# Particles Filter: a robot localization application





#### Particles Filter: a robot localization application

#### **OutLine**

- ☐ Introduction
- Basics
- Motion and Sensors Model

#### Inspired by:

Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg Probabilistic Robotics, Sebastian THRUN, Wolfram BURGARD, Dieter FOX, 2000









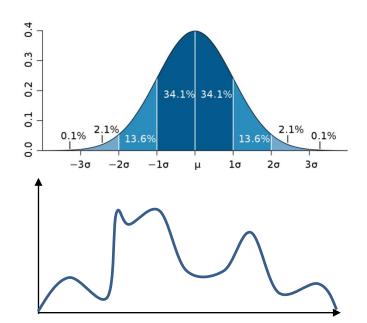
# Particles filter, What is the need?

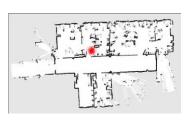


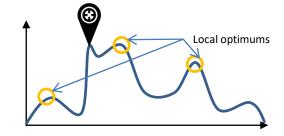
- Model distributions
  - ☐ For Gaussian distribution
    - → Kalman Filter
  - ☐ For Arbitrary distribution
    - $\rightarrow$  ?



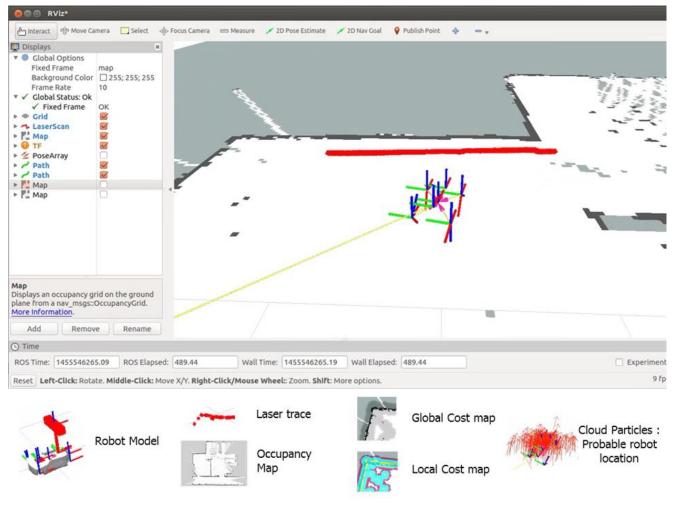
- Robot localization
- ☐ Function optimum finding













http://cpe-dev.fr/navigation-test/





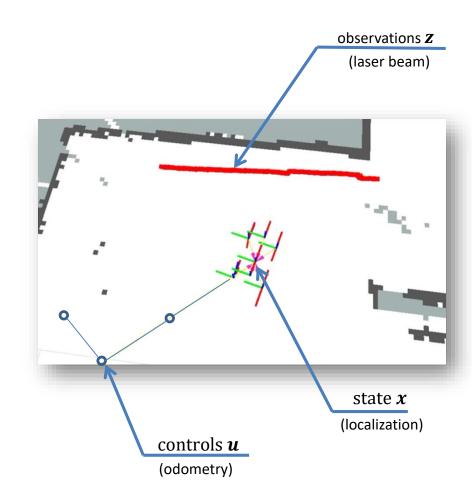
https://www.youtube.com/watch?v=OVoa11xd3vE





- $\square$  How to known a system state x:
  - ☐ Given observations **Z**
  - $\Box$  Given controls u

$$p(x \mid z, u)$$







Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

$$bel(x_t) = p(x_t \mid z_{1:t}, u_{1:t})$$

Definition of the belief



$$bel(x_t) = p(x_t|z_{1:t}, u_{1:t})$$

$$bel(x_t) = p(x_t|z_{1:t}, u_{1:t})$$

$$bel(x_t) = \frac{p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})}{p(z_t|z_{1:t-1}, u_{1:t})} \xrightarrow{\text{Bayes Law}} p(A|B) = \frac{p(B|A)p(A)}{p(B)}$$

$$= \eta \ p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})$$

$$= \eta \ p(z_t|x_t) \ p(x_t \mid z_{1:t-1}, u_{1:t}) \xrightarrow{\text{Markov assumption}} p(z_t|x_t, z_{1:t-1}, u_{1:t})$$

$$= \eta \ p(z_t|x_t) \ p(x_t \mid z_{1:t-1}, u_{1:t})$$

$$= \eta \ p(z_t|x_t) \ p(x_t \mid z_{1:t-1}, u_{1:t})$$

 $bel(x_t) = p(x_t|z_{1:t}, u_{1:t})$ 

$$bel(x_t) = \frac{p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})}{p(z_t|z_{1:t-1}, u_{1:t})}$$

$$= \eta \ p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})$$

$$= \eta \ p(z_t|x_t) \ p(x_t \mid z_{1:t-1}, u_{1:t})$$

Law of total probabilities 
$$P(A) = \int P(A|B) \cdot P(B) dB$$

$$= \eta \, p(z_t|x_t) \int p(x_t|x_{t-1}, z_{1:t-1}, u_{1:t}) \, p(x_{t-1}|x_{t-1}, u_{1:t}) \, dx_{t-1}$$



$$bel(x_t) = p(x_t|z_{1:t}, u_{1:t})$$

$$\begin{aligned} bel(x_t) &= \frac{p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})}{p(z_t|z_{1:t-1}, u_{1:t})} \\ &= \eta \ p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t}) \\ &= \eta \ p(z_t|x_t) \ p(x_t \mid z_{1:t-1}, u_{1:t}) \\ &= \eta \ p(z_t|x_t) \int \ p(x_t \mid x_{t-1}, z_{1:t-1}, u_{1:t}) \ p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) dx_{t-1} \\ &= \eta \ p(z_t|x_t) \int \ p(x_t \mid x_{t-1}, z_{1:t-1}, u_{1:t}) \ p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) dx_{t-1} \\ &= \eta \ p(z_t|x_t) \int \ p(x_t \mid x_{t-1}, u_t) \ p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) dx_{t-1} \end{aligned}$$



$$bel(x_t) = p(x_t|z_{1:t}, u_{1:t})$$

Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

$$bel(x_t) = \frac{p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})}{p(z_t|z_{1:t-1}, u_{1:t})}$$

$$= \eta \ p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})$$

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$$= \eta \ p(z_t|x_t) \int p(x_t \mid x_{t-1}, u_t) \ p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) dx_{t-1}$$
Future command  $u_t$  as no influence on current state  $x_{t-1}$ 

