## Projects for Numerical methods for Machine Learning

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## 1 Face recognition using SVD

You can consider images as vectors  $\mathbb{R}^{n_i}$ , hence a database of images of  $n_p$  persons in  $n_e$  different expressions can be represented by  $n_p$  different matrices  $A_p \in \mathbb{R}^{n_i \times n_e} (p=1,\ldots,n_p)$ .

The idea is to "model" the variation of faces of each person in the training set using an orthogonal basis of the subspace of  $\mathbb{R}^{n_i}$  spanned by the columns of  $A_p$ . This basis can be computed using the SVD, which enables us to write  $A_p$  as a sum of rank-one matrices: