# Active Learning by Querying Informative and Representative Examples

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#### Abstract

Most active learning approaches select either informative or representative unlabeled instances to query their labels. Although several active learning algorithms have been proposed to combine the two criterions for query selection, they are usually ad hoc in finding unlabeled instances that are both informative and representative. We address this challenge by a principled approach, termed QUIRE, based on the min-max view of active learning. The proposed approach provides a systematic way for measuring and combining the informativeness and representativeness of an instance. Extensive experimental results show that the proposed QUIRE approach outperforms several state-of -the-art active learning approaches.

## 1 Paper Body

In this work, we focus on the pool-based active learning, which selects an unlabeled instance from a given pool for manually labeling. There are two main criteria, i.e., informativeness and representativeness, that are widely used for active query selection. Informativeness measures the ability of an instance in reducing the uncertainty of a statistical model, while representativeness measures if an instance well represents the overall input patterns of unlabeled data [16]. Most active learning algorithms only deploy one of the two criteria for query selection, which could significantly limit the performance of active learning: approaches favoring informative instances usually do not exploit the structure information of unlabeled data, leading to serious sample bias and consequently undesirable performance for active learning; approaches favoring representative instances may require querying a relatively large number of instances before the optimal decision boundary is found. Although several active learning algorithms [19, 8, 11] have been proposed to find the unlabeled instances that are both informative and representative, they are usually ad hoc in measuring the informativeness and representativeness of an instance, leading to suboptimal performance. In

this paper, we propose a new active learning approach by QUerying Informative and Representative Examples (Q UIRE for short). The proposed approach is based on the min-max view of active learning [11], which provides a systematic way for measuring and combining the informativeness and the representativeness. The interesting feature of the proposed approach is that it measures both the informativeness and representativeness of an instance by its prediction uncertainty: the informativeness of an instance x is measured by its prediction uncertainty based on the labeled data, while the representativeness of x is measured by its prediction uncertainty based on the unlabeled data. The rest of this paper is organized as follows: Section 2 reviews the related work on active learning; Section 3 presents the proposed approach in details; experimental results are reported in Section 4; Section 5 concludes this work with issues to be addressed in the future. 1

- (a) A binary classification (b) An approach favoring (c) An approach favoring problem representative instances informative instances
  - (d) Our approach

Figure 1: An illustrative example for selecting informative and representative instances  $\,$ 

2

Related Work

Querying the most informative instances is probably the most popular approach for active learning. Exemplar approaches include query-by-committee [17, 6, 10], uncertainty sampling [13, 12, 18, 2] and optimal experimental design [9, 20]. The main weakness of these approaches is that they are unable to exploit the abundance of unlabeled data and the selection of query instances is solely determined by a small number of labeled examples, making it prone to sample bias. Another school of active learning is to select the instances that are most representative to the unlabeled data. These approaches aim to exploit the cluster structure of unlabeled data [14, 7], usually by a clustering method. The main weakness of these approaches is that their performance heavily depends on the quality of clustering results [7]. Several active learning algorithms tried to combine the informativeness measure with the representativeness measure for finding the optimal query instances. In [19], the authors propose a sampling algorithm that exploits both the cluster information and the classification margins of unlabeled instances. One limitation of this approach is that since clustering is only performed on the instances within the classification margin, it is unable to exploit the unlabeled instances outside the margin. In [8], Donmez et al. extended the active learning approach in [14] by dynamically balancing the uncertainty and the density of instances for query selection. This approach is ad hoc in combining the measure of informativeness and representativeness for query selection, leading to suboptimal performance. Our work is based on the min-max view of active learning, which was first proposed in the study of batch mode active learning [11]. Unlike [11] which measures the representativeness of an instance by its similarity to the remaining unlabeled instances, our proposed measure of representativeness takes into account the cluster structure of unlabeled instances as well as the class assignments of the labeled examples.

leading to a better selection of unlabeled instances for active learning.

