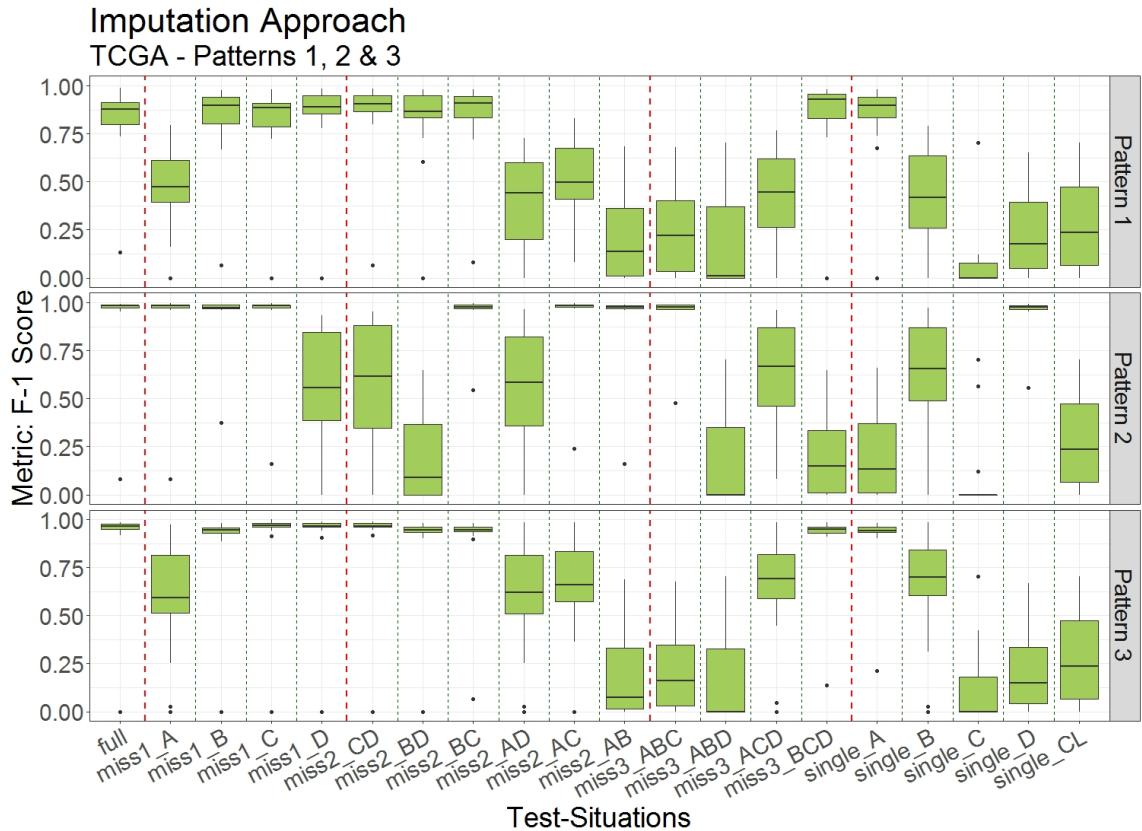


Figure 20: Results of the 'Imputation' approach on the TCGA data with induced block-wise missingness according to pattern 1,2 & 3.

4.1.4 Block-wise Approach

This part of the thesis introduces the results of the block-wise approach on the diverse patterns of block-wise missingness on the TCGA data - details on the approach itself can be found in section 2.6.

Figure 21 shows the boxplots for the average results of the 5-fold cross validation of the block-wise approach on the 14 TCGA data sets for the first three patterns of block-wise missingness. For each test-situation, the results of the block-wise approach are shown structured according to the weight

metric used to combine the block-wise predictions. The first thing that stands out is that the block-wise approach can provide predictions for any test-situation. As the block-wise approach combines the predictions of the single feature-blocks it has been trained with, it is flexibly applicable in different test-situations. Furthermore, it is worth mentioning that the performance in the test-situations with a single feature-block only - e.g. 'single_A' - is equal for the different weight metrics used for the aggregation of the block-wise predictions. That is meaningful, as the predictions in these test-situations only depend on a single feature-block, such that there is no aggregation of block-wise predictions. Regarding the performance, it is clear to see that it is the best when using the 'F-1 Score' as weight metric. For all patterns of block-wise missingness, in 15 out of the 20 different test-situations, the median F-1 score is the best with the 'F-1 Score' as weight metric. The only five situations in which the block-wise approach with the 'F-1 Score' as weight metric does not have the best results are the test-situations with a

it works best ?

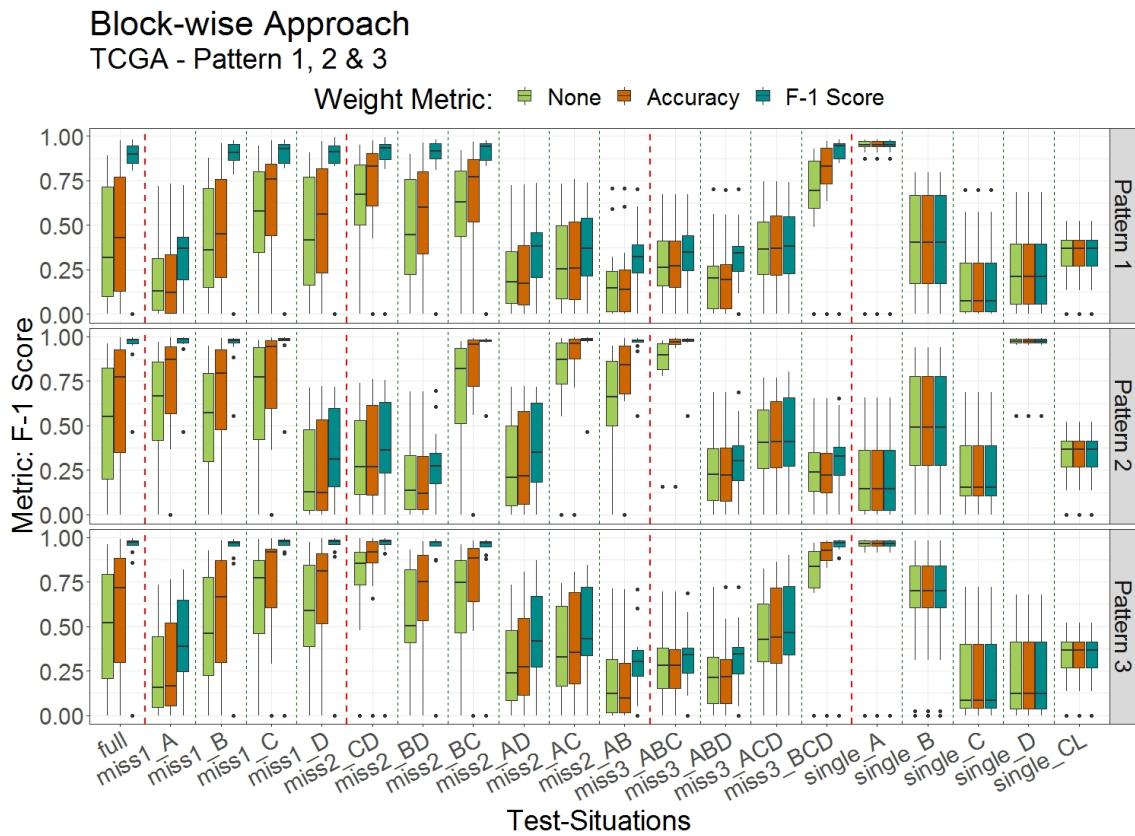


Figure 21: Results of the 'Block-wise' approach on the TCGA data with induced block-wise missingness according to pattern 1, 2 & 3.

single feature-block. In these test-situations, the used weight metric has no influence, as there is no aggregation of the block-wise predictions. Regarding the predictive performance, it is the same as with the previous approaches. In 'Pattern 1' and 'Pattern 3' the predictive performance is the best in the test-situations with the feature-block 'A' (in both patterns 'A' stands for the CNV block). While in 'Pattern 2' the block-wise approach has the best performance with the feature-block 'D' (in this pattern 'D' stands for the CNV block).

4.1.5 Fold-wise Approach

This part of the thesis introduces the results of the fold-wise approach on the diverse patterns of block-wise missingness on the TCGA data - details on the approach itself can be found in section 2.7.

Figure 22 shows the boxplots for the average results of the 5-fold cross validation of the fold-wise approach on the 14 TCGA data sets for the first three patterns of block-wise missingness. For each test-situation, the results of the fold-wise approach are shown structured according to the weight metric used to combine the fold-wise predictions. As the fold-wise approach combines the predictions of its diverse fold-wise fitted random forest models, it is flexibly applicable and can provide predictions for any test-situation. Furthermore, the performance of the fold-wise approach is identical for the different weight metrics in the test-situations that only consist of feature-blocks that are only available for a single fold in the training data. For example, with 'Pattern 1' the performance in the test-situations 'single_A', 'single_B', 'single_C' and 'single_D' is equal for the different weight metrics. That is reasonable, as in these test-situations only a single fold-wise fitted random forest model can create predictions, as the training-set only has a single fold that can be used for these test-situations - there is only one fold in the training data with an observed feature-block 'A', such that only this fold can be used to train a random forest model and create a prediction for the test-set 'single_A' then. Regarding the predictive performance, it is quite clear to see that it is the best when using the 'F-1 Score' as weight metric. With 'Pattern 1' the median F-1 score is the best in 15 out of the 20 test-situations with the 'F-1 Score' as weight metric. With 'Pattern 2' the median F-1 score is the best in 9 out of the 20 test-situations with the 'F-1 Score' as weight metric. With 'Pattern 3' the fold-wise approach also works the best with the 'F-1 Score' as weight metric - the median F-1 score is the best in 8 out of the 20 test-situations. As with the previous approaches, in 'Pattern 1' and 'Pattern 3' the predictive performance is the best in the test-situations that contain the feature-block 'A' (in both patterns 'A' stands

for the CNV block). While in 'Pattern 2' the block-wise approach has the best performance with the feature-block 'D' (in this pattern 'D' stands for the CNV block).

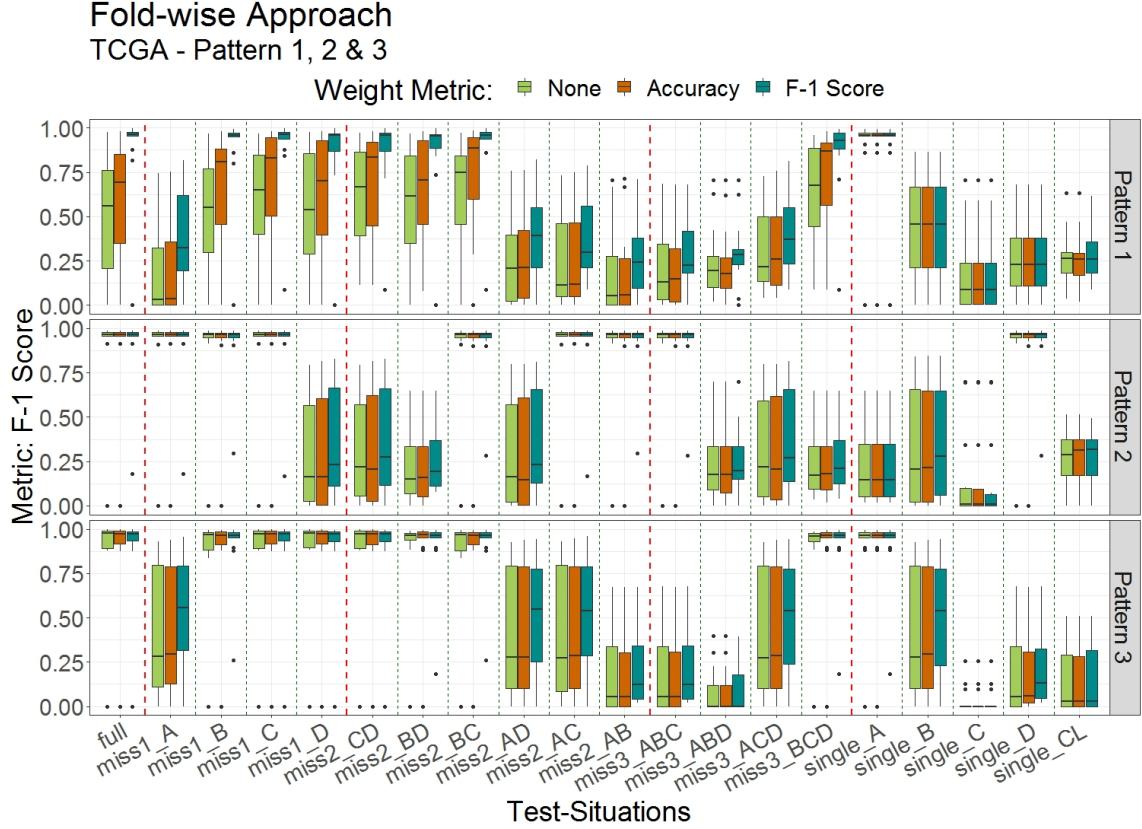


Figure 22: Results of the 'Fold-wise' approach on the TCGA data with induced block-wise missingness according to pattern 1, 2 & 3.

4.1.6 Comparison of the approaches

This part of the thesis compares the results of the different random forest based approaches on the TCGA data for its different patterns of block-wise missingness. For the comparison of the diverse approaches, only the best settings of each approach are used. For the block- & fold-wise approach the results were the best with the 'F-1 Score' as weight metric, and for the single-block approach, the performance was the best, when using the feature-block 'CNV' (in 'Pattern 1' and 'Pattern 3' 'A' stands for the CNV block | in 'Pattern 2' 'D' stands for the CNV block).

