

Interesting relationship of EVs versus a diesel car, weighing about 2900 lbs.<sup>1</sup>

Estimate the mechanical work at measured average 45mpg at average speeds, at 26% efficiency. Diesel fuel has about 139,000 BTU per gallon, so effectively 26% of this is applied to the mechanical work of moving the car at average speeds.

### Diesel car:

Fuel cost per gallon divided by fuel mileage (in MPG) gives *fuel cost per mile*:

$$\frac{\$/gal}{mileage} = \frac{\$}{mile}. \text{ At } \$5/\text{gallon, this comes to } \$0.11 / \text{mile}.$$

Now, an EV runs at about 90% efficiency, so if we calculate the mechanical work for the diesel car, and equate that to be the same work as moving an EV of similar size, design and weight, we can estimate the cost of electricity that would make the energy cost for the diesel and the EV the same. First mechanical work:

$$EC_{diesel} = 139,000 \frac{BTU}{gal}, \text{ diesel fuel energy content.}$$

$$\frac{EC_{diesel}}{mileage} = \text{energy expended, per mile. Now, apply efficiency:}$$

$$\left( \frac{EC_{diesel}}{mileage} eff_{diesel} \right) = \text{mechanical work, per mile. This comes to about } 0.24 \text{ kWh/mile. The}$$

above result is consistent with how economical the Cruze is to drive. A Tesla Series 3 weighs significantly more, as a mid-size car, not a compact, at between 3800 to 4200 pounds, but most losses at highway speeds are due to wind drag, not rolling friction.<sup>2</sup> 2022 Series 3 Long Range AWD published at 0.26 kWh/mi; 90% of that is 0.24 kWh/mile, so is the same as my Cruze estimate for mechanical work. Make all comparisons at same mechanical work, at 0.24 kWh/mi.

### EV:

$$\frac{\$}{kWh} \left[ \left( \frac{EC_{diesel}}{mileage} eff_{diesel} \right) / eff_{EV} \right] = \text{cost per mile for EV, using the same mechanical work}$$

per mile as above, but with EV losses included. The idea is to find where cost per mile is equal for both cases. Let  $x = \$/gal$  for the cost of diesel fuel. Let  $y = \$/kWh$  of the equivalent cost for the EV, equating costs per mile:

$$\frac{x}{mileage} = y \left[ \left( \frac{EC_{diesel}}{mileage} eff_{diesel} \right) / eff_{EV} \right], \text{ notice } mileage \text{ cancels.}$$

Solve for y:

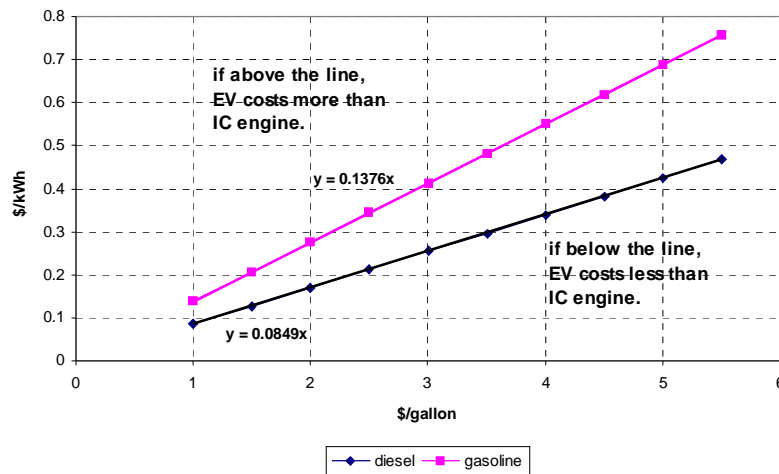
$$y = \frac{x eff_{EV}}{eff_{diesel} EC_{diesel}}$$

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<sup>1</sup> 2017 Chevy Cruze diesel, compact.

<sup>2</sup> 2022 Series 3: Lithium Ion Traction Battery w/11.5 kW Onboard Charger, 10 Hrs Charge Time @ 220/240V and 82 kWh Capacity, mid-size sedan.  $82\text{kWh}/(0.26\text{kWh/mi}) = 315 \text{ mi. range, est.}$  Tesla also publishes equivalent fuel mileage (MPGe) as combined/city/highway = 131 / 134 / 126, but I have no idea what that means. It's the cost that matters, not the quantities. One huge advantage of EV over IC type is no idling at stop signs. But so far, electric cars are really expensive.

With the above assumptions, with the units of \$/gallon for  $x$ , and \$/kWh for  $y$ , it's a linear relationship with a slope of 0.0849. At 28 mpg, 18% efficiency and 124,000 BTU/gal, a gasoline curve can also be made using the same basis, (\$0.14/mi at \$4/gal):



Below are some current charges for EVs. Remember, there are slow chargers and fast chargers, with the fast chargers being quite a bit more expensive and probably not very good for your battery:<sup>3</sup>

*On average, it costs between \$0.30- \$0.60 / kWh to charge an electric vehicle. Therefore, this means that a small car could cost about \$11.50 to \$23 to fully charge while a bigger or long-distance vehicle could cost between \$22.50 to \$45.*