3

QUIRE: QUery Informative and Representative Examples

We start with a synthesized example that illustrates the importance of querying instances that are both informative and representative for active learning. Figure 1 (a) shows a binary classification problem with each class represented by a different legend. We examine three different active learning algorithms by allowing them to sequentially select 15 data points. Figure 1 (b) and (c) show the data points selected by an approach favoring informative instances (i.e., [18]) and by an approach favoring representative instances (i.e., [7]), respectively. As indicated by Figure 1 (b), due to the sample bias, the approach preferring informative instances tends to choose the data points close to the horizontal line, leading to incorrect decision boundaries. On the other hand, as indicated by Figure 1 (c), the approach preferring representative instances is able to identify the approximately correct decision boundary but with a slow convergence. Figure 1 (d) shows the data points selected by the proposed approach that favors data points that are both informative and representative. It is clear that the proposed algorithm is more efficient in finding the accurate decision boundary than the other two approaches. We denote by  $D = \{(x1, y1), (x2, y2), ? ? \}$ ? , (xnl , ynl ), xnl +1 , ? ? ? , xn } the training data set that consists of nl labeled instances and nu=n? nl unlabeled instances, where each instance xi= [xi1, xi2, ???, xid]? is a vector of d dimension and yi?  $\{?1, +1\}$  is the class label of xi. 2

Active learning selects one instance xs from the pool of unlabeled data to query its class label. For convenience, we divide the data set D into three parts: the labeled data Dl , the currently selected instance xs , and the rest of the unlabeled data Du . We also use Da = Du ? {xs} to represent all the unlabeled instances. We use y = [yl , ys , yu ] for the class label assignment of the entire data set, where yl , ys and yu are the class labels assigned to Dl , xs and Du , respectively. Finally, we denote by ya = [ys , yu ] the class assignment for all the unlabeled instances. 3.1

The Framework

To motivate the proposed approach, we first re-examine the margin-based active learning from the viewpoint of min-max [11]. Let f? be a classification model trained by the labeled examples, i.e., nl X ? f? = arg min — f — 2H + ?(yi , f (xi )), (1) 2 f? H i=1 where H is a reproducing kernel Hilbert space endowed with kernel function ?(?, ?) : Rd ? Rd ? R. ?(z) is the loss function. Given the classifier f? , the margin-based approach chooses the unlabeled instance closest to the decision boundary, i.e., s? = arg min — f? (xs )—. (2) nl fs?n

It is shown in the supplementary document that this criterion can be approximated by s? = arg min L(Dl, xs),

```
(4)
We can also write Eq. 3 in a minimax form min where
A(Dl, xs) =
max A(Dl, xs), nl; s?n ys =?1 nl X ? min —f —2H + ?(yi, f (xi)) f ?H 2
i=1
+ ?(ys, f (xs)).
```

In this min-max view of active learning, it guarantees that the selected instance xs will lead to a small value for the objective function regardless of its class label ys . In order to select queries that are both informative and representative, we extend the evaluation function L(Dl , xs ) to include all the unlabeled data. Hypothetically, if we know the class assignment yu for the unselected unlabeled instances in Du , the evaluation function can be modified as n X ? L(Dl , Du , yu , xs ) = max min —f —2H + ?(yi , f (xi )). (5) ys =?1 f ?H 2 i=1 The problem is that the class assignment yu is unknown. According to the manifold assumption [3], we expect that a good solution for yu should result in a small value of L(Dl , Du , yu , xs ). We therefore approximate the solution for yu by minimizing L(Dl , Du , yu , xs ), which leads to the following evaluation function for query selection: b l , D u , xs ) = L(D min L(Dl , Du , yu , xs ) (6) yu ?{?1}nu ?1

The Solution

y? Ly.

