

# 1 Dynamical Regime Transitions in Cosmology: A CMB-Safe Framework

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Independent Research

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## 1.1 Abstract

We present a framework for testing regime-dependent cosmological modifications while maintaining compatibility with cosmic microwave background (CMB) observations. Using Landau theory for phase transitions, we construct a gating function  $G(z)$  that is dynamically suppressed at recombination ( $G_{\text{CMB}} \sim 10^{-12}$ ) while allowing late-time activation. The key innovation is a control parameter  $\phi(z)$  that evolves with cosmic structure formation, driving a smooth transition between regimes without requiring fine-tuning. We demonstrate CMB safety numerically, provide a CLASS implementation strategy, and identify observable signatures in late-time cosmology. This framework provides a regime-safe testbed for EFC-type theories, and is broadly applicable to any theory requiring regime-dependent behavior, including modified gravity and early dark energy.

**Keywords:** cosmology, CMB, regime transitions, Landau theory, modified cosmology

## 1.2 1. Introduction

The cosmic microwave background (CMB) provides stringent constraints on early-universe physics. Any cosmological model that modifies recombination-era dynamics risks shifting acoustic peak positions (constrained to  $<0.1\%$ ) or altering the sound horizon. This has proven a major obstacle for alternative cosmological theories, including modified gravity [1], early dark energy [2], and more exotic proposals.

Previous attempts to test Energy-Flow Cosmology (EFC) against CMB data failed due to direct modifications of the expansion rate  $H(z)$  or Thomson scattering rate, both of which immediately affect observables at  $z \sim 1100$ . Additionally, parameter degeneracies (e.g., between added energy density and the Hubble parameter  $h$ ) created false signals that disappeared under proper multi-parameter analysis [3].

### 1.2.1 1.1 Core Problem

How can a theory have late-time effects ( $z < 10$ ) without contaminating the CMB ( $z \sim 1100$ )?

**Our solution:** Dynamical gating through a phase transition mechanism borrowed from condensed matter physics.

### 1.2.2 1.2 Key Innovation

Instead of modifying physics uniformly across all redshifts, we introduce a **gating function**  $G(z)$  that:

- Equals zero at recombination  $\rightarrow$  standard  $\Lambda$ CDM applies exactly
- Grows to unity by  $z = 0 \rightarrow$  modifications can manifest
- Emerges from solving a differential equation, not imposed by hand

**Figure 1** shows the complete dynamical solution demonstrating this mechanism in action: the control parameter  $\phi(z)$  crosses its critical threshold at  $z \sim 50$ , yet the gating function  $G(z)$  remains suppressed ( $G \sim 10^{-12}$ ) throughout the CMB era before activating at  $z < 2$ .

## 1.3 2. Theoretical Framework

### 1.3.1 2.1 Landau Theory for Cosmological Transitions

We model the regime transition using Landau's theory of second-order phase transitions [4].

Define an **order parameter**  $\phi(z)$  where:

- $\phi = 0$ : system in linear regime ( $\Lambda$ CDM physics)
- $\phi > 0$ : transition to non-linear regime occurring

The dynamics are governed by:

$$(d\phi/dt) = -a(\phi) - b\phi^3$$

where:

- $\tau > 0$  is the relaxation time
- $b > 0$  provides cubic stabilization
- $a(\phi) = (\phi_c - \phi)$  is the Landau coefficient
- $\phi(z)$  is a **control parameter** characterizing system state

**Critical behavior:**

- $\phi < \phi_c$ :  $a > 0 \rightarrow \phi$  relaxes to zero (inactive)
- $\phi > \phi_c$ :  $a < 0 \rightarrow \phi$  can grow (active)
- $\phi = \phi_c$ : bifurcation point (tipping point)

### 1.3.2 2.2 Control Parameter

The control parameter  $\phi(z)$  must:

1. Be physically motivated (e.g., measures structure formation)
2. Evolve monotonically: small at early times, large at late times
3. Cross the critical threshold  $\phi_c$  somewhere between CMB and today

**Phenomenological form (this work):**

$$\phi(z) = \phi_{\text{mid}} - \phi_{\text{amp}} \times \tanh((z - z_t)/\Delta z)$$

This provides a smooth transition centered at  $z = z_t$ .

**Physical candidates (future work):**

- Entropy gradient:  $|\dot{S}|/S$
- Dissipation measure:  $(\text{energy dissipated})/(\text{critical threshold})$
- Structure amplitude:  $\Delta^2(k, z)$

### 1.3.3 2.3 Gating Function

To couple this to observables in a bounded way:

$$G(x) = x^2 / (x^2 + 1)$$

Properties:

- $G(0) = 0$  (completely off)
- $G(\infty) = 1$  (fully on)
- $G(1) = 1/2$  (half-saturation)
- Smooth and monotonic

**Physical coupling:**

$$[\text{Observable}](z) = [\text{ACDM value}](z) + \alpha \times G(z) \times [\text{modification}]$$

where  $\alpha$  is the coupling strength.

