



Safety verification for deep neural networks with provable guarantees

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Deep learning with everything



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Article metrics for:

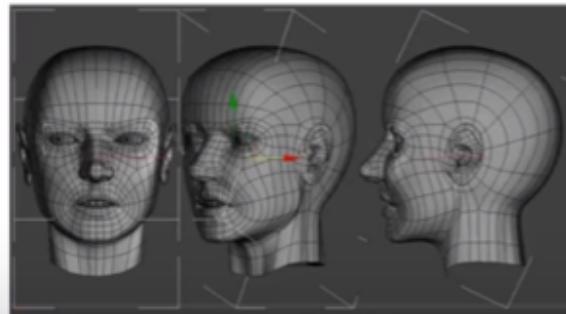
Dermatologist-level classification of skin cancer with deep neural networks

Andre Esteva, Brett Kuprel, Roberto A. Novoa, Justin Ko, Susan M. Swetter, Helen M. Blau & Sebastian Thrun

Nature 542, 115–118 (02 February 2017) | doi:10.1038/nature21056

Last updated: 24 July 2017 10:10:28 EDT

DeepFace Closing the Gap to Human-Level Performance in Face Verification



[Yaniv Taigman](#)
[Ming Yang](#)
[Marc'Aurelio Ranzato](#)
[Lior Wolf](#)
- 2014

97.35% accuracy
Trained on the largest facial dataset – 4M facial images belonging to more than 4,000 identities.



Unwelcome news recently...

Self-Driving Uber Car Kills Pedestrian in Arizona, Where Robots Roam

Leer en español

By DAISUKE WAKABAYASHI MARCH 19, 2018



Tesla Says Crashed Vehicle Had Been on Autopilot Before Fatal Accident

By GREGORY SCHMIDT MARCH 31, 2018



RELATED COVERAGE



Tesla Looked Like the F... Ask if It Has One. MARCH

Fatal Tesla Crash Raises New Questions About Autopilot System

U.S. Safety Agency Criticizes Tesla Crash Data Release

How can this happen if we have 99.9% accuracy?

<https://www.youtube.com/watch?v=B2pDFjlvrIU>

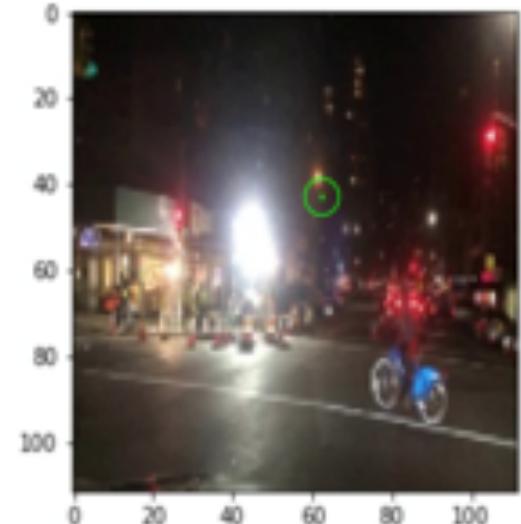
Should we worry about safety?



(a)



(b)



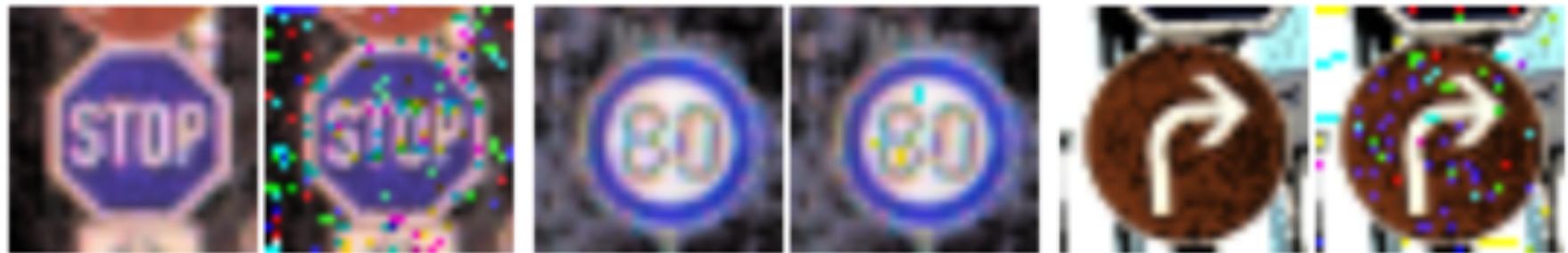
(c)

Red light classified as green with (a) 68%, (b) 95%, (c) 78% confidence after one pixel change.

- TACAS 2018, <https://arxiv.org/abs/1710.07859>

Can we verify that such behaviour cannot occur?

German traffic sign benchmark...



stop

30m
speed
limit

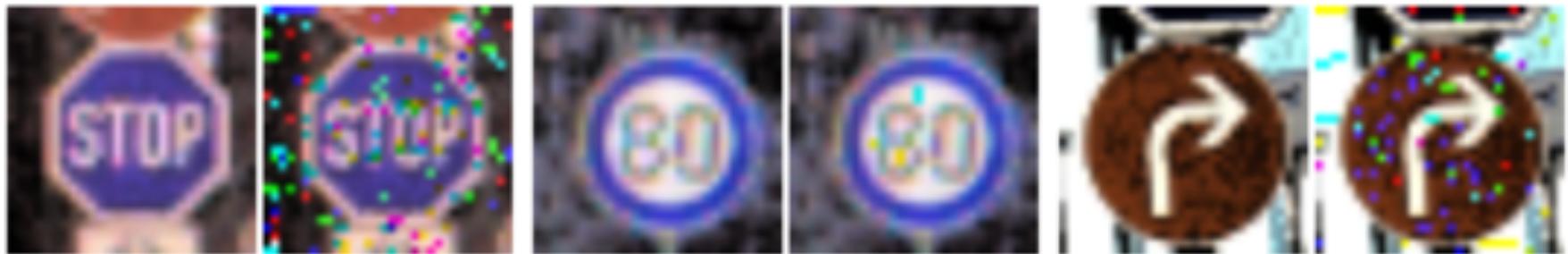
80m
speed
limit

30m
speed
limit

go
right

go
straight

German traffic sign benchmark...



stop

30m
speed
limit

80m
speed
limit

30m
speed
limit

go
right

go
straight

Confidence 0.999964

0.99

Aren't these artificial?



