Pool-seq uncertainty analysis

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Simple pairwise comparisons

Simulate a pairwise comparison between alleles at a single location without error.

```
# load dependencies
library(ggplot2)
library(tidyverse)
set.seed(172452)

# establish pairwise parameters

## allele frequencies for high and low populations
popH <- 0.3
popL <- 0.09
## absolute difference in allele frequencies
diff <- abs(popH - popL)
## scale data logarithmically
logdiff <- -log10(diff)
## print pairwise comparison value -- 'true' value
logdiff</pre>
```

[1] 0.6777807

Estimating 'effective coverage'

[1] 0.8772115

A simulated calculation of coverage using the math detailed in Tilk et al. 2019. In other words, my own miniature HAF-pipe functions. Our variable cvg_e is the 'theoretical coverage at which binomial sampling of reads would be expected to contain the observed amount of error from estimated frequencies.' Put another way, the estimated and theoretical root mean squared error (RMSE) rates will equal each other under 'effective coverage.'

```
# modulate pairwise comparison with coverage as a source of error
  # n is the number of sites, which in our case is just one
  n < -1
  ## estimated and true allele frequencies at one site
  AFtrue <- rbinom(100,100,0.38) / 100
  AFest <- rbinom(100,100,0.43) / 100
  ## effective coverage -- Tilk et al. 2019
  cvg e <- sum(AFtrue * (1 - AFtrue)) / sum((AFest - AFtrue) ^ 2)</pre>
  cvg_e
[1] 30.42092
  ## theoretical root mean squared error
  RMSEthe <- sqrt( sum(AFtrue * (1 - AFtrue)) / (cvg_e * n) )</pre>
  RMSEthe
[1] 0.8772115
  ## estimated RMSE
  RMSEest <- sqrt( sum((AFest - AFtrue) ^ 2) / n)
  RMSEest
```

In this case, with the code above, error introduced by variation in coverage would be evaluated via the magnitude of difference between theoretical and estimated RMSE values.

Tilk, Susanne, Alan Bergland, Aaron Goodman, Paul Schmidt, Dmitri Petrov, and Sharon Greenblum. 2019. "Accurate Allele Frequencies from Ultra-Low Coverage Pool-Seq Samples in Evolve-and-Resequence Experiments." *G3* 9 (12): 4159–68.

Coverage and pairwise allele frequency comparisons

Simulate a pairwise comparison between alleles at a single location with coverage error.

Simple plot of random allele frequencies

Pull allele frequencies from a distribution for 'low' and 'high' poolseq populations and plot them.

```
## the following code is from my professional website
expl_freqs <- readRDS('expl-freqs.Rds')
arm <- expl_freqs %>%
   filter(chrom=='2L') %>%
   slice(1:800)

D <- (sample(400:600,800,replace = TRUE))/1000
N <- (sample(300:600,800, replace = TRUE))/1000

sampledata <- tibble(
   "pos" = arm$pos,
   "N" = N,
   "D" = D
)</pre>
```

```
plt <- ggplot(data=sampledata, aes(pos/16)) +
   geom_line(aes(y = N, colour = "non-explorers")) +
   geom_line(aes(y = D, colour = "explorers"))
plt + labs(x = "Position (Mb)")</pre>
```

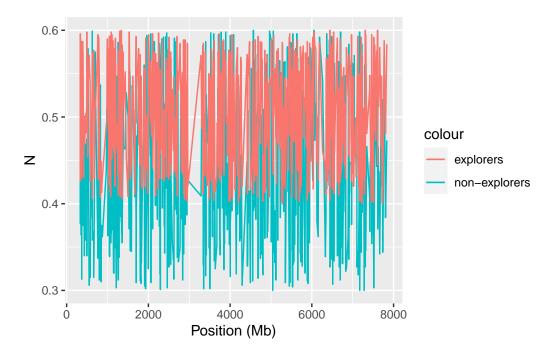


Figure 1: Allele differences between exploring and non-exploring flies.