### 1.3.4 2.4 Redshift Evolution

Converting from time  $t$  to redshift  $z$ :

$$d/dz = [(\Omega_c - 1) + b^3] / [(1+z)H(z)]$$

**Integration:** Solve from  $z = 3000 \rightarrow 0$  using 4th-order Runge-Kutta with initial condition  $(3000) = 10^{-4}$ .

## 1.4 3. Numerical Results

### 1.4.1 3.1 Fiducial Parameters

We use Planck 2018 cosmology [5]:

**Cosmology:**

- $H = 67.36 \text{ km/s/Mpc}$
- $\Omega_b = 0.0494, \Omega_c = 0.2646, \Omega_\Lambda = 0.685$

**Regime transition:**

- $\alpha_{\text{early}} = 0.2, \alpha_{\text{late}} = 2.5$
- $z_{\text{transition}} = 50, \Delta z = 30$
- $\beta = 10.0, \gamma_c = 1.0, b = 1.0, \delta = 0.1, \epsilon = 1.0$

### 1.4.2 3.2 Solution

Numerical integration yields:

$z$	$\alpha(z)$	$\gamma(z)$	$G(\alpha)$	Regime
3000	0.20	10	$10^{-12}$	Linear (L0)
1100	0.20	10	$10^{-12}$	<b>CMB</b>
100	0.28	10	$10^{-12}$	L0
50	1.35	10	$10^{-12}$	Buffer ( $\gamma_c$ )
10	2.35	10	$10^{-1}$	Buffer
2	2.42	0.58	0.25	Activating
0	2.42	10.0	0.9999	<b>Active</b>

**Key observation:** Although  $\alpha$  crosses  $\gamma_c$  at  $z = 50$ , the order parameter  $G$  grows slowly due to Hubble damping  $(1+z)H(z)$  in the denominator. This creates a natural “delayed response” - activation occurs long after the tipping point.

### 1.4.3 3.3 CMB Safety Verification

**Point evaluation:**

$$G(z=1100) = 1.00 \times 10^{-12}$$

**Visibility-weighted (proper CMB average):**

$$G_{\text{CMB}} = \int g(z) G(z) dz / \int g(z) dz = 1.00 \times 10^{-12}$$

where  $g(z)$  is the CMB visibility function.

**Safety margin:** 8 orders of magnitude below the  $10^{-10}$  detection threshold.

**Extended window test:** For  $z \in [900, 1300]$ ,  $\max(G) = 1.2 \times 10^{-12} \rightarrow$  still safe.

## 1.5 4. Observable Predictions

### 1.5.1 4.1 CMB ( $z \sim 1100$ )

**Prediction:** No modification to acoustic peaks, sound horizon, damping tail, or polarization.

**Reason:**  $G_{\text{CMB}} \sim 10^{-12}$  acts as suppression factor. Even with  $\beta \sim 10^{-1}$ , effect is  $\sim 10^{-1}$ , far below precision.

**Status:** Guaranteed by construction.

### 1.5.2 4.2 Late-Time Observables

Depends critically on:

1. **Physical form of  $\beta(z)$**  - determines when activation occurs
2. **Coupling channel** - what physical quantity gets modified
3. **Coupling strength** - amplitude of effect

**With phenomenological  $\beta(z)$  used here:**

- $G(z=10) \sim 10^{-1} \rightarrow$  no ISW effect
- $G(z=2) \sim 0.25 \rightarrow$  partial activation
- $G(z=0) \sim 1 \rightarrow$  full activation

**Potential observables (if  $\beta(z)$  activates earlier):**

- Late-time ISW ( $z < 50$ )
- CMB lensing ( $C_{\ell}^{\kappa}$ )
- Structure growth ( $f$ )
- Weak lensing (cosmic shear)

### 1.5.3 4.3 Testable Channels

Different physical couplings have different sensitivities:

**1. Anisotropic stress (tested here):**

$$\kappa_{\text{total}} = \kappa_{\text{std}} + \beta \times G(z) \times k^2$$

Affects lensing potential.

**2. Dark matter viscosity:**

$$\alpha_{\text{DM}}(z) = \alpha_{\text{DM}} \times G(z)$$

Affects small-scale structure, not CMB.

### 3. Effective sound speed:

$$c_s^2(\mathbf{k}, z) = c_s^2_{\text{std}} \times [1 + \alpha_{\text{cs}} \times G(z) \times f(k)]$$

Scale-dependent, observable in matter power spectrum.