*Level 3: These types of chargers are much more potent<sup>4</sup> than levels 2 and 1. It takes less time to charge at these stations, but not all cars can charge at these ports. Your car charge also needs to be below 80% charge to be charged at these ports. After your vehicle is at 80% of charge, the car starts charging a little slower. Level 3 chargers could take about fifteen minutes to charge your vehicle with 7kWh, covering around forty-five kilometers.*

*Level 2: These charger types are the most typical ones easily found anywhere in public. If your car is at 80% charge, it is better to charge it at a level 2 because it will charge at the same speed as a level 3 charger but at a cheaper cost. Level 2 chargers take between 5 to 12 hours to charge your car entirely.*

*Level 1: These chargers are ones you can have in your garage. It takes several hours to charge your car to 100% at home since the outlet has only 120 volts. If you have time, this would be a cheaper option. Charging at home will take between 8 to over 40 hours, depending on your car's battery size.*

For long distance, it's hard to imagine driving 300 miles, finding a Level 3 charger, and then having to wait 15 minutes for 45km (28mi), or in other words, around 2-1/2 hours before the next 300 miles. But I guess the inconvenience is worth the nearly insignificant difference in energy cost (sarc). Very different story with city driving, with Level 2.

<sup>3</sup> <https://www.mach1services.com/costs-of-using-car-charging-stations/>

<sup>4</sup> Higher voltage, as much as 800VDC. Some claim full charging to 80% in as little as a half an hour, at which point the power tapers off in order to limit damage to the battery.

### Anything to learn?

From the preceding, it would seem electric cars might be a good solution for cities, for people who can charge their own cars (have a garage, in other words) and work reasonably close to where they live (~25mi.). One thing to keep in mind is if demand is increased, costs go up, and one would expect the same for electricity. How much would demand go up?

It's estimated that 80% of the US population lives in cities, with some fraction of that qualifying to the criteria in the previous paragraph. Let's put it at half the city population would qualify, as a guess. It seems pretty clear from the previous information that EVs are not very appropriate for outside the cities. So, perhaps 40% of motor vehicles and the accompanying fuel demand could be replaced by EVs. Total gasoline consumption is between 370 and 390 million gallons per day the last few years, so assume 40% of 380 million gasoline demand is converted to electrical power.

$$40\% \times 380 \text{ million gallons} \times EC_{\text{gasoline}} = 5.524 \times 10^3 \text{ GWh, per day.}$$

where  $EC_{\text{gasoline}}$  is 123,000 BTU/gal, and GWh is Gigawatt-hours of energy.

This energy in gasoline is therefore  $2.016 \cdot 10^3$  tWh per year, tWh being terawatt-hours.

We can do the same sort of thing as earlier, and use the ratio of IC efficiency to EV efficiency to calculate electrical demand, but this time EV efficiency is 60%, not 90%, since we are talking about power generation, and have to include line losses from the plants to the vehicle, plus the vehicle's efficiency itself.

$$2.016 \times 10^3 \text{ tWh} \frac{\text{gasoline}_{\text{eff}}}{EV_{\text{eff}}} = 632 \text{ tWh of new generation required to replace gasoline.}$$

It's admittedly a rough estimate, but it could be compared to both installed power and produced power, mostly to dispell the notion that electricity is infinitely abundant. As of 2020, the EIA reported 4010 tWh per year being generated and consumed.

$$\frac{632}{4010} = 15.8\%$$

This is the amount of power generation that is needed to be added to supply the new electrical demand. Moreover, one of the reasons given for using EVs, given their inconvenience, is to slow down or stop climate change, so this only makes sense if renewables are what supplies the new demand. As of 2020, EIA has renewables (wind and solar) supplying about 20% of the power, or 802 tWh. (It has doubled since 2018!)

$$\frac{632}{802} = 78.8\%$$

This is the increase in generation required with existing renewables. EIA projects that solar will eventually eclipse wind for the major share of renewable power.

## Battery Charging

This is more of a description of natural limits, than any specific charger or battery. Batteries are subject to hysteresis and wear, just like about everything else. A high rate of charge can damage a battery, especially if it's already near full charge, usually taken as more than 80%. The chargers are subject to limits, too, such as current in a 120V wall plug charger probably shouldn't be more than 15 amps (breakers are usually about that; don't want high current in an extension cord!). High voltage Level 3 really need particular care, since they can cram a lot of electricity into a battery very quickly; and if they are more than 500V, have their own special safety requirements. A Level 2 probably would never exceed 50 amps, 30 amps is often given as a charging limit for some batteries.

Based on that, below are estimated charging times for a 15 A Level 1, a 30 A Level 2, and a 30 A Level 3 at 500V. This is based on the 82 kWh Series 3 Long Range battery capacity.

Level 3 at 500V	$30\text{ A} \cdot 500\text{ V} = 15 \cdot \text{kW}$	$\frac{82\text{ kWh}}{15\text{ kW}} = 5.5 \cdot \text{hr}$
Level 2 at 240V	$30\text{ A} \cdot 240\text{ V} = 7.2 \cdot \text{kW}$	$\frac{82\text{ kWh}}{7.2\text{ kW}} = 11.4 \cdot \text{hr}$
Level 1 at 120V	$15\text{ A} \cdot 120\text{ V} = 1.8 \cdot \text{kW}$	$\frac{82\text{ kWh}}{2.4\text{ kW}} = 34.2 \cdot \text{hr}$

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long range, 75kWh  
shorter, 38kWh  
Tesla LR Series 3, 82kWh