Real traffic signs in Alaska!

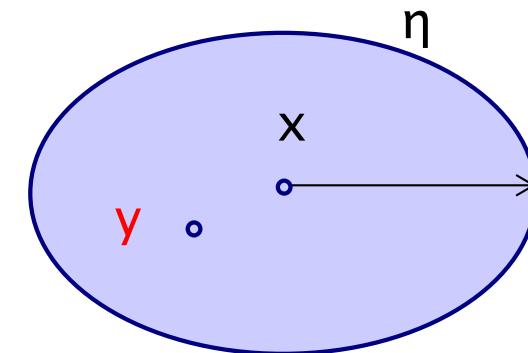
Need to consider **physical** attacks, not only digital...

This talk

- Progress in developing methodology to provide **provable guarantees** of safety of classification decisions
- Focus on **local robustness** against adversarial manipulations
- Automated verification
 - search/SMT: CAV 2017, <https://arxiv.org/abs/1610.06940>
 - game: TACAS 2018, <https://arxiv.org/abs/1710.07859>
- Reachability analysis
 - global optim: IJCAI 2018, <https://arxiv.org/abs/1805.02242>
- Testing with coverage guarantees
 - concolic: ASE 2018, <https://arxiv.org/abs/1805.00089>
- Probabilistic safety
 - Bayesian GP: AAAI 2019, <https://arxiv.org/abs/1809.06452>

Safety of classification decisions

- Safety assurance process is complex
- Here focus on **safety at a point** as part of such a process
 - same as pointwise robustness...
- Assume given
 - trained network $f : D \rightarrow \{c_1, \dots, c_k\}$
 - diameter for support region η
 - norm, e.g. L^2, L^∞
- Define safety as **invariance** of classification decision
 - i.e. $\nexists y \in \eta$ such that $f(x) \neq f(y)$
- Also wrt family of safe **manipulations**
 - e.g. scratches, weather conditions, camera angle, etc





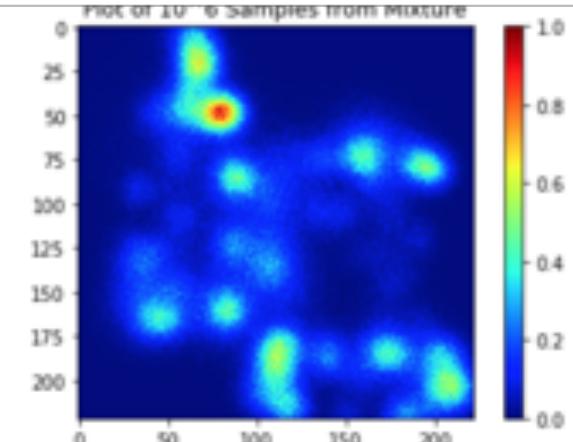
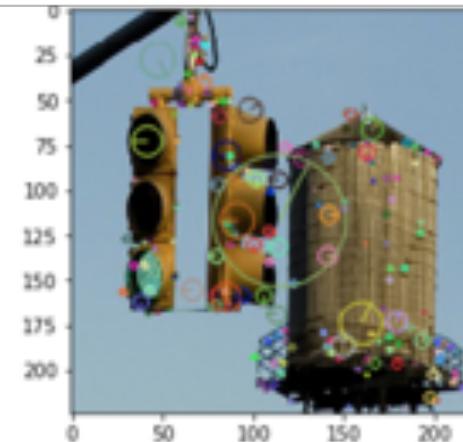
Safety verification

- Automated verification (= ruling out adversarial examples)
 - discretise the region, exhaustively search for misclassifications
 - provable guarantee of decision safety if adv. example not found
 - (assumptions needed to ensure finiteness of search)
- The approach
 - reduction to linear arithmetic (counting problem), use SMT
 - propagate verification layer by layer
- This differs from heuristic search for adversarial examples
 - no guarantee of precise adversarial examples
 - no guarantee of exhaustive search even if we iterate
- But scalability remains an issue, employ various heuristics...
- CAV 2017, <https://arxiv.org/abs/1610.06940>

Feature-based representation

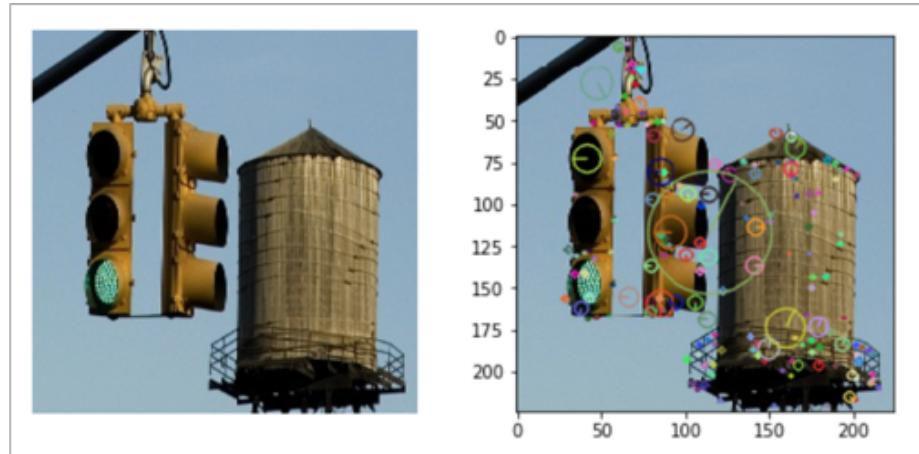
- Employ the SIFT algorithm to extract features
- Reduce dimensionality by focusing on **salient features**
- Use a Gaussian mixture model in order to assign each pixel a probability based on its **perceived saliency**

$$\mathcal{G}_{i,x} = \frac{1}{\sqrt{2\pi\lambda_{i,s}^2}} \exp\left(\frac{-(p_x - \lambda_{i,x})^2}{2\lambda_{i,s}^2}\right) \quad \mathcal{G}_{i,y} = \frac{1}{\sqrt{2\pi\lambda_{i,s}^2}} \exp\left(\frac{-(p_y - \lambda_{i,y})^2}{2\lambda_{i,s}^2}\right)$$



