

1 Stationary limit of the underdamped Fokker-Planck equation

2 Ideal Gas - Momentum in the microcanonical ensemble

3 Computer exercise - Monte Carlo integration

The algorithm can be implemented using the following python code snippet:

```
1  import numpy as np
2
3  A = 0
4
5  N = 100000
6  for _ in range(N):
7      x = np.random.uniform(-1, 1)
8      y = np.random.uniform(-1, 1)
9      if x**2 + y**2 <= 1:
10         A += 1
11
12  z = 4 * A / N
13  print(z)
```

With this, a value for π can be estimated, running the above code returns 3.14312. The ratio of A to N is directly proportional to another ratio, namely that of the area of a unit circle to the area of a square with side length 2. One could thus in principle calculate π by e.g. throwing darts onto a square surface with a circle drawn on it. This is because the number of "hits" can be assumed to be proportional to the hit probability, which again is directly proportional to the respective area. This method can only work if the distribution of random numbers is uniform and N is large enough.

Visualization:

