# OOPS Documentation

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## 1 Introduction

Let's talk about how scientific codes get written. Some graduate student named Steve has a tough problem to solve, so he learns just enough coding and numerical methods to solve his one problem. The code isn't pretty, but it doesn't have to be because it's simple and easy-to-use for Steve's one problem. Steve eventually graduates, but his advisor, Dr. Fred Smith, holds onto a copy of the code because it works so well.

Now enters Bob, a bright-eyed graduate student with enough stupidity ambition to pursue Dr. Smith's next tough problem and absolutely no coding experience. This tough problem happens to be somewhat similar to Steve's problem, so Dr. Smith starts Bob on Steve's old code. Roughly three months later, Bob has modified Steve's code and extended it to work with his problem, too. It's ugly and gross in every way, but it still runs decently quickly and is simple enough that no one cares. He graduates and quickly forgets about the code.

Dr. Smith repeats this cycle with three or four more graduate students, plus about a dozen undergraduates who pop into his research group along the way. Halfway through, Annie the undergrad notices that the code is an absolute trainwreck and decides to rewrite portions of it. Unfortunately, she has to graduate, so she only rewrites the portions that she needs for her project, and now the code is a horrible amalgam of modern object-oriented programming, Steve's hard-coded relics, and everyone else's half-baked tweaks which never should have seen the light of day. Naturally, the documentation is more sparse than an SPS activity without free food, so Dr. Smith's students spend half their time trying to decipher what has become known as "The Frankencode."

The Object-Oriented PDE Solver, or OOPS, is designed to alleviate as many of these problems as possible. By creating a flexible object-oriented design, even those relatively inexperienced with coding and numerical methods can quickly solve their problems without ever having to worry about much more than the PDE itself. At the same time, the framework is flexible enough that those who do need to worry about it can.

## 2 Getting Started with OOPS

Because the OOPS framework is currently so small and lightweight, the entire framework is compiled with each project without any extra library dependencies. We warn the user that this will likely change in a future release as the project grows in scope.

## 2.1 System Requirements

OOPS requires CMake 3.0 or later and a C++ compiler supporting C++11 or later. Some optional features require the bbhutil library from RNPL. This package is quite old and is only known to work on select Linux distributions (Ubuntu 16.04 and RHEL 7.0 have been tested) after a very onerous installation procedure. We recommend a Linux environment (native, virtual machines, or the Windows Subsystem for Linux should work), but any appropriately configured Windows or MacOS environment should work as well, albeit without the optional features depending on bbhutil.

The procedure for building OOPS in Linux is as follows:

```
cd <path to OOPS base directory>
mkdir build
cd build
ccmake ../
```

A configuration menu should appear. Press  $\tt c$  to generate the configuration file. The default options should be sufficient. Press  $\tt c$  again, then  $\tt g$  to generate the make files.

make

After this, all generated executables should appear in the build directory.

#### 2.2 Prior Preparation

OOPS tries to be a simple tool for scientific computing, but the documentation is neither a guide to scientific computing nor a guide to programming in C++. Therefore, the tutorials below do assume a basic knowledge of numerical methods (primarily how to solve ODEs and PDEs using finite-differencing techniques) and C++. No prior experience with CMake (for compiling) or JSON (for writing setup files) is assumed, and more complicated subjects like C++ templates are either ignored or hidden behind the scenes.

#### 2.3 Structure of OOPS

The most basic OOPS program contains the following components:

- A Domain object, which defines the space for your problem.
- One or more Grid objects, which subdivide a Domain into discrete points for numerical calculation.
- A Solver object, such as RK4, which will numerically solve any PDE fed into it.

 An ODE object, which provides the righthand side for a system of ODEs (such as a PDE discretized with finite-difference methods), boundary conditions, and initial conditions.

More complex codes will also make use of Parameter objects and Interpolator objects, but these are not much more difficult to add in. OOPS works as hard as possible to hide as many of the gory details behind the scenes.

## 2.4 Solving a Simple Initial Boundary Value Problem

For this project, we'll create a simple program using OOPS that solves the wave equation on a domain with Neumann (free) boundaries. Begin by building a new project directory for the program:

cd <path to OOPS base directory>
mkdir WaveEquation
cd WaveEquation
mkdir include
mkdir src

The include folder will contain any header files specific to the WaveEquation program, and src will hold the main file and any additional source files required.

Before we start writing our code, remember that the wave equation in one dimension takes the form

$$\partial_{tt}\phi - \partial_{xx}\phi = 0. ag{1}$$

OOPS can't solve this in its current form because the time integrator expects it to be first order in space. Therefore, we make the definition  $\pi = \partial_t \phi$ , which suggests the ODE system

$$\partial_t \phi = \pi, \tag{2}$$

$$\partial_t \pi = \partial_{xx} \phi. \tag{3}$$

OOPS can actually solve this as is because we can just define a second-order derivative operator, but it's just as easy to reduce the spatial order by defining  $\chi = \partial_x \phi$ , giving us the system

$$\partial_t \phi = \pi, 
\partial_t \pi = \partial_x \chi, 
\partial_t \chi = \partial_x \pi,$$
(4)

where the third equation comes from the commutability of partial derivatives. Despite the two systems being mathematically identical and producing solutions to the wave equation, they exhibit very different numerical properties, with the first-order system being more dispersive and the second-order system being more diffusive.

#### 2.4.1 wave.h

The next step is to construct our PDE. In the include directory, create a new file wave.h that reads as follows:

```
1 #ifndef WAVE_H
2 #define WAVEJH
4 #include <ode.h>
6 class Wave : public ODE {
    private:
       // Variable labels
       static const unsigned int U_PHI = 0;
       static const unsigned int U_PI = 1;
10
       static const unsigned int U_CHI = 2;
11
12
     protected:
13
       virtual void applyBoundaries(bool intermediate);
14
15
       virtual void rhs(const Grid& grid, double **u, double **dudt)↔
16
17
     public:
18
       Wave(Domain& d, Solver& s);
       virtual ~Wave();
20
21
22
       virtual void initData();
23 };
24
25 #endif
```

The ode.h file defines the ODE object, which defines an abstract class representing a system of ODEs (or a discretized system of PDEs). We declare a new class, Wave, which inherits from ODE and therefore reduces a lot of the work that we have to do.

Underneath the **private** label, we assign some variable names to our specific indices. This isn't necessary, strictly speaking, but it makes your code a lot more readable when we start writing the righthand-side routine.

For our protected methods, we have two virtual functions, applyBoundaries() and rhs(), which are both inherited from ODE. The method applyBoundaries() is used in the evolution function (which is also virtual and can be overwritten, but the default definition works well enough for this case) to fix the boundaries between each stage of the Solver object we'll attach later. The intermediate flag will be explained in more detail later, but it has to do with figuring out which data set needs to be modified. The rhs() method contains the righthand side of Eq. (4).

Lastly, inside the public region, we have a constructor and a destructor as well as initData(), which contains the initial data for the ODE. This is made public for convenience, as more advanced implementations may have a custom Parameter object, which can be used, among other things, to control the initial

conditions for a specific ODE.

#### 2.4.2 wave.cpp

The next file we need to create is wave.cpp, which is located inside src and contains the definitions for wave.h. We'll take this one piece at a time:

```
#include <wave.h>
#include <operators.h>
#include <iostream>
#include <cmath>
```

Clearly wave.h is the header file we just created. The file operators.h contains a set of pre-defined derivative operators. Next, we need access to the I/O and math functions from the Standard Template Library, so we go ahead and include those.

When we define our constructor, we have to make sure that we call the ODE constructor, ODE(const unsigned int n, const unsigned int id). The first argument, n, is the number of variables for our ODE object, and id is an identifier. For our simple program, id isn't really important, but it's a sort of baroque method for manually type-checking Parameters types and ODE objects. Basically id=0 just means that we can use the default Parameters object.

We are going to construct our ODE method with fourth-order derivative operators, so we need at least two ghost points at the boundaries to ensure that we get fourth-order accuracy. The if statement guarantees that this is the case and spits out an error promising that the solution will behave incorrectly if it is not.

Next, we need to set the domain and solver for our ODE. This should always be done in the constructor so that memory is allocated properly.

The last line needs a little bit of explanation. Whenever we assign a Domain object to our ODE, we need to allocate memory for every single variable at every single point. If this is done for a multi-stage Solver, such as RK4, we

also need to allocate this same amount of memory for each stage. Therefore, any time the Domain or Solver objects are changed, ODE automatically calls reallocateData(). When an ODE object is destroyed, it automatically deallocates this memory. However, the constructor doesn't automatically call this routine because we assign the Domain and Solver manually rather than through the setDomain() and setSolver() methods. Therefore we must explicitly call reallocateData().

The destructor doesn't need to do much because most of the heavy lifting is handled by ODE. Therefore, we leave it empty.

The next piece we need to implement is the rhs() function:

```
void Wave::rhs(const Grid& grid, double **u, double **dudt){
      // Go ahead and define some stuff we will need.
      double stencil3[3] = \{0.0, 0.0, 0.0\};
      double stencil5[5] = \{0.0, 0.0, 0.0, 0.0, 0.0\};
      double dx = grid.getSpacing();
      int shp = grid.getSize();
      // Calculate the left boundary. We switch to a different \hookleftarrow
            operator on the boundaries, which should
          just be ghost points that will be overwritten, anyway.
 9
      // Leftmost point.
10
      \mathtt{dudt} [\mathtt{U}_{\mathtt{PHI}}][0] = \mathtt{u}[\mathtt{U}_{\mathtt{PI}}][0];
11
      stencil3[0] = u[U_CHI][0];
      {\tt stencil3}\, [\, 1\, ] \; = \, {\tt u}\, [\, {\tt U\_CHI}\, ]\, [\, 1\, ]\, ;
13
      stencil3[2] = u[U_CHI][2];
14
      dudt[U_PI][0] = operators::dx_2off(stencil3, dx);
15
      stencil3\begin{bmatrix} 0 \end{bmatrix} = u \begin{bmatrix} U_PI \end{bmatrix} \begin{bmatrix} 0 \end{bmatrix};
16
      stencil3[1] = u[U_PI][1];
17
      \mathtt{stencil3} [2] = \mathtt{u} [\mathtt{U}_\mathtt{PI}] [2];
18
19
      dudt[U_CHI][0] = operators:: dx_2off(stencil3, dx);
20
      // Second leftmost point.
21
      dudt[U_PHI][1] = u[U_PI][1];
22
      {\tt stencil3} \, [\, 0 \, ] \, = \, u \, [\, {\tt U\_CHI} \, ] \, [\, 0 \, ] \, ;
23
      stencil3[1] = u[U_CHI][1];
24
      stencil3[2] = u[U_CHI][2];
25
      dudt[U_PI][1] = operators::dx_2(stencil3, dx);
26
      stencil3[0] = u[U_PI][0];
27
      stencil3[1] = u[U_PI][1];
stencil3[2] = u[U_PI][2];
28
29
      \mathtt{dudt} \left[ \, \mathtt{U\_CHI} \, \right] \left[ \, 1 \, \right] \; = \; \mathtt{operators} :: \mathtt{dx\_2} \left( \, \mathtt{stencil3} \; , \; \; \mathtt{dx} \, \right);
30
31
      // Now set all the interior points.
32
      for (int i = 2; i < shp - 2; i++){
33
         dudt[U_PHI][i] = u[U_PI][i];
34
35
         for (int j = 0; j < 5; j++){
36
            stenci15[j] = u[U_CHI][i - 2 + j];
37
38
         dudt[U_PI][i] = operators::dx_4(stencil5, dx);
39
40
         for (int j = 0; j < 5; j++){
            stencil5[j] = u[U_PI][i - 2 + j];
```

```
43
           dudt[U_CHI][i] = operators::dx_4(stencil5, dx);
44
45
46
        // Second rightmost point.
47
       dudt[U_PHI][shp - 2] = u[U_PI][shp - 2];
48
       stencil3[0] = u[U_CHI][shp - 3];
49
       stencil3 \begin{bmatrix} 1 \end{bmatrix} = u \begin{bmatrix} U_CHI \end{bmatrix} \begin{bmatrix} shp - 2 \end{bmatrix};
50
       \mathtt{stencil3} \, \big[ \, 2 \, \big] \, = \, \mathtt{u} \, \big[ \, \mathtt{U\_CHI} \, \big] \, \big[ \, \mathtt{shp} \, - \, 1 \, \big] \, ;
51
       dudt[U_PI][shp - 2] = operators::dx_2(stencil3, dx);
52
       53
54
       stencil3[2] = u[U_PI][shp - 1];
55
       dudt[U_CHI][shp - 2] = operators::dx_2(stencil3, dx);
57
        // Rightmost point.
58
       {\tt dudt} \, [\, {\tt U\_PHI} \, ] \, [\, {\tt shp} \, \, - \, \, 1 \, ] \, = \, {\tt u} \, [\, {\tt U\_PI} \, ] \, [\, {\tt shp} \, \, - \, \, 1 \, ] \, ;
59
       stencil3[2] = u[U_CHI][shp - 3];
60
       stencil3[1] = u[U_CHI][shp - 2];
61
       stencil3[0] = u[U_CHI][shp - 1];
62
       dudt[U_PI][shp - 1] = operators :: dx_2off(stencil3, dx);
63
       stencil3[2] = u[U_PI][shp - 3];
64
       stencil3 [1] = u[U_PI][shp - 2];
65
       \mathtt{stencil3} \hspace{.05cm} [\hspace{.05cm} 0\hspace{.05cm}] \hspace{.1cm} = \hspace{.1cm} \mathtt{u} \hspace{.05cm} [\hspace{.05cm} \mathtt{U\_PI}\hspace{.05cm}] \hspace{.05cm} [\hspace{.05cm} \mathtt{shp} \hspace{.1cm} - \hspace{.1cm} 1\hspace{.05cm}]\hspace{.05cm} ;
66
       dudt[U_CHI][shp - 1] = operators::dx_2off(stencil3, dx);
67
```

Before we go any further, we need to talk about spatial discretization in OOPS. The Domain object we attached to Wave earlier has one or more Grid objects attached to it. The Domain describes the physical bounds of the problem and includes some details about discretization that all Grid objects need to follow. One of these is ghost points. All Grid objects include ghost points, which are nonphysical points extending past the bounds reported by each Grid object. These are required for transferring data between different Grid objects, but they are also used in some numerical schemes (such as those common in fluid dynamics) for applying boundary conditions. Strictly speaking, these ghost points do not need to be set in the righthand side routine, but they can be.

Moving forward to the code itself, it is somewhat long, but it should be very straightforward. The left and right computational (not necessarily physical) boundaries are set with second-order derivative operators, and which require a 3-point stencil, and all the interior points use a full fourth-order derivative operator with a 5-point stencil. Every derivative operator takes an appropriately sized stencil and spatial interval. An important point to notice here is that the points on the right boundary are loaded into the derivative stencil backwards; essentially, we are using a forward difference operator rather than defining a unique backward difference operator.

After setting up the righthand side, we still need to define some boundary conditions. We're assuming a Neumann boundary, so this is easy to set up.

```
void Wave::applyBoundaries(bool intermediate){
unsigned int nb = domain->getGhostPoints();
```

```
// Grab the data at the leftmost grid and the rightmost grid.
3
     auto left_it = data.begin();
     auto right_it = --data.end();
5
     double **left:
     double **right;
     if (!intermediate) {
10
       left = left_it->getData();
11
12
       right = right_it->getData();
13
14
       left = left_it->getIntermediateData();
15
       right = right_it->getIntermediateData();
16
17
     unsigned int nr = right_it->getGrid().getSize();
18
19
     // Apply Neumann boundary condition.
20
     for (unsigned int i = 0; i < nb; i++){
21
       {\tt left[U\_PHI][i] = left[U\_PHI][nb];}
22
       left[U_PI][i] = left[U_PI][nb];
23
       left[U_CHI][i] = 0.0;
24
25
       right [U_PHI][nr - 1 - i] = right [U_PHI][nr - nb - 1];
26
       right [U_PI] [nr - 1 - i] = right [U_PI] [nr - nb - 1];
right [U_CHI] [nr - 1 - i] = 0.0;
27
28
29
30
  }
```

This is a great time to explain how spatial data is stored in OOPS. As mentioned previously, every <code>Domain</code> contains one or more <code>Grid</code> objects. These are stored in an <code>std::set</code> and sorted from left to right. Every <code>ODE</code> object maintains a set of <code>SolverData</code> objects, each of which are assigned a specific grid, and are also sorted from left to right. This makes it possible to store multiple grids on a single domain, thus allowing for different-sized grids in different regions of the solution. Hypothetically, this could also allow for adaptive mesh refinement, although that feature has not been implemented.

In any case, we need to make sure that we retrieve the leftmost and rightmost grids on the domain because those will be the ones containing the physical boundaries. If we're using a multi-stage Solver object, the intermediate flag tells us whether this data needs to come from the intermediate data stored between stages or the original data from the beginning of the time step. After that, applying the boundary condition itself is nearly trivial. Because we have a Neumann boundary, we set  $\chi = \partial_x \phi = 0$ , and we enforce this same condition in  $\phi$  and  $\pi$  by copying the physical boundary into the ghost points.

By this point, some of you are probably asking, "Wait a minute—can I do boundaries without ghost point? How does that work?" The applyBoundaries() function was designed with fluid-style boundaries in mind, which are really Dirichlet boundaries cleverly designed to simulate other boundaries. More traditional PDEs can exclude the applyBoundaries() function altogether and set their boundaries in the rhs() if they so choose.

The last piece for this file is setting the initial conditions. For simplicity,

we'll assume a Gaussian centered around x = 0.5. The code looks like this:

```
void Wave::initData(){
    // The center of our Gaussian.
    double x0 = 0.5;
3
    // Loop through every grid and start assigning points.
    for(auto it = data.begin(); it != data.end(); ++it){
      const double *x = it->getGrid().getPoints();
      unsigned int nx = it->getGrid().getSize();
      double **u = it->getData();
      for (unsigned int i = 0; i < nx; i++){
10
        double val = std::exp(-(x[i] - x0)*(x[i] - x0)*64.0);
11
        u[U_PHI][i] = val;
12
        u[U_PI][i] = 0.0;
13
        u[U_CHI][i] = -128.0*(x[i] - x0)*val;
14
15
    }
16
17 }
```

After our discussion on boundary conditions, the purpose of the loop should be more straightforward: we need to loop over every grid on our domain so we can set each of their points fit along a Gaussian.

#### 2.4.3 main.cpp

We're in the home stretch! With our ODE set up, all that's left is our main() function. Start by making a new file in the src directory called main.cpp.

```
1 #include <domain.h>
2 #include <grid.h>
з #include <rk4.h>
4 #include <cmath>
5 #include <cstdio>
6 #include <wave.h>
7 #include <polynomialinterpolator.h>
9 int main(int argc, char* argv[]){
     // Construct our domain and a grid to fit on it.
10
     Domain domain = Domain();
11
     int N = 101;
12
     double bounds [2] = \{0.0\};
     \mathtt{bounds} \, [\, 0 \, ] \,\, = \,\, \mathtt{domain.getBounds} \, (\,) \, [\, 0 \,] \, ;
14
15
     bounds [1] = domain.getBounds()[1];
     domain.addGrid(bounds, N);
16
17
     // Set up our ODE system.
18
     RK4 rk4 = RK4();
19
     {\tt PolynomialInterpolator interpolator} \ = \ {\tt PolynomialInterpolator} \ (4) \! \hookleftarrow \!
20
21
     Wave ode = Wave(domain, rk4);
22
     ode.setInterpolator(&interpolator);
     ode.initData();
23
24
```

```
double ti = 0.0;
25
      double tf = 5.0;
26
      \texttt{doublt} \ \texttt{dt} = \texttt{domain.getCFL}() * (\texttt{domain.getGrids}() . \texttt{begin}()) \rightarrow \leftarrow
27
           getSpacing();
      {\tt unsigned\ int\ M=(tf\ -ti)/dt;}
28
      ode.dump_csv("phi00000.csv", 0, 0);
29
30
      for (unsigned int i = 0; i < M; i++){
        double t = (i + 1)*dt;
31
         ode.evolveStep(dt);
32
33
        char buffer[12];
sprintf(buffer, "phi%05d.csv",i+1);
34
35
         ode.dump_csv(buffer, t, 0);
36
37
38
      return 0;
39
40 }
```

Inside the main function, we can see the procedure for constructing a Domain. When we create a new Domain object, it is generated with some defaults. The boundaries are automatically defined at x=0 and x=1.0, the number of ghost points is set to 3, and we have a Courant-Friedrichs-Lewy (CFL) factor of 0.5. This helps us set the time step to something guaranteed to be stable for our chosen spatial interval, although in practice this depends a lot on the particular equation we're solving. We can add a Grid to the Domain with the method addGrid(double bounds[2], unsigned int n), where bounds defines the spatial location of the Grid (which, in this case, is just the entire domain) and the number of physical points for the Grid. Now is a good time to note that the number of actual points on the grid is going to be n + 2\*nghosts, where nghosts is the number of ghost points, which will extend slightly beyond the region specified by bounds[].

The next step is constructing our Wave ODE object. We first start by picking a Solver for the time integration, which is RK4 in this case. We then construct an Interpolator object because it's required by the ODE class to transfer data between different-sized Grid objects, although this functionality is not important for our purposes. We then build our Wave object, assign the new Interpolator, and set the initial data.

Finally, we need to run our main loop. We calculate our time step, the number of total steps (because calculating t from the number of steps is less prone to numerical error than adding dt over and over), and run evolveStep(dt). We also dump our data to a .csv file every step so we can look at the results when we're done.

#### 2.4.4 Compiling the Project

By the end of this, you're asking, "We're done, right?"

The answer to that question is yes and no. We're done writing C++, but we still have one more step before we can compile our code and run the project. So, navigate to your main project directory (OOPS/WaveEquation), then create a new file called CMakeLists.txt and add the following:

```
_{1} cmake_minimum_required(VERSION 3.0)
project(WaveEquation)
  set (WAVE_INCLUDE_FILES
4
       include/wave.h
  set (WAVE_SOURCE_FILES
       src/wave.cpp
       src/main.cpp
9
10
11
12 set(SOURCE_FILES ${WAVE_INCLUDE_FILES} ${WAVE_SOURCE_FILES})
  add_executable(Wave ${SOURCE_FILES})
  target_include_directories(Wave PRIVATE ${←
       CMAKE_CURRENT_SOURCE_DIR } / include )
15 target_include_directories(Wave PRIVATE \{CMAKE\_SOURCE\_DIR\}/\longleftrightarrow
       include)
16 target_link_libraries(Wave oops ${EXTRA_LIBS})
```

After that, rerun CMake, compile, and you should have an executable, Wave, in the directory OOPS/build/WaveEquation, which will solve your wave equation when you run it.

#### 2.4.5 Afterthoughts

By this time, you're saying, "You said this would be simple! Why did it take so long? This seems like overkill for such a simple problem."