Game-based search

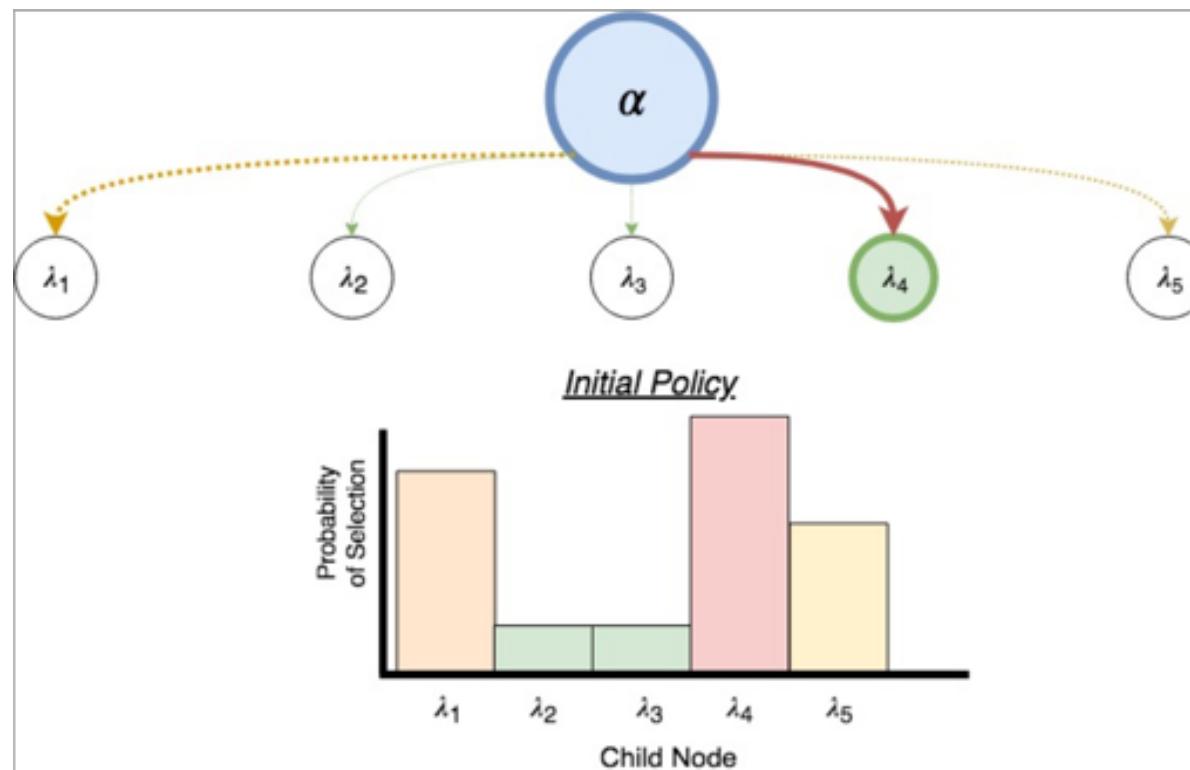
- Goal is finding adv. example, reward inverse of distance
- Player 1 selects the feature that we will manipulate



- Each feature represents a possible move for player 1
- Player 2 then selects the pixels in the feature to manipulate
- Use Monte Carlo tree search to explore the game tree, while querying the network to align features
- Method black/grey box, can approximate the maximum safe radius for a given input

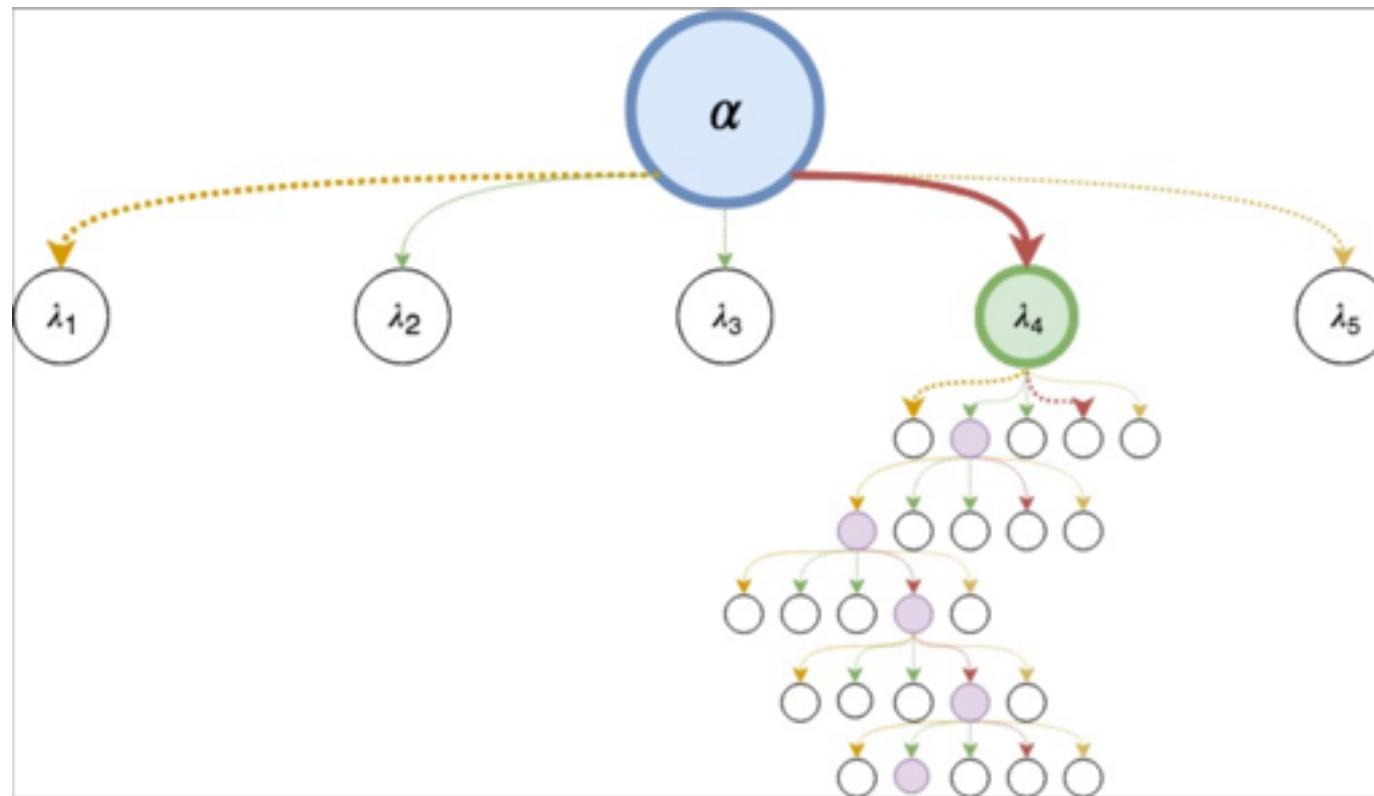
MCTS: selection/expansion

- The **root** of the tree represents the original image, and each **child** represents a potential manipulated image
- First, select a **manipulation** based on each player's strategy
- If the child has never been selected from previously then we "**expand**" the tree to select a new leaf.



