

Assignment 4

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March 19, 2014

- 1 Give a BNF grammar for the set of all strings consisting of the keyword begin, followed by one or more statements with a semi-colon after each statement, followed by the keyword end. Use the non-terminal $\langle \textit{statement} \rangle$ for a statement and do not give a production for it.

$\langle \textit{string} \rangle$	$:=$	begin ; $\langle \textit{phrase} \rangle$
$\langle \textit{phrase} \rangle$	$:=$	$\langle \textit{statement} \rangle$; $\langle \textit{phrase} \rangle$ end

- 2 Repeat Problem 1 except now use EBNF extensions wherever possible to simplify the grammar.

$\langle \textit{string} \rangle$	$:=$	begin ; $\langle \textit{statement} \rangle^?$
$\langle \textit{phrase} \rangle$	$:=$	$\langle \textit{statement} \rangle^* \text{end}^?$

- 3 Write a BNF grammar that can generate all strings in the language $a^n c^k b^m$ where $n > m \geq 1$ and $k = 0, 1, \text{ or } 2$. In other words, there are more a's than b's. There is at least 1 b. The a's and b's may be separated by nothing, 1 c or 2 c's. Hint: In the review problems you've seen a grammar for a language whose sentences are a string of a's followed by an equal number of b's. Think about how to extend that grammar to satisfy the specifications of this problem.

$\langle \textit{expression} \rangle$	$:=$	aa $\langle \textit{expression} \rangle$ b aaa $\langle \textit{expression} \rangle$ bb a $\langle \textit{expression} \rangle$ $\langle \textit{term} \rangle$
$\langle \textit{term} \rangle$	$:=$	c cc $\langle \textit{empty} \rangle$

- 4 Repeat Problem 3, but now use EBNF extensions to make your grammar as concise as possible.

$\langle \textit{expression} \rangle$	$:=$	(aa $\langle \textit{expression} \rangle$ b)* aaa $\langle \textit{expression} \rangle$ bb* a $\langle \textit{expression} \rangle^* \langle \textit{term} \rangle^?$
$\langle \textit{term} \rangle$	$:=$	c? cc?