

# Chapter - 4

## **Three Dimensional Transformation, Viewing and Projection**

# 3-D Projections

We can project the 3-D objects onto the 2-D plane. So Projection can be defined as a mapping of point  $P$  onto its image  $P'$  in the projection plane or view plane.

There are two basic projection methods:

- Parallel projection
- Perspective projection

# Projections

Transform 3D objects on to a 2D plane using ***projections***

## **2 types of projections**

*Perspective*

*Parallel*

In **parallel projection**, coordinate positions are transformed to the view plane along parallel lines.  
In **perspective projection**, object position are transformed to the view plane along lines that converge to a point called **projection reference point (center of projection)**

# PROJECTIONS

## PARALLEL

(parallel projectors)

### Orthographic

(projectors perpendicular to view plane)

### Multiview

(view plane parallel to principal planes)

### Axonometric

(view plane not parallel to principal planes)

Isometric

Dimetric

Trimetric

### Oblique

(projectors not perpendicular to view plane)

### General

## PERSPECTIVE

(converging projectors)

### One point

(one principal vanishing point)

### Two point

(Two principal vanishing point)

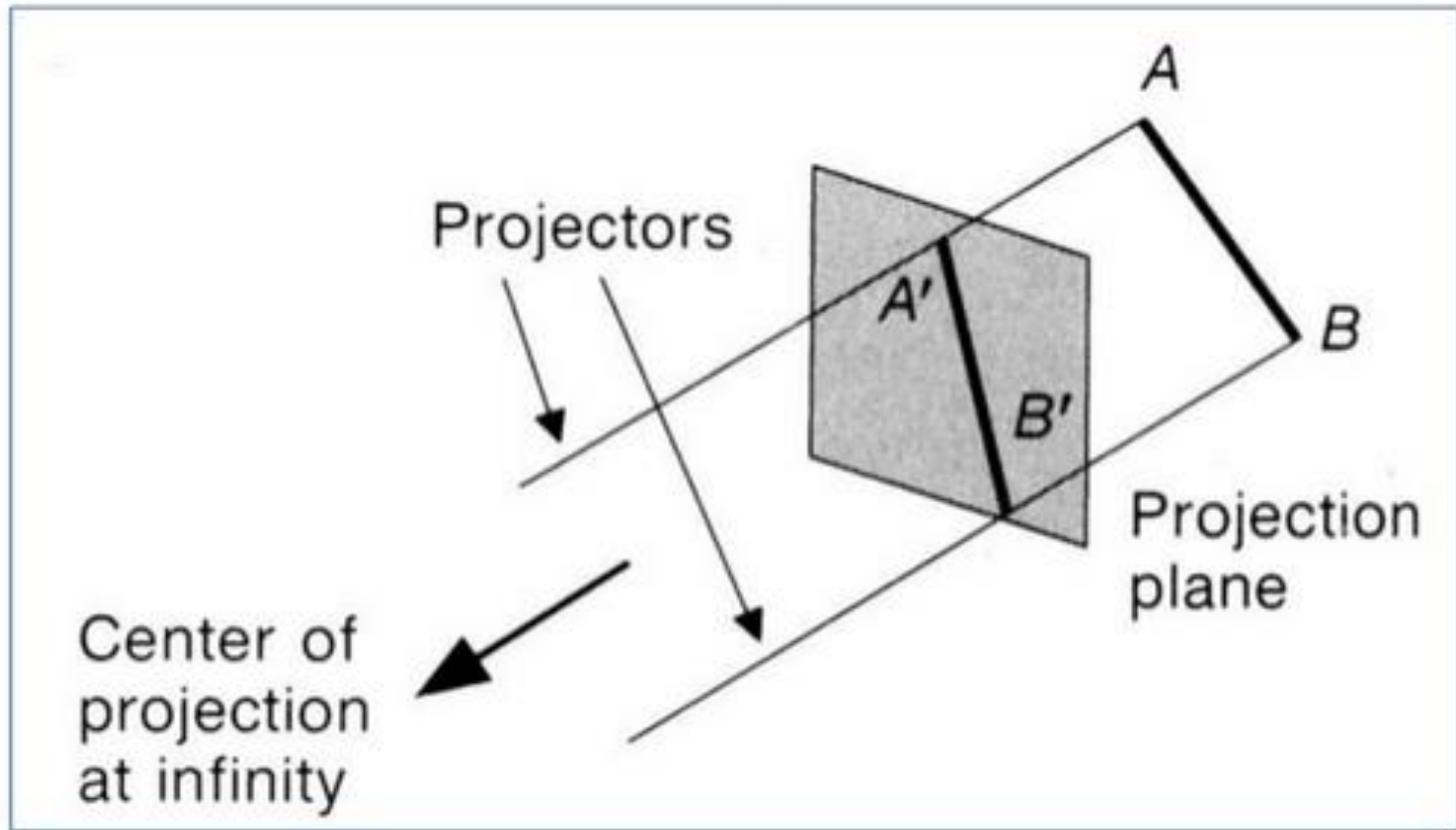
### Three point

(Three principal vanishing point)