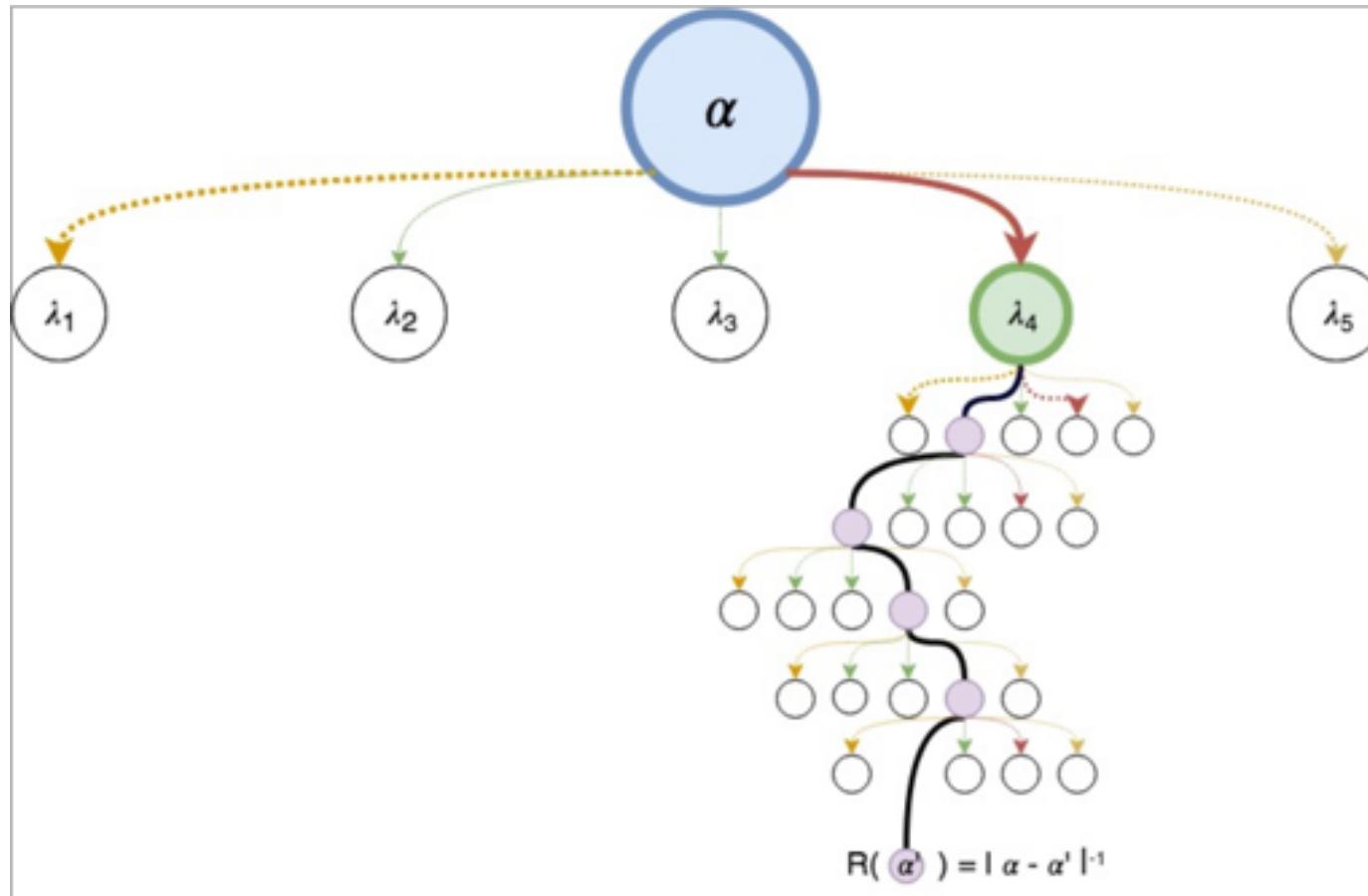
MCTS: simulation

- After a new child has been added to the tree, we approximate the reward of visiting this child by **continuously searching** the tree until we have **either** timed out or hit an adversarial example
- These nodes are **not** recorded as a part of the partial tree

