

Task 1

Vocabulary = { happy, new, year, holiday, term, starts, work, celebrations }
|Vocabulary| = 8

Prior:

$$P(c_1) = \frac{3}{5} = 0.6$$

$$P(c_2) = \frac{2}{5} = 0.4$$

Posterior: (with Add-One-Smoothing)

$$P(\text{happy}|c_1) = \frac{2+1}{7+8} = \frac{3}{15}$$

$$P(\text{new}|c_1) = \frac{2+1}{7+8} = \frac{3}{15}$$

$$P(\text{year}|c_1) = \frac{2+1}{7+8} = \frac{3}{15}$$

$$P(\text{holiday}|c_1) = \frac{1+1}{7+8} = \frac{2}{15}$$

$$P(\text{term}|c_1) = \frac{0+1}{7+8} = \frac{1}{15}$$

$$P(\text{starts}|c_1) = \frac{0+1}{7+8} = \frac{1}{15}$$

$$P(\text{work}|c_1) = \frac{0+1}{7+8} = \frac{1}{15}$$

$$P(\text{celebrations}|c_1) = \frac{0+1}{7+8} = \frac{1}{15}$$

$$P(\text{happy}|c_2) = \frac{0+1}{4+8} = \frac{1}{12}$$

$$P(\text{new}|c_2) = \frac{0+1}{4+8} = \frac{1}{12}$$

$$P(\text{year}|c_2) = \frac{0+1}{4+8} = \frac{1}{12}$$

$$P(\text{holiday}|c_2) = \frac{0+1}{4+8} = \frac{1}{12}$$

$$P(\text{term}|c_2) = \frac{1+1}{4+8} = \frac{2}{12}$$

$$P(\text{starts}|c_2) = \frac{2+1}{4+8} = \frac{3}{12}$$

$$P(\text{work}|c_2) = \frac{1+1}{4+8} = \frac{2}{12}$$

$$P(\text{celebrations}|c_2) = \frac{0+1}{4+8} = \frac{1}{12}$$

$$P(c_1|d) = \frac{3}{5} * \frac{3}{15} * \frac{3}{15} * \frac{3}{15} * \frac{1}{15} = \frac{81}{253125} = c_{map}$$

$$P(c_2|d) = \frac{1}{12} * \frac{1}{12} * \frac{1}{12} * \frac{1}{12} = \frac{2}{103680}$$

The model assigned the class c_1 to the document.

Task 2

Task 2: Maximum Entropy Classification

$$\begin{aligned}
 2.1) \quad P_{\lambda}(\text{SPAM} | x_1) &= \frac{\exp(\sum_i \lambda_i f_i(\text{SPAM}, x_1))}{\sum_{y'} \exp(\sum_i \lambda_i f_i(y', x_1))} \\
 &= \frac{\exp(0,2 \cdot 1 + 0 + 0,5 \cdot 1 + 0 + 0 + 0 + 0,1 \cdot 1 + 0)}{\exp(0,2 + 0,5 + 0,1) + \exp(-0,1 + (-0,2) \cdot 1 + 0 \cdot 1)} \\
 &= \frac{\exp(0,8)}{\exp(0,8) + \exp(-0,3)} \\
 &\approx \frac{2,22554}{2,22554 + 0,74081} \\
 &= \frac{2,22554}{2,96635} \approx 0,75026
 \end{aligned}$$

$$\begin{aligned}
 2.2) \quad \frac{A_{\lambda}}{\partial \lambda_6} &= \sum_{(y, x) \in (Y, X)} f_6(y, x) \\
 &= 0 + 0 + 0 + 0 + 1 + 1 = 2
 \end{aligned}$$

