

ASSIGNMENT 1

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Submitted by -

Anushthan Soren
S20290010027

Q1 Convert

a) $(4310)_5 = (\quad)_8 = (\quad)_{BCD}$

$$(4310)_5 = 0 \times 5^0 + 1 \times 5^1 + 3 \times 5^2 + 4 \times 5^3 \\ = (580)_{10}$$

8	580	
8	72	4
8	9	0
8	1	1
0	1	

$$\Rightarrow (580)_{10} = \underline{(1104)_8}$$

$$\Rightarrow (580)_{10} = \underline{\underline{(0101 \ 1000 \ 0000)_{BCD}}}$$

b) $(110.010)_2 = (\quad)_2 = (\quad)_8$

$$(110.010)_2 = 0 + 1 \times 12 + 1 \times (12)^2 \\ + 0 + 1 \times 12^{-2} + 0$$

$$= (156.00694)_{10} = \underline{\underline{(10011100.0000000011)_2}}$$

2	156	
2	78	0
2	39	0
2	19	1
2	9	1
2	4	1
2	2	0
2	1	0

$$12^2 \times 2 = 0 + (1/72)$$

$$(1/72) \times 2 = 0 + (1/36)$$

$$(1/36) \times 2 = 0 + (1/18)$$

$$(1/18) \times 2 = 0 + (1/9)$$

$$0.111 \times 2 = 0 + 0.222$$

$$0.222 \times 2 = 0 + 0.444$$

$$0.444 \times 2 = 0 + 0.888$$

$$0.888 \times 2 = 1 + 0.776$$

$$(100111.00 \cdot 00000001)_2 = (\underline{234.003})_8$$

$$\textcircled{c} (DADA \cdot B)_{16} = (\quad)_5$$

$$(DADA \cdot B)_{16} = (1101 \ 1010 \ 1101 \ 1010 \cdot \ 1011)_2$$

$$\begin{aligned} D &= 13 \\ A &= 10 \end{aligned} \quad = 10 \times 16^0 + 13 \times 16^1 + 10 \times 16^2 + 13 \times 16^3 + 11 \times 16^4 \\ &= (56026.6875)_{10}$$

5	56026		$0.6875 \times 5 = 3 + 0.4375$
5	11205	1	$0.4375 \times 5 = 2 + 0.1875$
5	2241	0	$0.1875 \times 5 = 0 + 0.9375$
5	448	1	$0.9375 \times 5 = 4 + 0.6875$
5	89	3	
5	17	4	
5	3	2	
5	0	3	

$$(56026.6875)_{10} = (\underline{3243101.3204})_5$$

Q2 Evaluate 9's and 10's complement of 54760, 003497.

$$\begin{aligned} \text{9's complement of } (54760)_{10} &= (10^5 - 1) - 54760 \\ &= 45239 \end{aligned}$$

$$\begin{aligned} \text{10's complement of } (54760)_{10} &= \text{9's complement} + 1 \\ &= 45240 \end{aligned}$$

$$\begin{aligned} \text{9's complement of } (003497)_{10} &= (10^6 - 1) - (003497) \\ &= 996502 \end{aligned}$$

$$\begin{aligned} \text{10's complement of } (003497)_{10} &= \text{9's complement} + 1 \\ &= 996503 \end{aligned}$$

Q3 2's complement of 1001100, 0011010

$$\text{2's complement of } (1001100)_2 = (0110011) + 1 = 0110100$$

$$\text{2's complement of } (0011010)_2 = (1100101) + 1 = 1100110$$

Q4 Perform binary subtraction with complements:

$$X = 1011100, Y = 1001011$$

a) $X - Y$

$$\begin{array}{r} 1011100 \\ - 1001011 \\ \hline \end{array}$$

$$\text{2's complement of } (1001011)_2 = (0110101)$$

$$\begin{array}{r} 1011100 \\ + 0110101 \\ \hline 0010001 \end{array}$$

Discard 1

$$\text{Ans} = (0010001)_2$$

Q8 (B) $Y-X$: 2's complement of $X = (10100011)_2 + 1$
 $= (10100100)_2$

$$\begin{array}{r} 01001011 \\ + 10100100 \\ \hline 11101111 \end{array} \Rightarrow \text{Ans} = \begin{matrix} \text{2's complement} \\ \text{of } 11101111 \end{matrix} = -\underline{\underline{00010001}}$$

(C) $-X-Y$: 2's complement of $X = (10100100)_2$
 2^8 complement of $Y = (10110101)_2$

$$\begin{array}{r} 10100100 \\ + 10110101 \\ \hline 10101101 \end{array} \Rightarrow \text{Ans} = \begin{matrix} \text{2's complement} \\ \text{of } 10101101 \end{matrix} = -(\underline{\underline{01010011}})$$