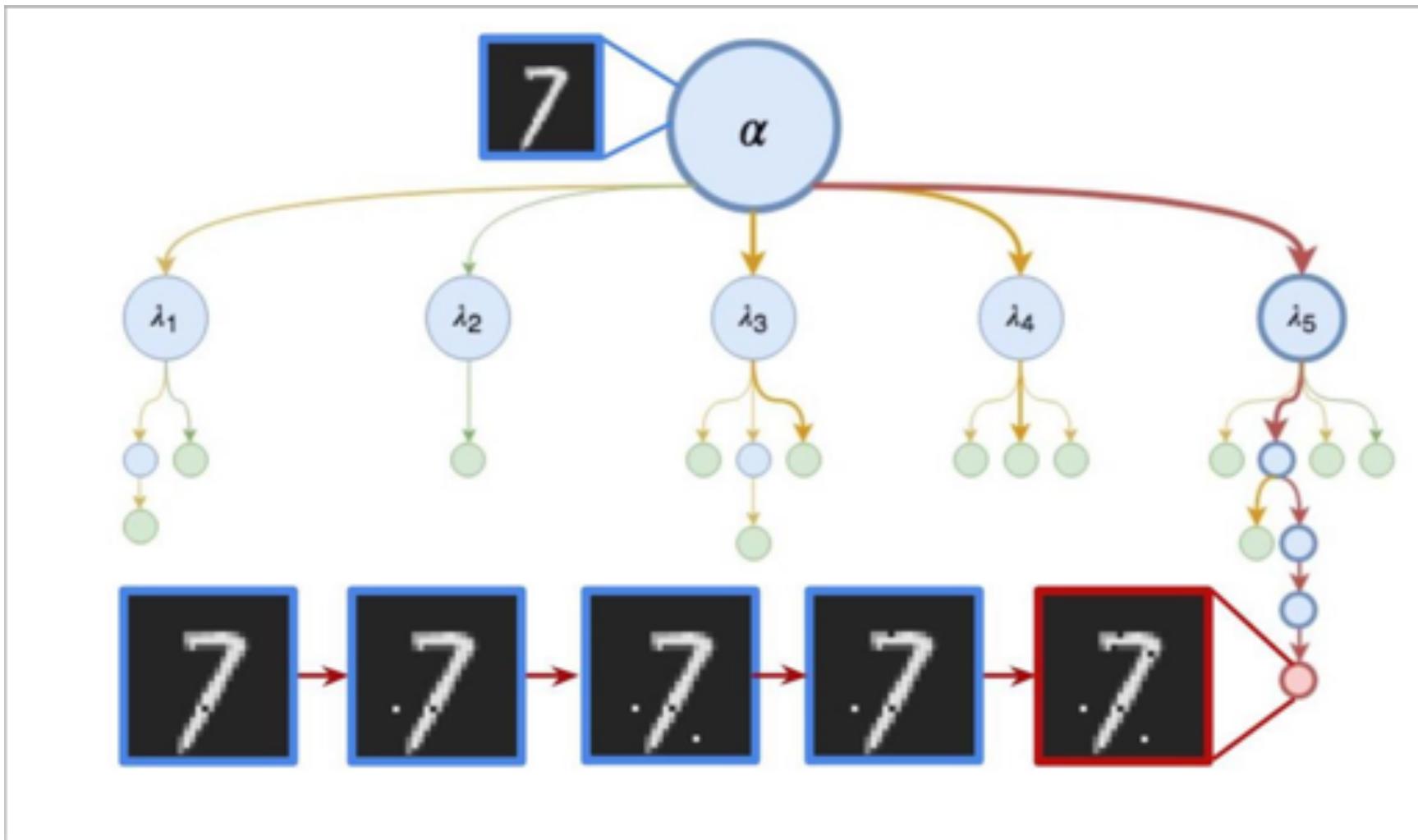


MCTS: backpropagation

- After we have terminated the tree, we **calculate the reward**, and **backpropagate** that reward up the tree to update our exploration policy (update each player's strategies)

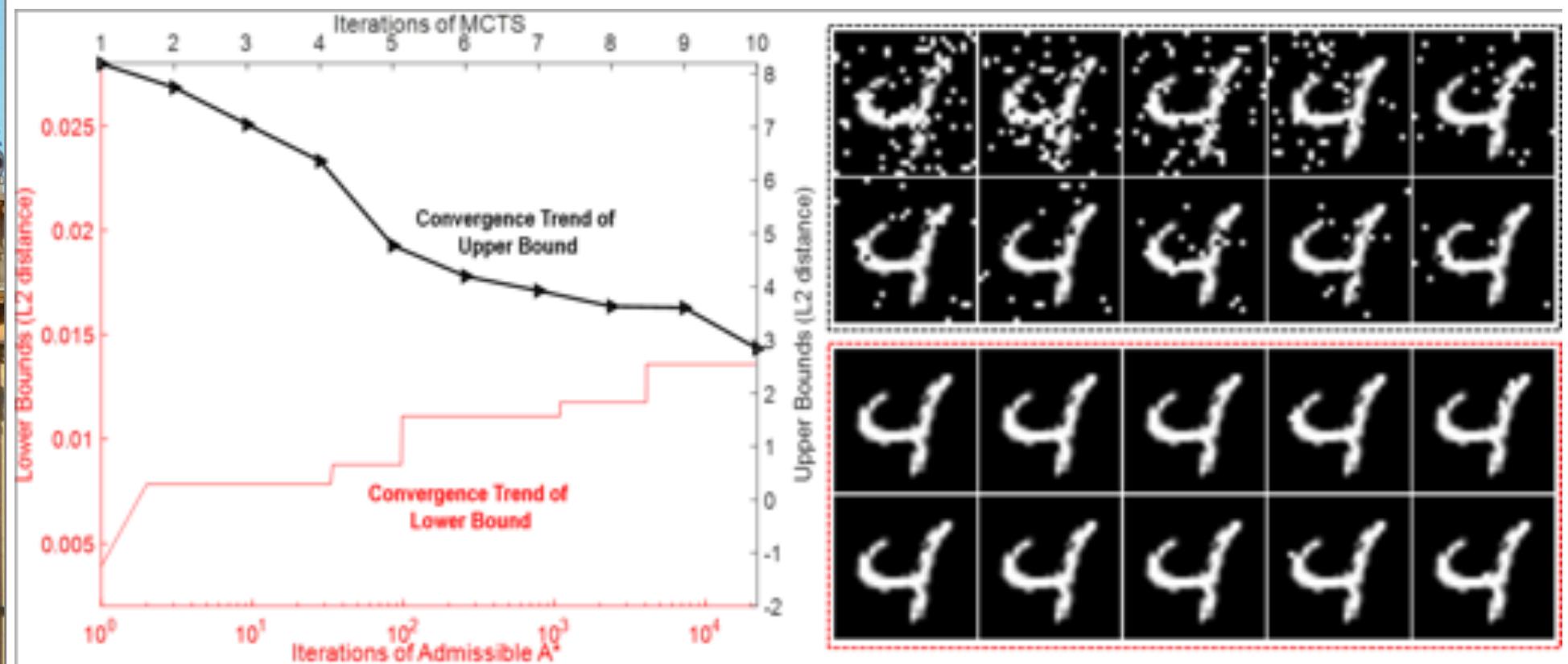


Tree expands until example is found



Now also lower bounds (MNIST)