You're probably right. If all you're trying to do is solve the wave equation, you really don't need all this machinery. But let's start by talking about all the things you didn't have to do. You didn't have to write your own numerical integrator, first of all. You just loaded up the standard RK4 integrator, attached it to the Wave object, and you were good to go. You also didn't have to worry about discretizing the Domain yourself. This isn't a terribly difficult process if all you need is a single uniform grid, but it takes out one more failing point in your code. You didn't have to write your own derivative operators. Again, these aren't difficult, but they do take time, especially if you want something more than the traditional second-order centered finite-difference operators. You didn't have to worry about boundary conditions getting applied correctly between the different stages of the numerical integrator, either; you just overloaded applyBoundaries, wrote out the boundaries you wanted, and let OOPS do the rest for you.

Now let's talk about what you can do thanks to OOPS. By just changing a few lines of code in your main function, you could change your problem from a single grid to three or four grids, perhaps to give you good resolution in the middle where the peak of the Gaussian is located and less resolution toward the edges where the data is more flat. OOPS automatically handles the data transfer between neighboring grids, including interpolating between different-sized grids (so long as they're a multiple of two apart). If the RK4 integrator isn't good enough for your problem, you can write a new integrator using the Solver

base class with just three functions (two of which are nearly identical). It will automatically work with all the rest of the OOPS machinery. If you're working on a complicated problem that requires some extra steps in the evolution method (ODE::evolveStep()), you can do that with the doAfter...() methods.

## 2.5 Adding Parameters

Right now, everything is hardcoded. If we wanted to try a different set of initial conditions, modify the number of Grid points, or change the Domain, we would have to recompile our code completely. This quickly becomes cumbersome as projects grow in size. An alternative would be reading in a file of parameters off the drive. To do so, we can use the genParams.py script to automatically generate Parameters and ParamParser classes when we compile the code.

#### 2.5.1 Creating a Setup File

The first step is to make a setup file. In the WaveEquation directory, add a new directory called scripts. Inside scripts, make a new file called wave.json. JSON is a data format originally intended for storing JavaScript objects, but its simple structure and wide use in web programming (courtesy of JavaScript) means that many languages, including Python, can read and write JSON files. Because JSON files are stored as plain text, so can we. Therefore, inside wave.json, add the following code:

```
"Wave" : {
2
3
       "name": "Wave",
       "id":1,
4
       "members":
            "name": "GridPoints",
            "type":"int",
            "min":7,
9
            "max":128000,
10
            "default":101
11
12
13
            "name": "GaussianSigma",
14
            "type": "double",
15
            "\min": 1 e-3,
            max: 1 e6,
17
            "default":0.125
18
19
20
     }
21
22
```

JSON stores all data as "key": value pairs, where value can be a string enclosed in quotes, a number, an array of comma-separated values (enclosed by square brackets, []), or an object (denoted by parentheses). Therefore, this file declares

an object Wave which has the variables "name", "id", and "members". The "name" variable dictates the prefix that will be used for the custom Parameters and ParamParser objects we'll use to read in the parameters file we'll write later. The "id" variable is a sort of primitive type-checking to check which ParamParser, Parameters, ODE objects are compatible with one another. It's barely used at this point and will likely be deprecated in a future release, but it's currently mandatory for the genParams.py script. The "members" variable is an array of objects, each one describing a different parameter.

Inside "members", every object has a "name", "type", and "default". The "name" field indicates how this parameter will be named in the code. For example, we will access "GridPoints" in the code with a function called getGridPoints(). The "default" field indicates the value that parameter should be initialized to within a Parameters object. The third variable, "type", can be "int", "double", "string", or "enum", and tells genParams.py what the C++ type should be for this parameter. String objects are the easiest, as they require no additional parameters. The numerical types, "double" and "int", require additional "min" and "max" fields to describe permissible parameter values. In this case, the "GridPoints" parameter will only be allowed to take values between 7 and 128000, and "GaussianSigma" must lie between  $10^{-3}$  and  $10^6$ . We will discuss "enum" objects in more depth later on.

Next, navigate to OOPS/scripts run the following command:

python3 genParams.py ../WaveEquation/scripts/wave.json

Make sure that no error messages occur, then check that OOPS/WaveEquation/include contains waveparameters.h and waveparser.h. If that's the case, look inside OOPS/WaveEquation/src and verify that waveparser.cpp is there.

#### 2.5.2 Setting up the Compiler

At this point, you *could* run genParams.py every single time you change wave.json, but forgetting to update your generated code is likely to become a common source of frustration and confusion as your project grows in size. It would be a lot more convenient to have genParams.py run whenever you compile your code. Inside the CMakeLists.txt file inside OOPS/WaveEquation, add the following lines before set(WAVE\_INCLUDE\_FILES...):

```
DEPENDS ${SETUP_SRC}

COMMAND ${PYTHON_EXECUTABLE} ${CMAKE_SOURCE_DIR}/scripts/
genParams.py ${SETUP_SRC}

COMMENT "Generating custom Parameters files"

WORKING_DIRECTORY ${CMAKE_CURRENT_SOURCE_DIR}

VERBATIM USES_TERMINAL
```

Essentially, we declare three new variables: \${PARAM\_SRC} contains the source files we're generating, \${PARAM\_INC} contains a list of header files being generated, and \${SETUP\_} contains a list of JSON setup scripts. Following that, we tell CMake to execute a custom command, which, in this case, is running genParams.py on \${SETUP\_SRC}.

Once this is done, we need to tell CMake to link Wave to the generated source files. The easiest way to do this is to modify the line set(SOURCE\_FILES...) to read

```
1 set (SOURCE_FILES \{WAVE\_INCLUDE\_FILES\} \{WAVE\_SOURCE\_FILES\} \{\leftarrow PARAM_INC} \{PARAM\_SRC\})
```

If we wanted to add multiple setup scripts, or if our setup script contained multiple parameter sets, we could just modify \${PARAM\_INC}, \${PARAM\_SRC}, and \${SETUP\_SRC} to reflect the additional files. At this point, it's a good idea to delete waveparameters.h, waveparser.h, and waveparser.cpp in their respective directories, try compiling the code, and ensure that everything gets generated correctly.

## 2.5.3 Using Parameters in OOPS

At this point, we've discussed how to generate some code for a custom Parameters class when we compile our code, but we still haven't actually used them. First, let's go to wave.h and make some tweaks. Add the following code into their respective sections:

This section is fairly straightforward: we need to maintain a pointer to our WaveParameters object, and so we also need a way to set it and retrieve it.

Next up is the wave.cpp file. The first change we'll make is to the constructor. Strictly speaking, this step is not necessary, but it is good practice. We need to initialize params to nullptr, otherwise its behavior is undefined.

We initialize params to nullptr, which guarantees that trying to use it without first setting it will result in a segmentation fault. Let's also go ahead and define getParameters() and setParameters():

```
void Wave::setParameters(WaveParameters *p){
   params = p;
}

WaveParameters* Wave::getParameters(){
   return params;
}
```

Next, we need to modify initData() so that we can use the GaussianSigma parameter we defined:

```
1 void Wave::initData(){
2    double sigma = params->getGaussianSigma();
3    ...
4    for(...){
5         ...
6    for(...){
7         double val = std::exp(-(x[i] - x0)*(x[i] - x0)/(sigma*sigma)) \cup ;
8         ...
9         u[U_CHI][i] = -2.0/(sigma*sigma)*(x[i] - x0)*val;
10    }
11  }
12
13 }
```

Every parameter added to the JSON setup script will have both a getter and a setter in the custom generated Parameters class. In this case, because we called our function "GaussianSigma", we have functions getGaussianSigma() and setGaussianSigma(double). Therefore, we can simply grab GaussianSigma from params and substitute that into our Gaussian initial data.

