

Table 2: **Bootstrap Robustness Analysis: Quantile Regression (1,000 Iterations)**

*To test the stability of the structural signal in quantile regression, we performed a bootstrap analysis with 1,000 resamples (with replacement) from the 1970–2025 dataset. The table reports the distribution of the relative improvement in Pseudo- $R^2$  for tail-risk prediction when adding the CARIA\_Peak signal to the baseline volatility model.*

Statistic	Value
Iterations	1,000
Positive Improvement Probability	<b>100.0%</b>
Mean Improvement ( $\Delta R^2$ )	<b>+26.3%</b>
95% Confidence Interval	[ <b>12.2%</b> , <b>45.7%</b> ]