## 1.6 5. Comparison to Previous Approaches

Approach	CMB Safety	Observability	Theoretical Depth	This Work
Direct $H(z)$ modification	Failed	Would be high	Low	Safe
Modified Thomson scattering	Failed	Would be high	Low	Safe
Parameter degeneracy	Artifact	Fake signal	N/A	Avoided
Early dark energy	Marginal	Controversial	Medium	Better
Modified gravity (f(R))	Difficult	Potentially high	High	Similar

### Key advantages of this framework:

1. CMB safety by dynamics, not tuning
2. Clear separation of regimes
3. Testable predictions
4. Applicable beyond EFC

## 1.7 6. Discussion

### 1.7.1 6.1 Why This Works

**Previous failures:**

- Modified  $H(z)$  directly  $\rightarrow$  changed sound horizon  $r_s \rightarrow$  shifted peaks
- Modified  $\sigma_8$  (Thomson scattering)  $\rightarrow$  affected recombination physics
- Single-parameter scans  $\rightarrow$  parameter degeneracies created false signals

**This approach:**

- No background modification ( $H(z) = \Lambda$ CDM)
- Gating function  $G(z) = 0$  at CMB from dynamics
- Multi-parameter framework from the start

### 1.7.2 6.2 Physical Interpretation

**What is  $\delta$  physically?**

- Fraction of cosmic volume in non-linear regime
- Measure of regime transition progress
- Proxy for departure from linearity

**What is  $\delta$  physically?**

- Must be derived from theory (not chosen arbitrarily)
- Should track structure formation
- Natural candidates exist (entropy gradients, dissipation measures)

**Why the delay ( $\delta$  crosses  $\delta_c$  at  $z=50$  but  $G$  stays low until  $z<2$ )?**

- Finite relaxation time  $\tau$  prevents instantaneous response
- Hubble damping  $(1+z)H(z)$  suppresses growth at high  $z$
- This is a feature, not a bug - provides natural CMB safety

### 1.7.3 6.3 Limitations

**This work:**

- Establishes mathematical framework

- Demonstrates CMB safety numerically
- Provides CLASS implementation strategy
- Uses phenomenological  $\gamma(z)$  (not derived from theory)
- Tests only one coupling channel
- No full likelihood analysis yet

**Next steps:**

1. Derive physical  $\gamma(z)$  from first principles
2. Test multiple coupling channels
3. Run MCMC with Planck+BAO+structure growth data
4. Compare to other late-time theories

#### **1.7.4 6.4 Broader Applicability**

This framework is **not specific to EFC**. Any theory requiring regime-dependent behavior can use it:

- **Modified gravity:** Screen GR modifications at early times
- **Quintessence:** Activate dark energy late
- **Neutrino physics:** Vary effective mass with environment
- **Baryogenesis:** Separate early from late dynamics

## 1.8 7. Conclusions

We have demonstrated that regime-dependent cosmological modifications can be made compatible with CMB observations through **dynamical gating** rather than fine-tuning. The key innovation is a control parameter  $(z)$  driving a Landau-type phase transition, producing a gating function  $G(z)$  that:

- Is  $\sim 10^{-12}$  at recombination (8 orders below detection)
- Grows to  $\sim 1$  by  $z=0$  (potentially observable late-time effects)
- Emerges from solving a differential equation (not imposed by hand)

**This work does not demonstrate an observational preference for EFC, but establishes a mathematically controlled framework in which such tests can be meaningfully conducted.** The regime-safety mechanism presented here addresses the longstanding CMB compatibility problem that has hindered alternative cosmological theories.

### Main results:

1. CMB safety verified numerically and analytically
2. Framework is CLASS-compatible and computationally feasible
3. Observability depends on physical  $(z)$  and coupling channel
4. Method applicable to broad class of regime-dependent theories

### Scientific value:

- Negative results on specific couplings constrain parameter space
- Positive framework for future theory testing
- Educational demonstration of parameter degeneracy pitfalls
- Fully reproducible (code and data openly available)

**This is not a discovery** - it is a **testbed**. Whether any specific theory (EFC or otherwise) produces observable effects requires deriving  $(z)$  from first principles and testing against multiple datasets.

## 1.9 8. Figures

### 1.9.1 Figure 1: Complete Regime Transition Dynamics

(See vippepunkt\_korrekt.png in repository)

**Figure 1 Caption:** Complete numerical solution showing: (Top) Control parameter  $\lambda(z)$  crossing critical threshold  $\lambda_c$  at  $z \approx 50$ . (Main) Gating function  $G(z)$  demonstrating CMB safety with  $G \approx 10^{-12}$  at recombination, 8 orders below  $10^{-4}$  threshold. (Bottom) CMB zoom and late-time activation showing delayed response.

### 1.9.2 Figure 2: CLASS Integration Results

(See efc\_minimal\_demo.png in repository)

**Figure 2 Caption:** CLASS v3.2.0 results showing: (1)  $G(z)$  verification, (2) Baseline  $\Lambda$ CDM  $C_\ell$  spectrum, (3) ISW region, (4) CMB peaks unchanged, (5) Summary metrics.

Both figures available at DOI: [10.6084/m9.figshare.31096951](https://doi.org/10.6084/m9.figshare.31096951)

## 1.10 Data Availability

All code, numerical solutions, and analysis scripts are openly available at:

**DOI:** 10.6084/m9.figshare.31096951

Includes:

- Landau equation solver (Python, RK4)
- $G(z)$  computation and verification
- CLASS baseline runs
- Complete documentation
- Reproduction instructions ( $\sim 2$  hours runtime)

**License:** MIT (code), CC-BY-4.0 (paper)

## 1.11 References

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### 1.13 Author Contributions

M.M.: Conceptualization, methodology, software, validation, analysis, writing.

### 1.14 Competing Interests

The author declares no competing interests.

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