Now, if you try to run this code now, you'll get a segmentation fault. We haven't actually loaded or assigned a WaveParameters object to Wave yet, which will be our next step. We need to modify main.cpp as follows:

```
2 #include <iostream>
3 #include <waveparameters.h>
4 #include <waveparser.h>
6 int main(int argc, char* argv[]){
    if(argc < 2){
       std::cout << "Usage: ./Wave <parameter file >\n";
       return 0:
9
10
11
    WaveParameters params;
12
    WaveParser parser;
13
    parser.updateParameters(argv[1], &params);
14
     // Construct our domain and a grid to fit on it.
16
    Domain domain = Domain();
17
18
    int N = params.getGridPoints();
19
20
21
    ode.setParameters(&params);
22
23
    ode.initData();
24
```

The first few lines tell the code to expect a parameter file along with the executable, so if it's not present, it tells the user how to run the program properly and quits. If there is a parameter file, we can go ahead and try to run the program. We create WaveParameters and WaveParser objects, then we use the WaveParser to read in our parameters and update WaveParameters accordingly. The next change is setting the resolution of our Grid using the supplied parameter instead of hard-coding it to 101. Finally, the last change is supplying the WaveParameters object to ode before we set the initial data.

At this point, make sure that your code compiles. It won't run yet because we haven't written a parameter file, but it should compile. Now, create a new file in the OOPS/WaveEquation/pars directory called wave.par:

```
[Wave]
GridPoints = 101
GaussianSigma = 0.125
```

The [Wave] header at the top indicates what Parameters object this belongs to. You can easily store multiple Parameters sets in a single file, which may be helpful if you want to maintain a set of parameters for your Grid and Domain setup, a different set for your ODE, and maybe a different set for output options.

Every parameter is specified as parameter = value. There is no semicolon at the end, and each new line is treated as a different parameter. Whitespace before and after parameter names and values is ignored, but everything is case-sensitive and must match the "name" variable specified in the JSON file to be read in correctly.

Now, let's run the code. You can either copy wave.par into the binary directory (OOPS/build/WaveEquation) or specify its relative path:

#### ./Wave <relative path if necessary>/wave.par

Your code should run and generate a whole mess of .csv files, just as before. If you examine the output using your favorite plotting program, it should look exactly the same. Here are some different things to try:

- Go into wave.par and erase one or both parameter assignments (don't get rid of the [Wave] header). Run your code again. It should still run without an issue because WaveParameters will simply use some default values.
- 2. See what happens as you change GridPoints. What happens if you set it outside the acceptable range specified in wave.json?
- 3. Play around with different values of GaussianSigma. In particular, what happens to the quality of the solution if you make GaussianSigma very small?
- 4. Try adding some new parameters on your own. Some good examples might be x0, the center of the Gaussian, or the minimum and maximum bounds on the Domain.

## 2.5.4 Adding an Enumerated Parameter

It happens quite frequently that we need a parameter describing a fixed set of values, such as different kinds of initial conditions, solution methods, or particular boundary conditions. A very common but inelegant solution is to assign each value a numerical index, then provide documentation on all the different cases. However, virtually every modern programming language, C++ included, allows for enumerated types, which are far more readable. The parameter generation system also supports enumerated types. Let's consider a new set of initial conditions: a sine wave. Go into wave.json and add the following object inside "members":

```
1 {
2     "name":"InitialConditions",
3     "type":"enum",
4     "value":[
5          "GAUSSIAN",
6          "SINE"
7     ],
8     "default":"GAUSSIAN"
9 }
```

Rather than specifying "min" and "max" variables, we add a "values" variable, which is an array of strings representing possible values for the enumerator. Go

ahead and compile the code again to make sure that you've added everything correctly. Now, go into wave.cpp, and let's modify initData() again:

```
void Wave::initData(){
2
      if(params->getInitialConditions() == WaveParameters::GAUSSIAN){
        for (...) {
 4
5
           for (...) {
 6
9
10
      else \quad if \, (\, params -\! > getInitialConditions \, (\,) \, =\! - \, WaveParameters :: SINE \, ) \, \{ \\
11
        for (...) {
12
13
           for (...) {
14
15
             double pi = 3.1415926;
             u[U_PHI][i] = std::sin(x[i]*pi);
16
             u[U_PI][i] = 0.0;
17
             u[U_CHI][i] = std::cos(x[i]*pi);
18
19
20
     }
^{21}
```

After compiling the code to make sure it works, the last step is to add the initial condition into the wave.par parameter file:

```
[Wave]
GridPoints = 101
GaussianSigma = 0.125
InitialConditions = SINE
```

Now rerun the code. It should no longer evolve a Gaussian pulse, but rather a sine wave.

## 3 Documentation

## 3.1 Domain Class

The Domain class defines the physical region a PDE should be solved on. It acts as a factory for Grid objects and contains the necessary parameters to construct them appropriately.

#### **Public Methods**

Domain() The constructor for a Domain object. By default, it sets the number of ghost points to three, the boundaries to [0, 1], and the CFL factor to 0.5.

- ~Domain() The destructor for a Domain object. It automatically clears all grids attached to the Domain.
- void setCFL(double cfl) Set the CFL factor. At the moment, this doesn't affect anything in the code itself. Future releases may use this to calculate a recommended time step.
- double getCFL() const Get the CFL factor.
- void setBounds(double bounds[2]) Set the bounds for the domain with an ordered pair. This will also clear any Grid objects still on the Domain.
- const double\* getBounds() const Get the bounds for the Domain as an ordered pair.
- void setGhostPoints(unsigned int n) Set the number of ghost points to
   use while constructing new Grid objects. This will clear any Grid
   objects still on the Domain.
- unsigned int getGhostPoints() const Get the number of ghost points used while constructing new Grid objects.
- std::set<Grid>& getGrids() Get a set containing all the different Grid
   objects currently on the Domain.
- Result addGrid(double bounds[2], unsigned int n) Using an ordered pair bounds[], add a new Grid with n uniformly spaced points to the Domain. It returns SUCCESS if it succeeded and BAD\_ALLOC if it failed.
- void clearGrids() Clear all Grid objects currently on the Domain.

## 3.2 Grid Class

The Grid class defines a 1d grid with uniform spacing. These are the building blocks for basically all calculations in OOPS.

#### **Public Methods**

- Grid(const double bounds[2], unsigned int n, unsigned int nghosts)

  The constructor for a new Grid with n points from bounds[0] to bounds[1],
  plus an additional nghosts ghost points on either end.
- Grid(const Grid& other) The copy construct for Grid. Because memory is allocated and deallocated in every Grid object, this performs a deep copy.
- ~Grid() This is the destructor for the Grid class. It frees all the memory allocated for the Grid points.

- Result rebuildGrid(const double bounds[2], unsigned int n, unsigned int nghosts) A function to rebuild a Grid, with the arguments being the same as the constructor, if something needs to change. It returns SUCCESS on success and BAD\_ALLOC if it fails.
- const double\* getPoints() const Get the array containing the physical location of every grid point.
- const unsigned int getSize() const Get the number of points, including ghost points, currently on the grid.
- const double getSpacing() const Get the space interval between points.
- const double\* getBounds() const Get the bounds, excluding ghost points,
   of the Grid as an ordered pair.
- bool operator < (const Grid& g) const Compare two Grid objects to each other. If the right bound for the Grid on the left side of the operator is less than the left bound for the Grid on the right side of the operator, this returns true. If the two Grid objects overlap at all, this will always return false, even if you flip the arguments.
- Boundary whichNeighbor(const Grid& g) const If two Grid objects share a boundary, this will return Boundary::LEFT or Boundary::RIGHT. Otherwise, it returns Boundary::NONE.

#### 3.3 Solver Class

The Solver class is an interface for numerical integrators. As such, it cannot be instantiated, but any numerical integrator, such as the included RK4 integrator, must be a descendant of the Solver class to work properly with the rest of the OOPS machinery. This particular class may be rewritten somewhat in the future to make it more consistent with the rest of OOPS.

#### **Protected Fields**

const int nStages The number of stages for the Solver, which is specified in the constructor.