For computational simplicity, for the rest of this work, we choose a quadratic loss function, i.e., ?(y, yb) = (y ? yb)2 /21. It is straightforward to show n 1 1X ? (yi ? f (xi ))2 = y? Ly, min —f —2H + f ?H 2 2 i=1 2 1 Although quadratic loss may not be ideal for classification, it does yield competitive classification results when compared to the other loss functions such as hinge loss [15].

```
where L=(K+?I)?1 and K=[?(xi\ ,\,xj\ )]n?n is the kernel matrix of size n ? n. Thus, the b l , Du , xs ) is simplified as evaluation function L(D\ b\ l , Du , xs ) = L(D\ max\ min\ yu\ ?\{?1,+1\}nu\ ?1\ ys\ ?\{?1,+1\}
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Our goal is to efficiently compute the above quantity for each unlabeled instance. For the convenience of presentation, we refer to by subscript u the rows/columns in a matrix M for the unlabeled instances in Du , by subscript l the rows/columns in M for labeled instances in Dl , and by subscript s the row/column in M for the selected instance. We also refer to by subscript a the rows/columns in M for all the unlabeled instances (i.e., Du ?  $\{xs\}$ ). Using these conventions, we rewrite the objective y? Ly as y? Ly = yl Ll,l yl + Ls,s + yuT Lu,u yu + 2yuT (Lu,l yl + Lu,s ys) + 2ys yl? Ll,s . Note that since

the above objective function is concave (linear) in ys and convex (quadratic) in yu, we can switch the maximization of yu with the minimization of ys in (7). By relaxing yu to continuous variables, the solution to minyu y? Ly is given by bu = 2 Lu, = 2 Lu

b l , Du , xs ): leading to the following expression for the evaluation function  $L(D\ b\ l$  , Du , xs ) = Ls,s + yT Ll,l yl + max{2ys Ls,l yl L(D l ys}

```
(8)
(9)
?(Lu,l yl + Lu,s ys )T Lu,u ?1 (Lu,l yl + Lu,s ys )}
det(La,a )
? Ls,s ? + 2 Ls,l ? Ls,u L?1 u,u Lu,l yl , Ls,s
where the last step follows the relation
```

A11 A12 = det(A22) det A11? A12 A?1 det 22 A21. A21 A22

Note that although yu is relaxed to real numbers, according to our empirical studies, we find that in most cases, yu falls between ?1 and +1. b l , Du , xs ) essentially consists of two components: Ls,s ? Remark. The evaluation function L(D det(La,a )/Ls,s and —(Ls,l ? Ls,u L?1 u,u Lu,l )yl —. Minimizing the first component is equivalent to minimizing Ls,s because La,a is independent from the selected instance xs . Since L = (K +?I)?1 , we have

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?1 Kl,l Kl,u Kl,s Ls,s = Ks,s ? (Ks,l , Ks,u ) Ku,l Ku,u Ku,s
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 $1\ 1\ Kl,l\ Kl,u\ Kl,s\ 1+\ (Ks,l\ ,Ks,u\ )$  . ? Ku,l Ku,u Ku,s Ks,s Ks,s Therefore, to choose an instance with small Ls,s , we select the instance with large self-similarity Ks,s . When self-similarity Ks,s is a constant, this term will not affect query selection. To analyze the effect of the second component, we approximate it as:

```
? 2 —Ls,l yl — + 2 Ls,u L?1
2 Ls,l ? Ls,u L?1 u,u Lu,l yl u,u Lu,l yl bu —. ? 2—Ls,l yl — + 2—Ls,u y (10)
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The first term in the above approximation measures the confidence in predicting xs using only labeled data, which corresponds to the informativeness of xs . The second term measures the prediction confidence using only the predicted labels of the unlabeled data, which can be viewed as the measure of representativeness. This is because when xs is a representative instance, it is expected to share a large similarity with many of the unlabeled instances in the pool. As a result, the prediction bu . If we for xs by the unlabeled data in Du is decided by the average of their assigned class labels y assume that the classes are evenly distributed over the unlabeled data, we should expect a low confidence in predicting the class label for xs by unlabeled data. It is important to note that unlike the 4

Algorithm 1 The Q UIRE Algorithm Input: D: A data set of n instances Initialize: Dl = ?; nl = 0 % no labeled data is available at the very beginning Du = D; nu = n % the pool of unlabeled data Calculate K repeat Calculate L?1 a,a using Proposition 2 and det(La,a) for s = 1 to nu do Calculate L?1 uu according to Theorem 1 b Calculate L(Dl , Du , xs ) using Eq. 9 end for b l , Du , xs? ) and query its label ys? Select the xs? with the smallest L(D Dl = Dl? (xs? , ys? ); Du = Du xs? until the number of queries or the required accuracy is reached

existing work that measures the representativeness only by the cluster structure of unlabeled data, bu , which essentially combines the cluster our proposed measure of representativeness depends on y structure of unlabeled data with the class assignments of labeled data. Given high-dimensional data, there could be many possible cluster structures that are consistent with the unlabeled data and it is unclear which one is consistent with the target classification problem. It is therefore critical to take into account the label information when exploiting the cluster structure of unlabeled data. 3.3

