COMP130014 编译

第十一讲: 指令选择

徐辉 xuh@fudan.edu.cn



大纲

- 一、AArch64指令集
- 二、phi指令处理
- 三、指令选择问题

一、AArch64指令集

指令集架构

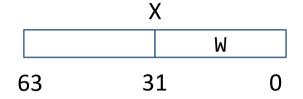
- 精简指令集(RISC)
 - 每条指令只做一件事(主要指内存访问和运算分离)
 - AArch/ARM、RISC-V
- 复杂指令集(CISC)
 - 一条指令可以包含多个底层操作(load-add-store)
 - X86 (Intel IA-32)、X86-64架构(AMD64)
- 其它
 - VLIW: Very long instruction word (Intel IA-64)
 - EPIC: Explicitly parallel instruction computing

目标指令集: ARM v8a

- 32位版本: ARM Cortex-A32
- 32/64位版本: ARM Cortex-A57/A72/A73等,代表芯片
 - Apple A8/A8x/A9/A9x/A10/A10x (iPhone, iPad)
 - Apple M1/M2 (iPhone, iPad, MacBook)
 - Qualcomm Kryo: 骁龙(Snapdragon 820)
- AArch64 vs ARM64 (Apple版本)

ARM-v8A寄存器:通用寄存器

- 通用寄存器: X0 X30 (64-bit)
 - W0-W30: 低32位



IR=>Assembly: 数据存取

• 栈(顶)寄存器: SP(16字节对齐)

```
%x = alloca i32
store i32 1, i32* %x
%x0 = load i32, i32* %x

sub sp, sp, 16
mov w0, 1
str w0, [sp]
ldr w0, [sp]
```

```
#: llc -00 -march=arm64 -filetype=asm foo.ll -o foo.s
```

在MacOS (M1)上编译和运行

```
#: as foo.s -o foo.o
#: ld foo.o -lSystem -syslibroot `xcrun -sdk macosx --show-sdk-
path` -e _start -arch arm64
```

或

#: gcc test.o -e _main -arch arm64

在x86上运行编译和运行ARM-v8A程序

安装qemu工具链

```
#: sudo apt install qemu qemu-system qemu-user
#: sudo apt install gcc-aarch64-linux-gnu
#: sudo apt install qemu-user-static libc6-arm64-cross
```

交叉编译程序

```
#: aarch64-linux-gnu-gcc hello.c
```

在虚拟机上运行程序

#: qemu-aarch64 -L /usr/aarch64-linux-gnu a.out

ARM-v8A指令: MOV

• MOV: 任意16位立即数,或左移16/32/48位

MOV <Wd>>, #<imm>

31	30	29	28	27	26	25	24	23	22 21)	5	4		0
sf	1	0	1	0	0	1	0	1	hw	imm16			Rd	
	0	20												

opc

For the 32-bit variant: is a 32-bit immediate which can be encoded in "imm16:hw".

For the 64-bit variant: is a 64-bit immediate which can be encoded in "imm16:hw".

<shift>

For the 32-bit variant: is the amount by which to shift the immediate left, either 0 (the default) or 16, encoded in the "hw" field as <shift>/16.

For the 64-bit variant: is the amount by which to shift the immediate left, either 0 (the default), 16, 32 or 48, encoded in the "hw" field as <shift>/16.

```
mov x1, 65535
mov x2, 65539
mov x3, 131070
```

```
mov x8, 3
movk x8, 1, lsl 16
```

ARM-v8A指令: 寻址模式

• 不支持直接寻址, 间接寻址

Addressing Mode	Offset										
Addressing Mode	Immediate	Register	Extended Register								
Base register only (no offset)	[base{, #0}]	-	-								
Base plus offset	[base{, #imm}]	[base, Xm{, LSL #imm}]	[base, Wm, (S U)XT(X W) {#imm}]								
Pre-indexed	[base, #imm]!	-	-								
Post-indexed	[base], #imm	[base], Xm ^a	-								
Literal (PC-relative)	label	-	-								

```
ldr x2, [x1]
ldr x2, [x1, 10]
ldr x2, [x1, x0]
ldr x2, [x1, 10]!
ldr x2, [x1], 10
ldr x2, [x1, x0, lsl 3]
```

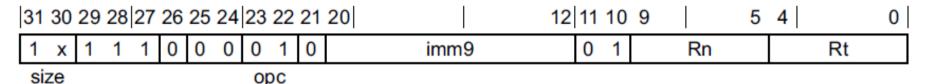
```
x2 = [x1 + 10]
x2 = [x1 + x0]
x1 = x1 + 10, x2 = [x1]
x2 = [x1], x1 = x1 + 10
x2 = [x1 + x0 * 8]
```

```
str w0, [x1]
str w0, [x1, 10]
str x2, [x1, x0]
```

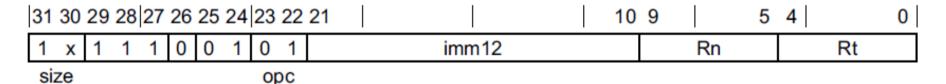
ARM-v8A指令: LDR(立即数)

ldr x2, [x1] ldr x2, [x1, 10] ldr x2, [x1, 10]!

