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Bytecode Analysis for Proof Carrying Code

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Abstract

Out of annotated programs proof carrying code systems construct and prove verification conditions that guarantee a given safety policy. The annotations may come from various program analyzers and must not be trusted as they need to be verified. A generic verification condition generator can be utilized such that a combination of annotations is verified incrementally. New annotations may be verified by using previously verified ones as trusted facts. We show how results from a trusted type analyzer may be combined with untrusted interval analysis to automatically verify that bytecode programs do not overflow. All trusted components are formalized and verified in Isabelle/HOL.

Keywords: Proof carrying code, bytecode, safety policy, type analyzer, Isabelle/HOL

1 Introduction

Proof carrying code (PCC) enables a code producer to convince a code consumer that a program is safe to execute. It associates to the program a machine-checkable proof of its safety. The code consumer checks this proof against a formula that guarantees safety of the program at hand. This formula is constructed individually for each program by a verification condition generator (VCG). In the earlier PCC systems [10] the VCG is a highly engineered component that tries to produce proof obligations that are easily prove- and checkable. This comes at the price of having a complex component that is difficult to understand and trust. A bug in the VCG can lead to provable verification conditions for unsafe programs. Foundational proof carrying code [3] remedies this by requiring the verification condition to directly express the desired safety property in terms of the machine semantics. A VCG in form

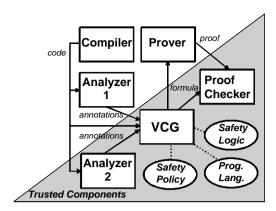


Fig. 1. PCC system architecture

of a proof tactic may still be applied. In this case all the formula transformations it does are inside the logic and must be verified. This typically leads to big proof objects. In addition verification conditions directly expressing safety require higher order logics, which hampers automatic proof generation. For some safety policies, such as type safety, correct instruction decoding, program counter in range etc., this is yet feasible as proofs can be extracted from sophisticated type systems [9]. A promising compromise between purely foundational and classical PCC is the Open Verifier [6] architecture. While verifying a powerful VCG as in [10] is a daunting task, it is possible to use a minimal VCG as trusted core. It delegates more complicated transformations to untrusted extensions that are obliged to certify their work. In [17] we follow a similar idea, except that in our case extensions are verified and thus trusted. We formalize a parameterized framework for a generic VCG in the theorem prover Isabelle/HOL. The framework defines signatures and specifies requirements for functions used as parameters by the generic VCG. By defining these parameters to a particular programming language, safety policy and safety logic one obtains an instantiated VCG. If one verifies that the instantiated parameters meet the framework's requirements the correctness and soundness proof for the generic VCG automatically carry over to the instantiated one. In this paper we will instantiate a VCG that checks for arithmetic overflow in Jinja bytecode programs. Jinja [8] is a downsized version of Java featuring object creation, inheritance, dynamic method calls and exception handling. As safety logic we use a first order expression language [16] deeply embedded into Isabelle/HOL.

A general problem in program verification is to find invariants for loops. Our VCG assumes that these are given in form of annotations in the code. It is the task of the code producer to find them. For many safety properties inductive invariants can be generated automatically using static program

analysis. The main contribution of this paper is to show how annotations can be gained from interval analysis and type inferences done by a Java bytecode verifier. In our previous papers annotations had to be added manually by the code producer. Since one has to verify annotations as part of the verification condition the analyzers must not be trusted. Any external tool whose results can be transformed to annotations in our first order expression language may be used. However, sometimes one knows that some analyzer can be trusted. For example in the Jinja formalization we have a completely verified bytecode verifier. Given a bytecode program it infers the types of registers and stack elements for all program positions. In this paper we will show how one can instantiate the generic VCG such that it combines trusted and untrusted information. Our aim are verification conditions that oblige us to verify untrusted parts and allow us to assume trusted facts. We call such verification conditions incremental as they only have some value, if their assumptions hold for a particular program. To check this, one has several possibilities. First, the assumptions may arise from a trusted and efficient analyzer. In this case the client can run this analyzer and hand the results over to the VCG as trusted parts. Second, we may use an analyzer that emits a certificate for each result. This is generally just another instance of PCC and could be handled by giving the analyzer's results directly to the VCG as untrusted facts. Instead of having one big VCG that combines the results of various untrusted sources, we can employ multiple ones. In this case we can prove the results of different analyzers in isolation.