 $= \eta \, p(z_t|x_t) \int p(x_t|x_{t-1}, u_t) \, p(x_{t-1}|z_{1:t-1}, \underline{u_{1:t-1}}) dx_{t-1}$ 



$$bel(x_t) = p(x_t|z_{1:t}, u_{1:t})$$

$$\begin{split} bel(x_t) &= \frac{p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t})}{p(z_t|z_{1:t-1}, u_{1:t})} \\ &= \eta \ p(z_t|x_t, z_{1:t-1}, u_{1:t})p(x_t \mid z_{1:t-1}, u_{1:t}) \\ &= \eta \ p(z_t|x_t) \ p(x_t \mid z_{1:t-1}, u_{1:t}) \\ &= \eta \ p(z_t|x_t) \int \ p(x_t \mid x_{t-1}, z_{1:t-1}, u_{1:t}) \ p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) dx_{t-1} \\ &= \eta \ p(z_t|x_t) \int \ p(x_t \mid x_{t-1}, u_t) \ p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) dx_{t-1} \\ &= \eta \ p(z_t|x_t) \int \ p(x_t \mid x_{t-1}, u_t) \ p(x_{t-1} \mid z_{1:t-1}, u_{1:t}) dx_{t-1} \end{split}$$

$$bel(x_t) = \eta p(z_t|x_t) \int p(x_t|x_{t-1}, u_t) bel(x_{t-1}) dx_{t-1}$$





Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

$$bel(x_t) = \eta \, \underline{p(z_t|x_t)} \int \underline{p(x_t|x_{t-1}, u_t)} \, bel(x_{t-1}) dx_{t-1}$$

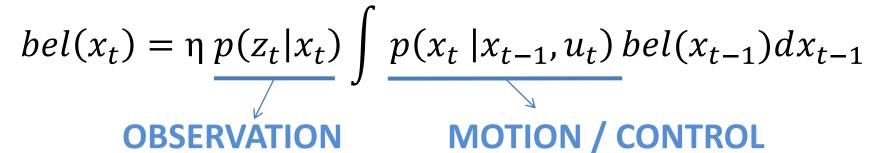
**OBSERVATION** 

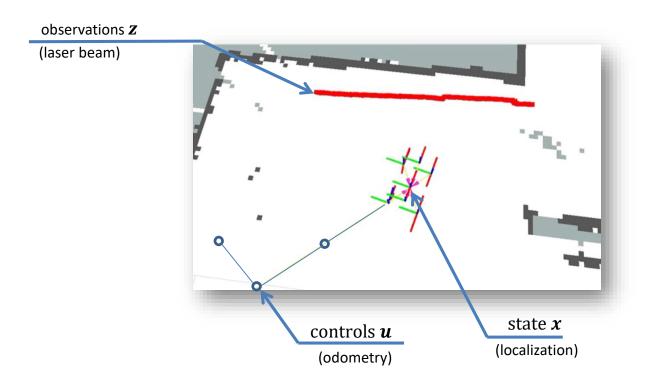
**MOTION / CONTROL** 

→ Correction step

→ Prediction step











## **Bayes Filter**

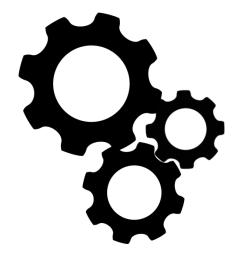
- ☐ Framework (template) for recursive state estimation
- ☐ Different possible instances depending:
  - Models for motion/control and observation (linear vs non-linear)
  - ☐ Parametric vs non-parametric filter
  - Dealing with Gaussian distribution or not





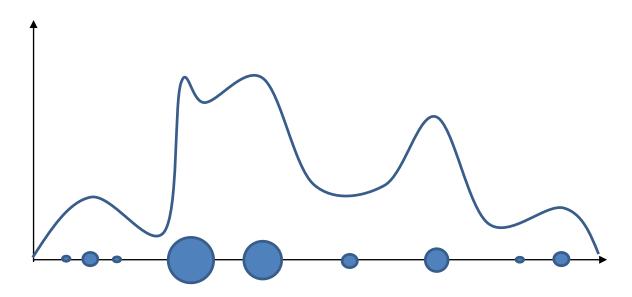






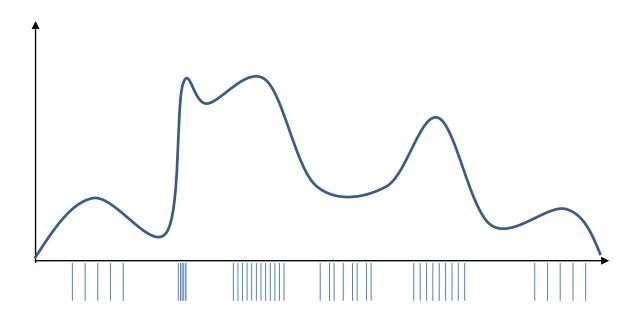
Particles Filter: Basics





Set of **samples** (particules) **are distributed** across the environnment. **Each sample is weighted** according to the distribution





The **heigher** the sample **weight** is, the more particules are **distributed around** 

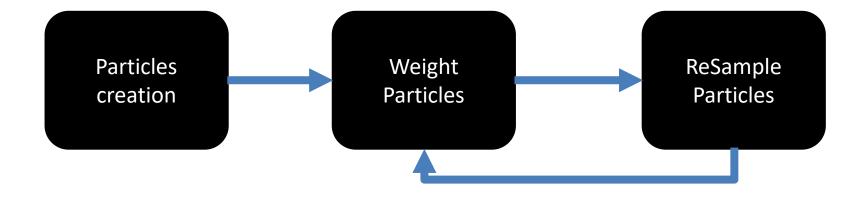


The resampling step is a probabilistic **implementation of the Darwinian idea of survival of the fittest**: It refocuses the particle set to regions in state space with high posterior probability.