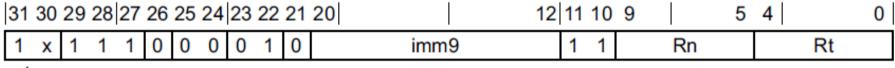
LDR <Xt>, [<Xn|SP>], #<simm>



LDR <Xt>, [<Xn|SP>{, #<pimm>}]



LDR <Xt>, [<Xn|SP>, #<simm>]!



size opc

<simm> Is the signed immediate byte offset, in the range -256 to 255, encoded in the "imm9" field.

<pimm> For the 32-bit variant: is the optional positive immediate byte offset, a multiple of 4 in the range 0 to 16380, defaulting to 0 and encoded in the "imm12" field as <pimm>/4.

For the 64-bit variant: is the optional positive immediate byte offset, a multiple of 8 in the range 0 to 32760, defaulting to 0 and encoded in the "imm12" field as <pi>pimm>/8.

ARM-v8A指令: LDR(寄存器/标签)

LDR $\langle Xt \rangle$, $[\langle Xn | SP \rangle$, $(\langle Wm \rangle | \langle Xm \rangle) \{$, $\langle extend \rangle \{\langle amount \rangle \} \}]$ 31 30 29 28 27 26 25 24 23 22 21 20 16 15 13 12 11 10 9 5 4 0 1 0 0 0 0 1 Rm option S 1 0 Rn Rt size opc ldr x2, [x1, x0] ldr x2, [x1, x0, lsl 3] LDR <Xt>, <label> |31 30 29 28 27 26 25 24 23 5 4 0

imm₁₉

opc

 $0 \times |0 \ 1 \ 1 |0 |0 \ 0$

<label> Is the program label from which the data is to be loaded. Its offset from the address of this instruction, in the range +/-1MB, is encoded as "imm19" times 4.

Rt

ARM-v8A指令: STR

STR <Wt>, [<Xn|SP>], #<simm> 31 30 29 28 27 26 25 24 23 22 21 20 12 11 10 9 5 4 0 1 x 1 1 1 1 0 0 0 0 0 0 0 imm9 0 Rn Rt size opc STR <Xt>, [<Xn|SP>, #<simm>]! 31 30 29 28 27 26 25 24 23 22 21 20 12 11 10 9 5 4 1 0 0 0 0 0 0 imm9 1 Rn Rt size opc STR <Xt>, [<Xn|SP>{, #<pimm>}] 31 30 29 28 27 26 25 24 23 22 21 10 9 5 4 0 imm₁₂ Rn Rt size opc STR $\langle Xt \rangle$, $[\langle Xn | SP \rangle$, $(\langle Wm \rangle | \langle Xm \rangle) \{$, $\langle extend \rangle \{\langle amount \rangle \} \}]$ 31 30 29 28 27 26 25 24 23 22 21 20 16 15 13 12 11 10 9 5 4 0 option 1 0 0 0 0 0 Rm Rn Rt size opc

复合类型如何翻译?

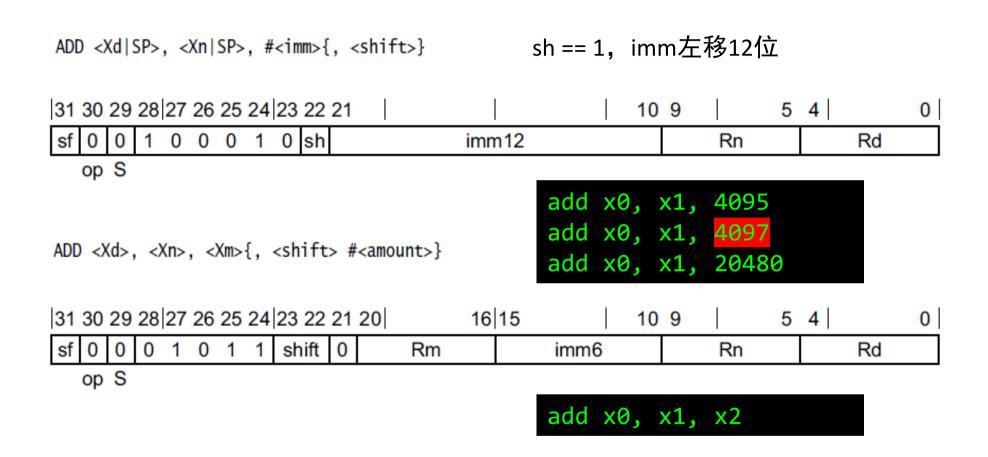
```
define i32 @main() {
    %1 = alloca [2 x i32]
    %2 = getelementptr [2 x i32], [2 x i32]* %1, i32 0, i32 0
    store i32 99, i32* %2
    %3 = load i32, i32* %2
    ret i32 %3
}
```

```
%mystruct = type { i32, i32 }
define i32 @main() {
  %1 = alloca %mystruct
  %2 = getelementptr %mystruct, %mystruct* %1, i32 0, i32 0
  store i32 1, i32* %2
  ret i32 0
}
```

IR=>Assembly: 算数运算

```
%r1 = add i32 %0, %1
%r2 = sub i32 %r1, 2
%r3 = mul i32 %r2, %1
%r4 = sdiv i32 %r3, %1
add w8, w0, w1
sub w8, w8, 2
mul w8, w8, w1
sdiv w0, w8, w1
```

ARM-v8A指令: 算数运算: ADD



For the 64-bit variant: is the shift amount, in the range 0 to 63, defaulting to 0 and encoded in the "imm6" field.