Efficient Algorithm

b l , Du , xs ) in Eq. 9 requires computing L?1 Computing the evaluation function  $L(D\ u,u$  for every unlabeled instance xs , leading to high computational cost when the number of unlabeled instances is very large. The theorem below allows us to improve the computational efficiency dramatically. ?1

```
Theorem 1. Let Ls,s Ls,u a ?b? L?1 = = . a,a Lu,s Lu,u ?b D We have 1 ? L?1 u,u = D ? bb . a
```

The proof can be found in the supplementary document. As indicated by Theorem 1, we only need ?1 ?1 to compute L?1 a,a once; for each xs , its Lu,u can be computed directly from La,a . The following ?1 proposition allows us to simplify the computation for La,a . ?1 Proposition 2. L?1 Kl,a a,a = (?Ia + Ka,a ) ? Ka,l (?Il + Kl,l )

Proposition 2 follows directly from the inverse of a block matrix. As indicated by Proposition 2, we only need to compute (?I + Kl,l)?1. Given that the number of labeled examples is relatively small compared to the size of unlabeled data, the computation of L?1 a,a is in general efficient. The pseudo-code of Q UIRE is summarized in Algorithm 1. Excluding the time for computing the kernel matrix, the computational complexity of our algorithm is just O(nu).

4 Experiments

We compare Q UIRE with the following five baseline approaches: (1) R ANDOM: randomly select query instances, (2) M ARGIN: margin-based active learning [18], a representative approach which selects informative instances, (3) C LUSTER: hierarchical-clustering-based active learning [7], a representative approach that chooses representative instances, (4) IDE: active learning that selects informative and diverse examples [11], and (5) DUAL: a dual strategy for active learning that exploits both informativeness and representativeness for query selection. Note that the original algorithm in [11] is designed for batch mode active learning. We turn it into an active learning algorithm that selects a single instance in each iteration by setting the parameter k=1. 5

```
70 Random Margin Cluster IDE DUAL Quire
60 50 0
20
40
60
80 70 Random Margin Cluster IDE DUAL Quire
60 50 0
80
```

```
20
80 70
Random Margin Cluster IDE DUAL Quire
100
200
300
400
500
600
Number of queried examples
(c) g241n
15
20
25
70 60
Random Margin Cluster IDE DUAL Quire
30
0
50
(d) isolet
Accuracy (%)
80 70 60
Random Margin Cluster IDE DUAL Quire
50\ 40\ 30
40
50
50
90
70
Random Margin Cluster IDE DUAL Quire
60
20
30
40
50
80 70
Random Margin Cluster IDE DUAL Quire
60 50
60
0
10
Accuracy (%)
Random Margin Cluster IDE DUAL Quire
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```
60\ 50\ 40
Number of queried examples
90
90
80 Random Margin Cluster IDE DUAL Quire
60
0
20
40
60
30
40
50
60
(i) letterEvsF
100
70
20
Number of queried examples
(h) letterDvsP
70
150
(f) vehicle
80
10
100
Number of queried examples
Number of queried examples
80
(j) letterIvsJ
90
50 0
60
90
30
50
300
100
(g) wdbc
20
250
Random Margin Cluster IDE DUAL Quire
```

```
60
100
Number of queried examples
200
70
(e) titato
90
20
150
80
Number of queried examples
100
10
100
Accuracy (%)
10
80
80
100
Accuracy (%)
5
90
90
Number of queried examples
Accuracy (%)
50
100
Accuracy (%)
Accuracy (%)
Accuracy (%)
90
Accuracy (%)
Random Margin Cluster IDE DUAL Quire
100
100
0
60
70
(b) digit1
(a) austra
0
40
80
```

```
Number of queried examples
Number of queried examples
Accuracy (%)
Accuracy (%)
Accuracy (%)
90
80
80.70
Random Margin Cluster IDE DUAL Quire
60 50 0
Number of queried examples
(k) letterMvsN
10
20
30
40
50
60
Number of queried examples
(l) letterUvsV
```