Cavalier

Cabinet

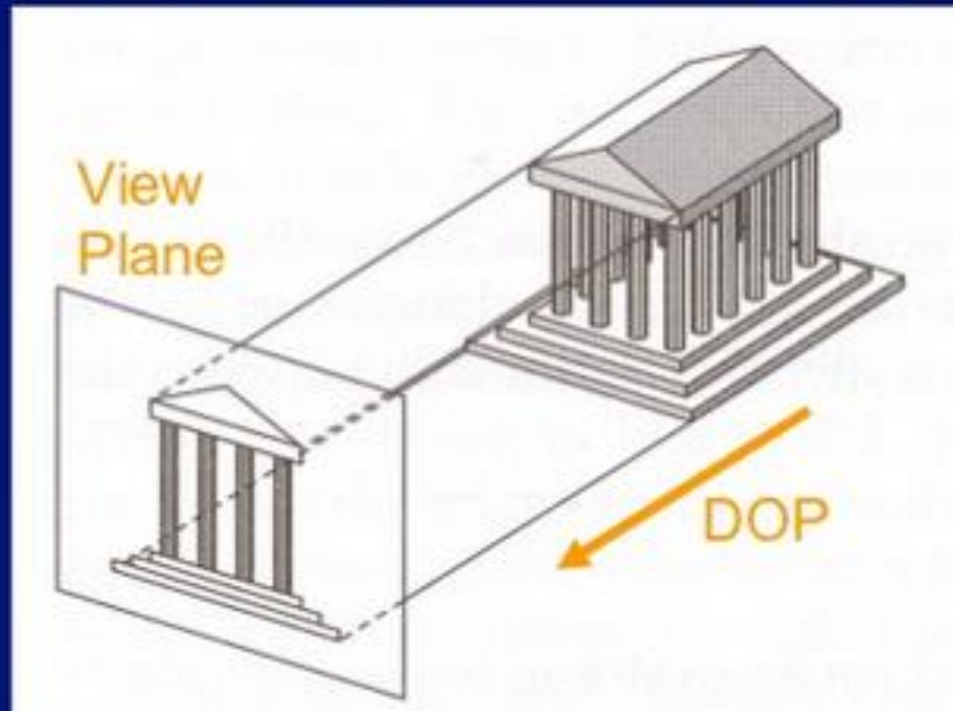
# Parallel Projection



# Parallel