ARM-v8A指令: 算数运算: SUB

SUB <Xd|SP>, <Xn|SP>, #<imm>{, <shift>}

31 30 29 28 27 26 25 24 23 22 21	10	9 5 4	0
sf 1 0 1 0 0 0 1 0 sh	imm12	Rn	Rd
op S			

SUB <Xd>, <Xn>, <Xm>{, <shift> #<amount>}

31 30	29	28	27	26	25	24	23 22	21	20 16	15	10	9	5	4	0
sf 1	0	0	1	0	1	1	shift	0	Rm	imm6			Rn	Rd	

op S

ARM-v8A指令: 算数运算: MUL/SDIV

MUL < Xd>, < Xn>, < Xm>

不支持立即数

31	30	29	28	27	26	25	24	23	22	21	20	16	15	14				10	9		5	4	0
sf	0	0	1	1	0	1	1	0	0	0	Rm		0	1	1	1	1	1		Rn		Rd	
													о0			Ra							

SDIV <Xd>, <Xn>, <Xm>

31 30 29 28	27 26 25 24 23 22 21 20	16 15 14 13 12 11	10 9 5	4 0
sf 0 0 1	1 0 1 0 1 1 0	Rm 0 0 0 0 1	1 Rn	Rd

ο1

ARM-v8A指令:复合算数运算

MADD < Xd>, < Xn>, < Xm>, < Xa>

31	30	29	28	27	26	25	24	23	22	21	20	16	15	14	10	9		5	4		0
sf	0	0	1	1	0	1	1	0	0	0	Rm		0	Ra			Rn			Rd	
													00								
MSI	UB	<xc< td=""><td>>,</td><td><xi< td=""><td>1>,</td><td><x< td=""><td>m>,</td><td><x< td=""><td>a></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></x<></td></x<></td></xi<></td></xc<>	>,	<xi< td=""><td>1>,</td><td><x< td=""><td>m>,</td><td><x< td=""><td>a></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></x<></td></x<></td></xi<>	1>,	<x< td=""><td>m>,</td><td><x< td=""><td>a></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></x<></td></x<>	m>,	<x< td=""><td>a></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></x<>	a>												

madd x0, x1, x2, x3 msub x0, x1, x2, x3

$$x0 = x1 * x2 + x3$$

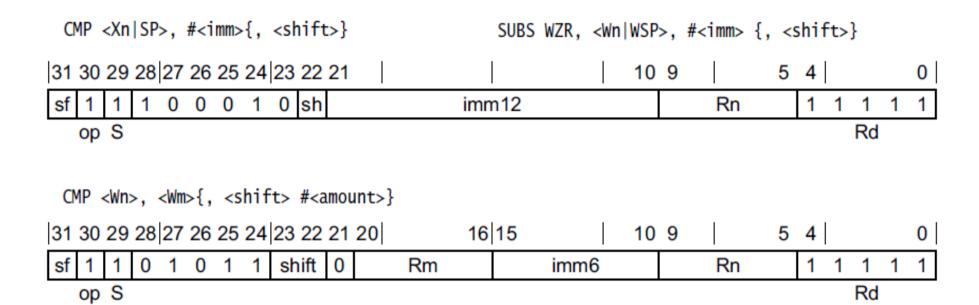
 $x0 = x1 * x2 - x3$

IR=>Assembly: 比较运算和结果获取

```
cmp w0, w1
%r1 = icmp sgt i32 %0, %1
                                  cset w0, gt
                                                    条件
%r2 = zext i1 %r1 to i32
                                  cmp w0, w1
%r1 = icmp sge i32 %0, %1
                                  cset w0, ge
%r2 = zext i1 %r1 to i32
                                  cmp w0, w1
%r1 = icmp eq i32 %0, %1
                                  cset w0, eq
%r2 = 7ext i1 %r1 to i32
                                  cmp w0, w1
%r1 = icmp ne i32 %0, %1
                                  cset w0, ne
%r2 = zext i1 %r1 to i32
                                  cmp w0, w1
%r1 = icmp sle i32 %0, %1
                                  cset w0, le
%r2 = 7ext i1 %r1 to i32
                                  cmp w0, w1
%r1 = icmp lt i32 %0, %1
                                  cset w0, lt
%r2 = zext i1 %r1 to i32
```

ARM-v8A指令: 比较运算: CMP

• 基于PSR(NZCV)寄存器实现



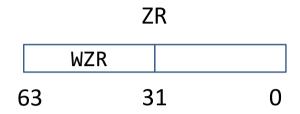
ARM-v8A指令: 读取NZCV

- 基于减法实现,更新CPSR寄存器:
 - N(31位): 符号标志位; 如果负, 则N=1
 - Z(30位): O标志位; 如果0, 则Z=1
 - C(29位): 进位标志位;
 - 无符号数:加法进位,或减法不借位,则C=1
 - V(28位):溢出标志位;有符号运算溢出,则V=1

