

HW0

January 7, 2020

1 CSE 152 Intro to Computer Vision Spring 2020 - Assignment 0

1.0.1 Instructor: David Kriegman

1.0.2 Assignment Published On: Wednesday, January 8, 2020

1.0.3 Due On: Thursday, January 16, 2020 11:59 pm

1.1 Instructions

- Review the academic integrity and collaboration policies on the course website.
- This assignment must be completed individually.
- All solutions must be written in this notebook
- Programming aspects of this assignment must be completed using Python in this notebook.
- If you want to modify the skeleton code, you can do so. This has been provided just to provide you with a framework for the solution.
- You may use python packages for basic linear algebra (you can use numpy or scipy for basic operations), but you may not use packages that directly solve the problem.
- If you are unsure about using a specific package or function, then ask the instructor and teaching assistants for clarification.
- You must submit this notebook exported as a pdf. You must also submit this notebook as .ipynb file.
- You must submit both files (.pdf and .ipynb) on Gradescope. You must mark each problem on Gradescope in the pdf.
- It is highly recommended that you begin working on this assignment early.
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1.2 Late policy - 10% per day late penalty after due date.

Welcome to CSE152 Intro to Computer Vision! This course gives you a comprehensive introduction to computer vision providing broad coverage including low level vision, inferring 3D properties from images, and object recognition. We will be using a variety of tools in this class that will require some initial configuration. To ensure smooth progress, we will setup the majority of the tools to be used in this course in this assignment. You will also practice some basic image manipulation techniques. Finally, you will need to export this Ipython notebook as pdf and submit it to Gradescope along with .ipynb file before the due date.

1.2.1 Piazza, Gradescope and Python

Piazza

Go to [Piazza](#) and sign up for the class using your ucsd.edu email account. You'll be able to ask the professor, the TAs and your classmates questions on Piazza. Class announcements will be made using Piazza, so make sure you check your email or Piazza frequently.

Gradescope

Every student will get an email regarding gradescope signup once enrolled in this class. All the assignments are required to be submitted to gradescope for grading. Make sure that you mark each page for different problems.

Python

We will use the Python programming language for all assignments in this course, with a few popular libraries (numpy, matplotlib). Assignments will be given in the format of browser-based Jupyter/Ipython notebook that you are currently viewing. We expect that many of you have some experience with Python and Numpy. And if you have previous knowledge in Matlab, check out the [numpy for Matlab users](#) page. The section below will serve as a quick introduction to Numpy and some other libraries.

1.3 Getting started with Numpy

Numpy is the fundamental package for scientific computing with Python. It provides a powerful N-dimensional array object and functions for working with these arrays.

1.3.1 Arrays

```
[ ]: import numpy as np

v = np.array([1, 0, 0])           # a 1d array
print("1d array")
print(v)
print(v.shape)                   # print the size of v
v = np.array([[1], [2], [3]])    # a 2d array
print("\n2d array")
print(v)
print(v.shape)                   # print the size of v, notice the difference
v = v.T                          # transpose of a 2d array

m = np.zeros([2, 3])             # a 2x3 array of zeros
v = np.ones([1, 3])              # a 1x3 array of ones
```

```

m = np.eye(3)           # identity matrix
v = np.random.rand(3, 1) # random matrix with values in [0, 1]
m = np.ones(v.shape) * 3 # create a matrix from shape

```

1.3.2 Array indexing

```

[:]: import numpy as np

m = np.array([[1, 2, 3], [4, 5, 6]]) # create a 2d array with shape (2, 3)
print("Access a single element")
print(m[0, 2])                      # access an element
m[0, 2] = 252                        # a slice of an array is a view into the
    → same data;
print("\nModified a single element")
print(m)                            # this will modify the original array

print("\nAccess a subarray")
print(m[1, :])                      # access a row (to 1d array)
print(m[1:, :])                     # access a row (to 2d array)
print("\nTranspose a subarray")
print(m[1, :].T)                    # notice the difference of the dimension
    → of resulting array
print(m[1:, :].T)                   # this will be helpful if you want to
    → transpose it later

# Boolean array indexing
# Given a array m, create a new array with values equal to m
# if they are greater than 0, and equal to 0 if they less than or equal 0

m = np.array([[3, 5, -2], [5, -1, 0]])
n = np.zeros(m.shape)
n[m > 0] = m[m > 0]
print("\nBoolean array indexing")
print(n)