$$\begin{aligned}
 \frac{B_{\lambda}}{\partial \lambda_6} &= \sum_{(y, x) \in (Y, X)} \sum_{y'} P_{\lambda}(y' | x) f_6(y', x) \\
 &= P_{\lambda}(\text{SPAM} | x_1) \cdot f_6(\text{SPAM}, x_1) + P_{\lambda}(\text{HAM} | x_1) \cdot f_6(\text{HAM}, x_1) \\
 &\quad + P_{\lambda}(\text{SPAM} | x_2) \cdot f_6(\text{SPAM}, x_2) + P_{\lambda}(\text{HAM} | x_2) \cdot f_6(\text{HAM}, x_2) \\
 &\quad + P_{\lambda}(\text{SPAM} | x_3) \cdot f_6(\text{SPAM}, x_3) + P_{\lambda}(\text{HAM} | x_3) \cdot f_6(\text{HAM}, x_3) \\
 &\quad + P_{\lambda}(\text{SPAM} | x_4) \cdot f_6(\text{SPAM}, x_4) + P_{\lambda}(\text{HAM} | x_4) \cdot f_6(\text{HAM}, x_4) \\
 &\quad + P_{\lambda}(\text{SPAM} | x_5) \cdot f_6(\text{SPAM}, x_5) + P_{\lambda}(\text{HAM} | x_5) \cdot f_6(\text{HAM}, x_5) \\
 &\quad + P_{\lambda}(\text{SPAM} | x_6) \cdot f_6(\text{SPAM}, x_6) + P_{\lambda}(\text{HAM} | x_6) \cdot f_6(\text{HAM}, x_6) \\
 &= P_{\lambda}(\text{HAM} | x_5) + P_{\lambda}(\text{HAM} | x_6) \\
 &= \frac{\exp(-0,2 + 0,4 + 0)}{\exp(0,2) + \exp(0,5 + (-0,1) + 0,1)} + \frac{\exp(-0,1 + 0,4 + 0)}{\exp(0,3) + \exp(0,2 + (-0,1) + 0)} \\
 &= \frac{\exp(0,2)}{\exp(0,2) + \exp(0,5)} + \frac{\exp(0,3)}{\exp(0,3) + \exp(0,1)}
 \end{aligned}$$

$$\begin{aligned} &\approx \frac{1,22140}{1,22140 + 1,64872} + \frac{1,34986}{1,34986 + 1,10517} \\ &= \frac{1,22140}{1,87012} + \frac{1,34986}{1,45503} \\ &\approx 0,65311 + 0,92772 \\ &= 1,58083 \end{aligned}$$

$$\frac{\partial A_\lambda}{\partial \lambda_6} - \frac{\partial B_\lambda}{\partial \lambda_6} = 2 - 1,58083 = 0,41917$$

Task 3

- $k=1$
 $P(\text{black}|x) = 0$
 $P(\text{white}|x) = \frac{1}{1} = 1$
- $k=3$
 $P(\text{black}|x) = \frac{1}{3}$
 $P(\text{white}|x) = \frac{2}{3}$
- $k=5$
 $P(\text{black}|x) = \frac{2}{5}$
 $P(\text{white}|x) = \frac{3}{5} = 1$

$$\frac{3}{5} < \frac{2}{3} < 1$$

In case of $k=5$ the kNN classifier has the lowest classification confidence.