Projection

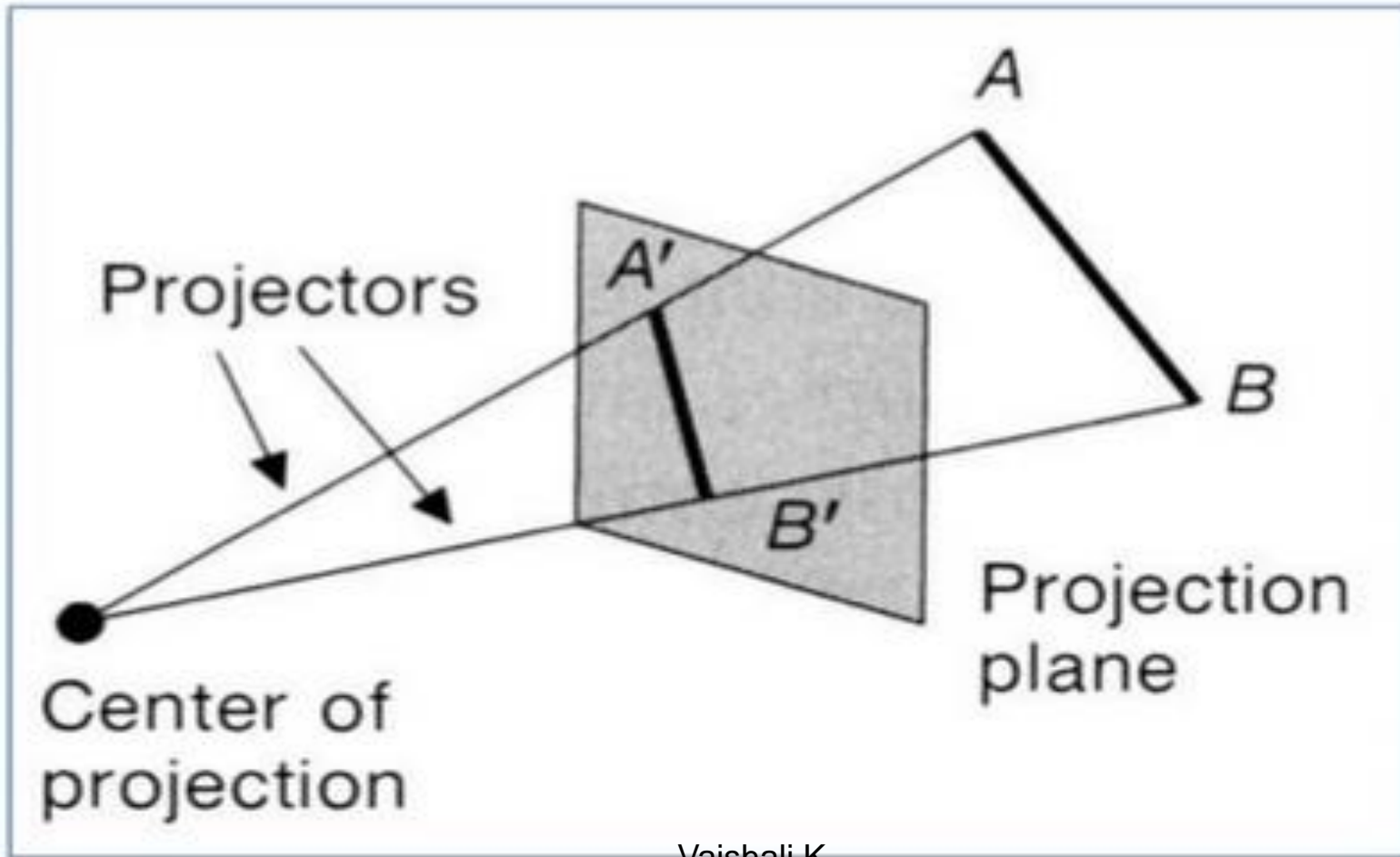
***Center of projection is at infinity***