..acquire/achieve
the best median
metric...
?

Pattern 1

Figure 23 shows the boxplots for the average results of the 5-fold cross validation of the diverse approaches on the 14 TCGA data sets with block-wise missingness in the training-set according to 'Pattern 1'. In the test-situations that do not contain the feature-block 'A', the predictive performance is in general much worse, as in the test-situations that contain the feature-block 'A' (in this pattern 'A' stands for the CNV block). The single-block and complete-case approach can not create predictions for all test-situations, while the fold-wise, block-wise, and imputation approach are able to do so. Regarding the predictive performance, the fold-wise approach has the best median metric in 11/20 test-situations, the block-wise approach has the best median metric in 3/20 test-situations and the imputation approach has the best median metric in 4/20 test-situations. The single-block approach never has the best median performance in any of the 20 test-situations, while the complete-case approach has the best median performance in only a single test-situation. In this setting, it is clear to say that the fold-wise approach has the best predictive performance. The second-best approach in this scenario is the imputation approach which is only marginally better than the block-wise approach. The single-block and complete-case approach have a rather bad predictive performance compared to the other three approaches. Additionally, these approaches have the drawback that they can not generate predictions for all possible test-situations.

Summary: The fold-wise approach has by far the best predictive performance and can create predictions for every test-situation. The imputation and block-wise approach can create predictions for all test-situations as well but have a worse predictive performance than the fold-wise approach. The complete-case and single-block approach are inflexible and can only provide predictions in certain test-situations. But even in these test-situations, the approaches are usually worse than at least one of the remaining approaches. The results with the balanced accuracy/ MCC as metric are similar - corresponding figures A-3/ A-4 can be found in the attachment.

one

Comparison of all Approaches

TCGA - Pattern 1

Approach: █ Fold-wise █ Block-wise █ Imputation █ Single-Block █ Complete-Case

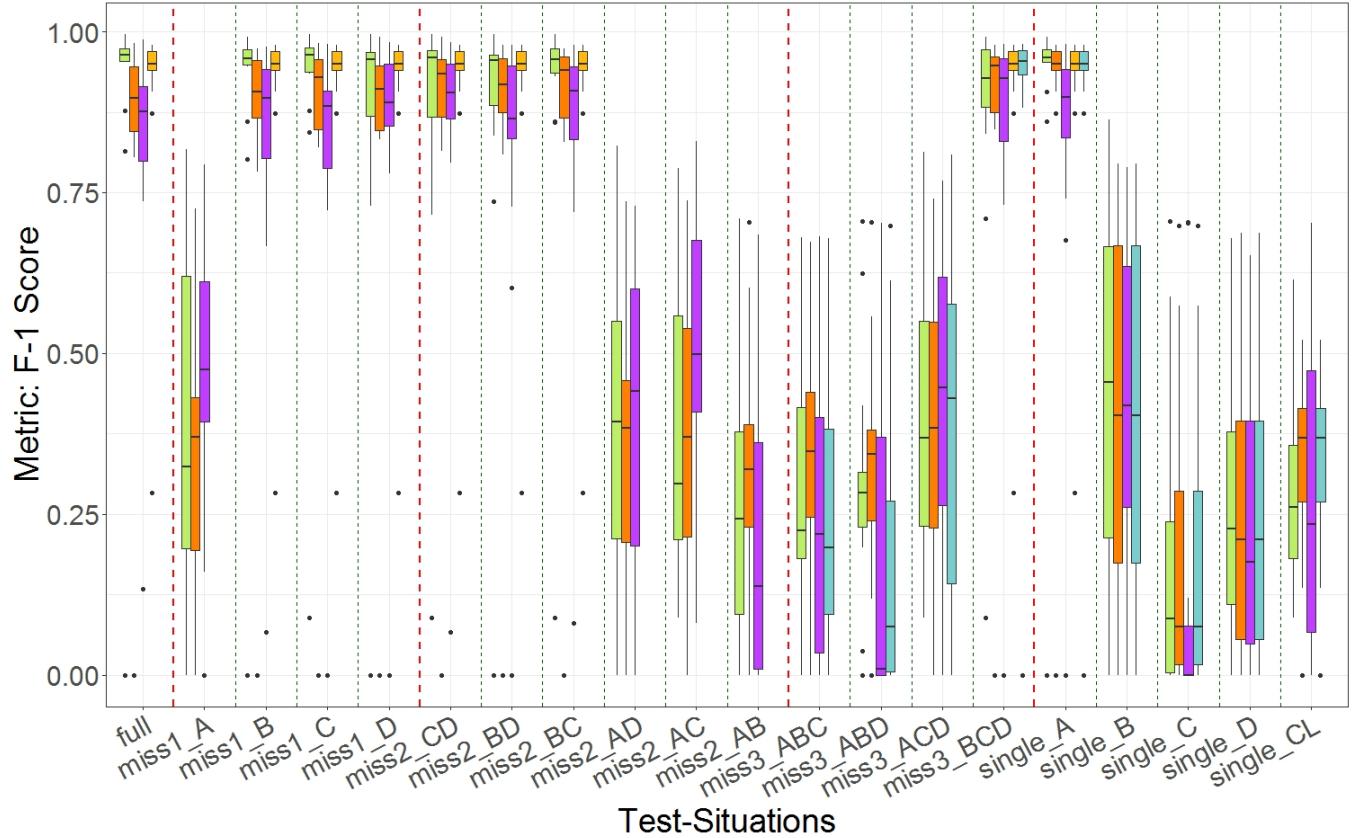


Figure 23: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 1.

Pattern 2

Figure 24 shows the boxplots for the average results of the 5-fold cross validation of the diverse approaches on the 14 TCGA data sets with block-wise missingness in the training-set according to 'Pattern 2'. In the test-situations that do not contain the feature-block 'D' the predictive performance is in general much worse, as in the test-situations that contain the feature-block 'D' (in this pattern 'D' stands for the CNV block). The complete-case approach **can not** create predictions for all test-situations, while the other four approaches are able to do so. Regarding the predictive performance, the imputation and block-wise approach **have each** the best median F-1 score in

...is not capable of
creating...

each have/
each acquire

8/20 test-situations each. The fold-wise, complete-case and single-block approaches never have the best median F-1 score in any test-situation. In this setting, it is clear to say **then** that the imputation and block-wise approach have the best predictive performance. The fold-wise approach has the worst median F-1 score in ten out of the 20 test-situations and is therefore the worst approach. The imputation approach has the worst median F-1 score in six test-situations, and the complete-case approach in four test-situations. The single-block approach can provide predictions only for test-situations

Comparison of all Approaches

TCGA - Pattern 2

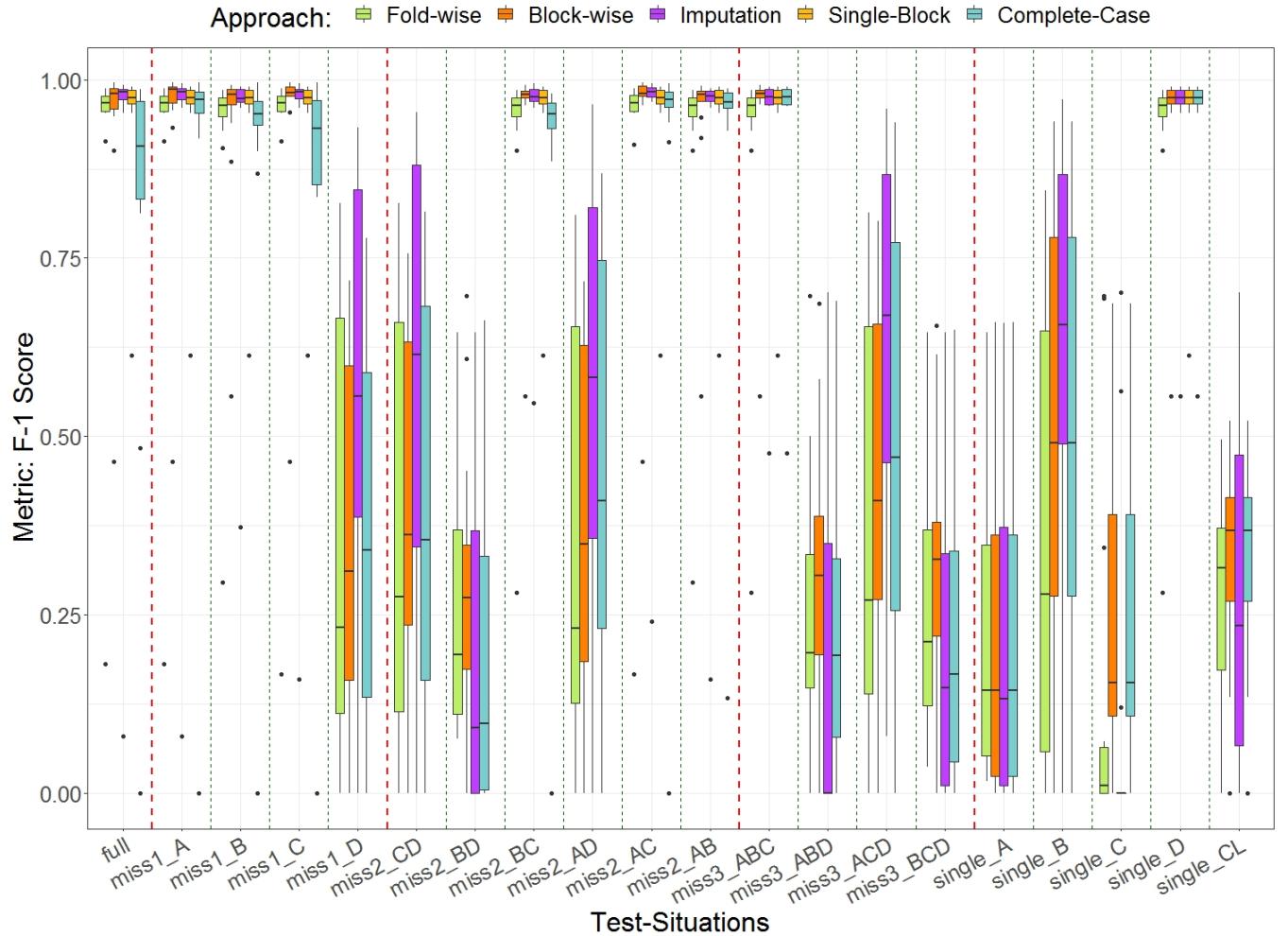


Figure 24: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 2.

with the feature-block 'D' and there is no single test-situation where this approach has the best median F-1 score, nor the worst.

Summary: The imputation and block-wise approach have the best predictive performance and can create predictions for every possible test-situation. The fold-wise and complete-case approach can create predictions for all test-situations as well, but have a worse predictive performance. Especially the fold-wise approach performs poor in this setting. The single-block approach is inflexible and can only provide predictions in certain test-situations - regarding the predictive performance the single-block approach never leads to the worst, nor to the best results. The results with the balanced accuracy/MCC as metric are similar - corresponding figures A-5/ A-6 can be found in the attachment.

Pattern 3

Figure 25 shows the boxplots for the average results of the 5-fold cross validation of the diverse approaches on the 14 TCGA data sets with block-wise missingness in the training-set according to 'Pattern 3'. In the test-situations that do not contain the feature-block 'A' the predictive performance is in general much worse, as in the test-situations that contain the feature-block 'A' (in this pattern 'A' stands for the CNV block). Except for the single-block and complete-case approach, all approaches can create predictions for all test-situations. Regarding the predictive performance, the block-wise approach has the best median F-1 score in ten out of the 20 test-situations. The imputation approach has the best performance in four test-situations, while the fold-wise approach has the best performance in only two test-situations. The complete-case and single-block approaches never have the best median F-1 score. In this setting, it is clear to say **then** that the block-wise approach has the best predictive performance. The worst approach in this setting is the imputation approach that has the **most** worst median F-1 scores. The single-block approach can provide predictions only for the test-situations with the feature-block 'A' and there is no single test-situation where this approach has the best median F-1 score, nor the worst.

Summary: The block-wise approach has the best predictive performance and can create predictions for every possible test-situation. The imputation and fold-wise approach can create predictions for all test-situations as well, but have a worse predictive performance than the block-wise approach. The single-block approach is inflexible and can only provide predictions in certain test-situations - regarding the predictive performance the single-block

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approach never leads to the best results. The results with the balanced accuracy/ MCC as metric are similar - corresponding figures A-7/ A-8 can be found in the attachment.