Probabilistic Robotics, Sebastian THRUN, Wolfram BURGARD, Dieter FOX, 2000







### How to obtain such samples?



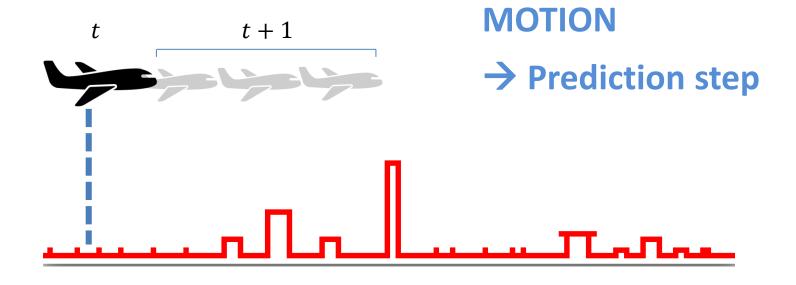


## Example









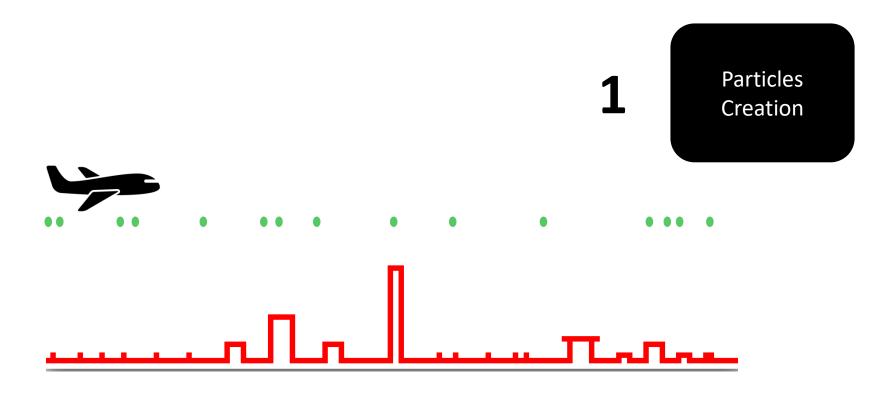
#### **OBSERVATION**

→ Correction step







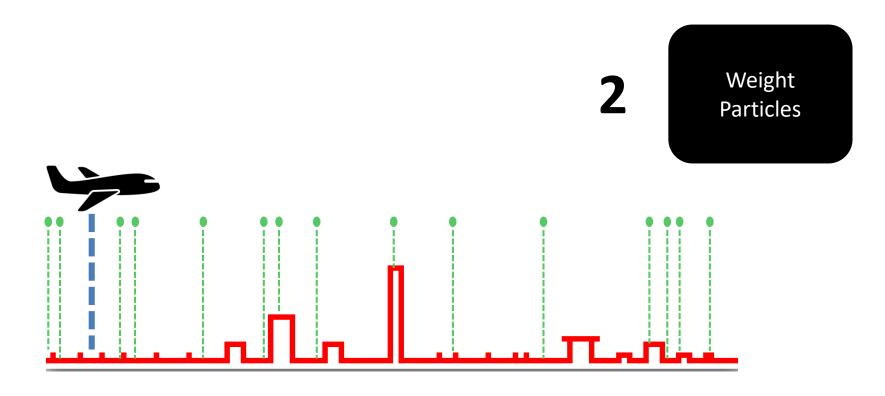


If no initial knowledge, uniform distribution of the particles accross the environment









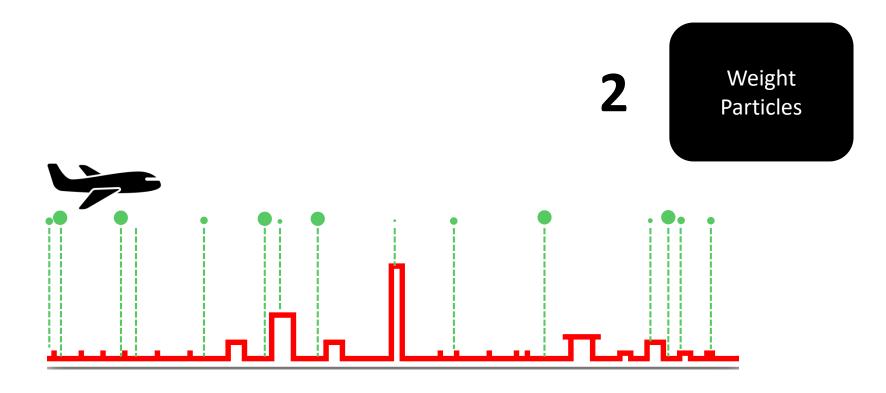
Weight particles according the current observation and the estimate observation at the particle position

Observation models is combined with an Error model (Gaussian error model is commonly used)









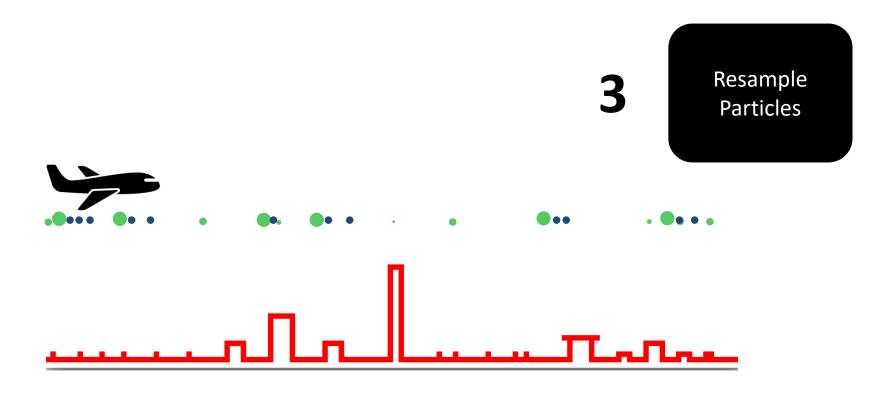
Weight particles according the current observation and the estimate observation at the particle position