- Direction of projection (DOP) same for all points

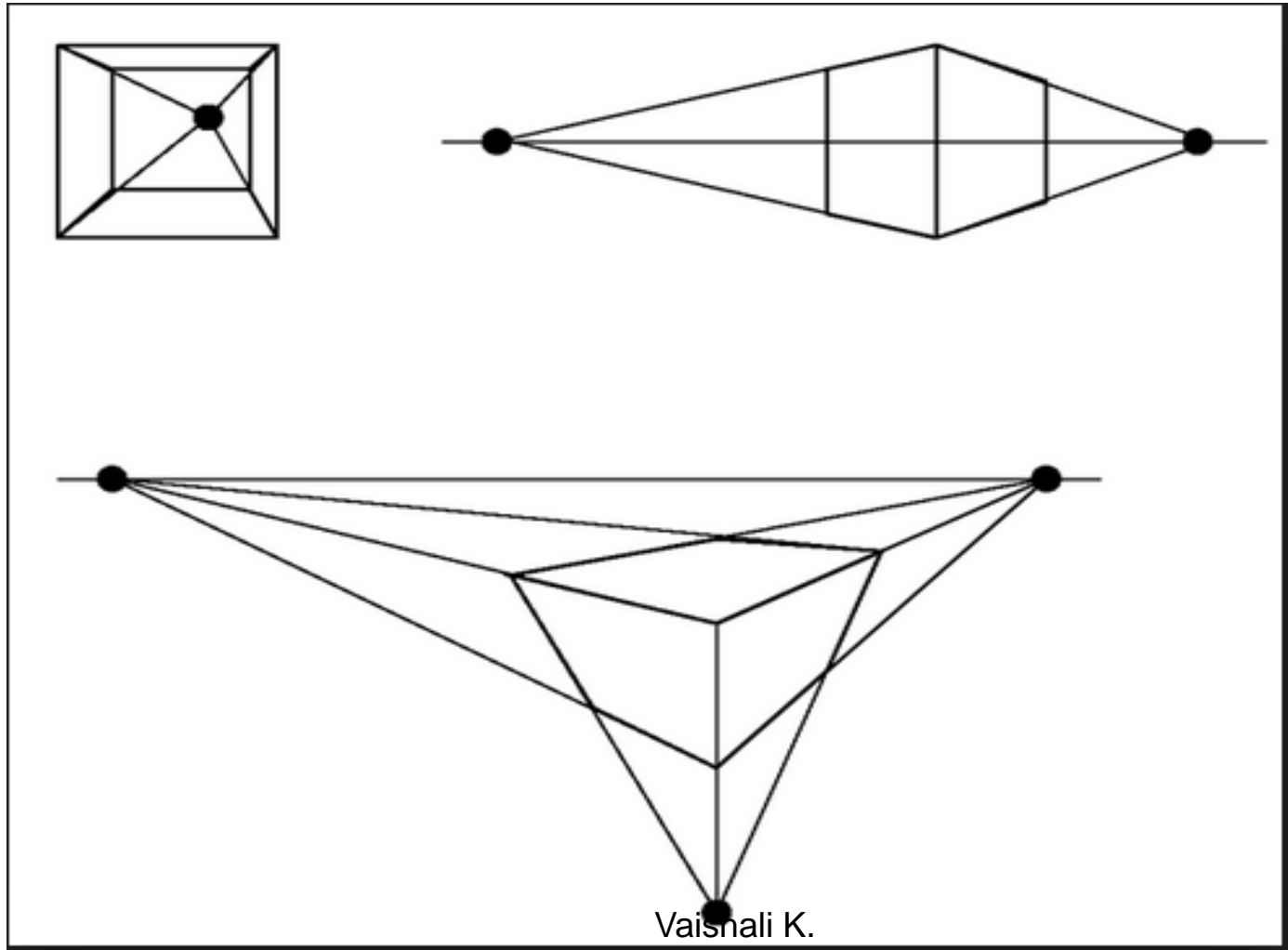




# Perspective Projection

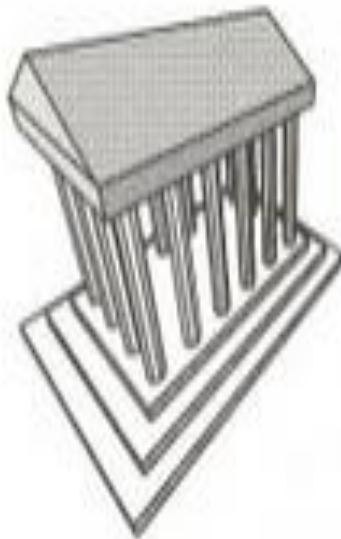


# Prospective Projection- One Point , Two Point , Three point





# Prospective Projection



3-Point



2-Point



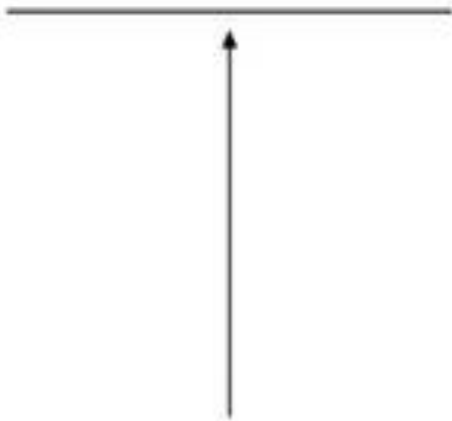
1-Point

# Perspective vs. parallel projections

- **Perspective projections pros and cons:**
  - **Size varies inversely with distance – looks realistic**
  - **Distance and angles are not (in general) preserved**
  - **Parallel lines do not (in general) remain parallel**
- **Parallel projection pros and cons:**
  - **Less realistic looking**
  - **Good for exact measurements**
  - **Parallel lines remain parallel**
  - **Angles not (in general) preserved**