2 PCC Framework

Our generic VCG constructs formulas out of annotated control flow graphs. The control flow of a program Π is determined by a parameter function succsF which yields for each position p a list of successor positions paired with branch conditions. The intuition is that $(p',B) \in set$ (succsF Π p) means that p' is directly accessible from p in situations where B holds. Formally, we write $\Pi,(p,m) \models B$ to say that a state (p,m), where p is the program counter and m the memory, satisfies some formula B. The safety policy is expected in form of a function sF from programs and positions to formulas, such that sF Π p expresses the safety condition we expect for program Π when we reach p at runtime. Analogously we write aF Π p for the annotation at position p. For each node p with successor p' with branch condition B the VCG constructs this proof obligation:

$$(sF\ \Pi\ p\ \bigwedge\ aF\ \Pi\ p\ \bigwedge\ B) \Rightarrow wpF\ \Pi\ p\ p'\ (sF\ \Pi\ p'\ \bigwedge\ aF\ \Pi\ p')$$

The safety formula sF Π p conjoined with annotation and branch condition

must imply the (weakest) precondition for the transition from p to p' and a postcondition consisting of the annotation and safety formula at p'. Note that the marked connectives Λ and \Longrightarrow are part of the safety logic, whereas Λ and \Longrightarrow are Isabelle/HOL's logical connectives. In addition to these proof obligations the VCG emits a safety constraint for initial states. States that satisfy the formula initF Π must satisfy the safety formula and annotation of the initial position ipc Π .

```
initF \ \Pi \Rightarrow (sF \ \Pi \ (ipc \ \Pi) \ \land \ aF \ \Pi \ (ipc \ \Pi))
```

Our framework requires that initF Π is instantiated such that it covers all initial states initS Π of a program Π . Note that initF Π yields a formula in the safety logic and may abstract properties of concrete initial states modeled by initS. The letters F and S in function names indicate whether they belong to the formula or the semantical level. Apart from initS we use a state transition relation effS Π to model the semantics of a program. We say a program is safe with respect to some safety policy sF, i.e. isSafe sF Π , if and only if all reachable states satisfy the safety policy.

```
isSafe sF \Pi = inv \Pi sF
where inv \Pi I = \forall (p,m) \in ReachableS \Pi. \Pi,(p,m) \models I \Pi p
ReachableS \Pi = \{(p,m) \mid \exists (p_0,m_0) \in initS \Pi. ((p_0,m_0),(p,m)) \in (effS \Pi)^* \}
```

The correctness theorem we have proven in Isabelle/HOL guarantees that a program Π is safe and has valid annotations if one can prove the generic verification condition for it.

theorem correct-vcq:

```
(VCGReqs ... wf initF succsF wpF sF aF \land wf \Pi \land \Pi \vdash vcg initF succsF wpF sF aF \Pi)

\longrightarrow (inv \Pi sF \land inv \Pi aF)
```

The predicate VCGReqs ... wf initF succsF wpF aF sF indicates that the parameter functions meet the requirements our framework demands. With ... we indicate that some parameters, such as Λ , \Rightarrow , initS and effS are suppressed for better readability. With vcg initF succsF sF aF we denote an instance of the generic VCG to particular setting of parameters. The wellformedness predicate wf is meant to check simple syntactic constraints on programs that help to simplify the definition of other parameter functions. The PCC framework only demands that it checks for sufficient annotations in programs. Our generic VCG requires at least one annotation per cycle in the control flow graph. In this case it constructs formulas for non annotated positions by pulling back the annotations of successor positions using wpF. Details can be found in [17]. Additional checks can be added to wf, but

one has to keep in mind that a code consumer is supposed to evaluate wf efficiently. We do not go into the details of the requirements VCGReqs poses onto the parameters. These can be found in [17] and in the Isabelle theories [2]. Most requirements are easy to prove for a particular instantiation. The hardest part is usually to verify that succsF and wpF are an abstraction of the concrete semantics defined by effS and initS. That is, if the semantics effS Π allows a transition from (p,m) to (p',m') then p' must be among the successors statically predicted by succsF Π p and the corresponding branch condition must hold for (p,m). In addition if (p,m) satisfies the precondition for some postcondition Q, i.e. $\Pi,(p,m) \models wpF$ Π p p' Q, then Q must be satisfied by (p',m'). If the resulting VCG shall be complete, that is safe programs yield provable verification conditions, stronger requirements are necessary. The wpF operator must then yield weakest(!) preconditions and succsF must give exact control flow information. In our instantiation to Jinja, we have proven both correctness and completeness of the VCG.