**Observation models** is **combined** with an **Error model** (Gaussian error model is commonly used)









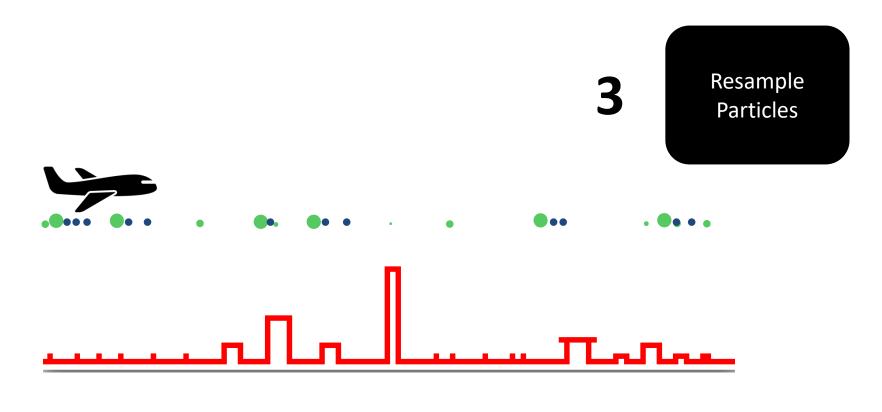
Resample Particles according their weight.

Spread new particles close to heigher weighted particles according to a motion model (also combined with an error model)









Resample Particles according their weight.

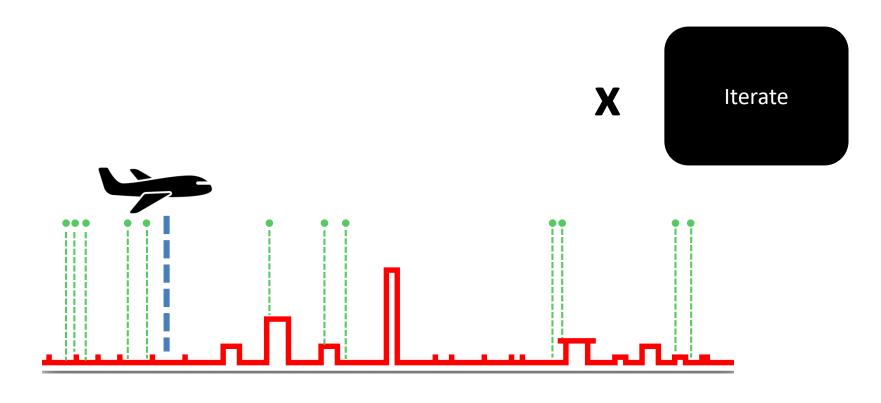
**Spread** new particles close to heigher weighted particles according to a motion model (also combined with an error model)

Remove old particles









Make Observation at t+1 (plane move)

**Weight Particles** 

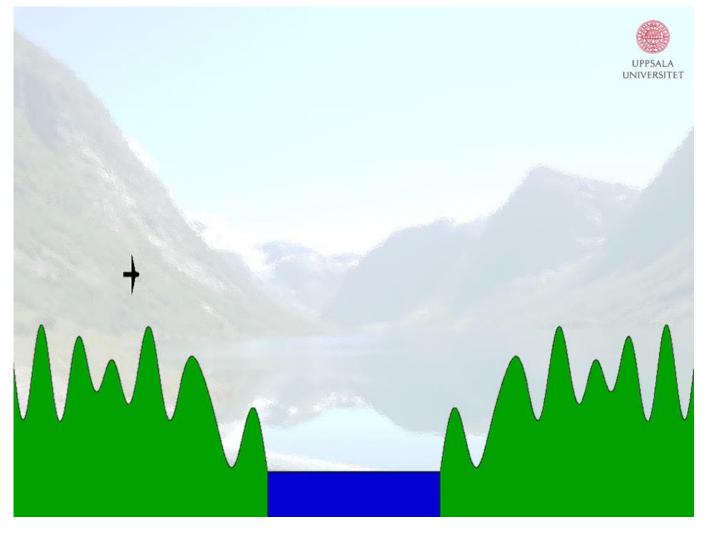
**Remove old Particles** 







### Example



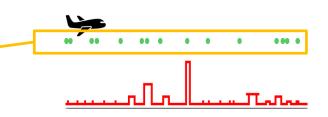


https://www.youtube.com/watch?v=aUkBa1zMKv4

- Mathematic explanation
  - $\Box$  let  $X_t$  the set of particules  $p_t^{[m]}$  such as

$$X_t := x_t^{[0]}, x_t^{[1]}, ..., x_t^{[M]}$$

Where  $1 \le m \le M$ 



☐ Inspired by Baye filter

$$x_t^{[m]} \sim p(x_t|z_{1:t},u_{1:t})$$

Particule m depends of a previous particule at t-1

$$x_t^{[m]} \sim p(x_t|u_t, x_{t-1}^{[m]})$$

Particule m get an importance factor according observation

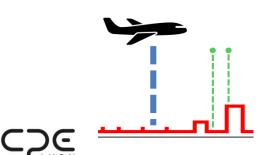


$$w_t^{[m]} = p(z_t | x_t^{[m]})$$

- Mathematic explanation
  - ☐ the particle set can be redefined as followed:

Importance Weight
$$X_{t} \coloneqq \left\{ \left\langle x_{t}^{[m]}, w_{t}^{[m]} \right\rangle \right\}_{m=1,...,M}$$

