

- Given a text
- Consider all suffixes
- sort them alphabetically

$T = \text{mississippi}\#$

$P = si$

#  
i#  
ippi#  
issippi#  
ississippi#  
mississippi#  
pi#  
ppi#  $\swarrow$   $P = (51)$   
sippi#  
sissippi#  
ssippi#  
ssissippi#

- 1) Suffixes that share a prefix are contiguous
- 2) Pattern is "positioned" before the occurrences  
 $\Rightarrow$  just scan to find  
 $\rightarrow$  occurrences

$\Rightarrow$  Suffix array : stores for every suffix the offset of the 1<sup>st</sup> character

1 2 3 4 5 6 7 8 9 10 11 12  
 $T = \text{m i s s i s s i p p i \#}$

SA  
 12  
 11  
 8  
 5  
 2  
 1  
 10  
 9  
 7  
 4  
 6  
 3

length of the text  
 SA :  $\Theta(N \log \sigma)$  BITS

$N = \# \text{ characters of the text}$

# SEARCH A PATTERN on [SA]

=> Binary search

$P = S_i$

(1)

=> pick the middle element of SA

SA
12
11
8
5
2
1
10
9
7
4
6
3

(2) 1 = mississippi compare with  $P = \underline{S}_i$

=>  $S > M$

=> P will be in the second part of the array

(3)

REPEAT

=> ~~pick~~ middle element

=> I do  $\lceil \log_2 n \rceil$  steps.

At step I compare (1P) characters at most

=> Cost of search =  $O(p \log_2 n)$

(OCCURRENCE)

=> When I've found position of ~~P~~

=> SCAN the SA and compare

=> BUT it's costly

=> Search for  $P \#$   
and  
 $P \$$

where  $\# < \Sigma < \$$   
as char of alphabet

$\Rightarrow$  2 BINARY SEARCHES TO FIND BEGINNING and the end  $\Rightarrow$   $\nmid$  know  $\#$  of occurrences

$\Rightarrow O(\underbrace{p \cdot \log n + \text{occurrences}}_{\substack{\text{only to} \\ \text{count}}})$  time  
To count and locate the occurrences

$\Rightarrow$  Counting occurrences  $O(p \cdot \log n)$  time

Retrieval  $O(p \cdot \log n + \text{occ})$  time

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Building SA (char \*T, int \*m, char \*\*SA)

for ( $i=0$ ;  $i < m$ ;  $i++$ ) {

SA[i] = T + i;

}

qsort(SA, m, sizeof(char \*), suffix\_cmp)

— 0 —

suffix\_cmp(char \*\*p, char \*\*q) {

return str\_cmp(\*p, \*q) }

$O(\overset{\text{scan}}{\frac{M}{B}} \cdot m \log n)$  I/Os

$O(m \cdot m \log n)$

# LCP-Array

↳ longest common prefix

(total number of characters shared the longest prefix by adjacent suffixes)

1 2 3 4 5 6 7 8 9 10 11 12  
T = m i s s i s s i p p i #

LCP	SA	
0	12	#
0	11	i#
1	8	i p p i #
4	5	ississippi#
0	2	ississippi#
0	1	mississippi#
1	10	pi#
0	9	p p i #
2	7	s i p p i #
1	4	s i s s i p p i #
3	6	s s i p p i #
	3	s s i s s i p p i #

$P_{n-1}$   
position

$$LCP(5, 9) = 0 = \min(4, 0, 0) = 0$$

Build SUFFIX-ARRAY (char \*T, char \*m, char \*\*SA)

for (i = 0; i < m; i++) {

SA[i] = T; }

QSORT(SA, m, sizeof(char \*), suffix\_cmp)

Suffix\_cmp(char \*\*p, char \*\*q)

return strcmp(\*p, \*q)

cost  $O\left(\frac{M}{B} \log n\right)$  ✓

Build SA (char \*T, char \*u, char ~~str~~ s)

for (i=0; i<n; i++) {

SA[i] = T + i; }

Qsort (SA, n, sizeof(char\*), suffix\_cmp)

}

suffix\_cmp (char \*p, char \*q) {

return str\_cmp(\*p, \*q)

⇒ Complexity  $O(\frac{n}{B} n \lg n)$

## SNOW-PLOW

- Require  $V$  array of unsorted items
- $H$  = sorted a min-heap over  $V$ -items
- set  $M = \emptyset$

while ( $M \neq \emptyset$ )

min = extract the minimum item from  $H$

next = read next item from  $V$

if ( $next < min$ )

put next in  $V$

else

put next in the heap

end if

end while

$$O\left(\frac{n}{B} \log_2 \frac{n}{2M}\right)$$

$\Rightarrow$  snow plow pushes sorted runs of  $B \log_2 \frac{n}{2M}$

$\Rightarrow$  keep with  $\log$  if ( $next < min$ )

and assuming RANDOM distribution of items

$$\left( (k-M) + M = k \right)$$

$\Rightarrow$   $M$  items ends up in  $V$   $p = \frac{1}{2} \Rightarrow$  I read  $k$  items

$$M = \frac{K}{2}$$

$$K = 2M$$

Build SA (char \*T, char \*u, char \*\*SA) {

for (i=0 ; i < u ; i++) {

SA[i] = T+i;

QSort (char SA, char u, size\_of (char \*), suffix\_cmp)

{

suffix\_cmp (char \*p, char \*\*q)

return string\_cmp (\*p, \*q)

$$O\left(\frac{n}{B} \cdot n \log n\right)$$