- Convergence of lower and upper bounds on maximum safe radius



- See arXiv:1807.0357

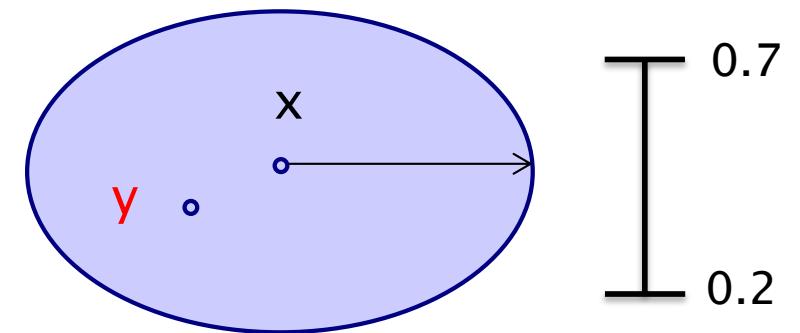
Evaluating safety-critical scenarios: Nexar

- Using our Game-based Monte Carlo Tree Search method we were able to reduce the accuracy of the network from 95% to 0%
- On average, each input took less than a second to manipulate (.304 seconds)
- On average each image was vulnerable to 3 pixel changes

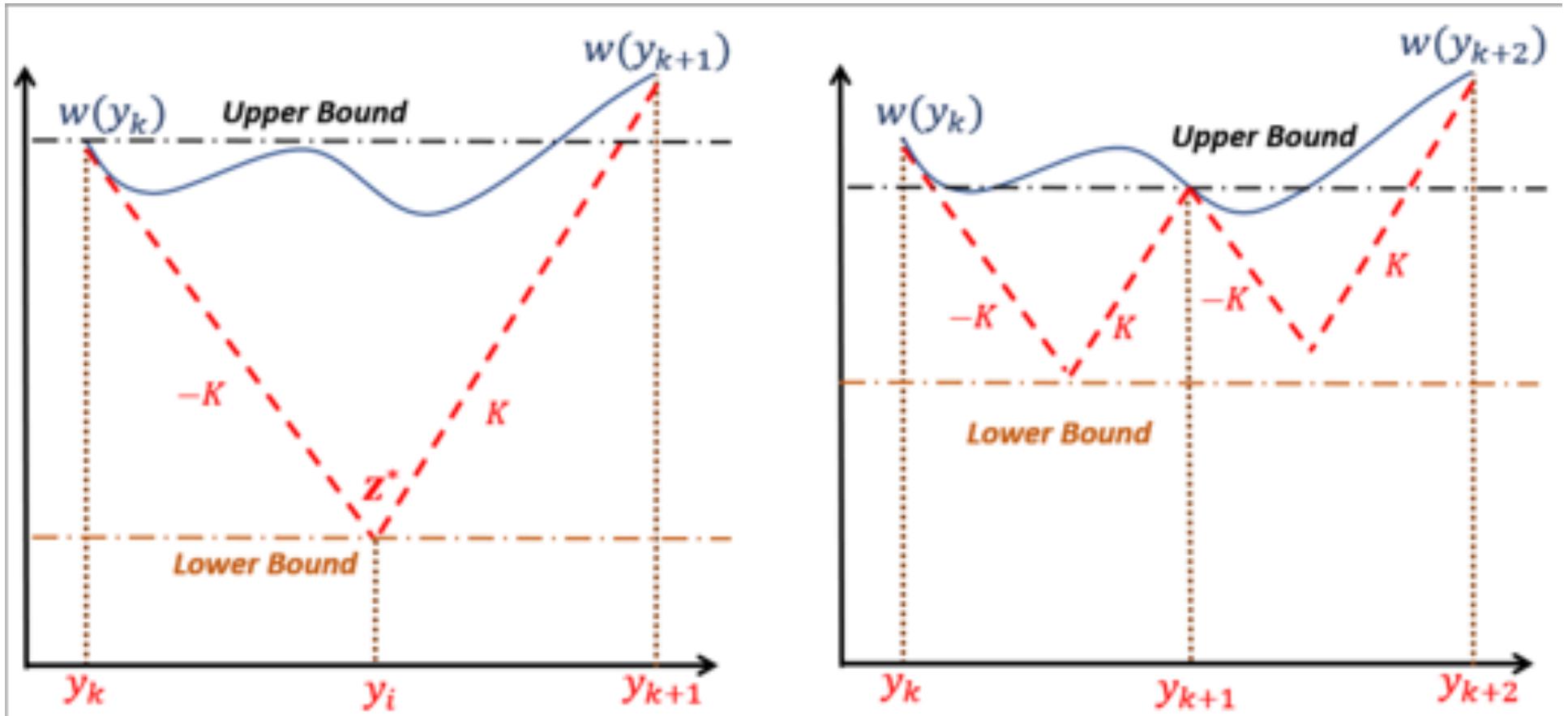


Alternative approach: reachability analysis

- Rather than search the discretized region, can we compute the **reachable values**?
- Under assumption of Lipschitz continuity
 - for $x \in \eta$, compute maximum/minimum value of $f(\eta)$
 - using global optimisation
 - **anytime** fashion
- Gives **provable guarantees**
 - **best/worst** case confidence values
 - pointwise confidence diameter
 - can average over input distribution
- Method **NP-complete**
 - wrt the number of input dimensions, not number of neurons
- IJCAI 2018, <https://arxiv.org/abs/1805.02242>