#### **Public Methods**

Solver (const int n) A basic constructor included to set the number of stages for a Solver. All subclasses must call this constructor in their initialization list.

int getNStages() const Get the number of stages for the Solver.

#### Unimplemented Public Methods

virtual Result setStageTime(double srcTime, double& destTime, double dt, unsigned int stage) Using srcTime and dt, determine what the proper time for stage is and store the result in destTime. Ideally, this should be implemented to return SUCCESS unless an invalid stage is requested, then it should return INVALID\_STAGE. This method is called before calcStage().

virtual Result calcStage(ODE \*ode, double \*data0[], double \*dataint[], double \*dest[], const Grid& grid, double dt, unsigned int stage)

This is the method currently used by the OOPS framework for calculating each stage of a Solver object. The first argument is the ODE, which contains the righthand-side function Solver should use. The argument data0 is a 2d array containing the current solution, dataint is a 2d array for the intermediate solution, and dest is the destination for the work data/righthand side calculated during this particular stage. The grid argument specifies what Grid the solver is operating on, dt is the size of the timestep, and stage is the stage for a multi-stage solver like RK4. Although ODE technically contains all the data and the Grid, it must be passed in because calcStage occurs in the middle of a loop over all the Grid objects. Be aware that this is likely to change in order to make the Solver class more consistent with the rest of OOPS.

virtual Result combineStages(double \*\*data[], double \*dest[], const
 Grid& grid, double dt, const std::vector<unsigned int> evolutionIndices)
 This function combines all the stages together. The data[] array is or ganized by [STAGE][VAR][INDEX] and contains all the work data from
 the previous calculations. The dest[] array contains the final result of
 the calculation. The Grid for this calculation is supplied, as is the time
 step and the number of variables for the equation. Because some systems,
 such as fluids, may evolve fewer equations than they actually contain, the
 evolutionIndices argument contains an std::vector that describes all
 the equations which should be evolved.

## 3.3.1 RK4 Child Class

An implementation of the classic 4th-order Runge-Kutta integrator. It is a four-stage solver and has no unique functions. It can be declared with its default constructor, RK4().

#### 3.4 ODE Class

ODE is an abstract class describing a generic system of differential equations. As a brief note, no ODE object is copyable because they store a considerable amount of dynamically allocated memory.

#### **Protected Fields**

- const unsigned int nEqs The number of independent equations in this system
- const unsigned int pID The ID associated with this ODE. This is used for identifying compatible Parameter objects.
- Domain \*domain The Domain this ODE is being solved on. This is how the ODE accesses all of the Grid objects it needs to construct the SolverData objects.
- std::set<SolverData> data A set containing all the SolverData objects for
  each Grid.
- Solver \*solver The Solver that should be used to calculate each step.
- Interpolator \*interpolator The Interpolator used to transfer solution data between differently sized Grid objects.
- max\_dx The maximum grid spacing across all Grid objects on the Domain.
- time The current evolution time.
- std::vector<unsigned int> evolutionIndices An std::vector containing the indices for the variables that should be evolved. By default, this is initialized to loop over all variables.

#### Protected Methods

- virtual void applyBoundaries (bool intermediate) A function to apply fluid-style boundary conditions after data is transferred between Grid objects. It is empty by default, so initial value problems and PDEs which apply their boundaries through the righthand side can simply not overwrite this function.
- virtual void doAfterStage(bool intermediate) An empty function which can be overwritten to perform specific tasks after the Solver stage completes but before the Grid exchange occurs.
- virtual void doAfterExchange(bool intermediate) An empty function which can be overwritten to perform specific tasks after the Grid exchange occurs but before the boundaries are applied.
- virtual void doAfterBoundaries(bool intermediate) An empty function which can be overwritten to perform specific tasks after the boundary conditions are applied but before the next stage is calculated.
- Result reallocateData() A function that clears and reallocates all of the data. This may be important if the Domain or any of its Grid objects change.

- void performGridExchange() This exchanges data between the ghost points of neighboring Grid objects, including taking care of interpolation.
- void exchangeGhostPoints(const SolverData &data1, const SolverData &data2) A helper function that performs a Grid exchange between two specific data sets.
- void interpolateLeft(const SolverData &datal, const SolverData &datar)
  A helper function for interpolation that assumes the SolverData to the left of the interface is finer.
- void interpolateRight(const SolverData &datal, const SolverData &datar)
  A helper function for interpolation that assumes the SolverData to the right of the interface is finer.
- Result addAuxiliaryField(std::string name) Add a new auxiliary field to the ODE object. The reallocateData() function must be called to allocate memory for the new field. It returns SUCCESS if the field was created successfully or FIELD\_EXISTS if a field with that name already exists.
- Result removeAuxiliaryField(std::string name) Remove an auxiliary field from the ODE object. Returns SUCCESS if the field was created successfully or UNRECOGNIZED\_FIELD if the field does not exist.
- std::set<ODEData>\* ODE::getAuxiliaryField(std::string name) Get a
  pointer to the specified auxiliary field. If the field does not exist, it returns
  nullptr instead.

#### **Public Methods**

- ODE (const unsigned int n, const unsigned int id) The constructor for ODE, which all subclasses must call in their initialization lists, which defines a new ODE object with n equations utilizing Parameter objects with the provided id.
- ~ODE() The destructor for the ODE, which clears all the data.
- Result setDomain(Domain \*domain) Set the Domain for the ODE. This will clear all existing data and reallocate it for the new Domain. It returns SUCCESS on success and an error, usually BAD\_ALLOC, on failure.
- Result setSolver(Solver \*solver) Set the Solver for the ODE. This will clear all existing data and reallocate it for the new Solver. It returns SUCCESS on success and an error, usually BAD\_ALLOC, on failure.
- Result setInterpolator(Interpolator \*interp) Set the interpolation method used by this ODE. It returns SUCCESS on success and an error on failure, usually BAD\_ALLOC.

virtual Result evolveStep(double dt) The evolution function for a single step. It is overwriteable in case a specific use-case scenario requires more flexibility than the default evolution function provides, but this is not a typical use-case scenario.

unsigned int getNEqs() const Get the number of equations in the ODE system.

Domain \*getDomain() Get the current Domain used by the ODE.

void setTime(double t) Set the current evolution time for the ODE.

double getTime() Get the current evolution time.

void output\_frame(char \*name, double t, unsigned int var) Write out the data from variable var labeled with time t to <name>.sdf. This requires the bbhutil library and must be explicitly enabled with the USE\_SDF option during the configuration. Otherwise, a warning is printed the first time it is called and no data is saved.

dump\_csv(char \*name, double t, unsigned int var) All the data is dumped to the specified file for the corresponding variable var in the format (t, x, data).

## Unimplemented Public Methods

virtual void initData() The initial conditions for the ODE.

virtual void rhs(const Grid& grid, double\*\* data, double\*\* dudt) The righthand-side function for this ODE. It takes a Grid object and the data corresponding to that Grid, then stores the calculated righthand-side in dudt.

#### 3.5 ODEData Class

The ODEData class is a utility used by ODE for storing general solution data. Note that the ODEData copy constructor is protected, so no instance of ODEData can be copied directly.

#### **Public Methods**

ODEData(unsigned int eqCount, const Grid& grid) The constructor for a ODEData object. It saves a reference to the Grid object it should be associated with and allocates memory for eqCount equations on that Grid.

virtual ~ODEData() The destructor for ODEData. It deallocates all the memory allocated in the constructor. Since this is virtual, ODEData can be safely used as a base class for more complex data structures, such as the SolverData class below.

- double\*\* getData() const Get a pointer to a 2d array of data organized
   by [vars] [points] representing ODE information on the Grid associated
   with the ODEData object.
- unsigned int getEqCount() const Get the number of equations that the ODEData object is storing data for.
- const Grid& getGrid() Get the Grid object associated with the ODEData
   object.