**State Hypothesis** 



☐ Algorithm

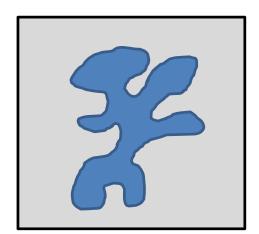
```
1:
           Algorithm Particle_filter(\mathcal{X}_{t-1}, u_t, z_t):
2:
                \mathcal{X}_t = \mathcal{X}_t = \emptyset
3:
                for m = 1 to M do
                                                                          _{	extstyle} How to get samples ?
                                     \sim p(x_t \mid u_t, x_{t-1}^{[m]})
4:
5:
                                                                          How to weight?
6:
7:
                endfor
8:
                for m = 1 to M do
                    draw i with probability \propto w_{\scriptscriptstyle t}^{[i]}
                                                                          How to get new particles?
9:
                     add x_t^{[i]} to \mathcal{X}_t
10:
11:
                endfor
12:
                return \mathcal{X}_t
```

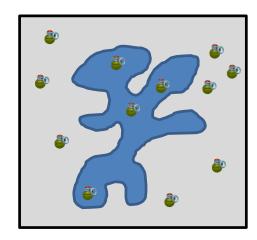
Probabilistic Robotics, Sebastian THRUN, Wolfram BURGARD, Dieter FOX, 2000



- ☐ How to get new particles?
  - ☐ Particles Filter also called **Sequential Monte Carlo**
  - What are Monte Carlo Method?
    - Basic (historical) Example : How to compute a lake area?







S total area
Stake lake area
N number of round shot
X number of Round Shot on the
ground

$$\frac{S}{S_{lake}} = \frac{N}{N - X}$$

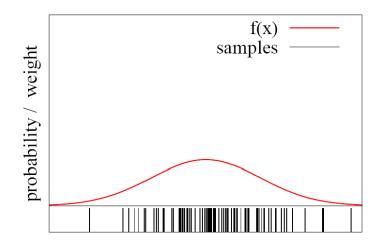
$$S_{lake} = \frac{(N-X)}{N} \times S$$

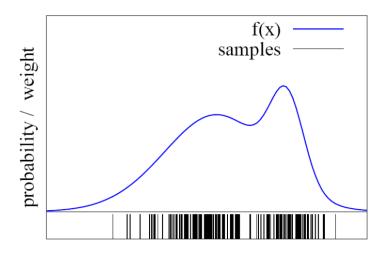




☐ How to get new particles?

Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg





The more particles fall into a region, the higher the probability of the region

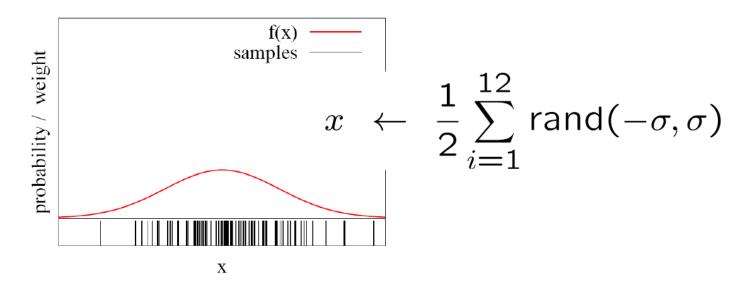
#### How to obtain such samples?





Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

- How to get new particles?
  - Closed Form Sampling is Only Possible for a Few Distributions
  - E.g Gaussian



How to sample from **other** distributions?

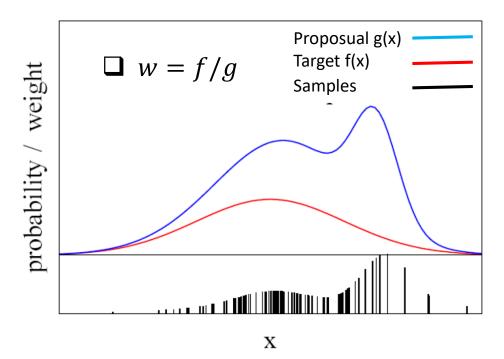




Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

- ☐ How to get new particles?
  - $\Box$  Use a different distribution g to generate samples from f
  - lacktriangle According for the "differences between  $m{g}$  and  $m{f}$ " using a

weight 
$$w = f/g$$





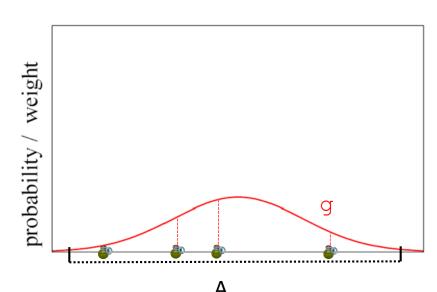


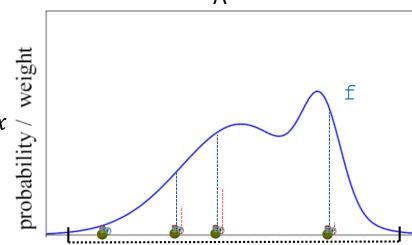
- ☐ How to get new particles?
  - **Explanations**

$$\frac{1}{M} \sum_{m=1}^{M} I(x^{[m]} \in A) \to \int_{A} g(x) dx$$

$$w^{[m]} = \frac{f(x^{[m]})}{g(x^{[m]})}$$

$$\frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} I(x^{[m]} \in A) w^{[m]} \to \int_{A} f(x) dx \text{ in proposed for } \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} u^{[m]} w^{[m]} = \frac{1}{\sum_{m=1}^{M} w^{[m]}} \sum_{m=1}^{M} u^{[m]} w^{[m]} = \frac{1}{\sum_{m=1}^{M} w^{[m]}} w^{[m]} = \frac{1}{\sum_{m=1}^{$$







- ☐ How to Weight?
- lacktriangle According for the "differences between g and f" using a weight w=f/g

$$w_{t}^{[m]} = \frac{target f(x_{t}^{[m]})}{proposual g(x_{t}^{[m]})}$$
$$\sim p(z_{t}|x_{t}^{[m]})$$