3 Incremental Verification

Once the requirements are proven for a particular setting of parameters, some of these parameters can be replaced by extended versions, without having to redo the proofs. A safety policy sF may be replaced by another safety policy sF' as no requirements depend on it.

```
lemma replace-sF:
```

```
VCGReqs \dots wf initF succsF wpF sF aF 
\longrightarrow VCGReqs \dots wf initF succsF wpF sF' aF
```

In addition one can always replace the wellformedness checker wf with a stronger version wf'.

lemma upgrade-wf:

$$(\forall \ \Pi. \ wf' \ \Pi \longrightarrow wf \ \Pi) \land VCGReqs \ \dots \ wf \ initF \ succsF \ wpF \ sF \ aF \\ \longrightarrow VCGReqs \ \dots \ wf' \ initF \ succsF \ wpF \ sF \ aF$$

Invariants can be used to upgrade successor functions. For this purpose we use a higher order functor upg, which upgrades a given successor function succesF by conjoining an invariant I with its branch conditions.

$$succsF \ \Pi \ p = [(p_1, B_1), \dots, (p_k, B_k)] \longrightarrow (upg \ I \ succsF) \ p = [(p_1, B_1 \ \bigwedge \ I \ p), \dots, (p_k, B_k \ \bigwedge \ I \ p)]$$
lemma $upgrade-succsF$:

$$((wf \ \Pi \longrightarrow inv \ \Pi \ I) \land VCGReqs \dots wf initF succsF wpF sF aF)$$

 $\longrightarrow VCGReqs \dots wf initF (upg \ I succsF) wpF sF aF$

Now imagine we have two analyzers for some programming language and we want to use both to verify some safety policy sF. Let aF_1 Π and aF_2 Π be the annotations we gain from both analyzers.

A simple solution is to instantiate a PCC system with the conjunction of both annotation sets. We take $aF_{12} = \lambda \Pi p$. $aF_1 \Pi p \wedge aF_2 \Pi p$ and prove the framework's requirements $VCGReqs \dots wf initF succsF wpF sF aF_{12}$. Then the code producer is obliged to give us a proof of $\Pi \vdash vcg initF succsF wpF sF aF_{12} \Pi$, which would guarantee $inv \Pi aF_{12}$ as well as $inv \Pi sF$. This approach is acceptable if neither analyzer is trustworthy. Otherwise, we repeat work as both annotation sets have to be proven.

Alternatively, we can instantiate two VCGs and do the verification incrementally. First we instantiate a VCG for a trivial safety policy that just enforces that the annotations aF_1 Π hold. We show the requirements

VCGReqs ... wf initF succsF wpF (λ Π p. True) aF_1 (1) and ask the producer to prove $\Pi \vdash vcg$ initF succsF wpF (λ Π p. True) aF_1 Π (2). For wellformed programs this gives us inv Π aF_1 , and enables us to apply lemmas upgrade-wf and upgrade-succsF to obtain another instantiation where

VCGReqs wf' initF (upg aF_1 succsF) wpF sF aF_2 (3) holds. With wf' Π we employ a stronger wellformedness checker. It guarantees wf Π and ensures inv Π aF_1 by checking a proof for (2). If wf' accepts the program the producer is asked to send a proof for $\Pi \vdash vcg$ initF (upg aF_1 succsF) wpF sF aF_2 Π (4), which guarantees the safety policy we are actually interested in, i.e. inv Π sF, as well as inv Π aF₂. This approach is superior to the first, if the second proof can make use of aF_1 Π , which now only appears on the left hand side of implications.