Comparison of all Approaches

TCGA - Pattern 3

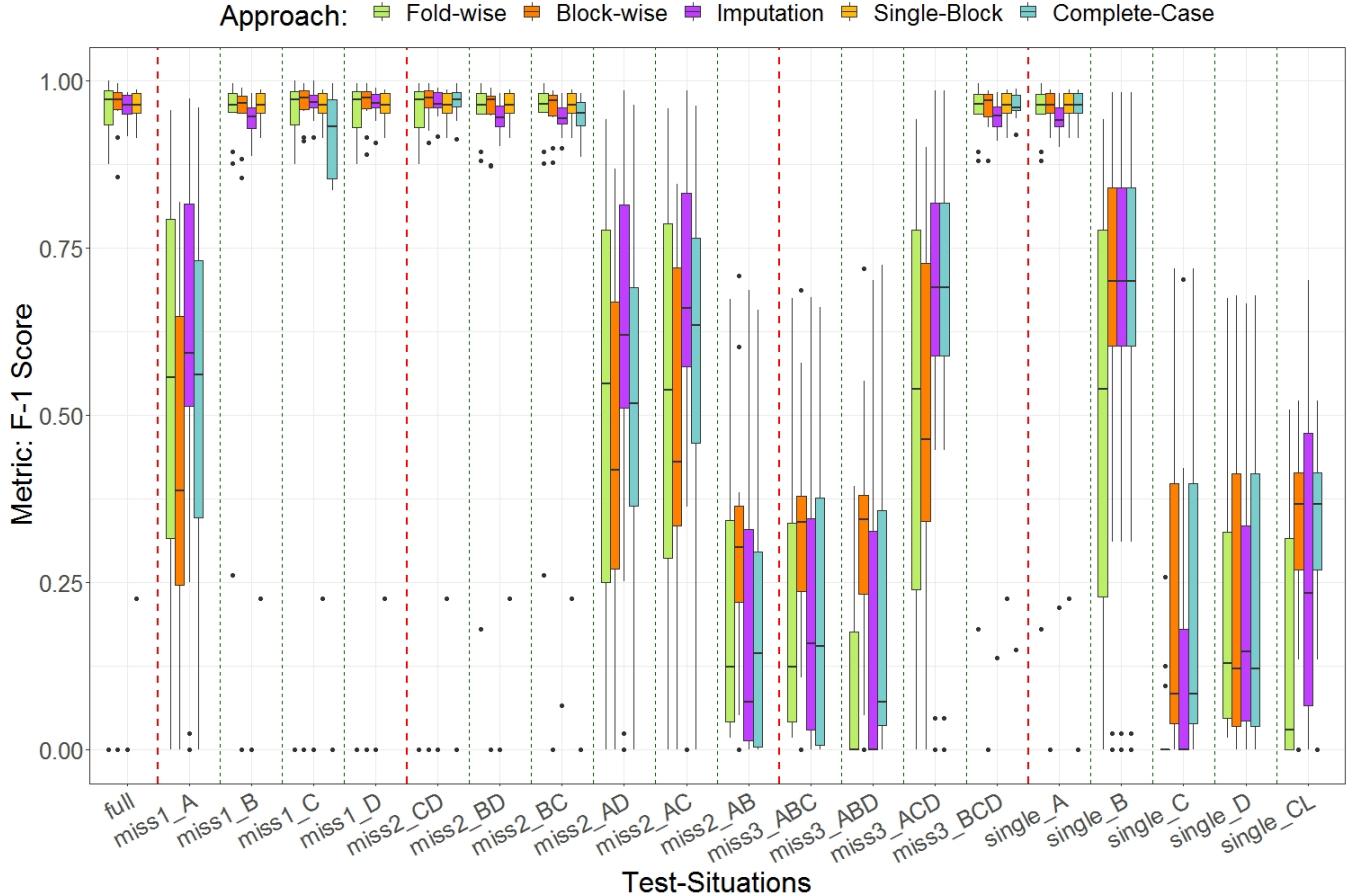


Figure 25: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 3.

4.2 Clinical asthma data

This subsection contains all cross validation results on the clinical asthma data for the different random forest adaptions, as well as for the adaptions of the priority-Lasso and the mdd-sPLS approach from Hagenberg [21]. Firstly the results of the different approaches are shown and explained separately before the results of the approaches are compared then.

4.2.1 Random Forest approaches

This part of the thesis introduces all results of the different random forest adaptions from this thesis on the clinical asthma data. Detailed information on the evaluation technique on the clinical asthma data can be found in the paragraph 'Evaluation Technique' of section 3.2.2.

Complete-Case Approach

This paragraph shows the results of the complete-case approach for the clinical asthma data - details on the approach itself in section 2.3.

Figure 26 shows the results of the 5-fold cross validation with the complete-case approach on the clinical asthma data. The resulting F-1 scores are between 0.81 and 0.87, whereby the median and mean are slightly above 0.83. As the observed feature-blocks for the observations in the test-sets differ, the predictions need to be generated separately for each fold in the test-set. To create predictions for a given fold in the test-set it is checked, whether the training-set contains complete-cases regarding the current held-out fold. If there are complete-cases, a random forest model is trained with these observations then and used to create predictions for the observations in the current held-out fold. In the 5-fold cross validation on the clinical asthma data, there was no single case, where the complete-case approach could not generate a prediction for a test-observation.

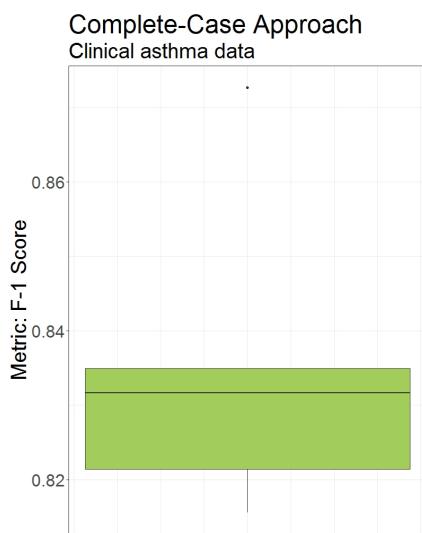


Figure 26: Results of the 'Complete-Case' approach on the clinical asthma data.

Single-Block Approach

This paragraph shows the results of the single-block approach for the clinical asthma data - details on the approach itself in section 2.4.

Figure 27 shows the results of the 5-fold cross validation with the single-block approach on the clinical asthma data. The x-axis shows the different feature-blocks that were used for the training of the random forest models - e.g. the boxplot on the far left in the figure shows the results of the 5-fold cross validation when training a random forest model on the 'Questionnaire'

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feature-block and using this model to predict on the test-set then. As the observations in the test-set are observed in different feature-blocks, the single-block approach can not always generate predictions for all observations in the test-set. Instead of evaluating the observations for which no prediction could be made as misclassified, the predictions for these observations equal the distribution of the predicted classes in the test-set - e.g. if the model labels three test-observations as 'positive' and seven as 'negative', the predicted probability for test-observations the model could not create predictions for, is set to 0.7 for 'negative'. The single-block approach with the 'Questionnaire' feature-block could always generate predictions for the on average 104.2 observations per held-out-fold. With the 'Clinical routine diagnostics' feature-block, on average one test-observation out of the 104.2 test-observations per held-out fold had to be guessed and with the 'Allergen sensitization' feature-block it were on average 8.2 test-observations per held-out fold. The remaining feature-blocks were only observed for a small fraction of the observations in the clinical asthma data, such that the average amount of test-observations that could not be predicted is much higher. For the 'Cytokine expression data' it were 74.4 out of 104.2 test-observations per held-out fold. With the 'Gene expression data I' it were 91 out of 104.2 test-observations per held-out fold and with the 'Gene expression data II' on average even 95. With a median F-1 score of 0.81 the best predictive

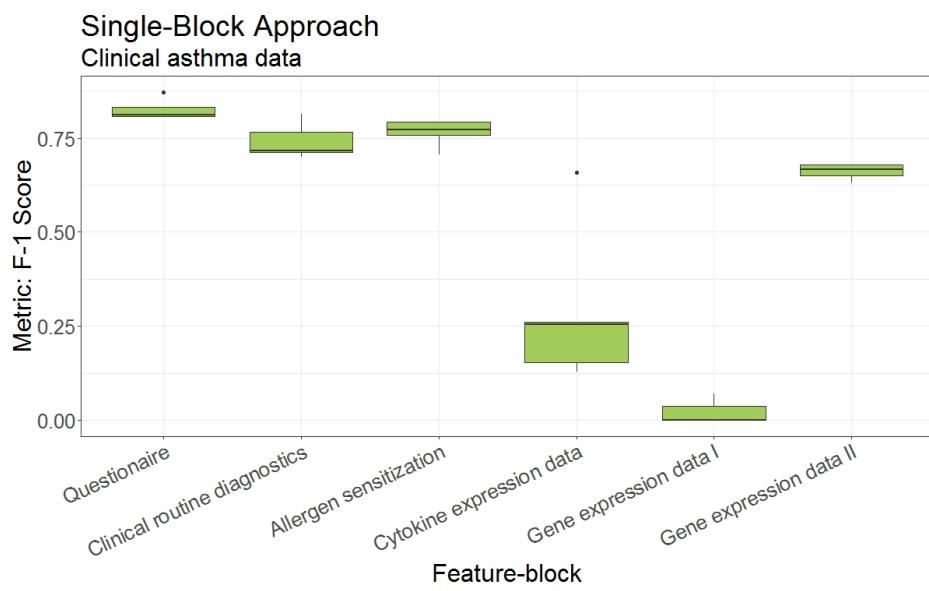


Figure 27: Results of the 'Single-Block' approach on the clinical asthma data.

performance is achieved with the 'Questionaire' feature-block. The second-best performance is achieved with the feature-block 'Allergen sensitization' that has a median F-1 score of 0.77. With any other feature-block, the median F-1 score is below 0.72.

Imputation Approach

This paragraph shows the results of the imputation approach for the clinical asthma data - details to the approach itself in section 2.5.

Figure 28 shows the results of the 5-fold cross validation with the imputation approach on the clinical asthma data as a boxplot. The resulting F-1 score metrics are between 0.83 and 0.87, whereby the median is above 0.84 and the mean around 0.85. As the observed feature-blocks for observations in the held-out fold differ, the predictions are generated separately for each fold in the held-out fold. To create a prediction for a given fold from the test-set, firstly the observed feature-blocks for the given fold have to be extracted. From the imputed training data, only the available feature-blocks of the current fold are **then** used to train a random forest model that is used to create predictions **then**.

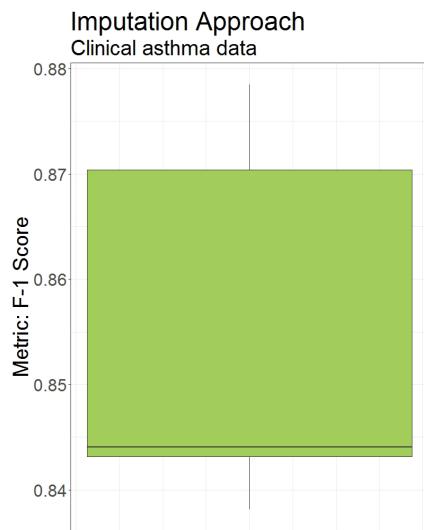


Figure 28: Results of the 'Imputation' approach on the clinical asthma data.

Block-wise Approach

This paragraph shows the results of the block-wise approach for the clinical asthma data - details on the approach itself in section 2.5.

Figure 29 shows the results of the 5-fold cross validation with the block-wise approach on the clinical asthma data. The results are split by the weight metric that was used to aggregate the diverse block-wise predictions. With this approach predictions were always possible for the observations in the test-set, as the block-wise fitted model is flexibly applicable to observations with different patterns of block-wise missingness. The predictive performance with the block-wise approach is the best when using the 'F-1 Score' as weight metric for the aggregation of the block-wise predictions. The median F-1

score metric is around 0.79, and around 0.78 when using the 'Accuracy' as weight-metric. When using no metric for the aggregation of the block-wise predictions, the performance is the worst - the median is 0.77. Even if the results are close, it can be said that the best performance is achieved when using the 'F-1 Score' as weight metric.

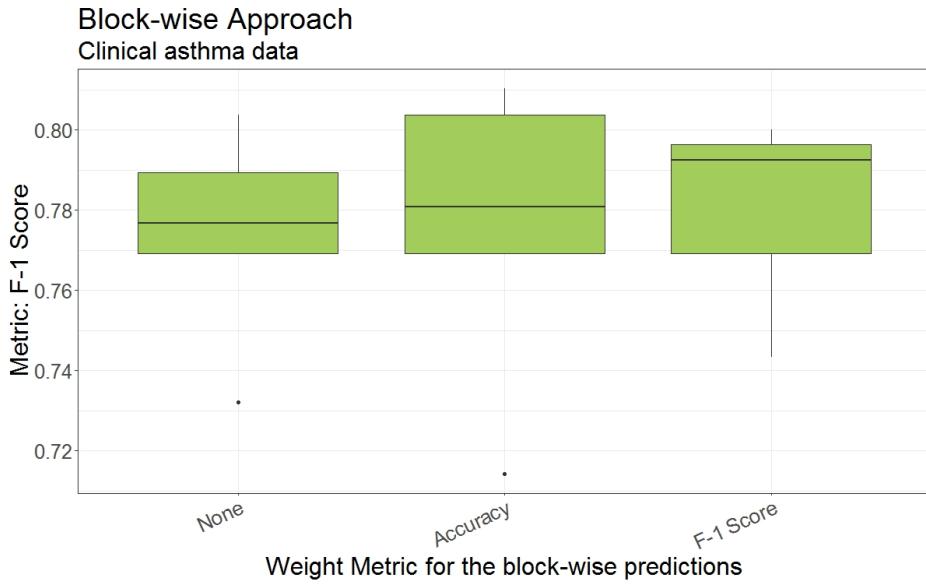


Figure 29: Results of the 'Block-wise' approach on the clinical asthma data.

Fold-wise Approach

This paragraph shows the results of the fold-wise approach for the clinical asthma data - details on the approach itself in section 2.6.

Figure 30 shows the results of the 5-fold cross validation with the fold-wise approach on the clinical asthma data. The results are split by the weight metric that was used to aggregate the diverse fold-wise predictions. As the fold-wise approach combines the predictions of its diverse fold-wise fitted random forest models, it is flexibly applicable and can provide predictions for each observation in the test-set. Regarding the predictive performance, it is clear to see that it is the best when using the 'F-1 Score' as weight metric. With the 'F-1 Score' as weight metric, the median F-1 score is around 0.83. With the 'Accuracy' as weight metric, the median is around 0.7 and when using no metric for the aggregation the median equals 0.65.