Result	N	Z	С	V
Greater than	0	0	1	0
Less than	1	0	0	0
Equal	0	1	1	0

mrs x0, nzcv

ARM-v8A寄存器:零寄存器

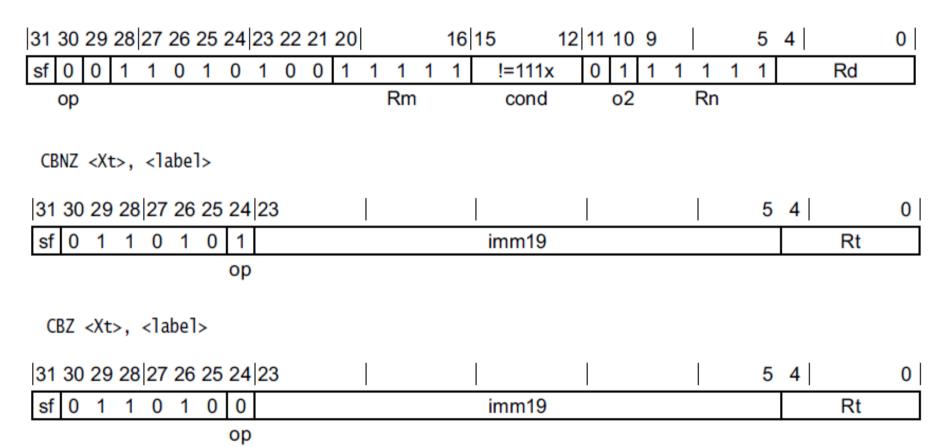


 mov x1, xzr
 x1 = 0

 mov w1, wzr
 w2 = 0

ARM v8a指令:条件指令(举例)

CSET <Xd>, <cond>



IR=>Assembly: 跳转语句

```
bb0:
    %r1 = icmp sgt i32 %0, %1
    br i1 %r1, label %bb1, label %bb2
bb1:
    br label %bb3
bb2:
    br label %bb3
bb3:
```

ARM-v8A指令: 跳转指令

B <label>

31 30 29 28 27 26 25				0
0 0 0 1 0 1		imm26		
ор				
B. <cond> <label></label></cond>				
31 30 29 28 27 26 25 24 23			5 4 3	0
0 1 0 1 0 1 0 0	imm	119	0 c	ond

Instruction	Branch offset range from the PC
Branch conditionally	±1MB
Branch Consistent conditionally	±1MB
Compare and branch if nonzero	±1MB
Compare and branch if zero	±1MB
Test bit and branch if nonzero	±32KB
Test bit and branch if zero	±32KB
	Branch conditionally Branch Consistent conditionally Compare and branch if nonzero Compare and branch if zero Test bit and branch if nonzero

add w0, w1, w2 cbz zero_set ... zero_set:

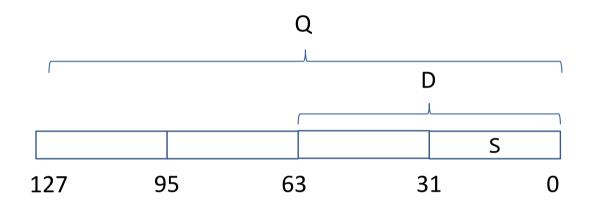
IR=>Assembly: 异或运算(逻辑NOT)

%r2 = xor i1 %r1, 0w0, w0, 1 eor EOR <Xd|SP>, <Xn>, #<imm> 31 30 29 28 27 26 25 24 23 22 21 16 15 10 9 5 4 sf 1 0 1 0 0 1 0 0 N Rn Rd immr imms opc EOR <Xd>, <Xn>, <Xm>{, <shift> #<amount>} 31 30 29 28 27 26 25 24 23 22 21 20 16 15 10 9 5 4 Rn sf 1 0 0 1 0 1 0 shift 0 Rm Rd imm6 Ν opc

Mnemonic	Instruction
AND	Bitwise AND
ANDS	Bitwise AND and set flags
EOR	Bitwise exclusive 0R
ORR	Bitwise inclusive 0R
TST	Test bits

向量寄存器和SIMD指令

• 向量寄存器: Q0-Q31



```
VLDR S0, [X0]
VLDR S1, [X1]
VADD.F32 S2, S0, S1
```

浮点数运算

VLDR Q0, [X0]
VLDR Q1, [X1]
VADD.I32 Q2, Q0, Q1

向量运算

IR=>Assembly: 函数

```
@g = global i32 10
define i32 @foo(i32 %0) {
   %x = alloca i32
   store i32 %0, i32* %x
   %g0 = load i32, i32* @g
   ret i32 %g0
}
define i32 @main() {
  %r0 = call i32 @foo(i32 1)
  ret i32 %r0;
```

```
foo:
    sub
           sp, sp, 16
   adrp
           x8, g
           x8, x8, :lo12:g
   add
           w0, [sp, 12]
   str
           w0, [x8]
   ldr
   add
           sp, sp, 16
   ret
main:
           x30, [sp, -16]!
   str
           w0, #1
   mov
           foo
   bl
   ldr
           x30, [sp], 16
   ret
g:
    .word
           10
```

