

# Table of Inputs and Outputs

## Dynamic Optimization of Tensegrity Systems

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### Optimizer Input

Input	Range	Explanation
$p$	4 - 8	Number of units in the circumferential direction
$q$	4 - 8	Number of units in the vertical direction
$L$	0.5 - 1 m	Vertical length of structure
$r_{ss}$	0.0005 - 0.0025 m	Radius of surface strings
$r_{si}$	0.0005 - 0.0025 m	Radius of internal strings
$r_b$	0.0001 - 0.005 m	Radius of bars
$C_2$	-0.1 - 0.1	Concentration of vertical units
$N_z$	-0.4 - 0.4	Position of central load
$2R/L_{rcc}$	0.5 - 3.0	Ratio of diameter to length - cylinder
$2R/L_{por}$	0.5 - 3.0	Ratio of diameter to length - paraboloid
$2R/L_{elp}$	0.25 - 1.5	Ratio of diameter to length - ellipsoid
$g_{max}$	10 g	Max g-force ceiling

### Environment Input

Input	Value	Explanation
$h$	1 m	Initial distance between bottom node and ground
$v_0$	-10 m/s	Initial vertical velocity
$m_{load}$	20 kg	Mass of central payload
$g$	-9.81 m/s <sup>2</sup>	Earth gravity
$\theta_y$	0: $\pi$ /6: $\pi$ /2	Rotations about $y$ -axis
$\theta_{x_{sp}}$	0: $\pi$ /18: $\pi$ /9	Rotations about $x$ -axis for sphere
$\theta_{x_{rcc}}$	0: $\pi$ /18: $\pi$ /9	Rotations about $x$ -axis for cylinder
$\theta_{x_{por}}$	0: $\pi$ /18: $\pi$ /9	Rotations about $x$ -axis for parabola

### Environment Output

Output	Explanation
m	Total system mass
$g_s$	Max acceleration in $G$ 's experienced by system
$\sigma_{ss_d}$	Max stress exceeding surface string limit
$\sigma_{si_d}$	Max stress exceeding internal string limit
$\sigma_{bc_d}$	Max stress exceeding bar compressed stress limit
$\sigma_{bt_d}$	Max stress exceeding bar tension stress limit
$V_c$	Volume constraint magnitude

### Material Properties

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Density of strings and bars	$\rho_s = 1123 \text{ kg/m}^3, \rho_b = 4705 \text{ kg/m}^3$
Elastic modulus of strings and bars	$E_s = 1 \times 10^8 \text{ Pa}, E_b = 60 \times 10^9 \text{ Pa}$
Damping coefficient of strings and bars	$c_s = 5 \times 10^6 \text{ Pa}, c_b = 0 \text{ Pa}$

Bar Material - Titanium

String Material - Nylon

## Optimization Function

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$$f = m + p_g + p_{\sigma_{ss}} + p_{\sigma_{si}} + p_{\sigma_{bc}} + p_{\sigma_{bt}} + p_{V_c}$$

Where:

$$p_i = \lambda_i * \gamma_i$$

$\lambda_i$  is the conditional multiplier based on the magnitude of the fitness error.

$n_i$  Normalizes the fitness function errors.

Where:

$$\gamma_g = 1^{12}$$

$$\gamma_{\sigma_{ss}} = 1$$

$$\gamma_{\sigma_{si}} = 1$$

$$\gamma_{\sigma_{bc}} = 1$$

$$\gamma_{\sigma_{bt}} = 1$$

$$\gamma_{V_c} = 1^{14}$$

and,

$$\lambda_g = \begin{cases} 0, & \text{if } g_s \leq g_{max} \\ (g_{max} - g_s)^2, & \text{if } g_s \geq g_{max} \end{cases}$$

$$\lambda_{\sigma_{ss}} = \begin{cases} 0, & \text{if } \sigma_{ss} \leq \sigma_{ss_{max}} \\ (\sigma_{ss_{max}} - \sigma_{ss})^2, & \text{if } \sigma_{ss} \geq \sigma_{ss_{max}} \end{cases}$$

$$\lambda_{\sigma_{si}} = \begin{cases} 0, & \text{if } \sigma_{si} \leq \sigma_{si_{max}} \\ (\sigma_{si_{max}} - \sigma_{si})^2, & \text{if } \sigma_{si} \geq \sigma_{si_{max}} \end{cases}$$

$$\lambda_{\sigma_{bc}} = \begin{cases} 0, & \text{if } \sigma_{bc} \leq \sigma_{bc_{max}} \\ (\sigma_{bc_{max}} - \sigma_{bc})^2, & \text{if } \sigma_{bc} \geq \sigma_{bc_{max}} \end{cases}$$

$$\lambda_{\sigma_{bt}} = \begin{cases} 0, & \text{if } \sigma_{bt} \leq \sigma_{bt_{max}} \\ (\sigma_{bt_{max}} - \sigma_{bt})^2, & \text{if } \sigma_{bt} \geq \sigma_{bt_{max}} \end{cases}$$

$$V_c = \begin{cases} 0, & \text{if } V_c \leq V_{c_{max}} \\ (V_{c_{max}} - V_c)^2, & \text{if } V_c \geq V_{c_{max}} \end{cases}$$