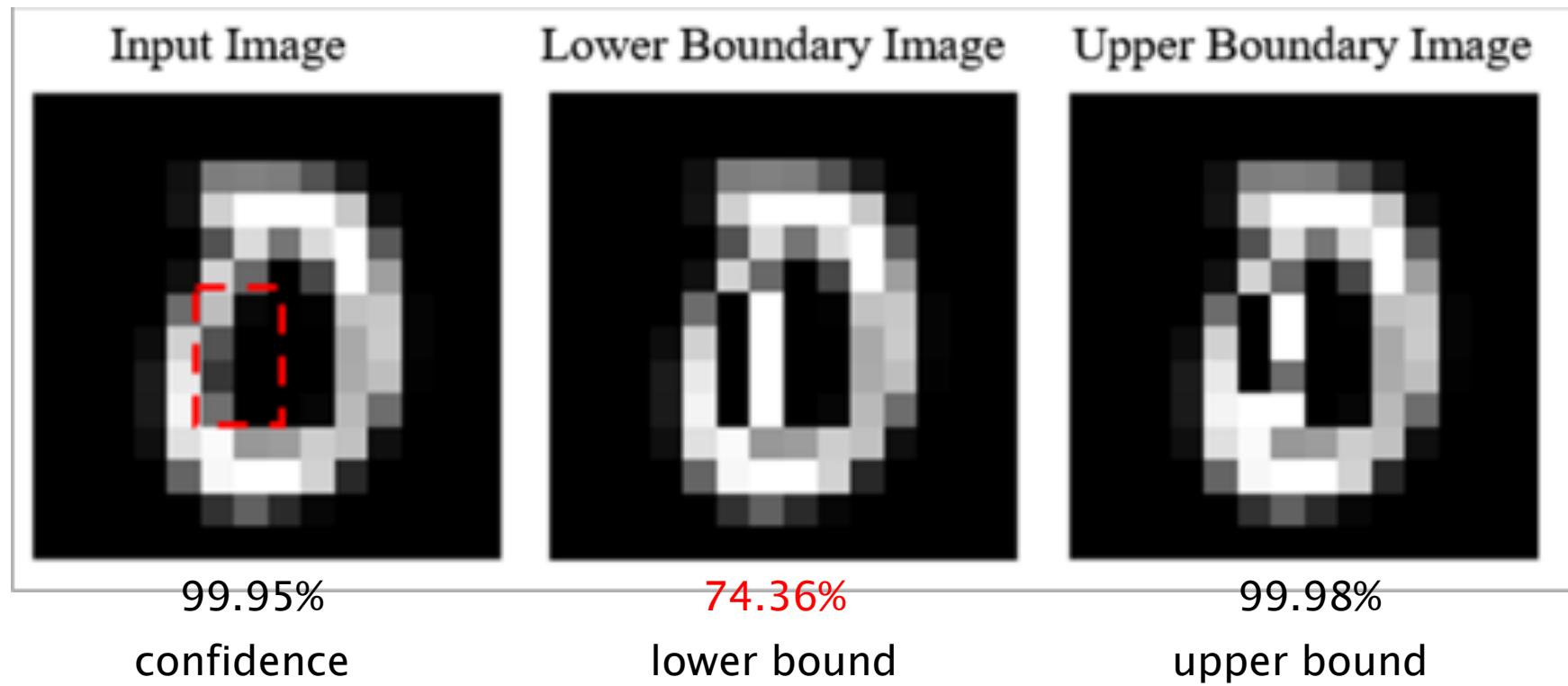
Global optimization: main idea



- Adaptive nested optimization, asymptotic convergence
 - construct a series of lower and upper bounds
- K – Lipschitz constant

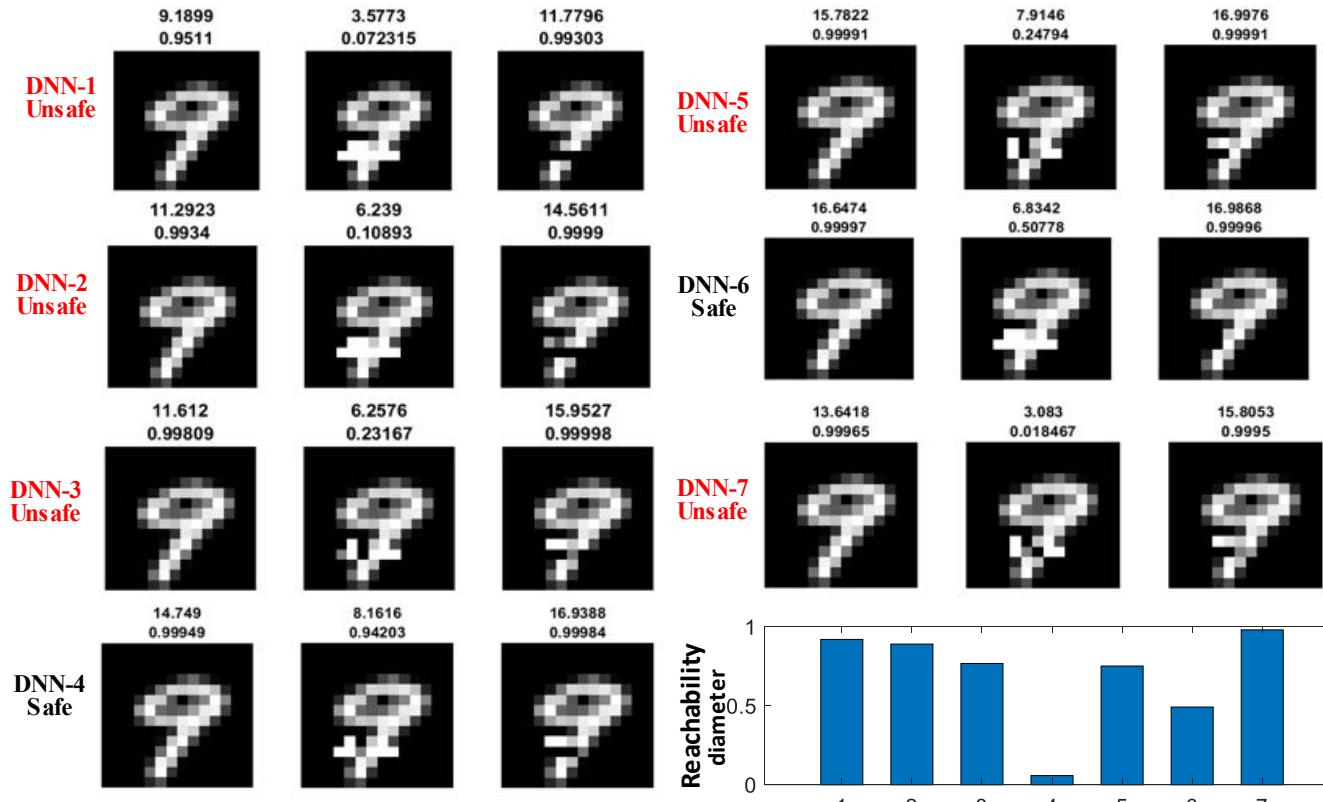
MNIST example

- Take an image and select a **feature** within it



- **Safety verification** for the **feature**
 - manipulating the feature can only reduce confidence to 74.36%