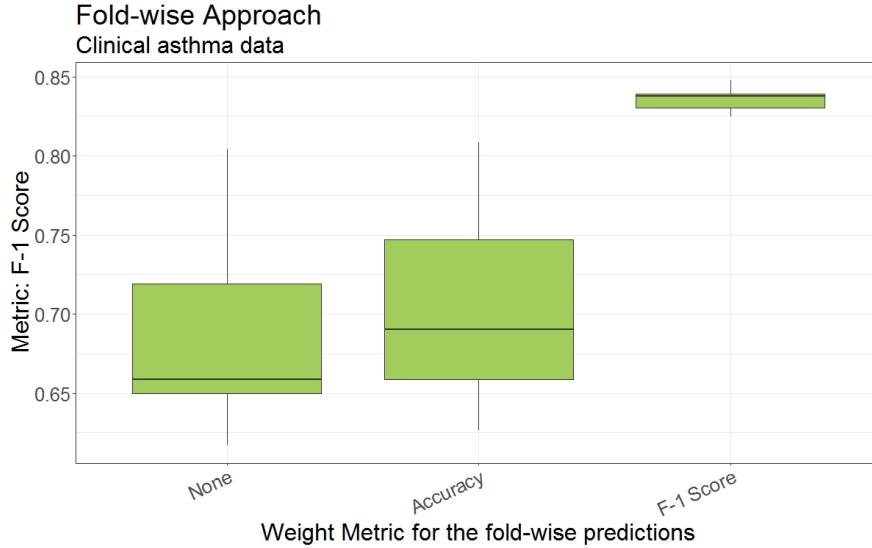


Figure 30: Results of the 'Fold-wise' approach on the clinical asthma data.

4.2.2 Priority-Lasso & mdd-sPLS

This part of the thesis introduces the predictive performances of the different priority-Lasso adaptions from Hagenberg [21] and of the mdd-sPLS method from Lorenzo et al. [48] on the clinical asthma data. These diverse methods can directly deal with block-wise missingness. In the beginning, the theoretical principles are briefly explained, before the predictive performance of the different approaches is investigated.

Theoretical principles - Priority-Lasso

The priority-Lasso is an extension of the lasso method. Lasso stands for *least absolute shrinkage and selection operator* and was introduced by Tibshirani in 1996 [49]. The lasso method is a regularised least squares estimator that adds the absolute values of all parameters as an additional penalty. The loss function is defined as:

$$\|y - \beta_0 \mathbb{1} - \mathbf{X}\boldsymbol{\beta}\|_2^2 + \lambda \sum_{j=1}^p |\beta_j| \quad (13)$$

In the equation 13 the parameter λ is a hyperparameter ≥ 0 . The bigger λ , the stronger the added penalty for each $\beta \neq 0$. The additional penalty leads

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to two major advantages over the regular least squares estimator. Firstly, the lasso model can be fitted on data with more features than observations. Secondly, the lasso method does variable selection, as only parameters of the important variables are estimated with a value different from 0.

In 2018 the priority-Lasso was introduced by Klau et al. [15] as an extension of the classical lasso method. The priority-Lasso can be applied to data with different feature-blocks. It is described as a “hierarchical regression method which builds prediction rules for patient outcomes [...] from different blocks of variables including high-throughput molecular data” [[15], p. 2]. Firstly the feature-blocks of the data are ordered in descending order of priority for the target variable. Then a separate lasso model is fitted to each of these feature-blocks. The models that were fitted on the later blocks (the later, the lower the importance of the block for the target variable) are only used to improve the prediction from the previous blocks. “In order to assure that later blocks only improve the prediction of the previous blocks, the fitted linear predictor of block m is used as the offset when fitting block $m + 1$ ” [21]. More details can be found in the second chapter of Hagenberg’s thesis [21] or in Klau et al. [15].

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Hagenberg [21] developed different adaptions of the priority-Lasso such that it can directly deal with block-wise missingness. As for the priority-Lasso a model is fitted on each feature-block of the data. Mainly there are two methods to deal with the missing data.

Lieber Doppelpunkt

(1) **Ignore:** The idea of this approach is that the “lasso model for every block is only fitted with the observations that have no missing values” [21]. For observations that have missing values in the current feature-block, no offset can be calculated for the next block. For these observations the offset (incl. intercept) “from the previous block is carried forward” [21]. For observations that lack values of the first feature-block, the offset for the second feature-block is either set to zero - *PL-ignore, zero* - or to the estimated intercept of the first feature-block - *PL-ignore, intercept*.

(2) **Impute:** As in the ”Ignore” approach, the lasso model fitted on each feature-block only uses the observations that have no missing values in this block. For observations with missing values the offset from the previous block is not carried forward, but imputed. “This has the advantage that instead of imputing a possibly very high number of covariates, only one value [- the offset -] is imputed” [21]. In the beginning, the unique patterns of block-wise missingness Q_m are extracted from all the observations that miss the feature-block m . Then for each pattern of block-wise missingness q ($q \in Q_m$) all observations from the training data that can be used for an imputation model are found. These observations need to be observed in the feature-block m and in at least one feature-block that is not observed in the pattern

that do have

q . Then for every pattern of block-wise missingness Q_m it is counted how many observations can be used for the imputation model. The pattern q that the training observations must have to be usable for the imputation model is either chosen according to the pattern “that has the most observations that can be used for the imputation model” [21] [*max. n*] or according to the pattern “that uses the most high priority blocks” [*max. blocks*] [21].

In total there are four different adaptions of the priority-Lasso - ‘ignore, zero’, ‘ignore, intercept’, ‘impute, max. n’ and ‘impute, max. blocks’. All models are fitted sequentially and only differ in the way how the offset is carried forward for observations with missing values and how predictions are done. Closer information on the theoretical principles of these adaptions can be found in chapter three of Hagenberg’s thesis [21].

Theoretical principles - mdd-sPLS

The mdd-sPLS method was introduced by Lorenzo et al. in 2019 [48] and can be applied in “supervised high dimensional settings with a large number of variables and a low number of individuals” [[48], p. 1]. In these settings, it can either be used for variable selection or as a prediction model. In the thesis of Hagenberg [21] it is used as a prediction method for the comparison with the diverse priority-Lasso adaptions. The mdd-sPLS method “is based on singular value decomposition (SVD) of the covariance matrix between the outcome Y and the covariates X” [21]. The maximising of the covariance between X and Y leads to latent variables for the covariates and the target variable. “The latent variables can then be used to approximate X and Y and regress \hat{Y} onto \hat{X} [(latent variables)]” [21]. Lorenzo et al. [48] use a soft-threshold covariance matrix for the SVD, such that all entries with an absolute value smaller than a threshold are set to zero - the method is called ‘covariance-thresholding sparse PLS’ (ct-sPLS). To combine the information from multiple feature-blocks, the ct-sPLS method is applied separately to all blocks. For the combination of the information in the different blocks “the weights from the SVD used to generate the latent variables are pooled. The pooling is performed in such a way that the subsequent regression is done in a common subspace over all blocks” [21]. This method is called ‘Multi-Data-Driven-sPLS (mdd-sPLS)’.

Missing values in the training data are mean imputed before the mdd-sPLS algorithm is applied. Only variables that have originally been missing and received a mean value as a first imputation get improved imputations then. To do this, another mdd-sPLS model is built. This model predicts the “variables used in the first model from information about the outcome and is used

to impute the missing values. The process of building a model to predict the outcome and then another model to impute the missing variables is repeated until convergence of the latent variables of the covariates” [21].

Missing values in the test data are imputed by a mdd-sPLS model on the observed data. Based on the complete data-set predictions can then be generated.

The mdd-sPLS method can be fitted directly on data with block-wise missing values and provide predictions for test observations with block-wise missing values. Further details on the theoretical properties can either be found in [48] or in Hagenberg’s thesis [21].

Naive block priority

In this setting, the analysis was performed with a block order that gives a higher priority to feature-blocks with less missing observations. This is a rather naive assumption, as the priority of the feature-blocks should be justified by a professional - e.g. a doctor. The results of the 5-fold cross validation on the clinical asthma data for the different priority-Lasso adaptions and the mdd-sPLS method are shown as boxplots in figure 31. The x-axis shows the different approaches and the y-axis the corresponding F-1 scores. The overall F-1 scores are between 0.75 and 0.88. Among the priority-Lasso adaptions, the worst median F-1 score with 0.81 has the ‘PL - impute, maximise blocks’ approach. The second worst priority-Lasso adaption is the ‘PL - impute, maximise n’ with a median F-1 score of 0.82. The priority-Lasso approaches ‘PL - ignore, zero’ and ‘PL - ignore, intercept’ both have a higher median F-1 score than the ‘imputation’ priority-Lasso adaptions. The median F-1 score for the ‘PL - ignore, zero’ approach is 0.82 and only slightly lower than of the ‘PL - ignore, intercept’ approach that has a median F-1 score of 0.83. The mdd-sPLS approach has a median F-1 score of 0.81 and is only slightly better than the ‘PL - impute, maximise blocks’ adaption. In this setting the ‘ignore’ priority-Lasso adaptions perform better than the ‘imputation’ priority-Lasso adaptions. The best performance is achieved with the ‘PL - ignore, intercept’ approach that has a median F-1 score of 0.83. The mdd-sPLS approach is the second worst approach and is only better than the worst priority-Lasso adaption - ‘PL - impute, maximise blocks’.

Among the priority-lasso adaptions, the ‘pl-impute, maximise blocks’ approach shows the worst median... ?

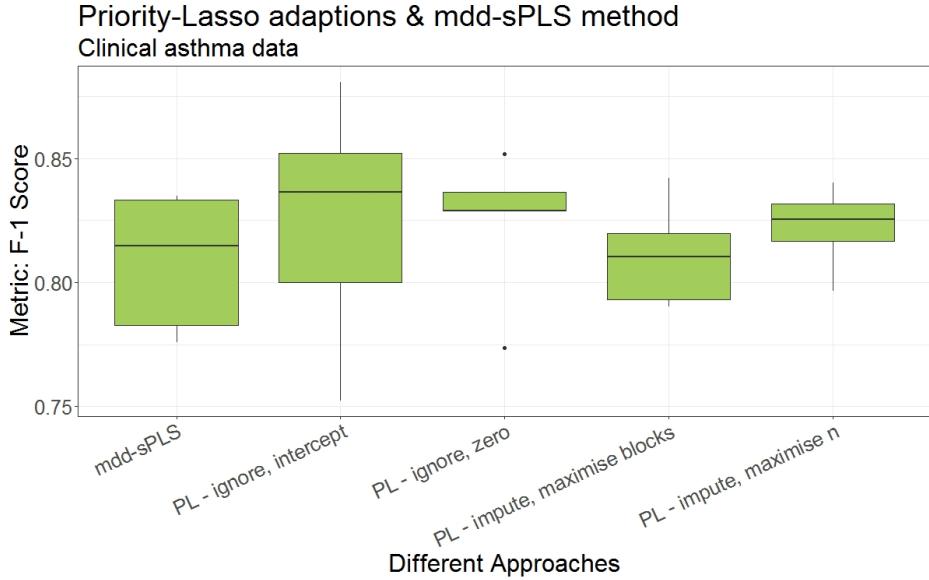


Figure 31: Results of the priority-Lasso adaptions and the mdd-sPLS approach on the clinical asthma data.

Influence of using different block combinations for the prediction

In this setting, the influence of different block combinations for the prediction is investigated. The priority of the feature-blocks is the same naive one as in the previous chapter. The different priority-Lasso adaptions are trained on all blocks, but the predictions are “based on a subset of the blocks, adding one after the other” [21]. The results for the different priority-Lasso adaptions are shown as boxplots in figure 32. The x-axis shows the different priority-Lasso adaptions and the y-axis the corresponding F-1 scores. For each approach the F-1 score is shown for the predictions based on the different block combinations - e.g. the red boxplots show the results of the diverse approaches when only using block 1 for the predictions, whereby the green boxplots show the results of the same approaches when using block 1, 2 and 3 for the predictions.

When using only block 1 for the prediction, the median F-1 score for the ‘ignore’ priority-Lasso adaptions are around 0.81, and for the ‘imputation’ priority-Lasso adaptions around 0.82. The addition of block 2 increases the median F-1 score for all approaches except for ‘PL - impute, maximise blocks’. The addition of block 3 increases the median F-1 scores for all approaches as well. When additionally using block 4 for the prediction it worsens the median F-1 score for all approaches except for ‘PL - ignore, intercept’. The

additions of block 5 and 6 lead to a big decrease in the predictive performance for all the different approaches.

The predictive performance is the best for all approaches when only using the feature-blocks 1, 2 and 3 for the predictions. The 'ignore' priority-Lasso adaptions perform better than the 'imputation' priority-Lasso adaptions in this setting. The best predictive performance is achieved with 'PL - ignore, zero' approach that has a median F-1 score of 0.88. As the mdd-sPLS always uses all feature-blocks for the prediction, the performance in this setting is the same as in the previous paragraph - median F-1 score of 0.81.

