# Assignment 2 - Report

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### **Gradient Check**

To check the gradient I computed for each layer the maximum of the absolute difference of the gradients, as in the equations below:

$$max(|W_i - W_{i num}|)$$
$$max(|b_i - b_{i num}|)$$

Where  $\cdot_{num}$  represents the numerical computed value. The

Table 1: Maximum absolute difference between the computed gradients for the parameter of each layer (first column) for different network configuration. The lists like [10, 10, 10] mean that there are 3 hidden nodes with 10 nodes each. For all the networks  $\lambda$  was set to 1.0.

$\overline{\text{Inner nodes}} \to$	[50]	[20, 10]	[10, 10, 10]
$\overline{W_1}$	7.01e-10	8.33e-10	6.71e-10
$b_1$	3.49e-10	2.33e-10	3.18e-10
$W_2$	5.51e-10	5.48e-10	4.97e-10
$b_2$	3.12e-10	2.86e-10	3.18e-10
$W_3$	-	4.58e-10	5.77e-10
$b_3$	-	3.05e-10	1.80e-10
$W_4$	-	-	4.90e-10
$b_4$	-	-	3.36e-10

### Test Multi-Layer

As suggested on the instructions I created a network with 2 hidden layers of 50 neurons each. Then I trained it on 45000 samples and validate it on 5000. The parameters I used were the one stated in the instructions :  $eta_min = 1e-5$ ,  $eta_max1e-1$ ,  $n_s = 5 \cdot 450$   $\lambda = 0.0001$  (but I guess thre was a typo,  $n_s$ 

was supposed to be  $n_s = 2 \cdot 450$ ).

The loss and the accuracy throughout the 2 cycles of training are shown in Figure 1. The accuracy I got on the test data is 50.17%.

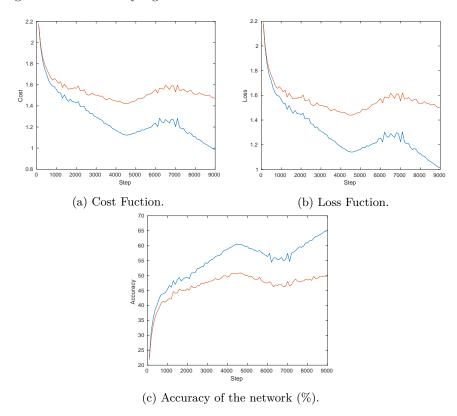


Figure 1: Training evolution of cost loss and accuracy on test and validation sets for the 2 layer network, with parameters  $eta_min=1e-5$ ,  $eta_max1e-1$ ,  $n_s=5\cdot 450~\lambda=0.0001$ , run for 2 cycles.

Then I tested with the same hyperparameters the 9 layer network described by the sequence of hidden states [50, 30, 20, 20, 10, 10, 10, 10]. The performance I get is 48.75%. For completeness I also polot again in Figure 2 the cost, loss and accuracy.

## Test Multi-Layer

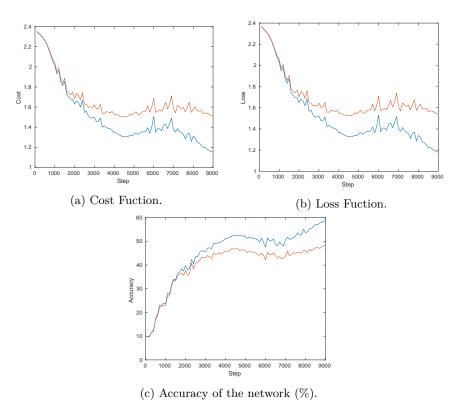


Figure 2: Training evolution of cost loss and accuracy for the 9-layer network.