Programming Task

```
1 import nltk
2 import pandas as pd
3 from nltk.tokenize import word_tokenize
4 from nltk.corpus import stopwords
5 from collections import Counter
6 from operator import itemgetter
7
8 class SVM_Classifier:
9     path = "04-assignment/code/"
10
11     def __init__(self):
12         self.corpus = self.generate_corpus("games-train.csv")
13         self.term_weights_dictionary = self.calc_term_weights_dictionary()
14
15
16     def generate_corpus(self, filename: str) -> pd.DataFrame:
17         """ Take data as an input and generate the corpus for classification.
18             The data-structure is a pandas DataFrame with two columns.
19             The labels are converted in binary values (1 = 'gut', -1='schlecht')
20             and the text is normalized. Some stopwords will be also removed.
21
22             Args:
23                 filename (str): name of the dataset
24
25             Returns:
26                 pd.DataFrame: Pandas DataFrame with two columns(label, text)
27         """
28
29         # import data
30         dataframe = pd.read_csv(self.path + filename, sep="\t", header=None)
31
32         # stops that will remain in the corpus
```

```
34 relevant_stops = set(['nicht', 'nichts', 'kein', 'kein', 'keine', 'keinem', 'keinen', 'keiner', 'keines'])
35
36 # stops to remove
37 stops = set(stopwords.words('german')) - relevant_stops
38
39
40
41 # process data to create corpus
42 label_col, text_col = (dataframe[1].tolist(), dataframe[3].tolist())
43 binary_label_col, normalized_text_col = ([], [])
44
45 for index in range(len(label_col)-1):
46
47     label, text = (label_col[index], text_col[index])
48
49     # covert the labels into binary values
50     # 'gut' = 1, 'schlecht' = -1
51     if label == 'gut':
52         binary_label_col.append(1)
53     else:
54         binary_label_col.append(-1)
55
56
57 # text normalization
58 normalized_text = word_tokenize(str(text).lower())
59
60 # remove stops
61 for token in normalized_text:
62     if token in stops: normalized_text.remove(token)
63
64 normalized_text_col.append(word_tokenize(str(text).lower()))
65
66
67 # create the corpus's data-structure
68 corpus = {'label': binary_label_col, 'text': normalized_text_col}
69
70 return pd.DataFrame(corpus)
71
72
73 def calc_term_weights_dictionary(self) -> dict:
74     """ Calculate the weight of each term and store them in a dictionary.
75     the weight is calculated with term-frequency * label.
76
77     Returns:
78         dict: store the weight as a value of a term
79     """
80     term_weights_dict = {}
81
82     for row in self.corpus.iterrows():
83         label, text = row[-1]
84
85         term_freq_dict = Counter(text)
86
87         for term in term_freq_dict:
```

```
89         if term not in term_weights_dict:
90             term_weights_dict.update({ term: label * term_freq_dict[term] })
91         else:
92             # sum the term frequencies
93             # if the class is 'schlecht' the term's frequency will be
94             # negative
95             term_weights_dict[term] += label * term_freq_dict[term]
96
97     return term_weights_dict
98
99
100
101
102
103
104 if __name__ == "__main__":
105     classifier = SVM_Classifier()
106     dictionary = classifier.term_weights_dictionary
107
108
109     sorted_term_weight_list = sorted(dictionary.items(), key=itemgetter(1))
110
111     print("-"*50, "\n Top 100 result for class 'gut': \n", "-"*50)
112     for term, weight in sorted_term_weight_list[::-1][:100]:
113         print(" ", weight, "\t", term)
114
115     print("\n"*3)
116
117     print("-"*50, "\n Top 100 result for class 'schlecht': \n", "-"*50)
118     for term, weight in sorted_term_weight_list[:100]:
119         print(" ", weight, "\t", term)
```

code/script.py

OUTPUT:

```
1 -----
2 Top 100 result for class 'gut':
3 -----
4 24534      spiel
5 22102      !
6 19037      ist
7 18307      es
8 15812      cool
9 14978      das
10 13549      .
11 12106      macht
12 10989      :
13 10854      super
14 10760      ich
15 10104      und
16 10019      )
17 9793      geil
```

| | | |
|----|------|----------|
| 18 | 8686 | aber |
| 19 | 8514 | gut |
| 20 | 8346 | sehr |
| 21 | 7933 | einfach |
| 22 | 7425 | man |
| 23 | 7323 | spa   |
| 24 | 7083 | , |
| 25 | 6499 | ein |
| 26 | 6411 | nur |
| 27 | 6316 | die |
| 28 | 4627 | echt |
| 29 | 4427 |    |
| 30 | 4038 | finde |
| 31 | 3973 | so |
| 32 | 3931 | zu |
| 33 | 3847 | noch |
| 34 | 3601 | viel |
| 35 | 3489 | nachbarn |
| 36 | 3476 | auch |
| 37 | 3024 | s  chtig |
| 38 | 2906 | kann |
| 39 | 2805 | suche |
| 40 | 2802 | f  r |
| 41 | 2692 | richtig |
| 42 | 2586 | der |
| 43 | 2569 | mich |
| 44 | 2531 | toll |
| 45 | 2478 | wenn |
| 46 | 2464 | ; |
| 47 | 2463 | game |
| 48 | 2439 | mit |
| 49 | 2390 | gutes |
| 50 | 2365 | dieses |
| 51 | 2252 | voll |
| 52 | 2128 | adden |
| 53 | 2127 | spiele |
| 54 | 2058 | liebe |
| 55 | 2051 | cooles |
| 56 | 2023 | top |
| 57 | 1967 | hammer |
| 58 | 1934 | tolles |
| 59 | 1900 | bin |
| 60 | 1765 | * |
| 61 | 1717 | mir |
| 62 | 1686 | neue |
| 63 | 1679 | hat |
| 64 | 1668 | geiles |
| 65 | 1647 | beste |
| 66 | 1637 | sind |
| 67 | 1623 | sonst |
| 68 | 1616 | immer |
| 69 | 1602 | ... |
| 70 | 1541 | weiter |
| 71 | 1531 | klasse |
| 72 | 1471 | muss |
| 73 | 1451 | alles |

```
74 1431 langweilig
75 1428 bitte
76 1420 freunde
77 1411 manchmal
78 1394 wie
79 1385 zeitvertreib
80 1350 app
81 1337 also
82 1329 spass
83 1298 ganz
84 1271 gibt
85 1250 lol
86 1240 is
87 1227 5
88 1202 sterne
89 1198 mega
90 1189 w  re
91 1176 was
92 1153 eine
93 1131 auf
94 1114 spielen
95 1087 l  uft
96 1062 k  nnte
97 1057 empfehlen
98 1057 dass
99 1040 ihr
100 1000 wirklich
101 991 weil
102 987 jeden
103 985 nie
```

```
-----
108
109 Top 100 result for class 'schlecht':
110 -----
```

```
111 -2016 nicht
112 -1837 mehr
113 -1183 seit
114 -987 update
115 -953 beheben
116 -902 komme
117 -721 rein
118 -711 ?
119 -711 ins
120 -678 weg
121 -641 event
122 -632 war
123 -619 st  rzt
124 -588 geht
125 -564 dem
126 -542 nichts
127 -534 st  ndig
128 -498 soll
129 -473 keinen
```


