Assignment 2: Dynamic Programming project

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1 Recursive function

```
struct maxS {
    int current;
                    // Current sum
                    // Overall max
    int max;
  struct maxS MaxSubarray(int array[], int size) {
    struct maxS ms;
                      // Base case
    if (size == 1) {
      ms.current = 0;
      ms.max = array[0];
11
    } else { // Recurse on array excluding last element.
      ms = MaxSubarray(array, size -1);
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    // Find maximum.
    ms.current += array[size -1];
    ms.current = (ms.current > 0) ? ms.current : 0;
    ms.max = (ms.current > ms.max) ? ms.current : 0;
19
21
    return ms;
```

rec.cpp

Where maxS is a struct holding the running sum and the overall maximum sum and MaxSubarray is the recursive function. For an array A of size n, we find the maximum subarray with MaxSubarray(A, n).

2 Pseudocode

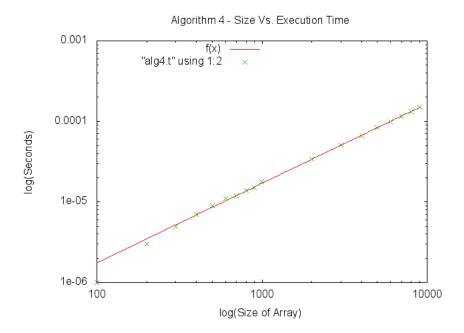
```
MaxSubarray(array, size):
    current = 0;
    max = 0;

for i=0 to size:
        current = current + array[i]
    if current < 0:
        current = 0
    else if current > max:
        max = current

return max
```

3 Running time

Using the Log-Log plot will give us a good hint for the asymptotic run times. The slope for the graph is 0.987956, meaning that the asymptotic run times is around $\Omega(n)$. Then looking at the code, it only looks at each element once, making it $\Omega(n)$



4 Theoretical correctness

```
Induction Proof. MS(k) will return the maximum subarray sum for the array A[0:k] Base case: If n=-1 then max=current=0 Inductive Step: maxSubarray(n-1).current+A[n] or 0 is the current largest sum starting from the left Proof:

Case if A[n]>0 then current=MS(n-1).current+A[n]>MS(n-1).current.

This number might also be the max value. So max=Greater(max,current) Case if A[n]>-maxSubarray(n-1) then maxSubarray(n-1)+A[n]<0 making the Null set greater. max=MS(n-1).max and current=0 Case else making A[n] negative but maxSubarray(n-1)+A[n]>=0 so it is still good to use for the next current: current+A[n+1]>A[n+1] max=MS(n-1).max and current=maxSubarray(n-1)+A[n] MS(n).max=max and MS(n).current=current
```

5 Implement

5.1 Algorithm 4

```
/*
* Enumeration
* Loop over each pair of indices i; j and compute the sum from k=i to j of a[k].

* Keep the best sum you have found so far.
```

```
using namespace std;
  int MaxSubarray(int a[], int n){
     int current = 0;
     int max = 0;
     int i;
     for (i = 0; i < n; i++){
       current += a[i];
       if(current \ll 0){
         current = 0;
       }else if(current > max){
         \max = current;
19
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21
22
     return max;
```

alg4.cpp

6 Test

Test were run on the ms_test.txt file given last project and large arrays given by student ids.

7 Compare

Well, there is a huge difference as seen on the Compare Plot. Algorithm 4, Dynamic Programming, is great because doesn't use any recurvive calls and doesn't need to hold much data. Algorithm 4 only needs to hold onto 2 integers (max and current) and the input integer array. Whereas algorithm 3, divide & conquer, needs to use memory on the stack for each recurvive call and needs to pass 4 integers back to the parent function.

WHAT THE HELL IS GOOD ABOUT D&C???