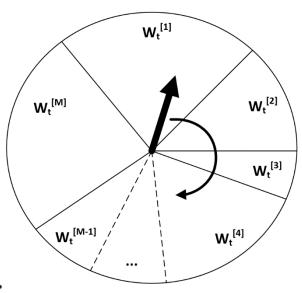
Cf Probabilistic Robotics, Sebastian THRUN, Wolfram BURGARD, Dieter FOX, 2000, Chapter 4



☐ How to get new particules?

$$X_t \coloneqq \left\{ \left\langle x_t^{[m]}, w_t^{[m]} \right\rangle \right\}_{m=1,\dots,M}$$

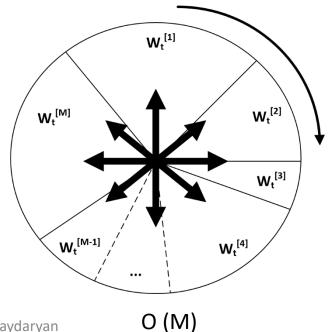
Roulette wheel



O (M Log M)

The more particles fall into a region, the higher the probability of the region

Stochastic universal sampling



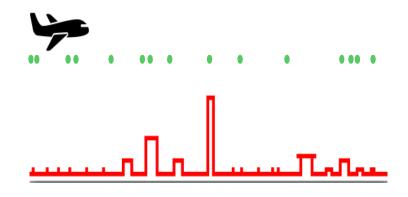






Example

```
Algorithm Particle_filter(\mathcal{X}_{t-1}, u_t, z_t):
1:
2:
                     \bar{\mathcal{X}}_t = \mathcal{X}_t = \emptyset
                     for m = 1 to M do
                          sample x_t^{[m]} \sim p(x_t \mid u_t, x_{t-1}^{[m]})
4:
                          w_t^{[m]} = p(z_t \mid x_t^{[m]})
5:
                          \bar{\mathcal{X}}_t = \bar{\mathcal{X}}_t + \langle x_t^{[m]}, w_t^{[m]} \rangle
6:
7:
                     endfor
8:
                     for m = 1 to M do
                           draw i with probability \propto w_t^{[i]}
9:
                          add x_t^{[i]} to \mathcal{X}_t
10:
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```



Probabilistic Robotics, Sebastian THRUN, Wolfram BURGARD, Dieter FOX, 2000



Example

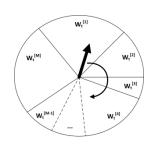
How to get samples ? 
$$x_t^{[m]} \sim p(x_t|u_t,x_{t-1}^{[m]})$$
 
$$u_t \sim Rand\ Uniform\ [-1,10] = \Delta x_t$$
 
$$x_t^{[m]} = x_{t-1}^{[m]} + \Delta x_t$$

How to weight?  $w_t^{[m]} \sim p(z_t | x_t^{[m]})$ 

$$w_t^{[m]} = \begin{cases} 0.9 & \text{if } z_t = esimate(\mathbf{z_t}^{[m]}) \\ 0.1 \end{cases}$$

How to get new particles?

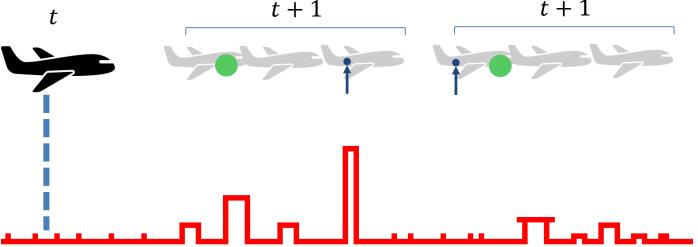




Example

for m = 1 to M do sample  $x_t^{[m]} \sim p(x_t \mid u_t, x_{t-1}^{[m]})$  $w_t^{[m]} = p(z_t \mid x_t^{[m]})$  $\bar{\mathcal{X}}_t = \bar{\mathcal{X}}_t + \langle x_t^{[m]}, w_t^{[m]} \rangle$ endfor

t+1



 $u_t \sim Rand\ Uniform\ [-1, 10] = \Delta x_t$ 

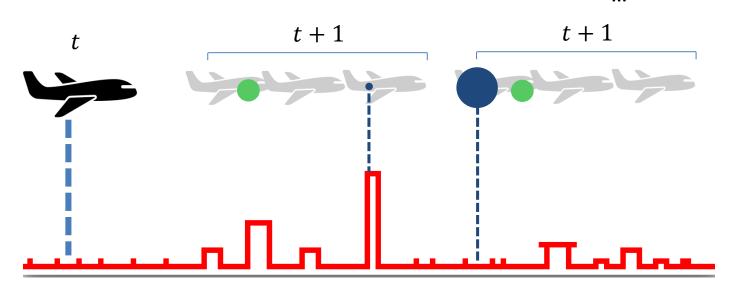




Example

for m = 1 to M do sample  $x_t^{[m]} \sim p(x_t \mid u_t, x_{t-1}^{[m]})$  $w_t^{[m]} = p(z_t \mid x_t^{[m]})$  $\bar{\mathcal{X}}_t = \bar{\mathcal{X}}_t + \langle x_t^{[m]}, w_t^{[m]} \rangle$ 

endfor



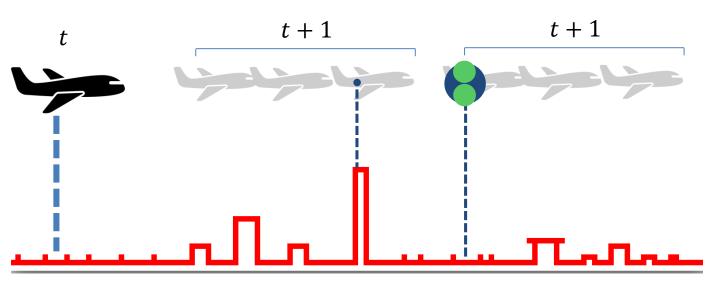
$$w_t^{[m]} = \begin{cases} 0.9 & \text{if } z_t = esimate(\mathbf{z_t}^{[m]}) \\ 0.1 \end{cases}$$



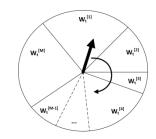


Example