If aF_1 Π comes from a trusted source, we have a third alternative. In this case we get $inv \Pi aF_1$ either by assumption or because we have a correctness proof of the analyzer, that is a proof of $\forall \Pi. wf' \Pi \longrightarrow inv \Pi aF$. In both cases the code producer can skip (2) and only has to prove (4). In this paper we will apply the second option for the Jinja bytecode verifier, which is proven correct in [8]. The types it infers for registers and stack elements can be trusted and must not be verified again inside verification conditions. Other example for trusted annotations are system invariants. These are properties maintained by the Jinja Virtual Machine for any wellformed program. For example, the Jinja virtual machine preallocates objects for system exceptions, e.g. OutOfMemory, and always keeps these objects at specific positions in the heap. This can be expressed as a safety logic formula and yields a system invariant.

4 PCC for Jinja Bytecode

Jinja bytecode is a down-sized version of Java bytecode and covers essential object oriented features: object creation, inheritance, dynamic method calls and exceptions. In this paper, we only use the basic arithmetic and move instructions. Our intervall analysis is not (yet) powerful enough to handle object references and method calls. Programs with these features can be verified in our PCC system, but require manual annotations. Fig. 2 shows a method that adds all numbers from 1 to n. The two safety checks prevent arithmetic overflow and enable our interval analyzer to generate a linear inductive invariant.

Each method is executed in its own frame, which contains a program counter, registers and an operand stack. Apart from that Jinja states contain a heap mapping references to objects. Program positions are triples (C, M, pc), where pc is the number of the current instruction in method M of class C. Registers and stack contain booleans, e.g. $Bool\ True$, integers, e.g. $Intg\ 5$, references, e.g. $Addr\ 3$, null pointers, e.g. Null or dummy elements, e.g. Unit.

 $\mathbf{datatype} \ val = Bool \ bool \ | \ Intg \ int \ | \ Addr \ addr \ | \ Null \ | \ Unit$

Each value has a type associated with it:

 $datatype ty = Boolean \mid Integer \mid Class cname \mid NT \mid Void$

Jinja programs are started in position ($Start, main, \theta$), with one method frame that contains an empty operand stack and uninitialized registers. The semantics of a Jinja program Π is defined by initS Π , the set of its intial states, and effS II, a relation mapping each state to its direct successors. We skip the formal definitions, as the instructions used here are simple enough: Push val pushes a constant value onto the operand stack. Store n removes the topmost stack value and stores it in register n. Load n copies the content of register nonto the stack. If IntLeq t jumps t instructions forward (backward if t is negative) if the upper stack value is less than or equal to the lower one and erases both. IAdd pops the two upper values and replaces them with their sum. Finally, Goto t jumps t instructions forward and Return terminates a method handing the topmost stack element over to the caller. To write annotations and to specify a safety policy we have to instantiate a safety logic. An easy way to do so would be to use the logic of the theorem prover Isabelle/HOL as safety logic by defining formulas semantically as predicates on Jinja states. We have used this shallow embedding technique in other instantiations [15], but decided to use a deeply embedded first order expression language here. A shallow embedding eases the definition and verification of a wpF function significantly, but makes the definition of a precise control flow function

```
Load n
                                          push input
    Push Inta 65536
                                          push bound
    IfIntLeq 20
                                          safety check
    Push Inta 0
                                          initialize Rq k
    Store k
                                          initialize Rq r
    Push Inta 0
    Store r
lp: Load k
    Load n
                                          if n \leq k goto ex;
   IfIntLeq 13
                                          else {
   Load r
   Push Intg 2147385346
                                          safety check
    IfIntLeq 10
    Load k
    Push Inta 1
    IAdd
                                          k := k + 1
    Store k
    {\tt Load}\ k
    {\tt Load}\ r
    IAdd
                                          r := r + k
    Store r
                                          qoto lp: }
    Goto -14
ex: Load r
    Return
```

Fig. 2. Example Program

harder. In the deep embedding succsF can extract information, such as types or jump targets, from structural analysis of annotations. This helps to limit the branches succsF yields for dynamic method invocations and exceptions. Moreover, the limitation to first order simplifies the proofs of the resulting verification conditions and allows us to use other tools than Isabelle/HOL for this purpose. The expression language we use is designed to adequately model Jinja states and can express weakest preconditions for all Jinja instructions [16]. In this paper we only need a small fragment of it:

```
datatype expr = Cn \ val \ | \ Rg \ nat \ | \ St \ nat \ | \ Ty \ expr \ ty \ | \ expr \ op \ expr \ | \dots op = \bot, | \_, | \bot, | \_, | \bot, | \bot, | \bot
```