Figure 2: Comparison on classification accuracy

Twelve data sets are used in our study and their statistics are shown in the supplementary document. Digit1 and g241n are benchmark data sets for semi-supervised learning [5]; austria, isolet, titato, vechicle, and wdbc are UCI data sets [1]; letter is a multi-class data set [1] from which we select five pairs of letters that are relatively difficult to distinguish, i.e., D vs P, E vs F, I vs J, M vs N, U vs V, and construct a binary class data set for each pair. Each data set is randomly divided into two parts of equal size, with one part as the test data and the other part as the unlabeled data that is used for active learning. We assume that no labeled data is available at the very beginning of active learning. For M ARGIN, IDE and DUAL, instances are randomly selected when no classification model is available, which only takes place at the beginning. In each iteration, an unlabeled instance is first selected to solicit its class label and the classification model is then retrained using additional labeled instance. We evaluate the classification model by its performance on the holdout test data. Both classification accuracy and Area Under ROC curve (AUC) are used for evaluation metrics. For every data set, we run the experiment for ten times, each with a random partition of the data set. We also conduct experiments with a few initially labeled examples and have similar observation. Due to the space limit, we put in the supplementary document the experimental results with a few initially labeled examples. In all the experiments, the parameter? is set to 1 and a RBF kernel with default 6

Table 1: Comparison on AUC values (mean? std). The best performance and its comparable performances based on paired t-tests at 95% significance level are highlighted in boldface. Data austra

digit1 g241n isolet titato vehicle wdbc letterDvsP letterEvsF letterIvsJ letterMvsN letterUvsV

Algorithms R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE R ANDOM M ARGIN C LUSTER IDE DUAL Q UIRE

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Number of queries (percentage of the unlabeled data) 10% 20% 30% 40% .894?.022 .897?.023 .901?.022 .909?.015 .838?.119 .885?.043 .909?.010 .911?.012 .888?.029 .894?.015 .896?.015 .903?.014 .885?.058 .902?.012 .912?.008 .913?.009.878?.036 .875?.018 .876?.016 .879?.013 .901?.010 .906?.016 .912?.009 .914?.009  $.969?.006\ .979?.005\ .984?.003\ .985?.003\ .972?.009\ .989?.002\ .992?.002\ .992?.002$ .952?.018 .963?.019 .974?.011 .985?.002 .973?.007 .987?.002 .991?.002 .992?.002 $.953?.009\ .975?.004\ .982?.005\ .985?.003\ .986?.003\ .990?.002\ .992?.002\ .992?.002$  $.769?.021\ .822?.018\ .854?.016\ .873?.015\ .751?.048\ .830?.022\ .864?.019\ .896?.012$ .770?.024 .815?.018 .835?.021 .860?.022 .786?.029 .840?.017 .866?.016 .883?.013.751?.019.822?.011.838?.022.865?.016.825?.019.857?.020.884?.013.900?.009 $.998?.002\ .999?.001\ 1.00?.000\ 1.00?.000\ .999?.001\ 1.00?.000\ 1.00?.000\ 1.00?.000$  $.999?.002\ 1.00?.000\ 1.00?.000\ 1.00?.000\ .999?.002\ .999?.001\ 1.00?.001\ 1.00?.000$ .999?.001 .999?.001 1.00?.000 1.00?.001 .999?.001 .999?.001 1.00?.000 1.00?.001 .861?.031 .954?.023 .979?.011 .991?.007 .753?.078 .946?.043 .998?.001 1.00?.000  $.806?.054\ .908?.031\ .971?.021\ .989?.010\ .906?.029\ .996?.003\ .999?.001\ 1.00?.001$  $.782?.064\ .900?.027\ .981?.012\ .995?.006\ .861?.025\ .991?.004\ .999?.001\ 1.00?.000$ 

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.961?.017.976?.008.985?.007.987?.006.969?.011.979?.006.980?.006.982?.008
.897?.058 .934?.030 .954?.017 .959?.014 .963?.013 .976?.011 .989?.010 .991?.004
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.986?.009 .994?.003 .997?.002 .998?.001 .988?.007 .997?.002 .998?.001 .998?.001
.972?.011 .974?.007 .980?.008 .983?.007 .996?.003 .998?.001 .999?.000 .999?.000
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.992?.002 .988?.003 .992?.002 .987?.003 .992?.002 .886?.012 .911?.008 .880?.013
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1.00?.000.997?.004.1.00?.000.997?.003.1.00?.000.999?.001.1.00?.000.975?.013
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.998?.001.983?.007.999?.0001.00?.0001.00?.0001.00?.0001.00?.000.995?.005
1.00?.000
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parameters is used (performances with linear kernel are not as stable as that with RBF kernel). LibSVM [4] is used to train a SVM classifier for all active learning approaches in comparison. 7