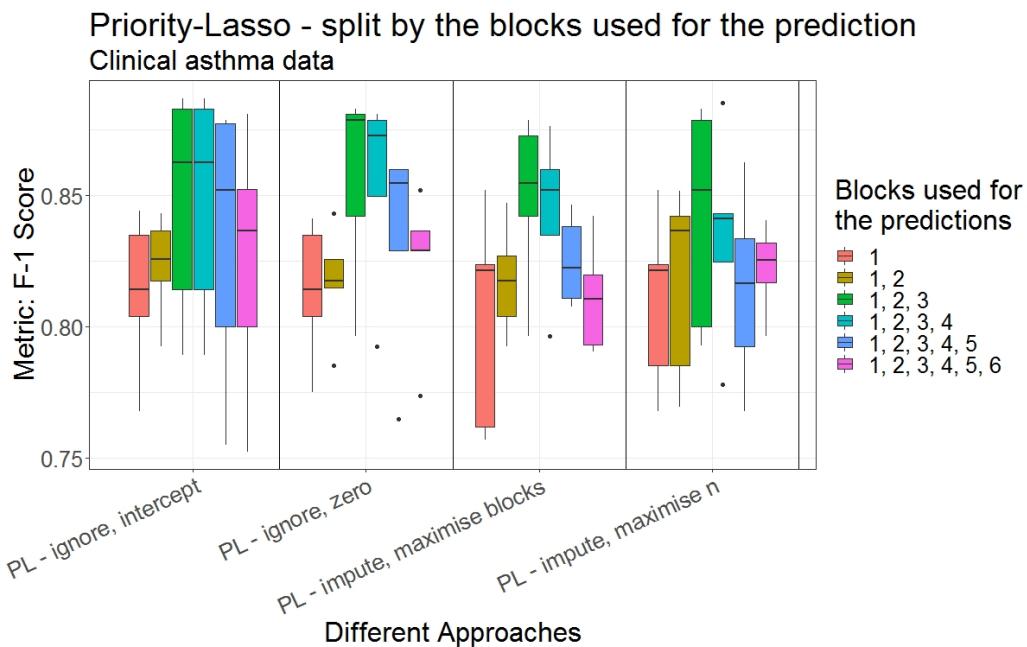


Figure 32: Results of the priority-Lasso adaptions on the clinical asthma data, when using subsets of blocks for the predictions.

Influence of different block priorities

One of the key features of the priority-Lasso is that the priority of the blocks can be set according to the needs of the user. In the previous two paragraphs, the priority of the blocks was set according to the number of missing observations in the feature-blocks. This does not necessarily reflect a professional opinion. Therefore the analysis of the approaches was repeated for a different order of the block priorities. The priority of the blocks was set according to the opinion of the project partner and set as follows (ascending order): cytokine expression data (ID 4), clinical routine diagnostics (ID 2),

questionnaire (ID 1), and lastly the allergen sensitisation (ID 3), the gene expression data I (ID 5) and the gene expression data II (ID 6) have the same priority. “With this block order, not all models with both gene expression data blocks could be estimated. Therefore, only the [...] block combinations where only one gene expression data block is included were analysed” [21]. Therefore one of the analyses is based on the feature-blocks 1, 2, 3, 4 and 5 and the other one based on 1, 2, 3, 4 and 6.

Block Priority [4, 2, 1, 3, 5]: In this part the predictive performance of the different priority-Lasso adaptions and the mdd-sPLS approach based on the feature-blocks 1, 2, 3, 4 and 5 are analysed - the priority is set to 4, 2, 1, 3, 5. The predictive performances of the different approaches are shown as boxplots in figure 33. The x-axis shows the different approaches and the y-axis the corresponding F-1 scores. For each approach, the F-1 scores are shown separately when the “predictions are based only on the block with the highest priority, based on the blocks with the two highest priorities and so on” [21].

The mdd-sPLS method always uses all feature-blocks for the prediction, such that there is only a single boxplot for this approach. The median F-1 score is around 0.81 and hence more or less the same as with the ‘naive block priority’. For the diverse priority-Lasso adaptions, the predictive performance based only on block 4 are rather bad. Adding the blocks 2 and 1 increases the predictive performance respectively for all approaches. The addition of block 3 does not change too much, while the addition of block 5 has two different effects. While the ‘ignore’ priority-Lasso adaptions can increase their median F-1 score, the median F-1 score of ‘imputation’ priority-Lasso adaptions is heavily reduced. The best predictive performance of the ‘ignore’ priority-Lasso adaptions is achieved on all five feature-blocks - the median F-1 score for ‘PL - ignore, zero’ is around 0.85 and slightly above the median F-1 score of the ‘PL - ignore, intercept’ approach. The ‘imputation’ priority-Lasso adaptions have the best predictive performance on the feature-blocks 4, 2, 1 and 3 - the predictive performance is the same for both approaches and the F-1 scores are only slightly below 0.85. Therefore the ‘PL - ignore, zero’ achieves the best performance in this setting. The differences between the predictive performance of the diverse priority-Lasso approaches is very low in this setting.

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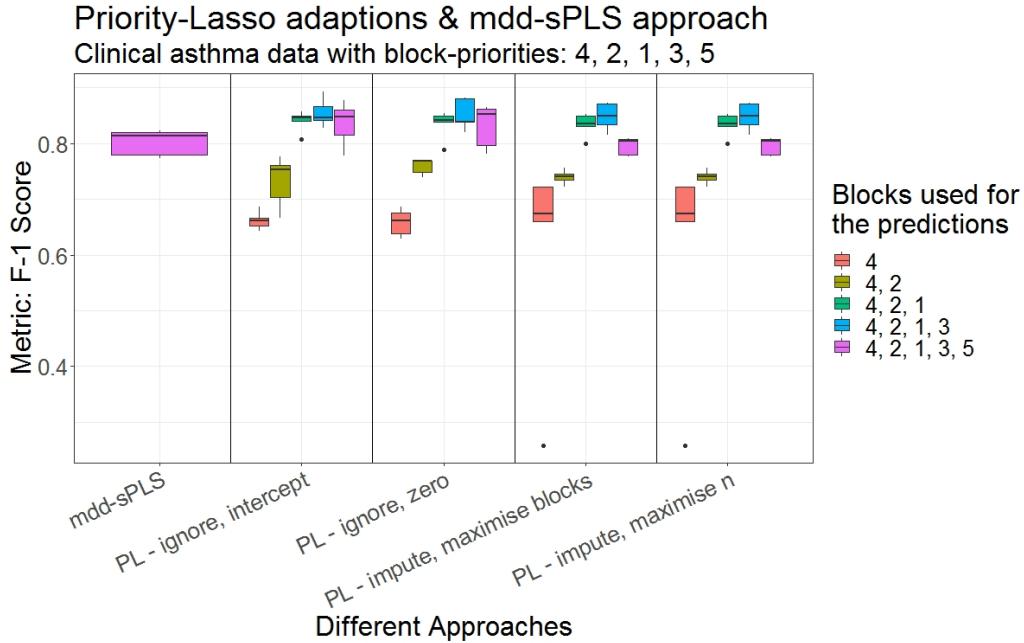


Figure 33: Results of the priority-Lasso adaptions and the mdd-sPLS approach on the clinical asthma data, when using subsets of blocks for the predictions and setting the block priorities according to the opinion of the project partner.

Block Priority [4, 2, 1, 3, 6]: In this part, the predictive performance of the different priority-Lasso adaptions and the mdd-sPLS approach based on the feature-blocks 1, 2, 3, 4 and 6 are analysed - the priority is set to 4, 2, 1, 3, 6. The predictive performances of the different approaches are shown as boxplots in figure 34. The x-axis shows the different approaches and the y-axis the corresponding F-1 scores. For each approach, the F-1 scores are shown separately when the “predictions are based only on the block with the highest priority, based on the blocks with the two highest priorities and so on” [21].

The mdd-sPLS method always uses all feature-blocks for the prediction, such that there is only a single boxplot for this approach. The median F-1 score is around 0.83 and therefore 0.2 higher than with the priority order [4, 2, 1, 3, 5] and also 0.2 better than with the naive block priority. For the diverse priority-Lasso adaptions, the predictive performance based only on block 4 is rather bad for all the different adaptions. The addition of the feature-blocks 2, 1 and 3 respectively leads to an improved median F-1 score for all the priority-Lasso adaptions. The addition of block 6 decreases the

predictive performance for all priority-Lasso adaptions. Therefore the best performance of the priority-Lasso adaptions is achieved based on the feature-blocks 4, 2, 1 and 3. Both 'ignore' priority-Lasso adaptions, as well as both 'imputation' priority-Lasso adaptions have a median F-1 score of around 0.85. Even though the predictive performance of the diverse approaches are quite similar, the 'PL - ignore, intercept' approach is minimally better than the other approaches regarding the median and mean F-1 score.

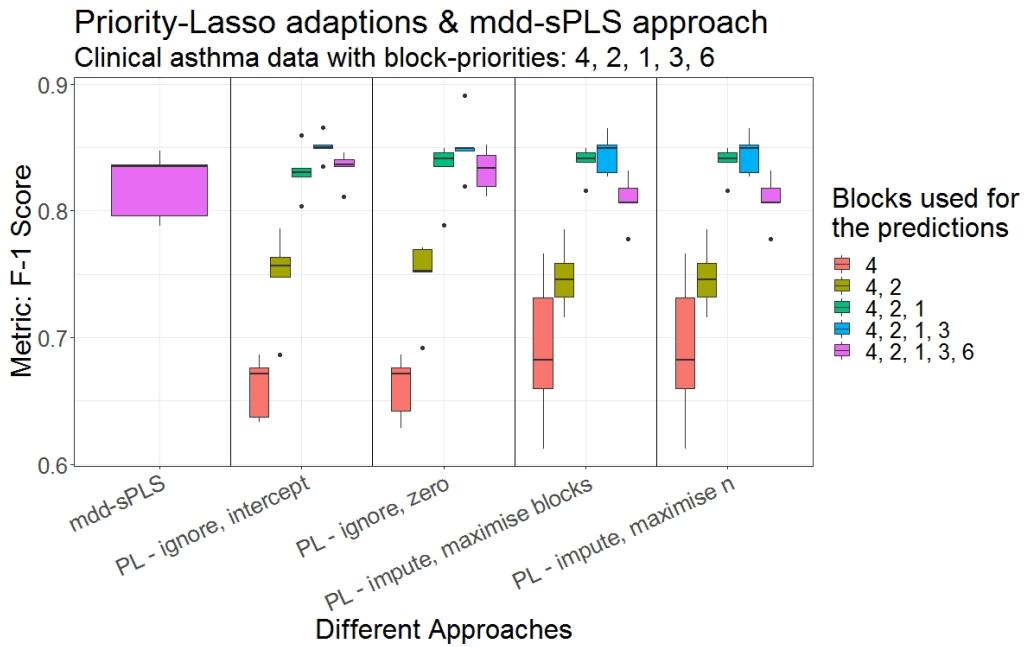


Figure 34: Results of the priority-Lasso adaptions and the mdd-sPLS approach on the clinical asthma data, when using subsets of blocks for the predictions and setting the block priorities according to the opinion of the project partner.

4.2.3 Comparison of the approaches

This chapter compares the different approaches from Hagenberg's thesis [21] and the different random forest based approaches from this thesis based on the clinical asthma data.

Only the best approaches of Hagenberg's and this thesis are used for the comparison on the clinical asthma data. The single-block approach had the best performance based on the 'questionnaire' feature-block. The block- and fold-wise approach had the best results with the 'F-1 Score' as weight metric. With the naive block order, the 'PL - ignore, intercept' approach had the best

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performance on the whole data-set and the 'PL - ignore, zero' approach with the feature-blocks 1, 2 and 3 for the prediction. With the adjusted block priorities, [4, 2, 1, 3, 5] the performance was the best for the 'PL - ignore, zero' approach on all five blocks. With the adjusted block priorities [4, 2, 1, 3, 6] the performance was the best for the 'PL - ignore, intercept' approach on the first four blocks. The mdd-sPLS approach had the best performance with the adjusted block priorities [4, 2, 1, 3, 6].

The predictive performances of the different approaches are shown as boxplots in figure 35. The x-axis shows the different approaches and the y-axis the corresponding F-1 scores. The approaches that are at the focus of this thesis are green, the priority-Lasso adaptions from Hagenberg's thesis [21] are purple and the mdd-sPLS approach from Hagenberg's thesis [21] is dark golden. For the single-block approach, the feature-block that was used is noted in the square brackets. For the block- and fold-wise approach the weight metric that was used for the aggregation is also noted in square brackets. For the different approaches from Hagenberg, the used feature-blocks for the prediction inclusive their priority is noted in square brackets. Among the approaches in figure 35, the block-wise approach has the worst performance - the median F-1 score is 0.79. The second worst approach is the single-block approach on the questionnaire feature-block with a median F-1 score of 0.81. The third worst performance is achieved by the complete-case approach - it has a median F-1 score of 0.83. The approaches 'mdd-sPLS [4, 2, 1, 3, 6]' and 'PL - ignore, intercept [1, 2, 3, 4, 5, 6]' are only slightly better than the complete-case approach and have a median slightly above 0.83. The fold-wise approach has a median F-1 score of 0.84 and is only slightly worse than the imputation approach that has a median F-1 score slightly above 0.84. The approaches 'PL - ignore, zero [4, 2, 1, 3, 5]' and 'PL - ignore, zero [4, 2, 1, 3]' both have a median F-1 score of 0.85, but the average F-1 score is considerably higher with the feature-blocks [4, 2, 1, 3]. The overall best performance has the approach 'PL - ignore, zero [1, 2, 3]'. The median F-1 score is close to 0.88 and therefore significantly better than of all other approaches. The results with the balanced accuracy / Matthews correlation coefficient (MCC) as metric are in the attachment in figure A-9 / A-10 - the results are about the same.