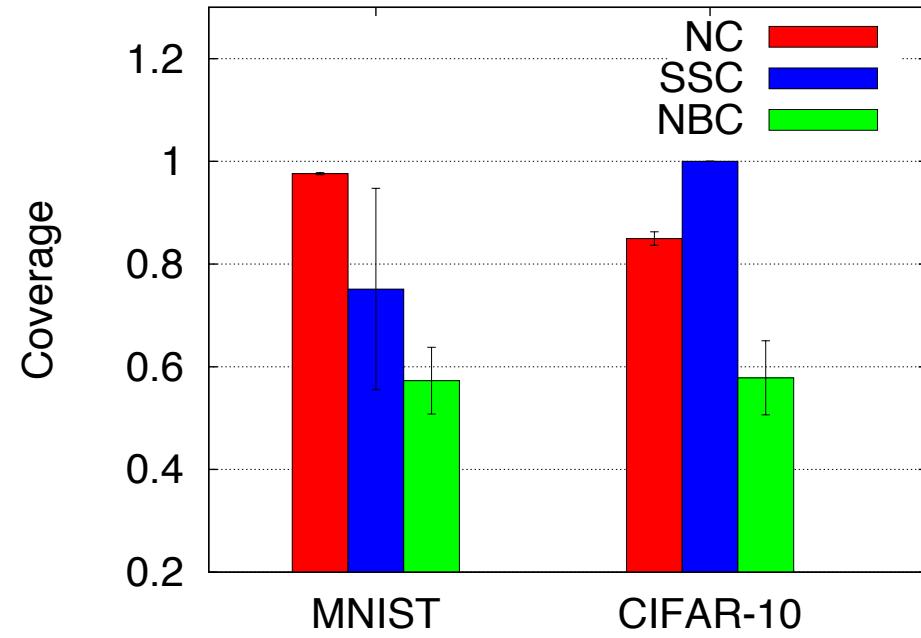
MNIST network comparison



- Showing pointwise **confidence diameter**
- Can obtain global **robustness evaluation** by averaging wrt the test data distribution

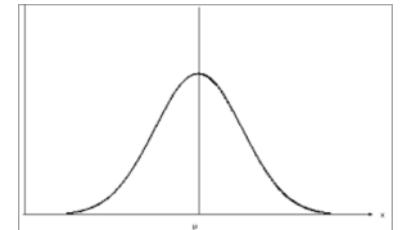
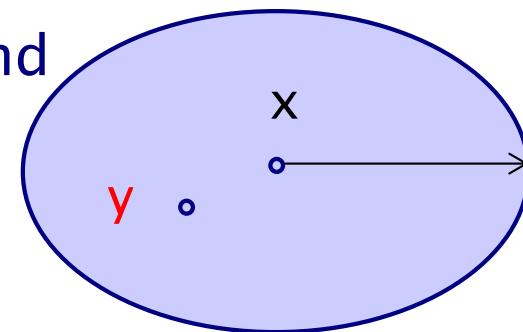
Safety testing, guaranteed coverage

- Often provable guarantees on network outputs beyond reach
- Concolic testing (concrete+symbolic)
 - for test goal, generate test cases
 - alternating between concrete execution & symbolic analysis
- Test coverage criteria
 - specified in quantified linear arithmetic over rationals
- Range of coverage metrics
 - neuron coverage (NC), neuron boundary coverage (NBC), modified condition/decision (MC/DC), Lipschitz continuity, etc



Probabilistic guarantees

- Requiring that no adversarial examples exist too strict
- Need to **probabilistic guarantees**: probability that local perturbations result in predictions that are close to original
- Work with Bayesian inference and
- Gaussian processes
- Define **safety with prob** $1-\varepsilon$

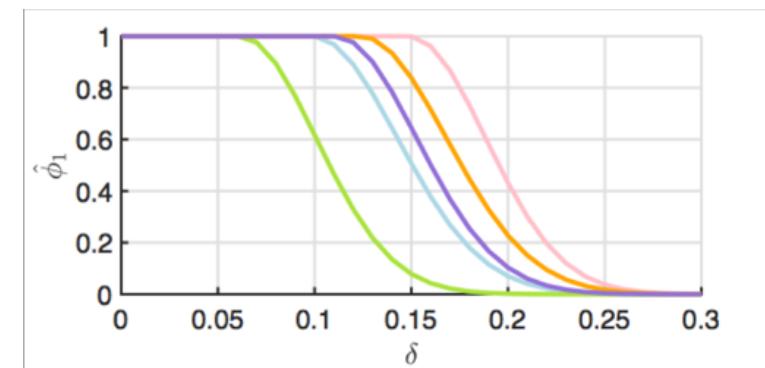
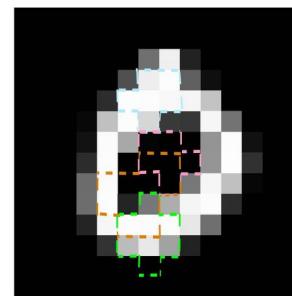


$$\text{Prob}(\exists y \in \eta \text{ s.t. } ||f(x)-f(y)|| > \delta \mid D) \leq \varepsilon$$

- i.e. **conditioned on training data D**
- NB differs from **pointwise thresholding** in Bayesian deep learning

Probabilistic guarantees for NNs

- Computation for general stochastic processes intractable
- For GPs, can obtain tight **upper bounds** by
 - approximating extrema of mean and variance for a test point
 - using Borell–TIS inequality
 - and solving optimization problems (analytical or convex opt)
- Applies to fully-connected (and convolutional) neural networks in the limit of infinitely many neurons...



- **Scalability** continues to be an issue for NNs



Conclusion

- Deep learning should be more **critically evaluated** when put into practice in safety– and security–critical situations
- Adversarial examples help in understanding the robustness of **DNN decision boundaries**
- Overviewed methods for **safety verification/testing** of deep neural networks
 - **search-based** and **feature-guided exploration**, with guarantees
 - **reachability computation** for Lipschitz continuous networks
 - **test coverage guarantees**
 - **probabilistic guarantees** in a Bayesian framework
- Future work
 - how best to use adversarial examples: training vs logic
 - scalability for probabilistic guarantees
 - more complex properties

Acknowledgements

- My group and collaborators in this work
- Project funding
 - ERC Advanced Grant
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- See also
 - **VERIWARE** www.veriware.org
 - PRISM www.prismmodelchecker.org