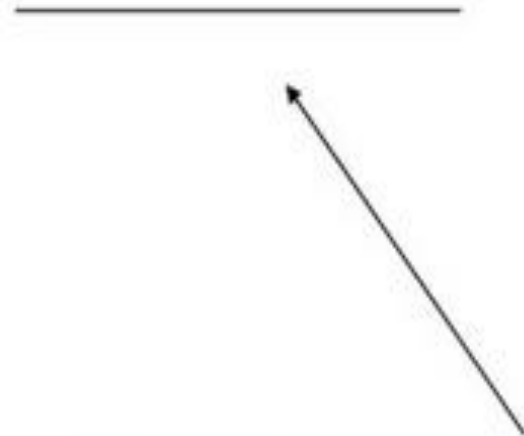
# Parallel Projection

- Orthographic projection



when the projection is  
perpendicular to the view  
plane

## Oblique projection



when the projection is not  
perpendicular to the view  
plane

# Orthographic Projection

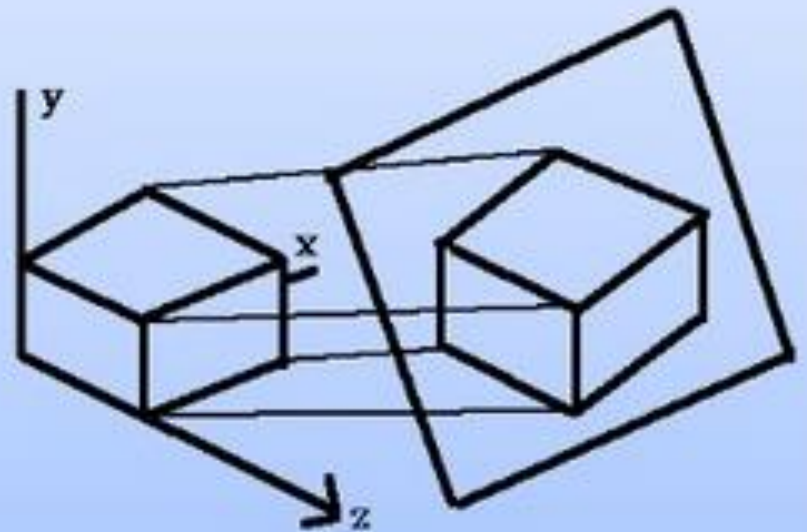
- Front, side and rear orthographic projection of an object are called **elevations** and the **top** orthographic projection is called **plan view**.
- all have projection plane perpendicular to a principle axes.
- Here length and angles are accurately depicted and measured from the drawing, so engineering and architectural drawings commonly employee this.
- However, As only one face of an object is shown, it can be hard to create a mental image of the object, even when several views are available.

## Axonometric orthographic projections

- Orthographic projections that *show more than one face of an object* are called **axonometric** orthographic projections.

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- The most common axonometric projection is an **isometric** projection where the projection plane intersects each coordinate axis in the model coordinate system at an equal distance.

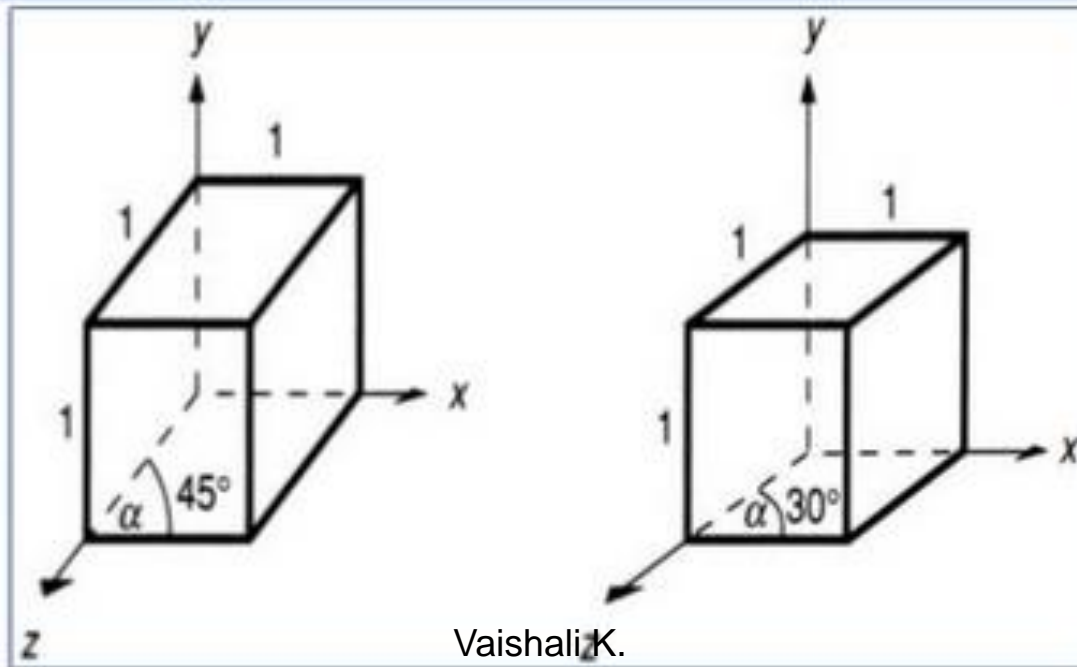




- 2 common oblique parallel projections:  
*Cavalier* and *Cabinet*

### Cavalier projection:

All lines perpendicular to the projection plane are projected with no change in length.



## Cabinet projection:

- Lines which are perpendicular to the projection plane (viewing surface) are projected at  $1/2$  the length .
- This results in foreshortening of the z axis, and provides a more “realistic” view.