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Comparison of all Approaches

Clinical asthma data

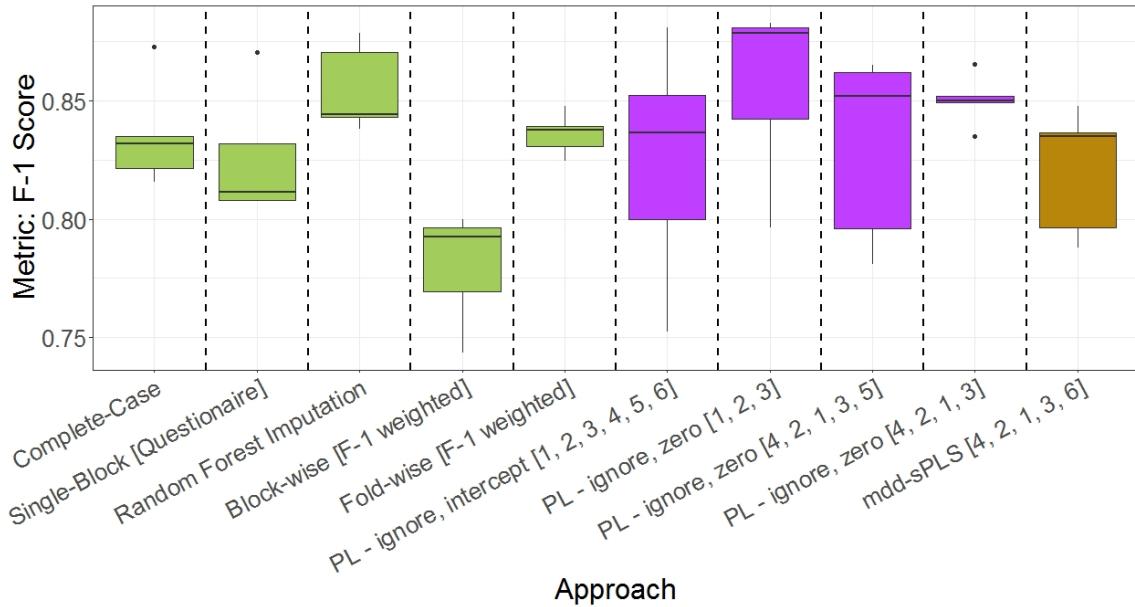


Figure 35: Comparison of the random forest adaptions, the priority-Lasso adaptions and the mdd-sPLS method on the clinical asthma data.

In summary, it can be said that the best performance was achieved by a priority-Lasso adaption that ignores three out of the six available feature-blocks for the prediction. The second and third best predictive performances were also achieved with priority-Lasso adaptions. The priority-Lasso adaptions, in general, perform better than the random forest adaptions on the clinical asthma data. Nevertheless, it has to be mentioned that the priority-Lasso adaptions highly depend on the priority of the blocks and the blocks that are used for the prediction. Without any prior knowledge about the data, the priority-Lasso adaptions need to be fitted with a naive block priority. The results on this naive block order can be much worse than with a block priority according to a professional opinion. Furthermore, it has to be mentioned that a 'selection bias' might have been introduced, as much more variants of the priority-Lasso have been tried out - especially with different block-priorities and different feature-blocks for the prediction - than with the random forest adaptions. The best random forest based approach on the clinical asthma data is the imputation approach, while the block-wise approach has by far the worst predictive performance. The second best random forest based approach was the fold-wise approach.

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5 Discussion and Conclusion

This chapter of the thesis discusses the results of the different approaches in the benchmark experiments, draws a conclusion to the approaches and gives an outlook for possible future research. Firstly, the results of the diverse random forest based approaches on the different data sources are compared and summarized. Then the diverse methods from Hagenberg's thesis [21] are compared and summarized, before the approaches from this thesis and the approaches from Hagenberg's thesis [21] are compared then. Subsequent a conclusion on the different approaches - advantages and potential disadvantages - is drawn and suggestions for future research are made.

The complete-case and single-block approach are the simplest random forest based approaches for data with block-wise missingness. In the diverse patterns of block-wise missingness in the TCGA data the single-block approach never has the best predictive performance in any test-situation, while the complete-case approach has the best performance in just a single test-situation. On the clinical asthma data these approaches are only better than the block-wise approach, whereby the block-wise approach had the worst predictive performance in this experiment. The imputation approach has the best predictive performance among all random forest based approaches in the clinical asthma data and on the TCGA data with block-wise missingness according to pattern 2. On the TCGA data with block-wise missingness according to pattern 1 and 3 the imputation approach has the second best results. The block-wise approach has its best predictive performance in all test-situations when using the 'F-1 Score' as weight metric for the aggregation of the block-wise predictions. This approach has the worst predictive performance on the clinical asthma data, but the best predictive performance on the TCGA data with block-wise missingness according to pattern 2 and 3. On the TCGA data with block-wise missingness according to pattern 1, the block-wise approach has a rather bad predictive performance and is only better than the single-block and complete-case approach. The fold-wise approach has its best predictive performance in all test-situations when using the 'F-1 Score' as weight metric for the combination of the fold-wise predictions. It is the second best random forest based approach on the clinical asthma data and the best approach on the TCGA data with block-wise missingness according to pattern 1. On the TCGA data with block-wise missingness according to pattern 2 and 3 the fold-wise approach has a bad predictive performance and is just better than the complete-case and single-block approach. In summary to the predictive performance of

the random forest based approaches, it can be said that the single-block and complete case approach have the worst predictive performances. The fold- and block-wise approach have a similar predictive performance. In settings, where the fold-wise approach performs good the block-wise approach performs bad and vice versa, such that one of these two approaches always resulted in a good predictive performance. Hence these two approaches seem to have a similar predictive power, whereby it depends on the test-situation which approach provides the better results. According to the benchmark experiments, the imputation approach has the best predictive performance among all the random forest based approaches.

The thesis of Hagenberg [21] contains diverse adaptions of the priority-Lasso and the mdd-sPLS method from Lorenzo et al. [48]. These approaches were evaluated on the clinical asthma data, whereby the diverse priority-Lasso approaches were evaluated with different block-priorities and different subsets of blocks used for the prediction. In all these diverse evaluations the 'priority-Lasso - impute' approaches ended up with worse results than the 'priority-Lasso - ignore' approaches. Hence the 'impute' approach with the priority-Lasso seems less promising than the 'ignore' approach. The two adaptions of the priority-Lasso 'ignore' approach have a very similar predictive performance. The results of the priority-Lasso approaches with the naive block-priority are the worst. When adjusting the priority of the blocks and/ or only using a subset of the available feature-blocks of the test-set for the prediction, the predictive performance of the priority-Lasso adaptions is increased. The best performance is achieved with the naive block priority, whereby only the first three feature-blocks are used for the prediction on the test-set. The mdd-sPLS approach always has a worse predictive performance than the 'priority-Lasso - ignore' approaches.

The approaches from Hagenberg's thesis [21] and the random forest based approaches that are at the focus of this thesis are compared on basis of the clinical asthma data. Among the random forest based approaches the 'imputation' and 'fold-wise' approach have the best predictive performance on the clinical asthma data - median F-1 score of ~ 0.84 . These approaches have a better predictive performance than the mdd-sPLS approach, as well as the best priority-Lasso approach on the naive block-priority [1, 2, 3, 4, 5, 6]. The priority-Lasso adaptions that outperform the 'imputation' and 'fold-wise' approach, were achieved with different block-priorities and using only a subset of available feature-blocks for the prediction. Hence the different priority-Lasso approaches were applied to the clinical asthma data with a wide range of possible settings. The best resulting priority-Lasso approaches outperform the best random forest based adaptions on the clinical asthma data. Compared to the priority-Lasso adaptions, the random

forest based adaptions were applied to clinical asthma data only once and no prior knowledge was needed. When fitting the priority-Lasso adaptions to the clinical asthma data without any prior knowledge, the predictive performance is actually worse than with the 'imputation' and 'fold-wise' approach. Hence it has to be mentioned that a 'selection bias' might have been introduced, as more variants of the priority-Lasso have been tried out - especially with different block-priorities and different feature-blocks for the prediction - than with the random forest adaptions. Therefore the choice of the approach highly depends on the prior knowledge of the data. If the user does not know which feature-blocks might be more important than others for the target-variable, the random forest based approaches seem to be the better choice. Especially the fold- and block-wise approach should be used in these situations, as these approaches use the OOB metric to estimate the predictive importance of a single fold/ feature-block and automatically rate the importance of the diverse folds/ feature-blocks. If the user knows which feature-blocks might be more important than others for the target variable the 'ignore' priority-Lasso adaptions can be recommended. With these approaches the user can set the priority of the feature-blocks according to their needs - this is not possible with the different random forest based adaptions.

In summary it can be said, that the priority-Lasso adaptions are the more appropriate approach if the user knows something about the relevance of the single feature-blocks. If the relevance of the single feature-blocks for the target variable is unknown, it is recommendable to apply the imputation-, fold- and block-wise approaches, as for these approaches no prior knowledge to the data is needed.

For further research it might be very interesting to compare the predictive performances of the random forest based approaches and the approaches from Hagenberg's thesis [21] not only on the clinical asthma data, but also on the TCGA data with its different patterns of block-wise missingness. Furthermore it might be interesting to combine the idea of the 'Block Forests' paper [14] with the fold-wise approach. With the fold-wise approach a random forest model is fit on basis of a single fold and multiple feature-blocks, whereby the split point selection is done without the incorporation of the block structure. Combining the idea of the fold-wise approach and the idea of incorporating the block structure for the split point selection from the 'Block Forests' paper [14] seems promising.

6 Attachment

6.1 Availability of data and materials

The whole repository of this master thesis can be found on 'Github':
https://github.com/rollator3000/MS_omics

It contains the whole code and sources that were used in this master thesis. A documentation and README - with a short documentation to the structure of the repository, short explanations to the different scripts and a brief summary of the different approaches - is also included.

The whole code was written in R - version 3.6.1. The used libraries and their corresponding versions are listed in the README.

The clinical asthma data is not part of the repository because of data protection regulations. For the TCGA data, only the subsetted data sets are part of the repository, as the original TCGA data sets are too big to be uploaded. If interested in the original TCGA data of this thesis contact me via e-mail: 'f.ludwigs@yahoo.de'

6.2 Acknowledgements

I want to thank Dr. rer. nat. Roman Hornung for his good supervision of the thesis, the provision of the processed TCGA data and for his constant feedback - especially during COVID-19.

I would also like to thank Matthias Assenmacher, who took care of my access to the LRZ servers and could always help quickly.

I also want to thank J. Hagenberg for the good communication and successful cooperation of our master theses.

6.3 Figures

Impurity functions (3), (4) and (5) for a binary target variable

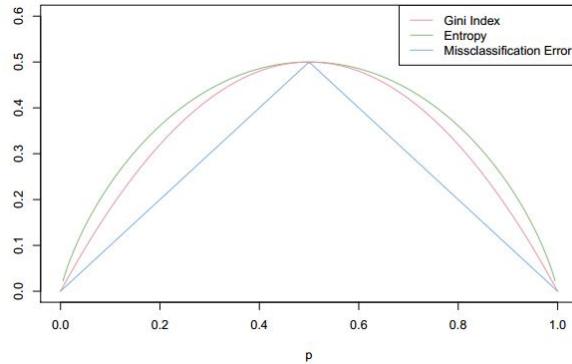


Figure A-1: The different impurity functions (3), (4) and (5) plotted for a given fraction of a binary target variable within any node N [[27], p. 13]

Predictive performance of a random forest model on the single feature-blocks of the 14 TCGA data sets

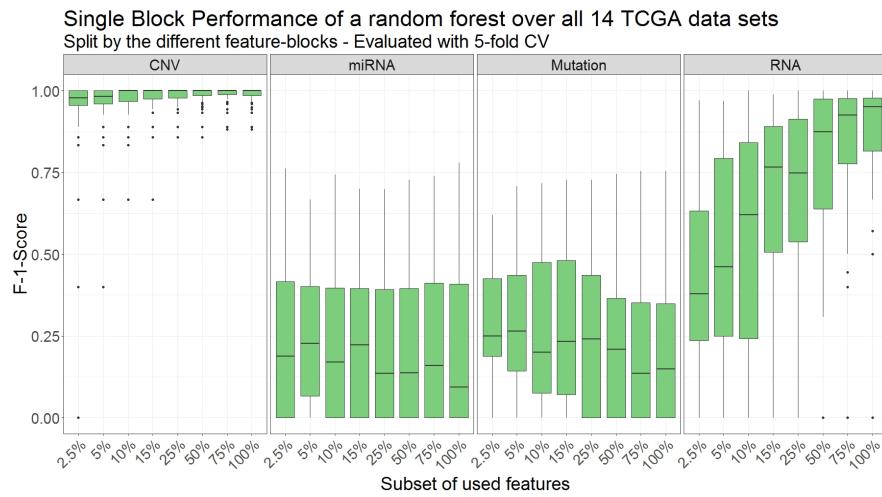


Figure A-2: The F-1 score of a random forest model evaluated on the single omics feature-blocks for a range of possible subsets. The results were obtained on basis of the 14 TCGA data sets.