#### 3.5.1 SolverData Child Class

The SolverData class is a utility used by ODE to store solution data for a particular Solver. Note that the SolverData copy constructor is private, so no instance of SolverData can be copied directly. It descends directly from the ODEData class, whose double\*\* data field is assumed to be the primary solution.

#### **Public Methods**

- SolverData(unsigned int eqCount, unsigned int nStages, const Grid&grid) The constructor for a SolverData object. It saves a reference to the Grid object it should be associated with and allocates memory for eqCount equations for nStages Solver stages.
- ~SolverData() The destructor for SolverData. It deallocates all the memory allocated in the constructor.
- double\*\* getIntermediateData() const Get a pointer to the 2d array of data organized by [vars][points] which stores the intermediate data used in a Solver.
- double\*\*\* getWorkData() Get a pointer to the 3d array of data organized by [stage][vars][points]. This is used to store the various results needed from each stage of a Solver.

#### 3.6 Interpolator Class

An Interpolator object provides machinery for a generic interpolation scheme. Typically this should be a centered scheme, although there is nothing preventing a subclass from doing a non-centered stencil. However, such Interpolator schemes should not be used to interpolate Grid objects.

#### **Protected Fields**

const unsigned int nStencil The size of the interpolation stencil.

double \*stencil The stencil for this Interpolator. This is allocated dynamically when the scheme is created and destroyed when the destructor is called.

#### **Public Methods**

- Interpolator (const unsigned int n) The constructor for this Interpolator, which builds a new scheme with a stencil of size n. This must be called in the initialization list of subclasses.
- ~Interpolator The destructor for this Interpolator. It releases the allocated memory.
- double\* getStencil() Get a pointer to the interpolation stencil, which will be an array of size nStencil.

unsigned int getStencilSize() Get the size of the interpolation stencil.

#### Unimplemented Public Methods

virtual double interpolate() Interpolate to calculate a point. It's generally expected that this will be a centered scheme with an even number of points in the stencil (linear, cubic, etc.), but this is by no means required if the Interpolator will not be used for Grid interpolation.

#### 3.6.1 PolynomialInterpolator Child Class

An interpolator for n-point centered polynomial interpolation.

#### Public Methods

PolynomialInterpolator (const unsigned int n) Construct a new PolynomialInterpolator for an n-point polynomial interpolation scheme.

## 3.7 operators Namespace

The operators.h file defines a number of finite-difference operators inside the operators namespace. All operators unless otherwise specified assume a uniform grid spacing.

**Differential Operators** All differential operators take a fixed-size double array as a stencil and a double for the grid spacing.

- double dx\_2(const double u[3], const double dx) A 2nd-order centered first derivative operator.
- double dx\_2off(const double u[3], const double dx) A 2nd-order forward-difference first derivative operator. The corresponding backward-difference operator is used by entering the points in backwards.
- double dx\_4(const doube u[5], const double dx) A 4th-order centered first derivative operator.

- double dxx\_2(const double u[3], const double dx) A 2nd-order centered second derivative operator.
- double dxx\_2off(const double u[4], const double dx) A 2nd-order forward-difference second derivative operator. The corresponding backward-difference operator is used by entering the points in backwards.
- doubl dxx\_4(const double u[5], const double dx) A 4th-order centered second derivative operator.

Kreiss-Oliger Dissipation Operators All Kreiss-Oliger dissipation operators take a fixed-size double array as a stencil and a double for the grid spacing.

- double ko\_dx(const double u[7], const double dx) A (4th?)-order centered-difference operator for Kreiss-Oliger dissipation.
- double ko\_dx\_2(const double u[5], const double dx) A 2nd-order centered-difference operator for Kreiss-Oliger dissipation.
- double ko\_dx\_off1(const double u[4], const double dx) A (1st?)-order operator for Kreiss-Oliger dissipation at the leftmost point in the stencil.
- double ko\_dx\_off2(const double u[5], const double dx) A (2nd?)-order operator for Kreiss-Oliger dissipation at the 2nd-leftmost point in the stencil.
- double ko\_dx\_off3(const double u[6], const double dx) A (3rd?)-order operator for Kreiss-Oliger dissipation at the 3rd-leftmost point in the stencil.

#### 3.8 ParamReader Class

The ParamReader class is designed to read a parameter file from the disk.

#### 3.8.1 Parameter File Structure

Parameter files are reminiscent of (and slightly more stringent than) classic Windows .ini files. Each file is divided into sections denoted by square brackets, such as [Section]. The # character is a comment character, and anything past it to the end of the line will be ignored. Parameter names are denoted by a single alphanumeric phrase and are assigned to a value by an equals sign. A simple file might look like this:

```
1 # A parameter file for some simulation.

2 [Grid]

3 # The number of grid points to use.

4 nx = 64

5 [InitialConditions]
```

```
7 # Set up Gaussian initial data.
8 init_id = ID_GAUSSIAN
9 init_gaussian_sigma = 10.0
10 init_gaussian_A = 10.0
```

Whitespace before and after parameter and value names is ignored. Values may contain whitespace inside their names, but parameters may not. Therefore, string\_data = Some String of Data is a valid entry, but string data = Some String of Data will return an INVALID\_PARAMETER error. Each line is treated as a new parameter.

#### 3.8.2 Reading Parameter Files

Parameter files are parsed into an std::map of std::map data structures. The first map contains all the parameters for a specific section, with that section name acting as the key. The second map contains the values for each parameter, with its name acting as the key. Therefore, to read a parameter file, you must know the section and parameter name.

#### **Public Methods**

ParamReader() The default constructor for a ParamReader object.

- ~ParamReader() The destructor for a ParamReader object.
- ParamResult readFile(std::string fname) Read a file fname off the disk and load it into memory. It returns a ParamResult indicating success or failure.
- bool hasSection(std::string section) Check if a particular section exists. Returns true if so, false if not.
- bool hasParameter(std::string section, std::string parameter) Check if a particular parameter exists in a section. Returns true if so, false if not.
- std::string readAsString(std::string section, std::string parameter)
  Read parameter in section as a string. If the parameter exists, it returns the value. Otherwise, it prints a warning to std::cout and returns "NULL".
- double readAsDouble(std::string section, std::string parameter) Read a parameter value as a double. If it exists and is a numerical value, it will return its value. If the parameter does not exist or is not a number, it will print a warning to std::cout and return 0.0.
- double readAsInt(std::string section, std::string parameter) Read a parameter value as an integer. If it exists and is an integer, it will return its value. If the parameter does not exist or is not an integer, it will print a warning to std::cout and return 0.

void clearData() Clear all the data that this ParamReader has read in.

#### ParamResult Enumerator

SUCCESS The file was loaded successfully.

BAD\_FILENAME The file does not exist or could not be opened.

SYNTAX\_ERROR A syntax error, such as a missing = sign, an unclosed section bracket, or a parameter declared on the same line as a section.

BAD\_TYPE Currently unused.

MULTIPLE\_DEFINITIONS The parameter file contains a previously written section.

UNSECTIONED\_PARAMETER A parameter was defined at the head of the file before a section was declared.

INVALID\_PARAMETER A parameter name contains invalid characters.

INVALID\_VALUE A value name contains invalid characters.

The ParamReader class can read in multiple files and store them, but they cannot share section names without first clearing the data. Parameters defined multiple times within a single section will be overwritten by the last defintion.

## 3.9 Parameters Class

The Parameters class is a simple class for representing the parameters an ODE object might need. While it is a concrete class and can be declared, it is most useful as a base class for more complicated ODE objects. It only has a few useful methods in its basic form.

#### Methods

Parameters (unsigned int id) /\*Protected\*/ A constructor designed to build a Parameters object with a specific id. This should be used in the initialization list for a subclass, otherwise id=0 and cannot be changed. It is protected so that it can only be used in this fashion.