1 word = 4 byte

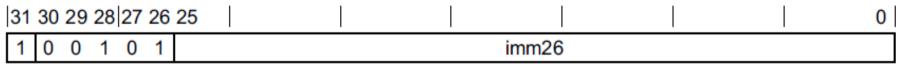
调用规约

- •参数传递: X0-X7
- 返回值: XO-X1
- Caller-saved Registers: X9-X15 (临时寄存器)
- Callee-saved Registers: X19-X28
- X29: 一般用于栈帧基指针
- X30: 一般用于返回地址
- SP: 栈顶指针

ARM-v8A指令: 函数调用

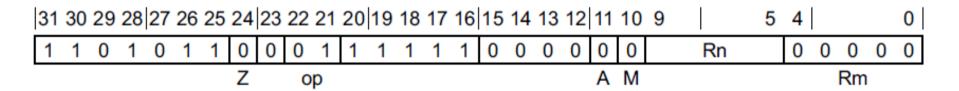
• 跳转并将X30设置为PC+4

BL < label>



op

BLR <Xn>



IR=>Assembly: 取址(全局变量)

op

Mnemonic	Instr	uctio	n												
ADRP	Comp	ute ac	ldre	ss of	4KB p	age at	a PC-relat	tive offse	et	4KB对分	齐: 末属	[12位	立为()	
ADR	Comp	ute ac	ldre	ss of l	label a	it a PC	-relative o	ffset.		adrp add	x8, g		:1o	12:g	
								5	戉:	adrp add		g@l		E @PAGI	EOFF
ADRP <xd>,</xd>	<labe< td=""><td>l></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></labe<>	l>													
31 30 29 28	8 27 26	6 25	24	23								5	4		0
1 immlo 1	0 0	0	0					im	mhi					Rd	
ор															
ADR <xd>, <</xd>	label:	>													
31 30 29 28	3 27 26	6 25	24	23								5	4		0
0 immlo 1	0 0	0	0					im	mhi					Rd	

二、phi指令处理

phi指令的引入

```
if(a==0) {
    a = a + b;
}
let r = a + c;
```

```
bb1:
    %r1 = icmp eq i32 %a1, 0
    br i1 %r1, label %bb2, label %bb3
bb2:
    %a2 = add i32 %a1, %b1
    br label %bb3
bb3:
    %a3 = phi i1 [%a1, %bb1], [%a2, %bb2]
    %r1 = add i32 %a3, %b1
```

消除phi指令方式一: 还原store-load

```
bb1:
    %a = alloca i32
    %r1 = icmp eq i32 %a1, 0
    store i32 %a1, i32* %a
    br i1 %r1, label %bb2, label %bb3
bb2:
    %a2 = add i32 %a1, %b1
    store i32 %a2, i32* %a
    br label %bb3
bb3:
    %a3 = load i32, i32* %a
    %r1 = add i32 %a3, %b1
```

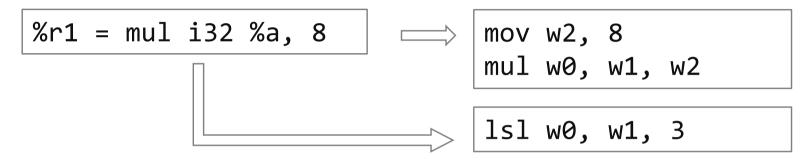
消除phi指令方式二:使用伪指令

```
bb1:
    %r1 = icmp eq i32 %a1, 0
    %a3 = %a1
    br i1 %r1, label %bb2, label %bb3
bb2:
    %a2 = add i32 %a1, %b1
    %a3 = %a2
    br label %bb3
bb3:
    %a3 = phi i1 [%a1, %bb1], [%a2, %bb2]
    %r1 = add i32 %a3, %b1
```

三、指令选择问题

IR指令存在多种ASM翻译方式

一条IR指令, 多种ASM翻译方式



IR指令组合, 多种ASM翻译方式

```
%p = getelementptr i32, i32* %array, i32 0, i32 1
%v = load i32, i32* %p

add x1, x1, 4
ldr w0, [x1]

ldr w0, [x1, 4]
```

数据流分析

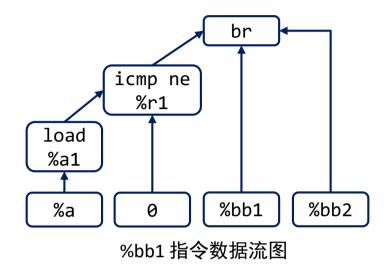
```
store
r = a * b + c;
                                                  add
%r1 = load i32 %a;
                                                 i32 %r5
%r2 = load i32 %b;
                                         mul
%r3 = mul i32 %r1, %r2;
                                       i32 %r3
%r4 = load i32 %c;
                                         load
                               load
                                                  load
%r5 = add i32 %r3, %r4;
                                                i32 %r4
                              i32 %r1
                                       i32 %r2
store i32 %r5, %r;
                              i32* %a
                                       [i32* %b]
                                                          i32* %r
                                                i32* %c
                                          指令数据流图
```