```

1.3.3 Operations on array

Elementwise Operations

```

[:]: import numpy as np

a = np.array([[1, 2, 3], [2, 3, 4]], dtype=np.float64)
print(a * 2)                      # scalar multiplication
print(a / 4)                      # scalar division
print(np.round(a / 4))
print(np.power(a, 2))
print(np.log(a))

```

```

b = np.array([[5, 6, 7], [5, 7, 8]], dtype=np.float64)
print(a + b)           # elementwise sum
print(a - b)           # elementwise difference
print(a * b)           # elementwise product
print(a / b)           # elementwise division

```

Vector Operations

```

[:]: import numpy as np

a = np.array([[1, 2], [3, 4]])
print("sum of array")
print(np.sum(a))        # sum of all array elements
print(np.sum(a, axis=0)) # sum of each column
print(np.sum(a, axis=1)) # sum of each row
print("\nmean of array")
print(np.mean(a))       # mean of all array elements
print(np.mean(a, axis=0)) # mean of each column
print(np.mean(a, axis=1)) # mean of each row

```

Matrix Operations

```

[:]: import numpy as np

a = np.array([[1, 2], [3, 4]])
b = np.array([[5, 6], [7, 8]])
print("matrix-matrix product")
print(a.dot(b))        # matrix product
print(a.T.dot(b.T))

x = np.array([1, 2])
print("\nmatrix-vector product")
print(a.dot(x))         # matrix / vector product

```

1.3.4 Matplotlib

Matplotlib is a plotting library. We will use it to show the result in this assignment.

```

[:]: # this line prepares IPython for working with matplotlib
%matplotlib inline

import numpy as np
import matplotlib.pyplot as plt
import math

x = np.arange(-24, 24) / 24. * math.pi
plt.plot(x, np.sin(x))

```

```
plt.xlabel('radians')
plt.ylabel('sin value')
plt.title('dummy')

plt.show()
```

This brief overview introduces many basic functions from a few popular libraries, but is far from complete. Check out the documentations for [Numpy](#) and [Matplotlib](#) to find out more.

1.4 Problem 1 Image operations and vectorization (3pts)

Vector operations using numpy can offer a significant speedup over doing an operation iteratively on an image. The problem below will demonstrate the time it takes for both approaches to change the color of quadrants of an image.

The problem reads an image "house.png" that you will find in the assignment folder. Two functions are then provided as different approaches for doing an operation on the image.

Your task is to follow through the code and fill in the "piazza" function using instructions on Piazza.

```
[ ]: import numpy as np
import matplotlib.pyplot as plt
import copy
import time

img = plt.imread('house.png')          # read a JPEG image
print("Image shape", img.shape)        # print image size and color depth

plt.imshow(img)                        # displaying the original image
plt.show()

[ ]: def iterative(img):

    image = copy.deepcopy(img)          # create a copy of the image matrix
    for x in range(image.shape[0]):
        for y in range(image.shape[1]):
            if x < image.shape[0]/2 and y < image.shape[1]/2:
                image[x,y] = image[x,y] * [0,1,1]    #removing the red channel
            elif x > image.shape[0]/2 and y < image.shape[1]/2:
                image[x,y] = image[x,y] * [1,0,1]    #removing the green
                ↪channel
            elif x < image.shape[0]/2 and y > image.shape[1]/2:
                image[x,y] = image[x,y] * [1,1,0]    #removing the blue channel
            else:
                pass
    return image

def vectorized(img):
```

```

image = copy.deepcopy(img)
a = int(image.shape[0]/2)
b = int(image.shape[1]/2)
image[:a,:b] = image[:a,:b]*[0,1,1]
image[a,:b] = image[a,:b]*[1,0,1]
image[:a,b:] = image[:a,b:]*[1,1,0]

return image