for m = 1 to M do draw i with probability  $\propto w_t^{[i]}$ add  $x_t^{[i]}$  to  $\mathcal{X}_t$ endfor



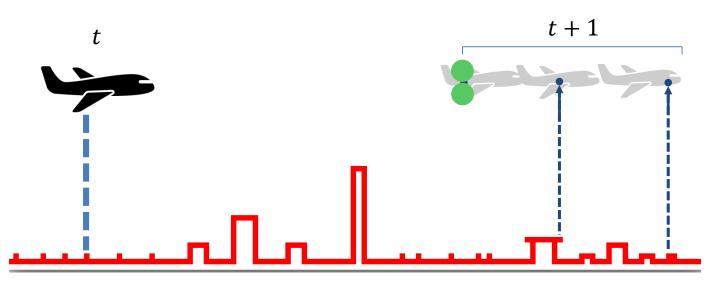




Example

 $\begin{aligned} &\text{for } m = 1 \text{ to } M \text{ do} \\ &\text{sample } x_t^{[m]} \sim p(x_t \mid u_t, x_{t-1}^{[m]}) \\ &w_t^{[m]} = p(z_t \mid x_t^{[m]}) \\ &\bar{\mathcal{X}}_t = \bar{\mathcal{X}}_t + \langle x_t^{[m]}, w_t^{[m]} \rangle \\ &\text{endfor} \end{aligned}$ 

• • •

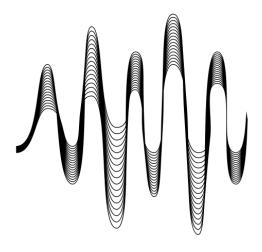












# Motion and Sensors data Modeling





- Odometry model (e.g vehicule) Thrun S. and Burgard W. and Fox D. Probabilistic Robotics (book), 2005
  - ☐ Hypothesis:
  - $\square$  Robot in pose  $(\overline{x}, \overline{y}, \overline{\theta})$  needs to go to  $(\overline{x}', \overline{y}', \overline{\theta}')$
  - Odometry information can be defined as a set of rotations and translations  $u=(\delta_{rot1},\delta_{trans},\delta_{rot2})$

$$\delta_{trans} = \sqrt{(\overline{x}' - \overline{x})^2 + (\overline{y}' - \overline{y})^2}$$

$$\delta_{rot1} = atang2(\overline{y}' - \overline{y}, x' - \overline{x}) - \overline{\theta}$$

$$\delta_{rot2} = \overline{ heta}$$
'-  $\overline{ heta} - \delta_{rot1}$ 

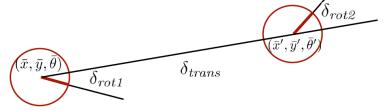


Image: Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg





☐ Odometry model (e.g vehicule)

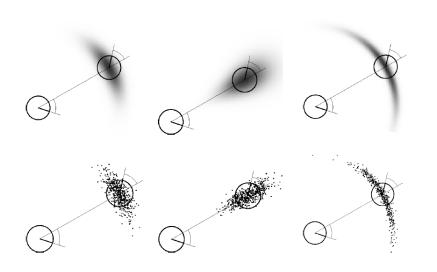
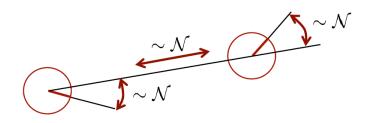


Image from: Thrun S. and Burgard W. and Fox D. Probabilistic Robotics (book), 2005.

■ Noise in Odometry (e.g Gaussian Noise)



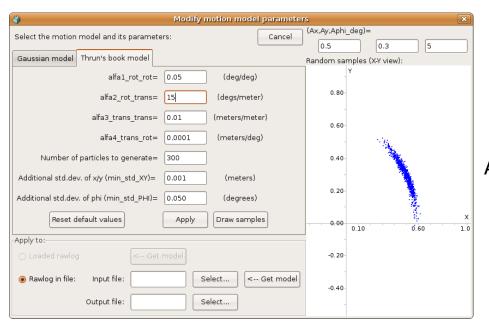
Approximation for stand deviation computation:

$$\sigma_{rot1} = \alpha_1 |\delta_{rot1}| + \alpha_2 \delta_{trans} 
\sigma_{trans} = \alpha_3 \delta_{trans} + \alpha_4 (|\delta_{rot1}| + |\delta_{rot2}|) 
\sigma_{rot2} = \alpha_1 |\delta_{rot2}| + \alpha_2 \delta_{trans}$$





☐ Odometry model (e.g vehicule)



$$\hat{\delta}_{trans} = \delta_{trans} + \epsilon_{trans} \qquad \epsilon_{trans} \sim \mathcal{N}(0, \sigma_{trans}^2) \\
\hat{\delta}_{rot1} = \delta_{rot1} + \epsilon_{rot1} \qquad \epsilon_{rot1} \sim \mathcal{N}(0, \sigma_{rot1}^2) \\
\hat{\delta}_{rot2} = \delta_{rot2} + \epsilon_{rot2} \qquad \epsilon_{rot2} \sim \mathcal{N}(0, \sigma_{rot2}^2)$$

#### Approximation for stand deviation computation:

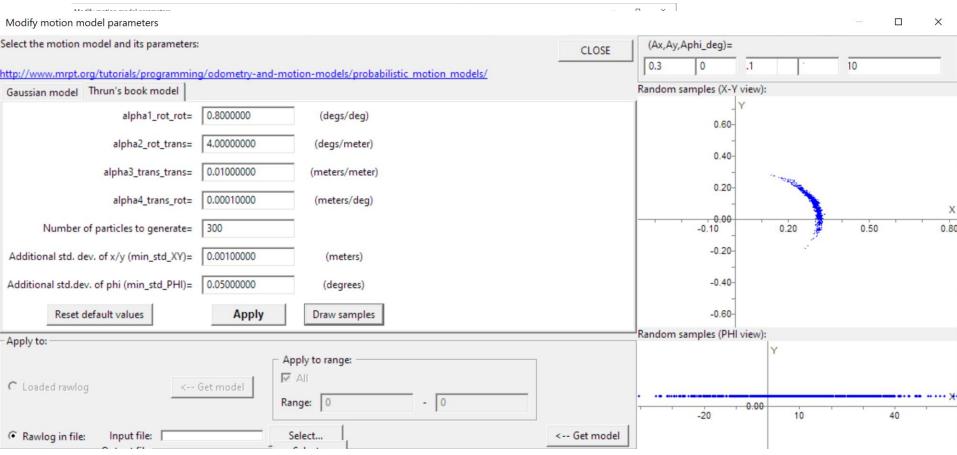
$$\sigma_{rot1} = \alpha_1 |\delta_{rot1}| + \alpha_2 \delta_{trans} 