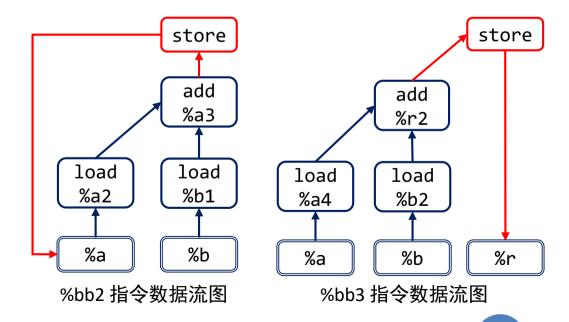
翻译汇编指令满足拓扑顺序即可

单个基本块的数据流图:可能有环

```
if(a==0) {
    a = a + b;
}
let r = a + c;
```

```
bb1:
   %a1 = load i32, i32* %a
    %r1 = icmp eq i32 %a1, 0
    br i1 %r1, label %bb2,
               label %bb3
bb2:
   %a2 = load i32, i32* %a
   %b1 = load i32, i32* %b
   %a3 = add i32 %a2, %b1
    store i32 %a3, i32* %a
    br label %bb3
bb3:
   %a4 = load i32, i32* %a
   \%b2 = load i32, i32* \%b
   %r2 = add i32 %a4, %b2
    store i32 %r2, i32* %r
```

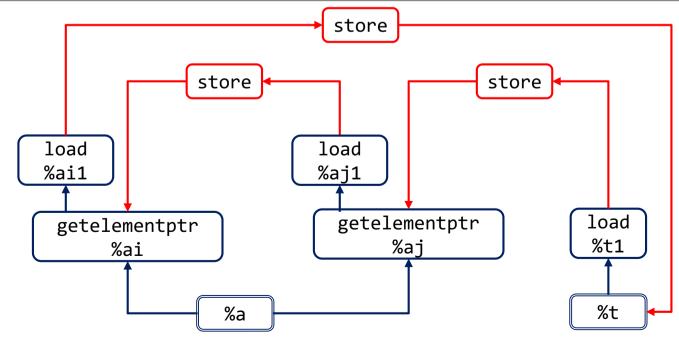




数组的情况:多种load-store顺序

```
a[i] = a[j]
a[j] = t
t = a[i]
```

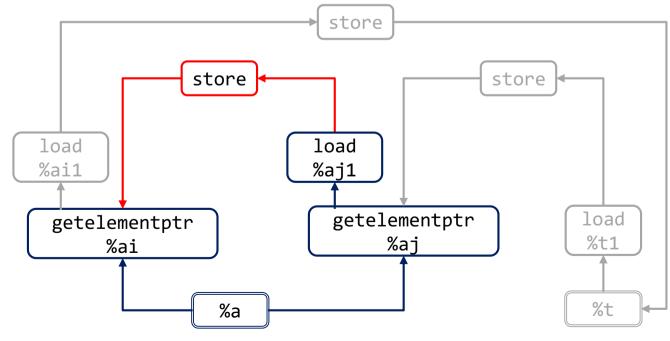
```
%ai = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 i
%aj = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 j
%aj1 = load i32, i32* %aj
store i32 %aj1, i32* %ai
%t1 = load i32, i32* %t
store i32 %t1, i32* %aj
%ai1 = load i32, i32* %ai
store i32 %ai1, i32* %t
```



数组的情况:内存同步问题

```
a[i] = a[j]
a[j] = t
t = a[i]
```

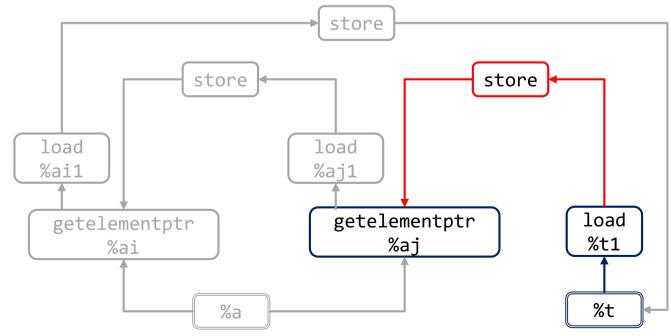
```
%ai = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 i
%aj = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 j
%aj1 = load i32, i32* %aj
%t1 = load i32, i32* %t
store i32 %t1, i32* %aj
%ai1 = load i32, i32* %ai
store i32 %ai1, i32* %t
```



数组的情况:内存同步问题

```
a[i] = a[j]
a[j] = t
t = a[i]
```

```
%ai = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 i
%aj = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 j
%aj1 = load i32, i32* %aj
store i32 %aj1, i32* %t
store i32 %t1, i32* %aj
%ai1 = load i32, i32* %ai
store i32 %ai1, i32* %t
```