```

```

[:]: # The code for this problem is posted on Piazza. Sign up for the course if you
      → have not. Then find
      # the function definition included in the post 'Welcome to CSE152' to complete
      → this problem.
      # This is the only cell you need to edit for this problem.
def piazza():
    pass

# Run the function
image_iterative, image_vectorized = piazza()

```

```

[:]: # Plotting the results in sepearate subplots

plt.subplot(1, 3, 1) # create (1x3) subplots, indexing from 1
plt.imshow(img)      # original image

plt.subplot(1, 3, 2)
plt.imshow(image_iterative)

plt.subplot(1, 3, 3)
plt.imshow(image_vectorized)

plt.show()           #displays the subplots

plt.imsave("multicolor_house.png",image_vectorized) #Saving an image

```

1.5 Problem 2 Further Image Manipulation (18pts)

In this problem you will solve a jigsaw puzzle using the 'jigsaw.png' provided with the homework. The solution of this jigsaw is the house image we used above. There are a total of 16 jigsaw pieces of size 128x128x3 which together make up the 512x512x3 image. Not only is the image of the house jumbled spatially, but some of the channels in jigsaw pieces are also permuted i.e. **RGB** to **BGR** and **GRB**.

Your task is to put all the pieces to their respective locations and correct the channel permutations. To achieve this task, you are required to complete the three helper functions that will be used to solve this puzzle. You are **NOT** allowed to use any function other than the three provided here. To get full credit, you need to write vectorized code

```
[ ]: def getTile(jigsaw, tile_idx):

    '''
    This function returns a particular jigsaw piece

    jigsaw      : 512x512x3 np.ndarray
    tile_idx    : tuple containing the (i,j) location of the piece

    piece       : 128x128x3 np.ndarray
    '''

    assert isinstance(tile_idx,tuple), 'tile index must be a tuple'
    assert len(tile_idx) == 2, 'tile index must specify the row and column_
    ↪index of the jigsaw'

    # Write your code here
    piece = np.zeros((128,128,3))    # modify piece
    return piece.copy()

def permuteChannels(tile, permutation):

    '''
    This function performs a permutation on channel

    tile        : 128x128x3 np.ndarray
    permutation  : tuple containing (i,j,k) channel indices
    tile_permuted : 128x128x3 np.ndarray
    '''

    assert tile.shape == (128,128,3), 'tile size should be 128x128x3'
    assert isinstance(permutation, tuple), 'permutation should be a tuple'
    assert len(permutation) == 3, 'There are only 3 channels'

    #Write your code here
    tile_permuted = tile            # modify tile_permuted
    return tile_permuted.copy()

def putTile(board, tile, tile_idx):

    '''
    This function put a jigsaw piece at a particular location on the board

    board : 512x512x3 np.ndarray
    tile  : 128x128x3 np.ndarray
    tile_idx : tuple containing the (i,j) location of the piece
    img   : 512x512x3 np.ndarray
    '''
```

```

    assert board.shape == (512,512,3), 'canvas size should be 512x512x3'
    assert tile.shape == (128,128,3), 'tile size should be 128x128x3'
    assert isinstance(tile_idx,tuple), 'tile index must be a tuple'
    assert len(tile_idx) == 2, 'tile index must specify the row and column'
    →index of the jigsaw'

    # Write your own code here
    img = board.copy()    # modify img
    return img

TILE_SIZE = 128
source = □
    →[(0,0),(0,1),(0,2),(0,3),(1,0),(1,1),(1,2),(1,3),(2,0),(2,1),(2,2),(2,3),(3,0),(3,1),(3,2),

# Fill in the target list with the corresponding piece locations
target = □
    →[(0,0),(0,1),(0,2),(0,3),(1,0),(1,1),(1,2),(1,3),(2,0),(2,1),(2,2),(2,3),(3,0),(3,1),(3,2),
#Fill in the respective channel permutations
channelPermutation = □
    →[(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2),
        □
    →(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2),(0,1,2)]

jigsaw = plt.imread('jigsaw.png')[:, :, :3]
board = np.ones(jigsaw.shape)

for i in range(16):
    tile = getTile(jigsaw, source[i])
    tile = permuteChannels(tile, channelPermutation[i])
    board = putTile(board, tile, target[i])

print("Jigsaw Puzzle")
plt.imshow(jigsaw)
plt.show()
print("Solution")
plt.imshow(board)
plt.show()

```

1.6 Mathematics Background Check (9pts)

The last portion of this homework, is a small quiz to ascertain your particular background in maths. Questions are from the topics of Linear Algebra, Probability and Calculus.