We have expressions for constants, register and stack access, type checking as well as arithmetic and logical operations. When evaluated on a Jinja state all these expressions yield a Jinja value. The formal definition of $eval::prog \Rightarrow state \Rightarrow expr \Rightarrow val$ is in [16]. Here it is only important to know that expressions are considered valid formulas if they evaluate to $Bool\ True$.

$$\Pi, s \models F \equiv (eval \ \Pi \ s \ F = Bool \ True)$$

To define the provability judgment ⊢ one usually gives a calculus of introduction and elimination rules. However, if we want to do the proofs in Isabelle/HOL we can also define provability semantically.

```
\Pi \vdash F \equiv \forall s \in ReachableS \ \Pi. \ \Pi, s \models F
```

We decided for this option, as it trivializes the correctness and completeness

requirement for the safety logic. Formulas are considered provable if we can prove in Isabelle/HOL that they hold for all reachable states. Using these expressions, we instantiate a safety policy that prohibits arithmetic overflow. We simply check that each addition yields a result that is below MAXINT, which is 2147483647 for Java.

The instantiation work lies in defining the successor function succsF and a weakest precondition operator wpF and proving that they meet the requirements the framework poses on them. The first order expression language is designed to be expressive enough to define a complete wpF, that is a function that exactly reflects the semantics effS at the level of formulas. The wpF operation is defined via substitutions on formulas [16]. We do not show its definition as the principle it follows is straightforward. Whenever an instruction changes the value of some subexpression, we substitute it with an expression that compensates this effect. For example in case of IAdd we substitute each occurrence of St θ in the postcondition with St θ \perp St I. All the requirements for wpF follow easily from this lemma we have been able to prove:

$$wf \ \Pi \land (p,m) \in ReachableS \ \Pi \land ((p,m),(p',m')) \in (effS \ \Pi)$$

 $\longrightarrow eval \ \Pi \ (p,m) \ (wpF \ \Pi \ p \ p' \ Q) = eval \ \Pi \ (p',m') \ Q$

It says that evaluating the postcondition in the successor state amounts to evaluating the weakest precondition in the current state.

5 Program analysis

Since we are interested in supporting verification in different safety policies we use a general purpose static analyzer. It is an implementation of a generic abstract interpretation framework as presented in [7]. It transforms programs into a control flow graph representation, where the edge labels reflect the original commands and conditions. These labels have to be accurately interpreted by each abstract domain implementation and give raise to the abstract semantics in form of abstract transfer functions of type $D \to D$, D is an abstract domain. Replacing the labels in the control flow graph by the corresponding abstract transfer functions leads to the representation of the abstract semantics equation system. Any adequate iterative solver can solve it and provide a post-fixpoint as a safe approximation for it, provided the convergence is guaranteed.

```
Load i st 0 := \operatorname{rg} i

Push v st 0 := v

If False n st 0 = \operatorname{ff}; st 0 = \operatorname{tt}

Pop Nop "pop"
```

Fig. 3. Encoding bytecode instructions in labels

5.1 Adjustment of the analyzer to bytecode

The main challenge in analyzing bytecode programs, is that the instructions have implicit parameters given by the functionality for the virtual machine. Furthermore stack manipulations blur the dependency of the effects in terms of the registers. In contrast to other methods [13] we do not translate the bytecode program into an intermediate language, but implement domains that encode an abstraction of the virtual machine. This decision was due to our bad experience with an intermediate language. The only drawback we have to put up with is that the resulting implementations are only useful for bytecode-like languages.