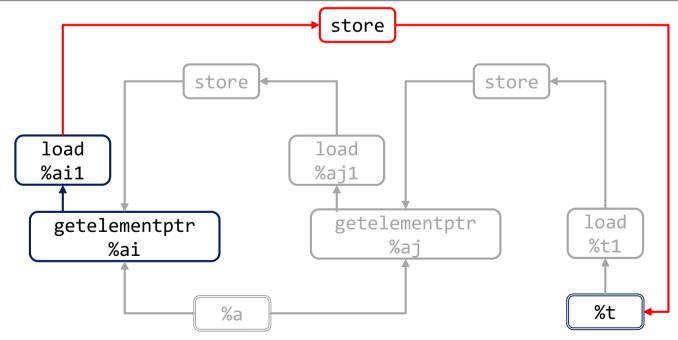


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数组的情况:内存同步问题

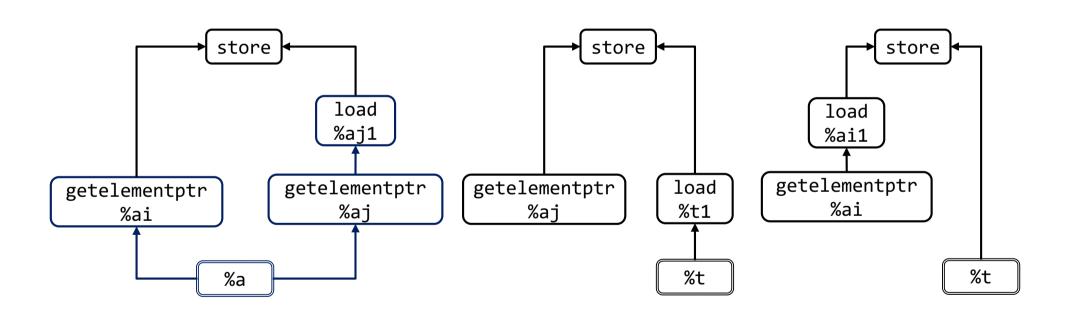
```
a[i] = a[j]
a[j] = t
t = a[i]
```

```
%ai = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 i
%aj = getelementptr [10 x i32], [10 x i32]* %a, i32 0, i32 j
%aj1 = load i32, i32* %aj
store i32 %aj1, i32* %ai
%t1 = load i32, i32* %t
store i32 %t1, i32* %aj
%ai1 = load i32, i32* %ai
store i32 %ai1, i32* %t
```



指令选择图:有向无环图

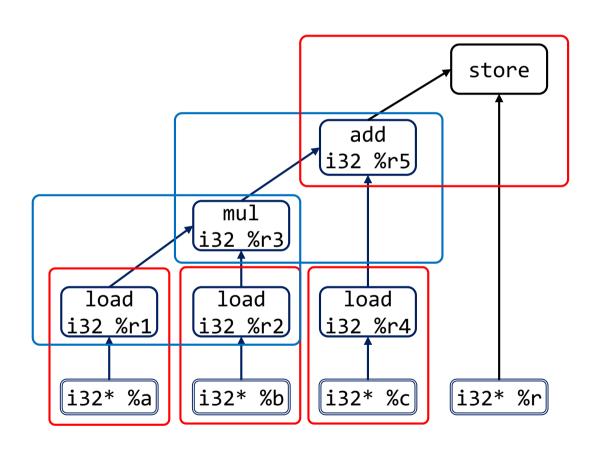
- 翻译汇编指令满足拓扑顺序即可
- 除了store外,函数调用也应当作为同步原语



- 输入Selection DAG, 如何铺树(图)使得最终的汇编代码:
 - 体积小(指令数少)
 - 运算快

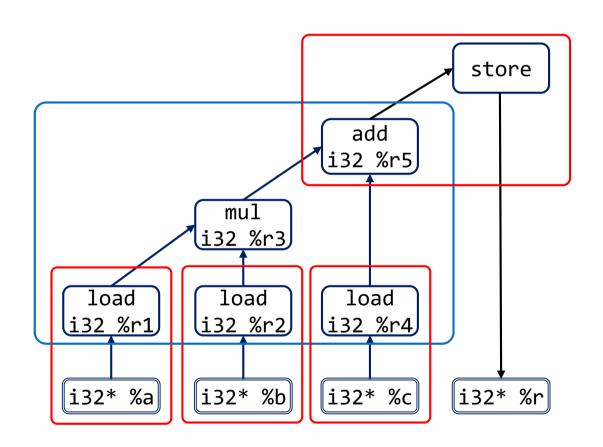
指令	开销
LDR	4
STR	1
ADD/ADD	1
SUB/SUBS	1
MUL	3
MADD/MSUB	3
SDIV	4-20
MOV	1
ADR/ADRP	1
B/BL/RET	1
CBZ/TBZ	1

指令运行开销假设 (Arm Cortex-A72)



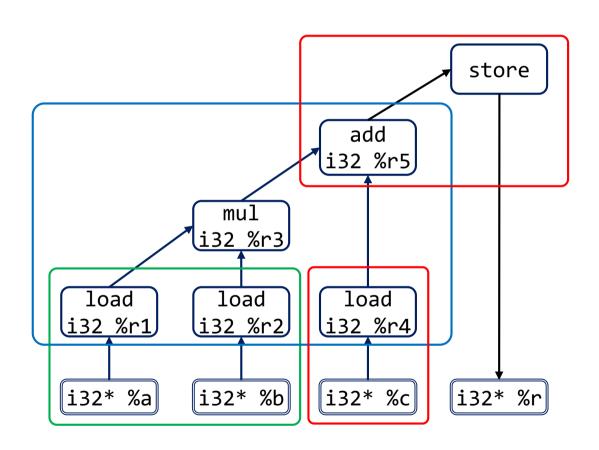
```
ldr w1, [sp, .a]
ldr w2, [sp, .b]
ldr w3, [sp, .c]
mul w3, w1, w2
add w5, w3, w4
str w5, [sp, .r]
```