Comparison of the approaches on the TCGA data with induced block-wise missingness according to pattern 1 - Balanced Accuracy

Comparison of all Approaches

TCGA - Pattern 1

Approach: █ Fold-wise █ Block-wise █ Imputation █ Single-Block █ Complete-Case

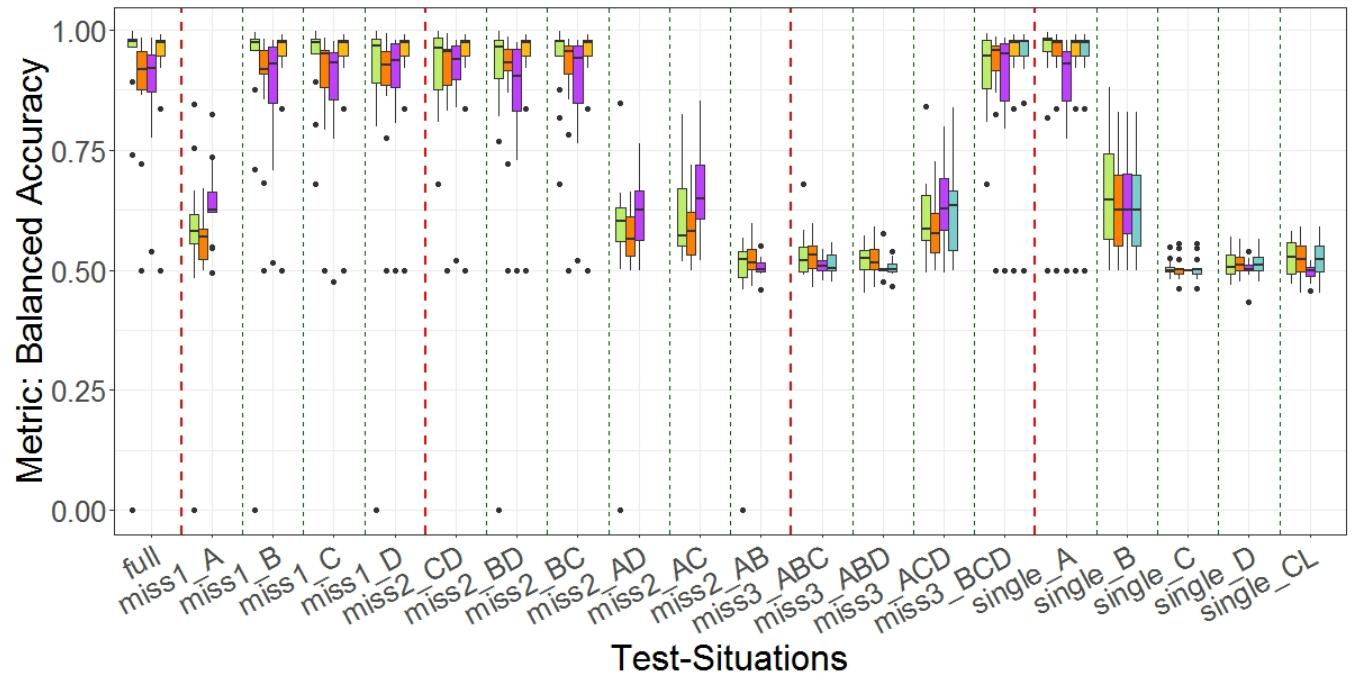


Figure A-3: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 1 - Balanced Accuracy metric

Comparison of the approaches on the TCGA data with induced block-wise missingness according to pattern 1 - MMC

Comparison of all Approaches

TCGA - Pattern 1

Approach: ■ Fold-wise ■ Block-wise ■ Imputation ■ Single-Block ■ Complete-Case

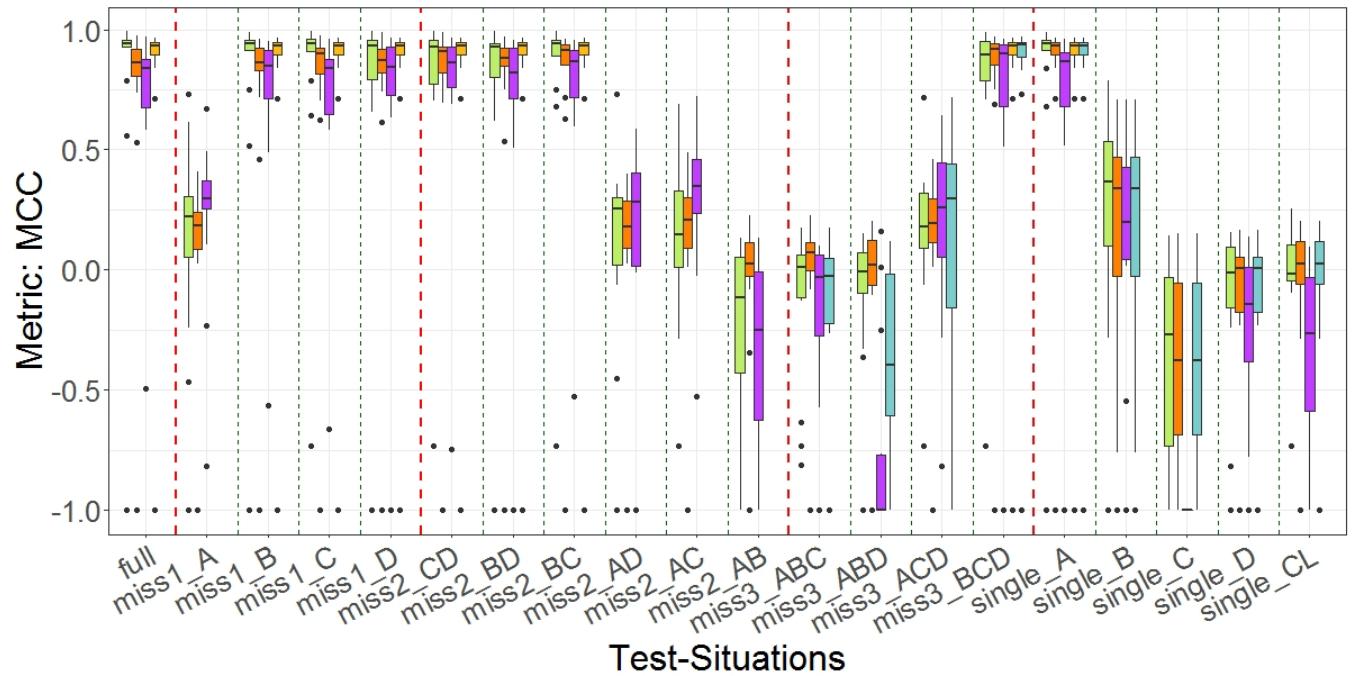


Figure A-4: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 1 - MMC metric

Comparison of the approaches on the TCGA data with induced block-wise missingness according to pattern 2 - Balanced Accuracy

Comparison of all Approaches

TCGA - Pattern 2

Approach: ■ Fold-wise ■ Block-wise ■ Imputation ■ Single-Block ■ Complete-Case

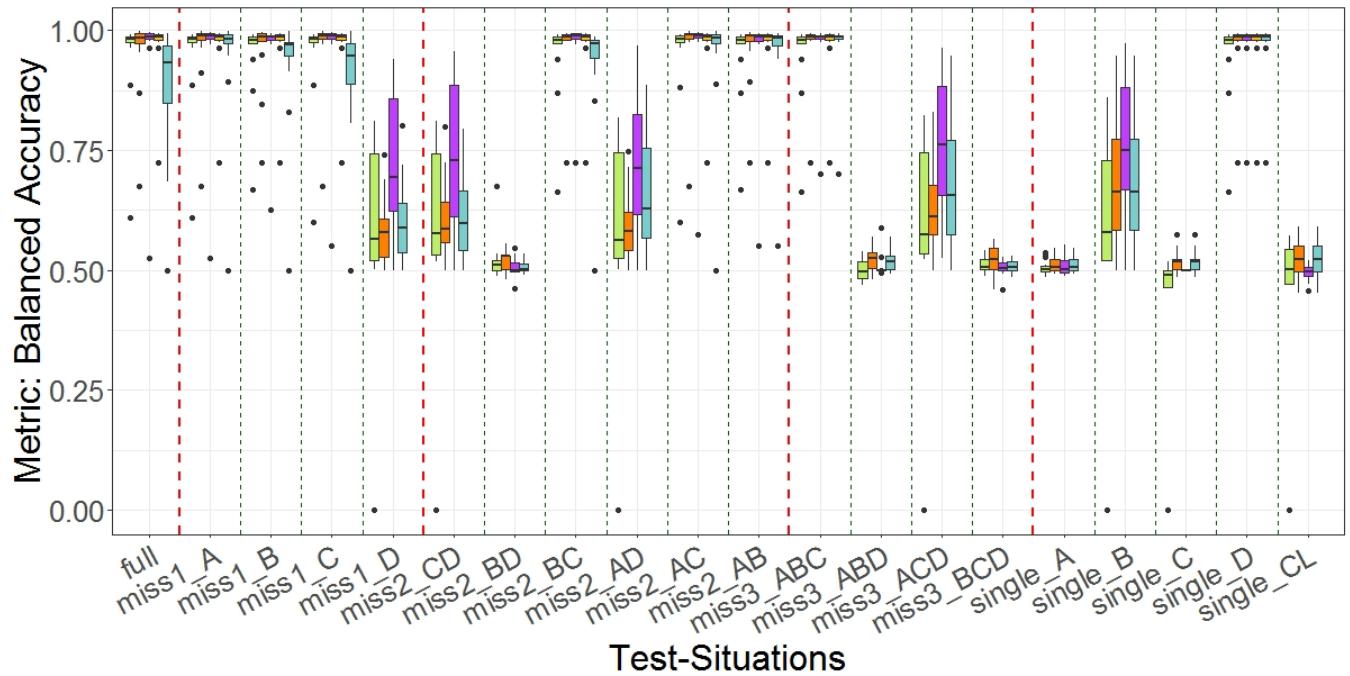


Figure A-5: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 2 - Balanced Accuracy metric

Comparison of the approaches on the TCGA data with induced block-wise missingness according to pattern 2 - MMC

Comparison of all Approaches

TCGA - Pattern 2

Approach:  Fold-wise  Block-wise  Imputation  Single-Block  Complete-Case

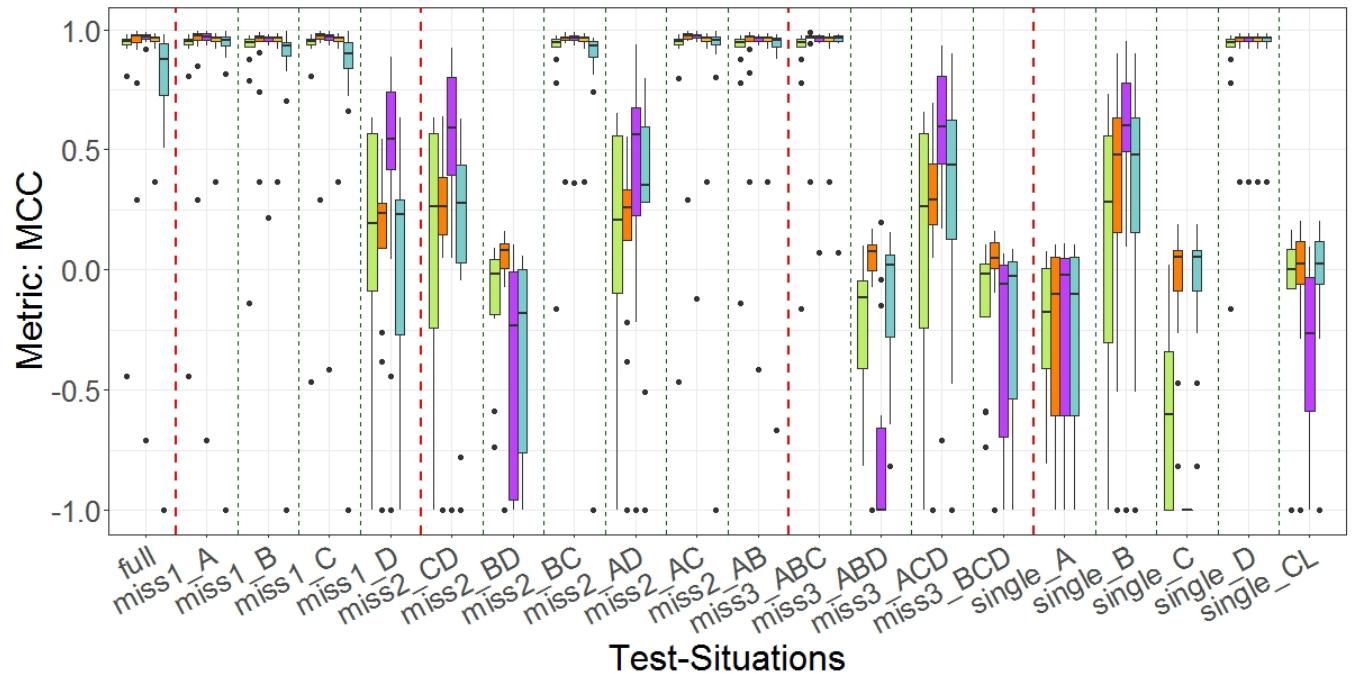


Figure A-6: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 2 - MMC metric

Comparison of the approaches on the TCGA data with induced block-wise missingness according to pattern 3 - Balanced Accuracy