The first step we have to mention is the encoding of the bytecode instructions into the labeling language. Some encodings are given in Fig.3. Any abstract domain implementation has to interpret the labels accurately in the sense of this transformation. For example when interpreting Push v, encoded by st 0:=v, the abstract transfer function should take into account that the abstraction of the stack has to mimic the behavior of the stack on the virtual machine. A label x := e can encode any assignment of the expression e to the variable x. But interpreting an assignment may differ from domain to an other. For example interpreting st 0 := v for a bytecode language dose not simply consist in storing the value v in the variable st 0 but should rather reflect the fact that the stack elements move down. The main reason for this is that we leave the labeling language common to all domain implementations and use it to encode different imperative or bytecode languages. For readability we note variables and expressions in a near notation to the JVM, where st i and rg j refer to the i^{th} stack position and to the j^{th} register. Conditional jumps must have two successors, where the condition evaluates to tt or to ff. This is in Fig.3 reflected by the two labels assigned to the successor edges in the case of IfFalse n.

$$e_s ::= x \in regs | v \in \mathbb{V} | e_s \ bin \ e_s | un \ e_s$$

Fig. 4. Stack expressions

$$\begin{array}{ll} \operatorname{rg} \ i := \operatorname{st} \ 0 & \lambda(a,e :: es).(a[i \mapsto eval \ a \ e], map(\lambda e.e[a[i]/\operatorname{rg} \ i]) \ es) \\ \\ \operatorname{st} \ 0 := v & \lambda(a,es).(a,e_v :: es) \\ \\ \operatorname{st} \ 0 := \operatorname{st} \ 0 + \operatorname{st} \ 1 & \lambda(a,e_1 :: e_2 :: es).(a,(e_1+e_2) :: es) \end{array}$$

Fig. 5. Some transfer functions for :=

5.2 Interval analysis for the bytecode

We implemented interval analysis as a result of lifting the lattice of intervals, a special case of some values lattice \mathbb{V} , to the lattice $\mathbb{V} \to \mathbb{V}$, where \mathbb{V} represents the set of variables we are interested in. This transformation is done by a functor which has minimal assumptions on the implementation of the lattice of values, whence the techniques we present are applicable to all such liftings. Lattices for values have to approximate values of the programming language by abstract values (\mathbb{V}). This is ensured by a function $\alpha: val \to \mathbb{V}$. They also have to provide an arithmetic and a logic in order to reflect the operations $+, *, -, \leq, >, =, \text{etc.}...$ For intervals we use a standard arithmetic, widening and narrowing as described in [11]. We abstract numerical constants c by the interval [c, c]. We used the intervals [0, 0], [1, 1] and [0, 1] to represent ff, tt, and the unknown truth value.

Dealing with the stack

The set of variables \mathcal{V} we are interested in is composed by the registers regs and the stack elements svars i.e. $\mathcal{V} = regs \uplus svars$. The key to a precise bytecode analysis, is to keep track of what the values on the stack stand for. This is of great use in the exploitation of the branching conditions, since these are usually expressed in terms of stack elements. For this purpose we associate an expression to each stack position, which is a safe description of the associated value in terms of the registers. The syntax of stack expressions is given in Fig.4. Since the shape of the stack changes along the program, we represent it by a list. Hence the lattice of our insensitive liftings, and thus also interval analysis, is $\mathcal{LV} = (regs \to \mathbb{V}) \times (sexpr\ list)$.

Transfer functions

The transfer functions are strict in the sense if an expression evaluates to $\perp_{\mathbb{V}}$, the next abstract state is unreachable and hence will be $\perp_{\mathcal{LV}}$. Since we analyze

```
\begin{array}{l} bcond \ (\mathsf{st} \ 0 = \mathsf{ff}) \ (a,e :: es) \ = \\ \mathbf{case} \ e \ \mathbf{of} \\ \\ \mathsf{rg} \ i \ bin \ \mathsf{rg} \ j \Rightarrow \\ \mathbf{let} \\ v_i = a[i] \ \sqcap_{\mathbb{V}} \ varncond \ \underline{bin} \ a[j] \\ v_j = a[j] \ \sqcap_{\mathbb{V}} \ varncond \ \overline{bin} \ a[i] \\ \mathbf{in} \ (a[i \mapsto v_i; j \mapsto v_j], es) \\ \mathsf{rg} \ i \ bin \ e' \Rightarrow (a[i \mapsto \ varncond \ bin \ (eval \ a \ e')], es) \\ \neg e' \Rightarrow \ bcond \ (\mathsf{st} \ 0 = \mathbf{tt})(a, e' :: es) \\ \_ \Rightarrow (a, es) \end{array}
```