\sigma_{trans} = \alpha_3 \delta_{trans} + \alpha_4 (|\delta_{rot1}| + |\delta_{rot2}|) 
\sigma_{rot2} = \alpha_1 |\delta_{rot2}| + \alpha_2 \delta_{trans}$$

https://www.mrpt.org/tutorials/programming/odometry-and-motion-models/probabilistic\_motion\_models/





☐ Odometry model (e.g vehicule)





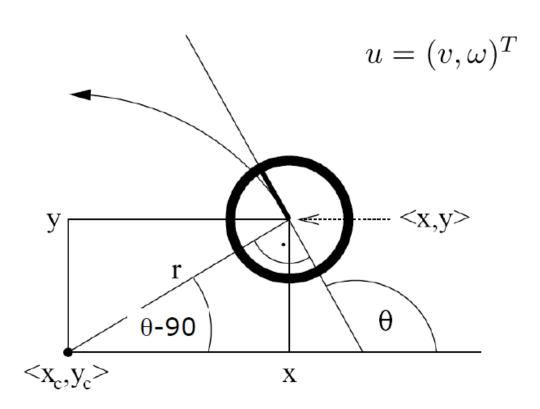






☐ Velocity model (e.g vehicule)

Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg







Velocity model (e.g vehicule)

Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

$$\begin{pmatrix} x' \\ y' \\ \theta' \end{pmatrix} = \begin{pmatrix} x \\ y \\ \theta \end{pmatrix} + \begin{pmatrix} -\frac{v}{\omega}\sin\theta + \frac{v}{\omega}\sin(\theta + \omega\Delta t) \\ \frac{v}{\omega}\cos\theta - \frac{v}{\omega}\cos(\theta + \omega\Delta t) \\ \omega\Delta t + \gamma\Delta t \end{pmatrix}$$

Term to account for the final rotation



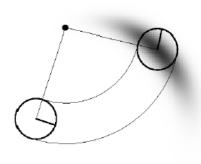


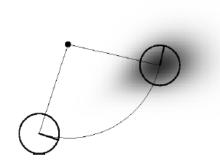


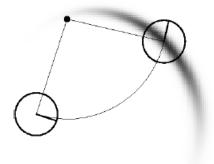


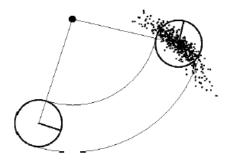
☐ Velocity model (e.g vehicule)

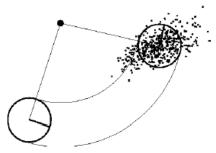
Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

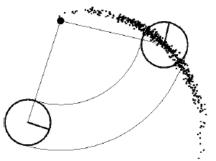


















## **Sensor Model**

Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

#### **Model for Laser Scanners**

Scan z consists of K measurements.

$$z_t = \{z_t^1, \dots, z_t^k\}$$

 Individual measurements are independent given the robot position

$$p(z_t \mid x_t, m) = \prod_{i=1}^k p(z_t^i \mid x_t, m)$$





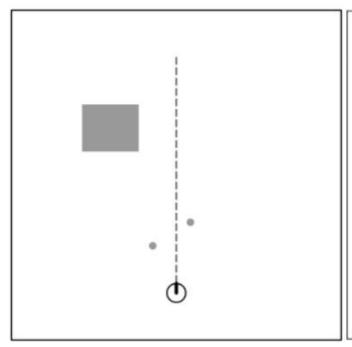


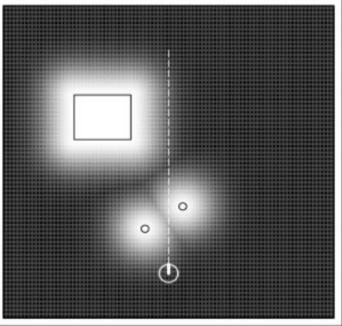


#### Sensor Model

Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

## **Beam-Endpoint Model**







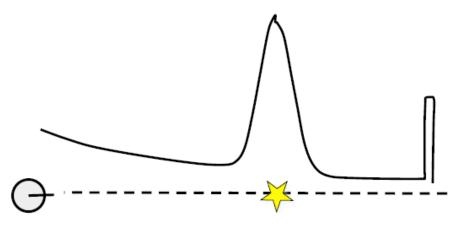


## Sensor Model

Slid from :Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg

#### Ray-cast Model

- Ray-cast model considers the first obstacle long the line of sight
- Mixture of four models









# References





#### References (1/2)

- Cyrill Stachniss, Robot Mapping Courses, UNI Freiburg
- Probabilistic Robotics, Sebastian THRUN, Wolfram BURGARD, Dieter FOX, 2000
- The particule Filter explained without equations, Andreas Svensson, UPPSALA UNIVERSITET
- Lectures video :
  - https://www.youtube.com/watch?v=5Pu558YtjYM
  - https://www.youtube.com/watch?v=aUkBa1zMKv4





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