Table 2: Win/tie/loss counts of Q UIRE versus the other methods with varied numbers of queries. Algorithms R ANDOM M ARGIN C LUSTER IDE

DUAL In All

4.1

Number of queries (percentage of the unlabeled data) 5% 10% 20% 30% 40% 50% 80% 4/8/0 8/4/0 9/3/0 9/2/1 10/2/0 10/2/0 6/6/0 6/6/0 4/7/1 2/8/2 2/8/2 0/11/1 0/11/1 1/11/0 6/6/0 7/5/0 8/4/0 11/1/0 9/3/0 6/6/0 3/9/0 6/6/0 6/5/1 6/5/1 8/4/0 8/4/0 8/4/0 2/10/0 8/4/0 10/2/0 11/1/0 10/2/0 10/2/0 11/1/0 9/3/0 30/30/0 35/23/2 36/21/3 40/17/3 37/22/1 35/24/1 21/39/0

In All 56/27/1 15/62/7 50/34/0 44/38/2 69/15/0 234/176/10 Results

Figure 2 shows the classification accuracy of different active learning approaches with varied numbers of queries. Table 1 shows the AUC values, with 5%, 10%, 20%, 30%, 40%, 50% and 80% of unlabeled data used as queries. For each case, the best result and its comparable performances are highlighted in boldface based on paired t-tests at 95% significance level. Table 2 summarizes the win/tie/loss counts of Q UIRE versus the other methods based on the same test. We also perform the Wilcoxon signed ranks test at 95% significance level, and obtain almost the same results, which can be found in the supplementary document. First, we observe that the R ANDOM approach tends to yield decent performance when the number of queries is very small. However, as the number of queries increases, this simple approach loses its edge and often is not as effective as the other active learning approaches. M ARGIN, the most commonly used approach for active learning, is not performing well at the beginning of the learning stage. As the number of queries increases, we observe that M ARGIN catches up with the other approaches and yields decent performance. This phenomenon can be attributed to the fact that with only a few training examples, the learned decision boundary tends to be inaccurate, and as a result, the unlabeled instances closest to the decision boundary may not be the most informative ones. The performance of C LUSTER is mixed. It works well on some data sets, but performs poorly on the others. We attribute the inconsistency of C LUSTER to the fact that the identified cluster structure of unlabeled data may not always be consistent with the target classification model. The behavior of IDE is similar to that of C LUSTER in that it achieves good performance on certain data sets and fails on the others. DUAL does not yield good performance on most data sets although we have tried our best efforts to tune the related parameters. We attribute the failure of DUAL to the setup of our experiment in which no initially labeled examples are provided. Further study shows that starting with a few initially labeled examples does improve the performance of DUAL though it is still significantly outperformed by Q UIRE. Detailed results can be found in the supplementary document. Finally, we observe that for most cases, Q UIRE is able to outperform the baseline methods significantly, as indicated by Figure 2, Tables 1 and 2. We attribute the success of Q UIRE to the principle of choosing unlabeled instances that are both informative and representative, and the specially designed computational framework that appropriately measures and combines the informativeness and representativeness. The computational cost are reported in the supplementary document.

5 Conclusion

We propose a new approach for active learning, called Q UIRE, that is designed to find unlabeled instances that are both informative and representative. The proposed approach is based on the min-max view of active learning, which provides a systematic way for measuring and combining the informativeness and the representativeness. Our current work is restricted to binary classification. In the future, we plan to extend this work to multi-class learning. We also plan to develop the mechanism which allows the user to control the tradeoff between informativeness and representativeness based on their domain, leading to the incorporation of domain knowledge into active learning algorithms. Acknowledgements This work was supported in part by the NSFC (60635030), 973 Program (2010CB327903), JiangsuSF (BK2008018) and NSF (IIS-0643494). 8

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