

Assignment 0

Sterling Kohel

September 10, 2014

- 1 What is the 32-bit complement representation of the number -10117?**

$$10117_{10} = 0000000000000000010011110000101_2$$

$$\text{flip bit} = 11111111111111111101100001111010_2$$

$$\text{add 1} = 11111111111111111101100001111011_2$$

- 2 Prove the following statement: Assume x and y are positive integers. If the digits of y are the digits of x , but just rearranged, then $(x - y) \bmod 9 = 0$.**

Let $C = \text{some constant}$.

$x - C = \text{multiple of } 9$

Since y contains the same digits as x , $y - C = \text{multiple of } 9$.

$$(x - C - (y - C)) \bmod 9 = 0$$

$$(x - C - y + C) \bmod 9 = 0$$

$$(x - y) \bmod 9 = 0 \quad \square$$

- 3 Is the converse of the previous statement, which you just proved, true? If so, prove it. If not, provide a concrete counterexample. In either case you must clearly state what the converse actually is.**

The converse of 2 is:

if $(x - y) \bmod 9 = 0$ then the digits of y are the digits of x , but just rearranged

Counterexample:

$$x = 45$$

$$y = 9$$

$$(45 - 9) \bmod 9 = 0 \text{ however } 9 \text{ is not a rearrangement of } 45.$$