Fig. 6. Treatment of one case of branching conditions

only well formed programs, the existence and the type correctness of the stack elements at different program positions is guaranteed by the bytecode verifier. Some of the transfer functions for the "assignments" are listed in Fig. 5. The interesting case is when the label corresponds to a Store i instruction. The associated abstract value to register i will change and hence for consistency all stack expressions referring to register i have to be updated. Replacing every occurrence of rg i in the expressions on the stack by the actual value v_i of register i updates these accurately. In the second line of Fig. 5 we associate to a value in the labeling language v a sexpr expression $e_v = \alpha(v)$. With eval a e we perform a bottom-up evaluation of the expression e in the abstract state aby simply looking up variables in a, abstracting constants by α , and otherwise recurrively applying the operations defined by \mathbb{V} . The transfer functions for the branching conditions use the expressions on the stack in order to restrict the next abstract state. We consider the case where the value on top of the stack is supposed to be false in the next states. If the approximation of this value is $\alpha(tt)$, then the next state will be unreachable, otherwise we restrict the next state according to the function bcond shown in Fig.6. The interesting case is when the boolean condition is of the form x bin b, where $x \in regs$. In this case the lifting functor updates the abstract value v_x associated to x by $v_x \sqcap_{\mathbb{V}} varncond \ bin \ v_b$, where v_b is the abstract value the expression b evaluates to, and varncond is a function specific to each domain of values and gives a best way to restrict an abstract value given a binary operator and the value of the right hand side, where the binary condition is supposed not to hold. Domains for values have also to provide a function varcond for the analogous scenario, but where the binary condition is supposed to hold. bin is a binary operator such that $x \ bin \ y \Leftrightarrow y \overline{bin} \ x$ holds. The other cases are similar.

Finally, every domain implementation has to make a function toAnnotation available, which transforms a domain element to a formula in the safety logic used for annotations. It implements the concretization function γ .

6 Bytecode Verification

The Jinja Bytecode Verifier infers the types for register and operand stack values. Encoded into our safety logic these facts become expressions of the form Ty $(Rg \ \theta)$ $(Class \ Start)$ \bigwedge \ldots \bigwedge Ty $(St \ \theta)$ Integer \bigwedge \ldots Using the type safety proof of [8] we can easily derive the following theorem, which allows us to trust the Bytecode Verifier's result.

$$wtP \ (bcv \ \Pi) \ \Pi \longrightarrow inv \ \Pi \ (conv-Ty \ (bcv \ \Pi))$$

When the Jinja type checker wtP accepts the types bcv Π , inferred by the bytecode verifier, as a welltyping for a program Π , then we can convert these types to formulas that hold at runtime. Following the schema from §3 we upgrade succsF with these type constraints and strengthen the wellformedness checker with wtP (bcv Π). That is, we verify VCGReqs . . . (λ Π . wf $\Pi \wedge wtP$ (bcv Π)) initF (upg (λ Π . conv-Ty (bcv Π)) succsF) wpF sF aF, which gives us a correct VCG for Jinja.

7 System Overview

7.1 Generating Verification Conditions

Fig. 7 shows the process of synthesizing the verification condition, which is common to both consumer and producer. Java classfiles are converted into Jinja ML representation by J2ML, a tool we implemented using Perl and Jissa[1]. Jissa decodes binary classfiles to a textual assembly notation, which Perl then transforms to a ML representation of Jinja bytecode. In ML we have the interval analyzer as well as executable versions for the VCG and the BCV available. The latter two are automatically generated from their Isabelle/HOL formalizations, which we have verified. First, we run the interval analysis to obtain invariants for loops. These are then given to the VCG together with the program code. We have instantiated the VCG with a successor function that internally uses the Bytecode Verifier to construct branch conditions with type information for registers and stack. These are helpful for proof construction as many of our Jinja specific proof rules have type constraints. To construct proofs we consider two different techniques: First one can employ a theorem prover. Although other first order provers with proof objects and sufficient support for arithmetics could be employed, we rather tend to use Isabelle/HOL for this purpose as well. It may not be the best prover as it is built for interactive verification, but it enables us to define the provability judgment semantically. The second technique is to use a proof producing program analysis.