This portion is worth very little credits, and in order to obtain said credits, a solid attempt is required! If any of these topics/questions seem unfamiliar to you, then now would be a good time to brush up on some basics!

1.6.1 Part 1 - Linear Algebra (5pts)

1. Consider the following vectors,

$$\mathbf{v}_1 = \begin{bmatrix} 1 \\ -1 \\ 2 \end{bmatrix}, \mathbf{v}_2 = \begin{bmatrix} 0 \\ 1 \\ -1 \end{bmatrix}$$
$$\mathbf{v}_3 = \begin{bmatrix} 2 \\ -3 \end{bmatrix}, \mathbf{v}_4 = \begin{bmatrix} 0 \\ 1 \\ -5 \end{bmatrix}$$

1. What is $\mathbf{v}_1 + \mathbf{v}_2$?
 2. What is $\mathbf{v}_1 \bullet \mathbf{v}_2$?
 3. What is $\mathbf{v}_1 \times \mathbf{v}_2$?
 4. Express the operation in Part 1 in terms of matrix multiplication.
 5. Now explain why $\mathbf{v}_3 \bullet \mathbf{v}_4$ is not defined.
2. Consider the following matrices,
- $$A = \begin{bmatrix} 1 & 2 \\ 3 & 3 \end{bmatrix}, B = \begin{bmatrix} 1 & 2 \\ 2 & 4 \end{bmatrix}$$
1. What is the transpose of A? Is A Symmetric? Is B Symmetric?
 2. What is the rank of B?
 3. What is the determinant of A?
 4. What is the trace of A?
 5. Is B invertible? How many linearly independent columns does B have?
 6. What is the nullspace of B? What is its dimension?
 7. Write the general form of a 2x2 Rotation Matrix. Denote this as R.
 1. What is its determinant?
 2. What is $R^T R$
 8. Does the equation $Ax = b$ have a solution for all b ? Can you say the same for the equation $Bx = b$?
3. Consider the following matrix
- $$C = \begin{bmatrix} 1 & 6 \\ 1 & 2 \end{bmatrix}$$
1. What are the eigenvalues and eigenvectors of C?

1.6.2 Part 2 - Calculus (3 pts)

1. Note the following definitions and answer the questions below.

$$\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}, f(\mathbf{x}) = x_1^2 x_2, \quad g(y) = y^3 + 2y^2, \quad h(x) = \sin(x)$$

1. What is the gradient of $f(\mathbf{x})$?
2. What is the Hessian of $f(\mathbf{x})$?
3. What are the local minimum and maxima of $g(y)$?
4. What is the derivative of $(h \circ g)(y)$ w.r.t y ?

1.6.3 Part 3 - Probability (1 pts)

1. Let A and B be two random events with $P(A) = x, P(B) = y$.
 1. Assume A and B are independent events. Now answer the following questions.
 1. What is $P(A|B)$?
 2. What is $P(AB)$?
 3. What is $P(A \cup B)$?
 2. Now answer the same questions given that A and B are mutually exclusive.
2. Let X be a random event with $E(X) = 0.2$ and $E(X^2) = 0.5$. What is the Variance of X ?

** Submission Instructions **

Remember to submit a pdf version of this notebook to Gradescope. Please make sure the contents in each cell are clearly shown in your final pdf file. To convert the notebook to PDF: 1. You can find the export option at File \rightarrow Download as \rightarrow PDF via LaTeX 2. You can first export as HTML and then convert to PDF