Q8 Perform BCD addition and subtraction:

a) $X = 0100$, $Y = 0101$

(i) $\begin{array}{r} 0100 \\ + 0101 \\ \hline 1001 \end{array}$

(ii) 2's complement of Y
 $= 1011$

$$\begin{array}{r} 0100 \\ + 1011 \\ \hline 1111 \end{array}$$

Ans = $-(2^8 \text{ complement of } 1111)$
 $= -0001$

$$\textcircled{B} \quad X = 1000, Y = 1001$$

$$\begin{array}{r} 01000 \\ + 10101 \\ \hline 10001 \end{array}$$

$$\begin{array}{r} \\ + 0110 \text{ (Adding 6)} \\ \hline 10111 \end{array}$$

$$\Rightarrow \text{Ans} = 0001\ 0111 \\ = (17)_{10}$$

$$\text{(ii) } 2^3 \text{ complement of } Y = 10111$$

$$\begin{array}{r} 01000 \\ + 10111 \\ \hline 11111 \end{array}$$

$$\text{Ans} = -(2^3 \text{ complement of } 11111) \\ = -00001$$

$$\text{Q6} \quad (49)_{10} \equiv (0110001)_2, \quad (29)_{10} \equiv (0011101)_2$$

2	49	
2	24	1
2	12	0
2	6	0
2	3	0
2	1	1
0	0	1

2	29	
2	14	1
2	7	0
2	3	1
2	1	1
0	0	1

$$\text{(iv) } (29) + (-49), \quad \text{expected ans} = -(20)_{10}$$

$$2^3 \text{ complement of } (0110001)_2 = (1001111)_2$$

$$\begin{array}{r} 1111 \\ 0011101 \\ + 1001111 \\ \hline 1101100 \end{array}$$

$$\Rightarrow \text{Ans} = -(2^3 \text{ complement of } 1101100)$$

$$= -(0010100)_2 = -(20)_{10}$$

$$(ii) (-29) + (49), \text{ expected ans} = (20)_10$$

2^7 's complement of $(001110)_2 = (110001)_2$

$$\begin{array}{r} & 1 & 1 \\ & 1100011 \\ + & 0110001 \\ \hline 1) & 0010100 \end{array} \Rightarrow \text{Ans} = (0010100)_2 \\ \underline{\text{Discarded}} \\ \equiv (20)_10 \\ \underline{\text{verified}}$$

$$(iii) (-29) + (-49) \quad (29)_10$$

2^7 's complement of $(001110)_2 = (110001)_2$

2^8 's complement of $(011000)_2 = (100111)_2$

$(49)_10$

$$\begin{array}{r} & 1 & 1 & 1 \\ & 1100011 \\ + & 1001111 \\ \hline 1) & 0110010 \end{array} \Rightarrow \text{Ans} = -(\text{2}^7 \text{ complement of } 0110010) \\ \underline{\text{Discard}} \\ = - (1001110)_2$$

Q7 (Q) 16's complement of C3DF

$$= 15's \text{ complement} + 1 - \text{C3DF}$$

$$= FFFF - \text{C3DF} + 1$$

$$= 3C21$$

$$\begin{array}{r} \text{FFFF} \\ - \text{C3DF} \\ \hline \text{3C20} \end{array}$$

(B) Convert C3DF to binary:

$$(C3DF)_{16} \equiv (1010\ 0011\ 1011\ 1111)_2$$

(C) 2's complement of $(1010\ 0011\ 1011\ 1111)_2$

$$\equiv (0101\ 1100\ 0100\ 0001)_2$$

$$(D) (0101\ 1100\ 0100\ 0001)_2 = (5C41)_{16}$$

$$(C3DF)_{16} > (5C41)_{16}$$

Q 111011 ÷ 101 = 001011 remainder: 0100

$$\begin{array}{r}
 \text{111011} \\
 \text{101) } \overline{\text{111011}} \\
 -101 \\
 \hline
 1001 \\
 -101 \\
 \hline
 01001 \\
 -101 \\
 \hline
 0100
 \end{array}$$

Q9 111011×101

$$\begin{array}{r}
 111011 \\
 \times 101 \\
 \hline
 111011 \\
 6000000x \\
 \hline
 100100111
 \end{array}$$

Q10 let base = r

$$(x-3)(x-6) = x^2 - (r+1)x + 6(r+2)$$

$$r+1 = 9 \quad ; \quad 2r+2 = 18$$

$$\underline{r=8}$$