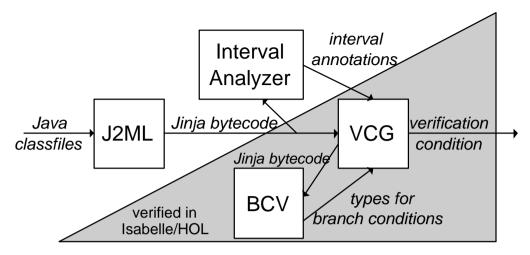


Fig. 7. Generation of Verification Conditions for Jinja

7.2 Proof Construction with Isabelle

For the entry point of the loop (lp) in Fig. 2 the interval analysis gives us this expression:

$$Cn\ (Intg\ 0) \leqslant Rg\ r \land Rg\ r \leqslant Cn\ (Intg\ 2147385346) \land Cn\ (Intg\ 0) \leqslant Rg\ k \land Rg\ k \leqslant Cn\ (Intg\ 65535) \land Rg\ n \leqslant Cn\ (Intg\ 65535)$$

If we use this annotation, we obtain a verification condition that is automatically provable by Isabelle's simplifier. The simplifier automatically translates expressions in our first order language into HOL propositions using rewriting rules for eval. For example, here is a rule that turns \bot into Isabelle's +.

eval
$$\Pi$$
 s (Ty e Integer) = Bool True \wedge eval Π s (Ty e' Integer) = Bool True \longrightarrow eval Π s (e \downarrow e') = the-Intg (eval Π s e) + the-Intg (eval Π s e')

Note that this rule has type constraints as side conditions. These can automatically be discharged with the type information put into branch conditions by the BCV. After simplification the resulting HOL formulas can be given to Isabelle's decision procedures. For the example above linear arithmetics suffices. If we remove the inner safety check from our example program, interval analysis cannot find an inductive invariant any more, because it does not know the relationship between $Rg\ k$ and $Rg\ n$, i.e. $2 + Rg\ n = (Rg\ k) + (Rg\ k + Cn\ Intg\ 1)$. However, if we manually add this relationship as invariant, the program can be verified automatically, but now requires a fragment of bounded arithmetics to find an upper bound for multiplication expressions.

7.3 Proof producing program analysis

After the analyzer reaches a post-fixpoint, it should return a proof that the found annotations are correct, i.e. form valid Hoare triples. This would avoid reverifying the annotations as in the former case, which needs the presence of special decision procedures, e.g. bounded arithmetic if the programming

language admits multiplication. We developed this technique independently from [12] and have almost finished implementing it for interval analysis. More details in [5]. This technique is attractive due to the short proofs we get. Intuitively, since the analyzer infers these invariants, their correctness proofs will rely on a small set of theorems, which express that the analyzer manipulates domain elements correctly. Proof producing analysis gives raise to sound yet incomplete efficient proof-producing decision procedures, which may be helpful to verify the analyzed programs.

7.4 Proof Checking

Isabelle can record proof objects in LF style [4]. These can be transmitted to the consumer side. There Isabelle's proof checker finds out whether the received proof fits the verification condition, which is computed as Fig. 7 shows. The proof checker is a relatively small and simple ML program, and can thus be trusted without a machine checked proof.

8 Conclusion

Our generic VCG can be instantiated such that it makes use of trusted and untrusted analysis results. It can be instrumented such that only the first need to be verified. In this paper we employ an untrusted interval analyzer and a trusted type analyzer (BCV) to verify automatically that Jinja programs do not overflow. This is a major improvement to our previous work [17] [15] [16], where we annotated programs manually. Our formalization of Jinja and PCC is about 51k lines of Isabelle/HOL. It demonstrates that it is feasible to have a fully verified trused code base for a PCC system. In the future we try to extend on this work in various angles. More advanced program analysis techniques are planned to be implemented. Jinja's bytecode is going to be extended towards the Verificard bytecode [14], which now almost covers the entire Java bytecode. A downside of our generic verification conditions is that they contain a lot of redundant and irrelevant information. We plan to improve this by using optimizing postprocessing functions. In the Open Verifier [6], untrusted extensions are used to abstract the exact results of the core verifier. This is analogous, except that we rather try to employ verified optimizers.

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