

$$A := \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 1 & 1 & 0 \end{bmatrix} \quad B := \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} \quad x(n) := \sum_{j=0}^{n-1} A^{n-1-j} \cdot B$$

$$\begin{aligned} x(1) &= \begin{bmatrix} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} & x(2) &= \begin{bmatrix} 1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 1 \end{bmatrix} & x(3) &= \begin{bmatrix} 1 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \end{bmatrix} & x(4) &= \begin{bmatrix} 1 \\ 1 \\ 2 \\ 4 \\ 7 \\ 11 \end{bmatrix} & x(5) &= \begin{bmatrix} 1 \\ 1 \\ 2 \\ 4 \\ 8 \\ 15 \end{bmatrix} \\ x(6) &= \begin{bmatrix} 1 \\ 1 \\ 2 \\ 4 \\ 8 \\ 16 \end{bmatrix} & x(7) &= \begin{bmatrix} 1 \\ 1 \\ 2 \\ 4 \\ 8 \\ 16 \end{bmatrix} \end{aligned}$$

$$A^2 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 2 & 1 & 0 & 0 & 0 & 0 \\ 3 & 2 & 1 & 0 & 0 & 0 \\ 4 & 3 & 2 & 1 & 0 & 0 \end{bmatrix} \quad A^3 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 3 & 1 & 0 & 0 & 0 & 0 \\ 6 & 3 & 1 & 0 & 0 & 0 \end{bmatrix} \quad A^4 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \\ 4 & 1 & 0 & 0 & 0 & 0 \end{bmatrix}$$