Comparison of all Approaches

TCGA - Pattern 3

Approach: █ Fold-wise █ Block-wise █ Imputation █ Single-Block █ Complete-Case

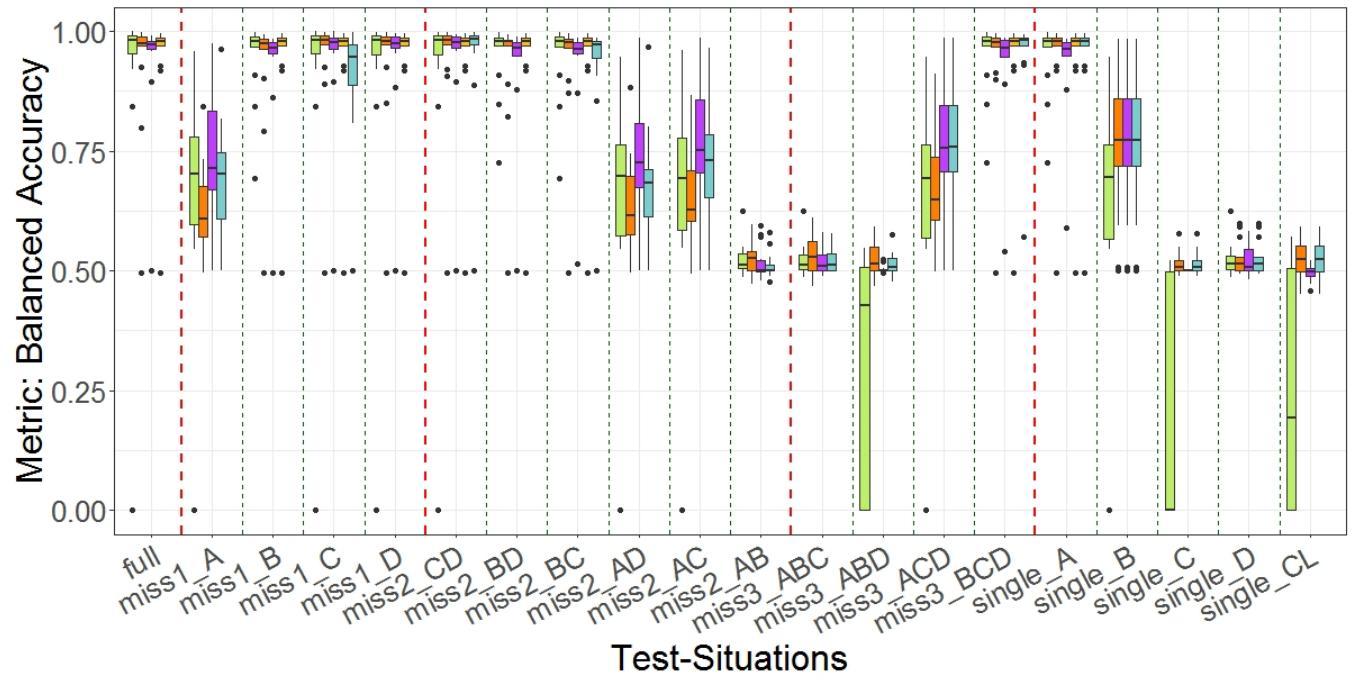


Figure A-7: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 3 - Balanced Accuracy metric

Comparison of the approaches on the TCGA data with induced block-wise missingness according to pattern 3 - MMC

Comparison of all Approaches

TCGA - Pattern 1

Approach: Fold-wise Block-wise Imputation Single-Block Complete-Case

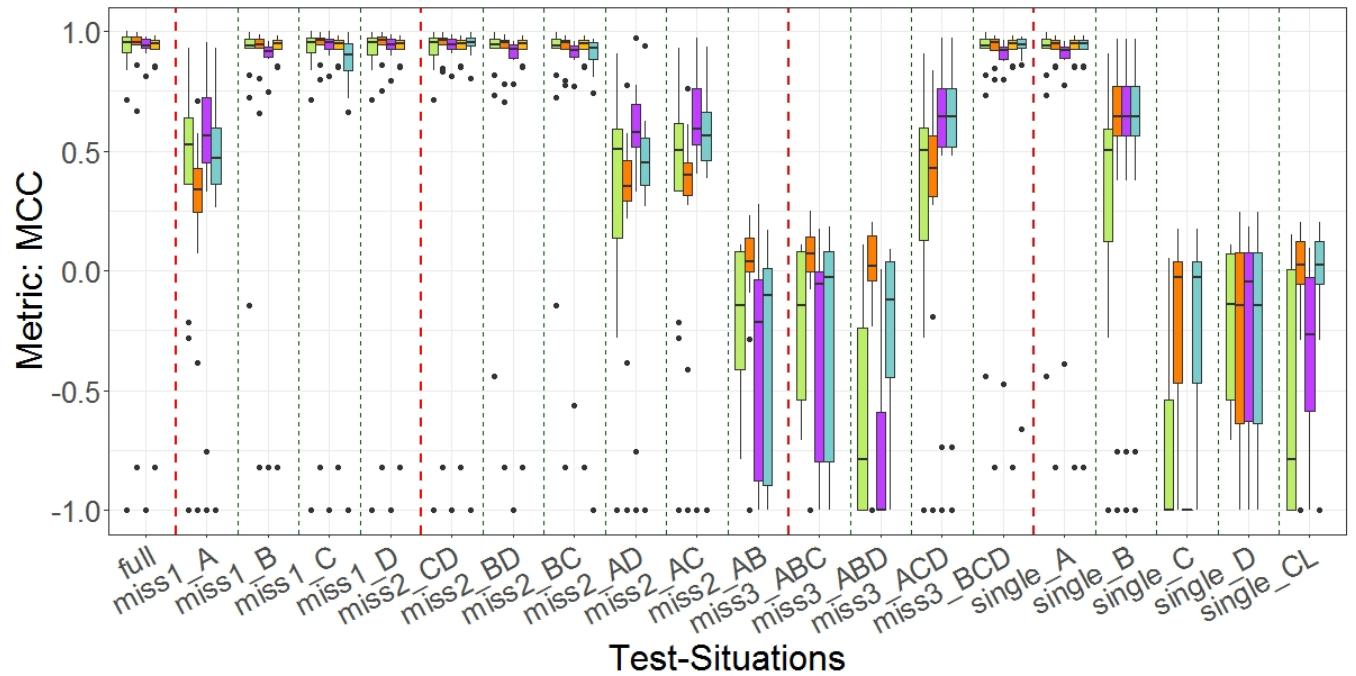


Figure A-8: Comparison of the different approaches on the TCGA data with induced block-wise missingness according to pattern 3 - MMC metric

Comparison of the approaches on the clinical asthma data - Balanced Accuracy

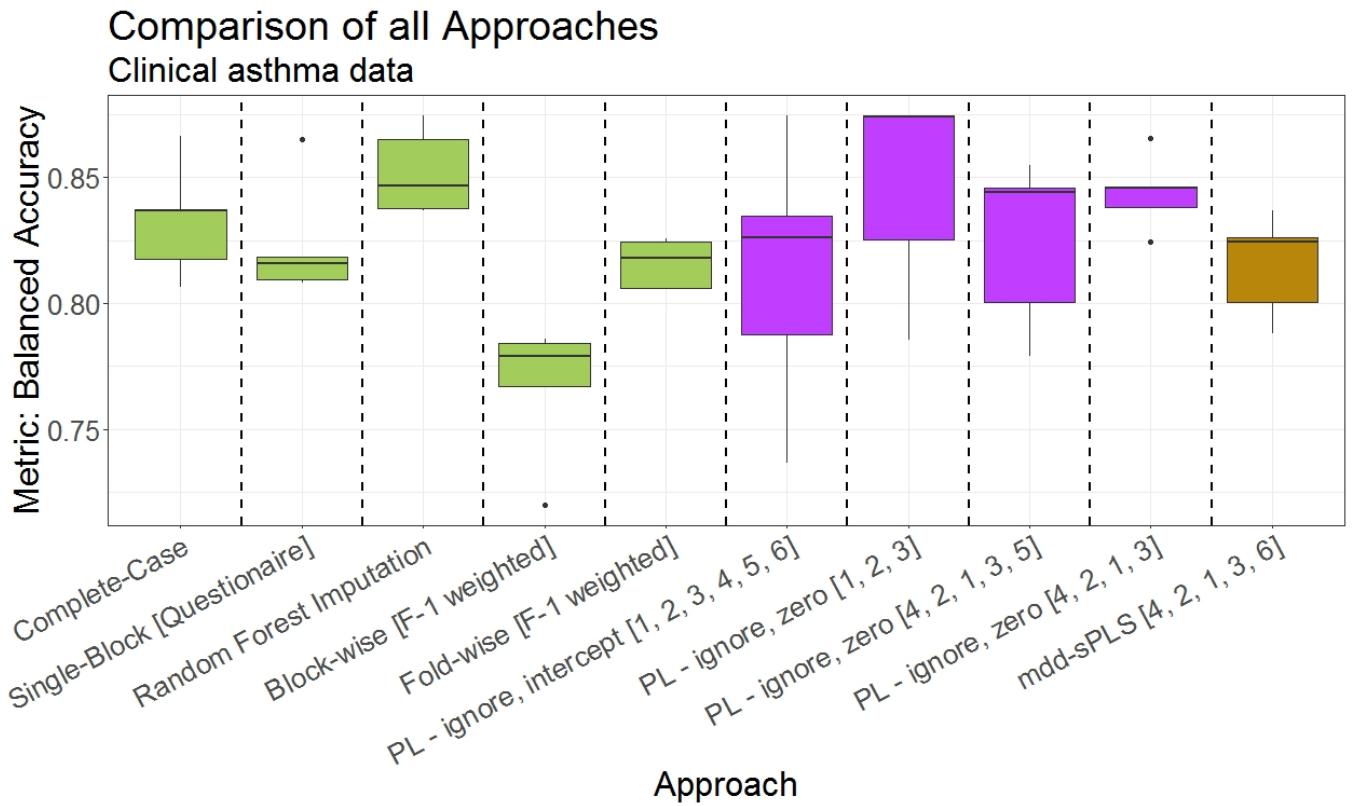


Figure A-9: Comparison of the random forest adaptions, the priority-Lasso adaptions and the mdd-sPLS method on the clinical asthma data - Balanced Accuracy

Comparison of the approaches on the clinical asthma data - MMC

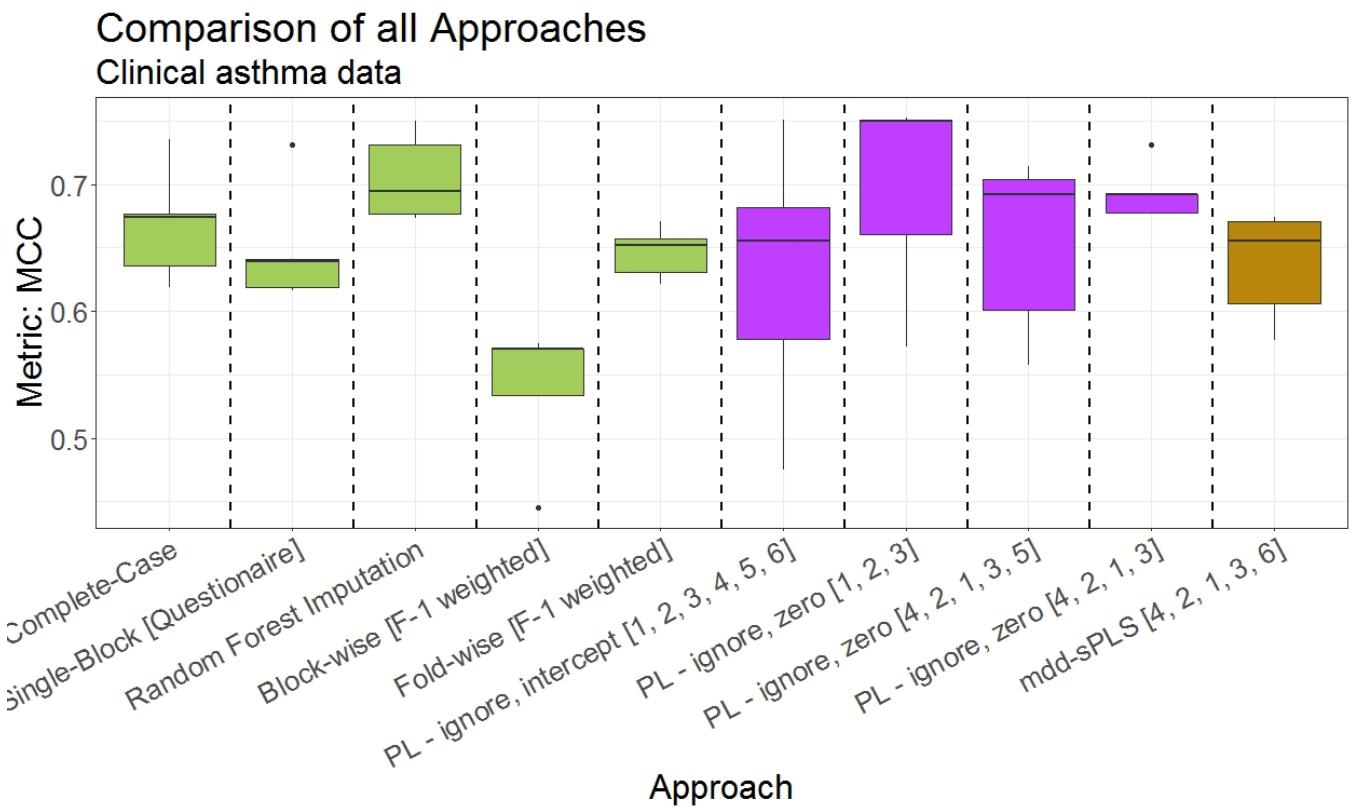


Figure A-10: Comparison of the random forest adaptions, the priority-Lasso adaptions and the mdd-sPLS method on the clinical asthma data - MMC

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