| | | |
|-----|------|---------------|
| 130 | -453 | heute |
| 131 | -419 | letzten |
| 132 | -408 | verbindung |
| 133 | -407 | gar |
| 134 | -367 | neu |
| 135 | -359 | komm |
| 136 | -355 | ab |
| 137 | -353 | server |
| 138 | -350 | deinstalliert |
| 139 | -343 | anfangen |
| 140 | -321 | tagen |
| 141 | -318 | fehler |
| 142 | -308 | starten |
| 143 | -303 | vorne |
| 144 | -303 | schei   |
| 145 | -302 | schei   |
| 146 | -299 | nix |
| 147 | -279 | gel  scht |
| 148 | -269 | startet |
| 149 | -257 | behebt |
| 150 | -255 | l  sst |
| 151 | -246 | werde |
| 152 | -226 |   ffnen |
| 153 | -221 | 22 |
| 154 | -218 | wieder |
| 155 | -218 | steht |
| 156 | -217 | stern |
| 157 | -210 | m  glich |
| 158 | -208 | obwohl |
| 159 | -202 | nun |
| 160 | -198 | mist |
| 161 | -191 | dann |
| 162 | -190 | support |
| 163 | -189 | 0 |
| 164 | -176 | gestern |
| 165 | -170 | spielstand |
| 166 | -168 | null |
| 167 | -165 | % |
| 168 | -157 | schl  ssel |
| 169 | -154 | l  dt |
| 170 | -150 | kotzen |
| 171 | -145 | -.- |
| 172 | -143 | wurde |
| 173 | -137 | 1 |
| 174 | -137 | gekauft |
| 175 | -136 | anmelden |
| 176 | -136 | zynga |
| 177 | -134 | behoben |
| 178 | -133 | entt  uscht |
| 179 | -132 | sauer |
| 180 | -130 | bekomme |
| 181 | -129 | wollte |
| 182 | -127 | raus |
| 183 | -125 | investiert |
| 184 | -121 | zur  ck |
| 185 | -121 | passiert |

| | | |
|-----|------|----------------|
| 186 | -119 | bildschirm |
| 187 | -118 | beendet |
| 188 | -115 | sofort |
| 189 | -115 | deinstallieren |
| 190 | -114 | abzocke |
| 191 | -113 | belohnung |
| 192 | -113 | scheisse |
| 193 | -112 | installiert |
| 194 | -112 | dauernd |
| 195 | -111 | beim |
| 196 | -108 | laden |
| 197 | -106 | langsam |
| 198 | -106 | installieren |
| 199 | -105 |   rgerlich |
| 200 | -104 | andauernd |
| 201 | -103 | wochen |
| 202 | -99 | seid |
| 203 | -98 | trotz |
| 204 | -97 | sekunden |
| 205 | -96 | morgen |
| 206 | -95 | zeigt |
| 207 | -94 | angezeigt |
| 208 | -93 | pl  tzlich |
| 209 | -91 | bricht |
| 210 | -89 | m  ll |