Parameters() /\*Public\*/ A public default constructor.

unsigned int getId() const /\*Public\*/ Get the id for this Parameters object. This is useful for making sure that a Parameters object assigned to a specific ODE is actually compatible; if the id does not match, OOPS will not allow the assignment.

#### 3.10 ParamParser Class

The ParamParser class is an abstract class which should be used to fill out Parameter objects with information collected by ParamReader. Except in rare circumstances, it is unlikely you will ever have to extend ParamParser to read your parameter files; the genParams.py script described below should be used for that instead.

#### **Public Methods**

ParamParser(unsigned int id) A constructor which sets the id for this ParamParser. It must match the id in the Parameters objects it is designed to work with.

bool checkId(Parameters\* params) const Check if params has an id that matches this particular ParamParser.

unsigned int getId() const Get the id for this ParamParser.

#### Unimplemented Public Methods

void updateParameters(std::string fname, Parameters\* params) Update params with the data specified in the parameter file fname. The id of params must match the id for this particular ParamParser.

## 3.11 genParams.py Script

OOPS also features a Python script, genParams.py, that will accept a JSON setup file and generate custom Parameters and ParamParser objects.

## 3.11.1 Writing Setup Files

Because Python has a wonderfully simple JSON parser available, the setup file for a new Parameters object and its parser is written in JSON. A sample is available in the scripts folder in the OOPS base directory, and it reads as follows:

```
"Test":{
2
       "name" "Test",
3
      "id":1,
      "members":
5
           "name": "InitialConditions",
           "type": "enum",
           "value":[
9
             "GAUSSIAN",
10
             "FLAT"
           ],
"default":"GAUSSIAN"
12
```

The first layer is expected to be the definition for a Parameters object. It must define three variables: "name", "id", and "members".

The "name" variable is the head for all generated files. For example, "name": "Test" will generate the class TestParameters inside testparameters.h. The "id" field is an integer that indicates what id should be used for this Parameters object and any ODE object that uses it. The "members" field is a list of objects, each object representing a new parameter.

All "member" entries must define "name", "type", and "default". The "name" field corresponds to the name to print into the variable. The "type" field indicates the C++ type for the variable. Finally, the "default" field indicates how "name" should be set inside the constructor of the new Parameters object. You are responsible for ensuring that your variables and their corresponding values lead to valid C++ code. A future version of genParams.py may perform some limited syntax checking to ensure that names do not include forbidden characters, but this is rather low on the list of priorities at the moment.

If "type" is "enum", the "value" variable must also be defined as a list of enumerator values. Number types (e.g., "int" or "double") will also require "min" and "max" fields for generating the parser, but they are not currently necessary.

The output Parameters file of the setup file described above is

```
1 #ifndef TEST_PARAMETERS_H
2 #define TEST_PARAMETERS_H
4 #include <parameters.h>
  class TestParameters : public Parameters {
6
    public:
      enum InitialConditions{
9
        GAUSSIAN,
        FLAT,
10
11
12
      {\tt TestParameters}\,(\,)\ :\ {\tt Parameters}\,(\,1\,)\,\{
13
        mInitialConditions = GAUSSIAN;
14
15
        mKOSigma = 0.0;
16
```

```
inline void setInitialConditions(InitialConditions val){
18
        mInitialConditions = val;
19
20
21
      inline InitialConditions getInitialConditions(){
22
        return mInitialConditions;
23
24
25
      inline void setKOSigma(double KOSigma){
26
        {\tt mKOSigma} = {\tt KOSigma};
27
28
29
      inline double getKOSigma(){
30
        return mKOSigma;
31
32
33
34
    private:
      InitialConditions mInitialConditions;
35
      double mKOSigma;
36
37 };
зэ #endif
```

As you can see, it will define a new class declaring all member variables as private with public getters and setters. The constructor will assign each variable its proper default value and set the correct id in the initialization list. Enumerators will be defined in the public section. For a small setup file like this, obviously writing a single header file isn't much work, but very complex ODE objects may require a Parameters object with dozens of different settings corresponding to different initial conditions, and you'll also have to write a parser to read all those parameters from a parameter file, check for invalid settings, and ignore unspecified parameters. It quickly becomes extremely tedious to write it by hand, and it's much simpler to generate a setup file and let genParams.py do all the work.

#### 3.11.2 Running genParams.py

Running the script is easy:

```
python3 genParams.py <filename1.json> <filename2.json> ...
```

The script will load in each setup file one at a time and generate C++ code for each Parameters object specified in the JSON setup file consisting of three files: header files for Parameters and ParamParser, and a source file for ParamParser. It expects that your JSON setup file will be located either in the root of your project directory or within a scripts file in your project directory. From here, it will automatically place the header and source files in their proper directories. We highly recommend that you modify your local CMakeLists.txt file to run genParams.py automatically during the build. See Sec. 2.5.2 for details.

## 3.12 plotData.py Script

You've got a great OOPS code written, but now you need to check that your output actually works. OOPS doesn't feature any sophisticated data analysis or plotting tools (nor are any planned for the immediate future), but it does contain a simple Python script to let you look at all those .csv files you just generated. Copy OOPS/scripts/plotData.py into the directory with all your data files, and run

python3 plotData.py <filenames>

(Yes, it does support regex arguments. You will not need to manually input all the data files.) The script will scan through all the data files, look for the maximum and minimum values along the vertical axis, plot each frame, and save it to a .png image. For example, if your data all have names like data\*.csv, all your plots will be saved in plots\_data/data\*.png.

This script is not intended to be a full analysis or plotting utility. If you need something more sophisticated, there are plenty of tutorials online for using Python, MATLAB, Mathematica, and other software packages to read in and manipulate .csv data.

The plotData.py script does require the Matplotlib and NumPy modules to work. These can be installed via pip, conda, or your favorite package manager.

## 4 Question and Answer

## 4.1 How do I...

I need to add a Solver that doesn't work like ODE expects. Can I do this? Sure. The evolveStep() method in ODE is virtual and can be overwritten for this purpose. Really byzantine solvers may not work well with SolverData, but the ODEData class is a more basic data structure containing only a Grid reference and an array of solution data, which may work better depending on the situation.

How do I plot OOPS .csv data? Each row has the format (time, position, value). These .csv files can be loaded into your favorite data analysis software and manipulated that way. If you just need a quick look at your data, try using plotData.py in the OOPS/scripts directory. Instructions on using it are located in Sec. 3.12.

## 4.2 Extending OOPS

I want to add to this project. Can I? Possibly. In most circumstances, forking the project is more appropriate. As the goal of OOPS is to be an easy-to-use PDE solver with a self-consistent design, code maintenance is a serious responsibility. Jacob, as the owner and maintainer for the project, doesn't have

the time to patrol ten different people's work for code quality. Consequently, if you don't have an institutional connection to him, permission to edit the repository directly is unlikely.

If I can't edit it, can I request a feature? We can't guarantee anyone on the project has the time or interest to add new features, but feel free to make requests or suggestions.

What if I have an idea to do something easier? We really want this project to be easy to use. If you have good ideas to make things more consistent, more streamlined, or easier to use without sacrificing flexibility, don't keep it a secret. Let us know. Fork the project and show us how it will work.

## 4.3 Troubleshooting

#### 4.3.1 Parameters

I keep getting segmentation faults when I try to access a parameter inside my ODE class. Make sure ODE.setParameters() is called before ODE.initData() or any other function that may access the Parameters object.

#### 4.3.2 Python

None of the OOPS Python scripts will run! Make sure that your Python installation is up to date. OOPS should complain if you don't have at least Python 3.0 installed. If a more modern installation doesn't work, please let us know.

I'm having problems getting the plotData.py script to run. The plotData.py script requires both Matplotlib and NumPy to work. Install them using pip, conda, or another package manager. If you have them installed, try updating them. If you still encounter issues running them, please let us know.