方式一



```
ldr w1, [sp, .a]
ldr w2, [sp, .b]
ldr w4, [sp, .c]
madd w5, w1, w2, w4
store w5, [sp, .r]
```

方式二

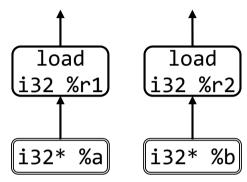


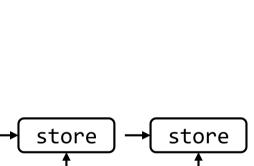
```
ldp w1, %r2, [sp, .a]
ldr w3, [sp, .c]
madd w5, w1, w2, r4
store w5, [sp, .r]
```

方式三

load + load/store + store

• 假设a和b的地址连续





i32* %a

[i32* %b]

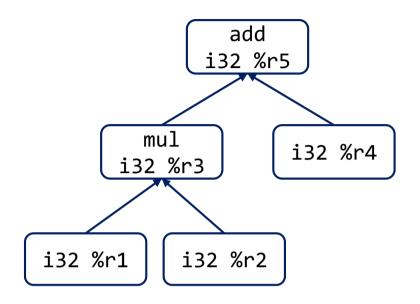
开销: 8

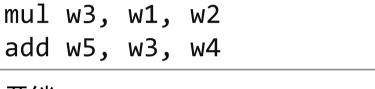
开销: 4

开销: 2

开销: 1

mul + add

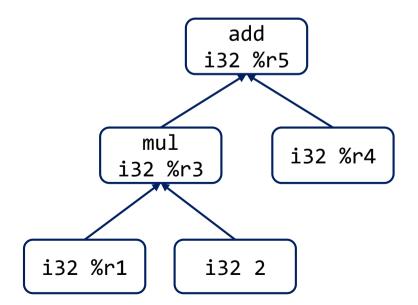




开销: 4

madd w5, w1, w2, w4

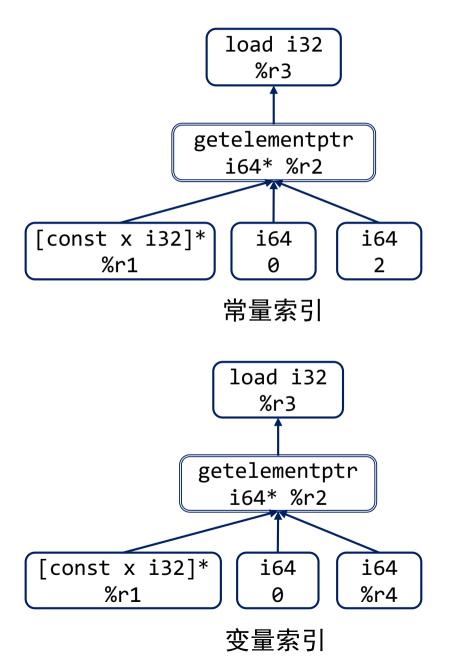
开销: 3



mov w0, 2 mul w3, w1, w0 add w5, w3, w4

开销:5

load + getelementptr: 数组



```
add .w2, w1, 16
ldr .w3, [w2] 开销: 5
ldr %w3, [w1, 16] 开销: 4
```

```
mov w0, 8
mul w2, w4, w0
add w2, w1, w2
ldr w3, [w2] 开销: 9

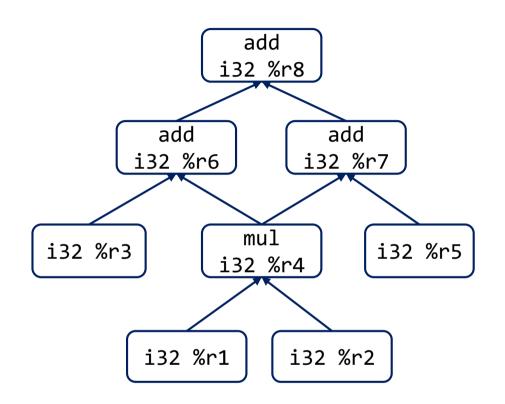
mov %w0, 8
mul %w2, w4, w0
ldr %w3, [w1, w2] 开销: 8

ldr %w3, [w1, w4, lsl 3]
```

铺树问题解法

- 贪心算法: Maximal Munch
 - 每次选择覆盖节点最多、开销最低的规则
 - 拓扑排序: 生成汇编指令
 - 局部最优
- 动态规划
 - 从树根开始, 递归搜索每个节点的最优方案

贪心法不一定能得到最优解: mul + add



```
mul w4, w1, w2
add w6, w3, w4
add w7, w4, w5
add w8, w6, w7
```

开销: 6

```
madd w6, w1, w2, w3
madd w7, w1, w2, w5
add w8, w6, w7
```

开销: 7

参考资料

- Arm® Architecture Reference Manual for A-profile architecture
- 在线模拟器: http://163.238.35.161/~zhangs/arm64simulator/

